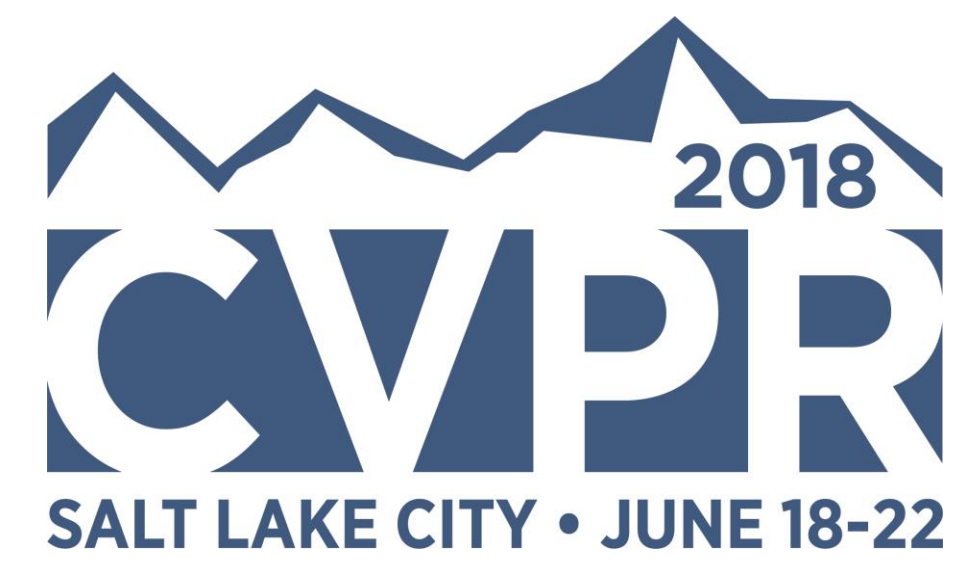




# Mining Point Cloud Local Structures by Kernel Correlation and Graph Pooling

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## Motivations

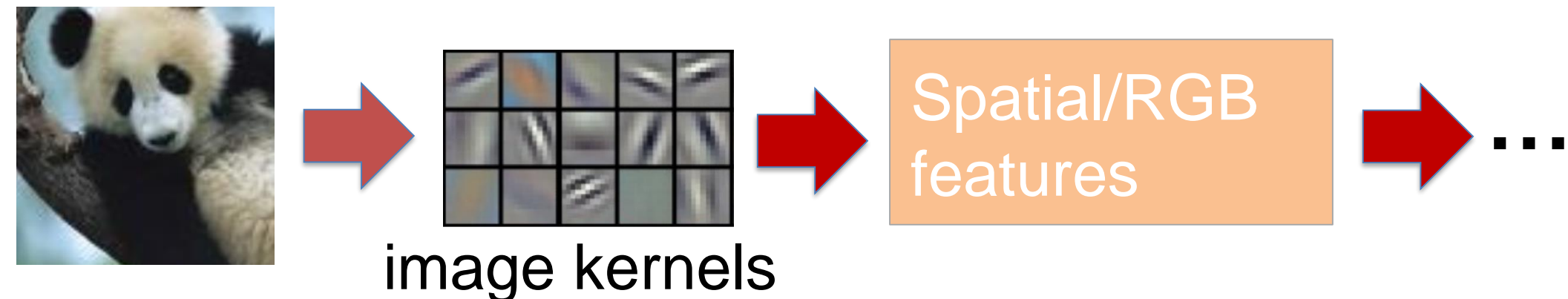
- Irregular organization in point clouds makes CNN not directly applicable.
- Point clouds are often converted to organized representations (voxel/multi-view) before deep networks.
- PointNet by Qi et al. directly consumes unordered point clouds but is difficult to capture local shape information.
- PointNet++/KdNet are time-consuming.

## Goal

Efficient learning of local features in 3D point clouds.

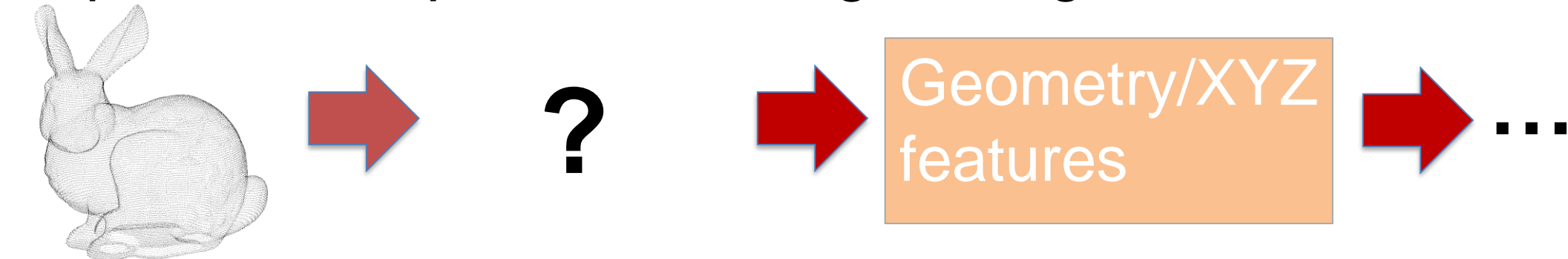
## Intuition

2D image: pixels with ordered organization.



CNN: find out “image kernels” with a measure of affinities to a local image patch (convolution).

3D point cloud: points with irregular organization.



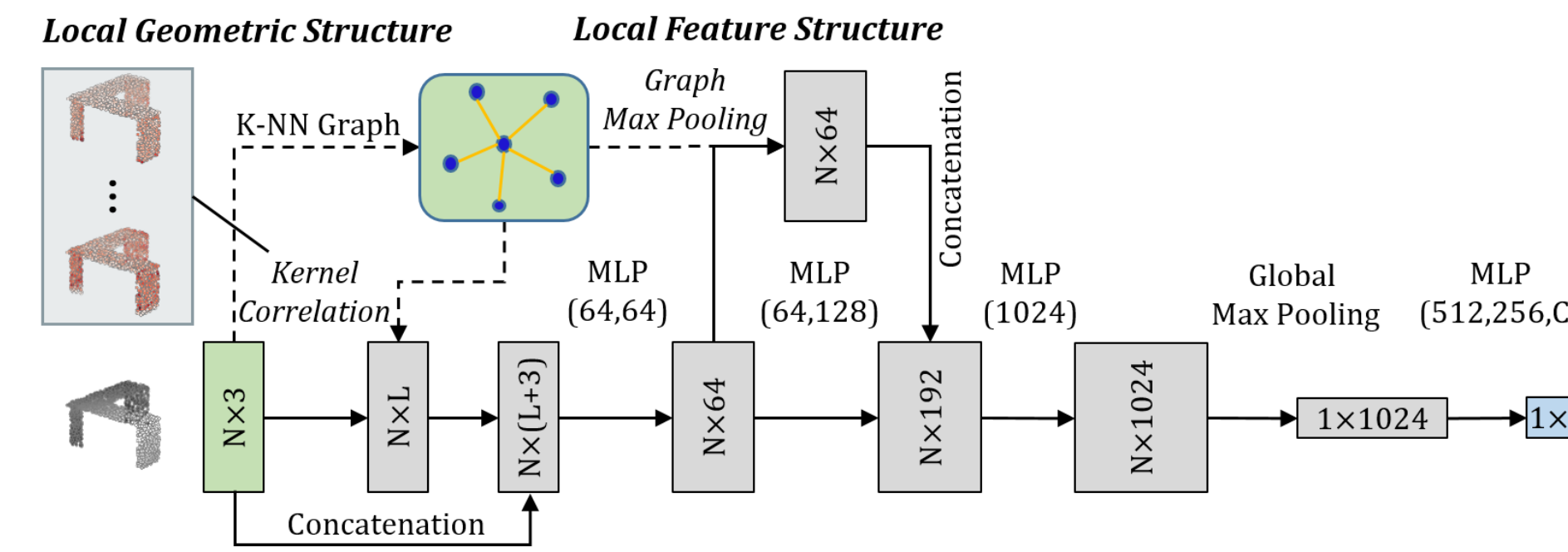
Our KCNet: find out “point kernels” with a measure of affinities to a set of local points (kernel correlation).

## Key Ideas

- Kernel correlation to extract local geometric structures.
- Graph max pooling to improve feature robustness.

## KCNet Architecture

### Classification Network



### 1. Extract Local Geometric Structures

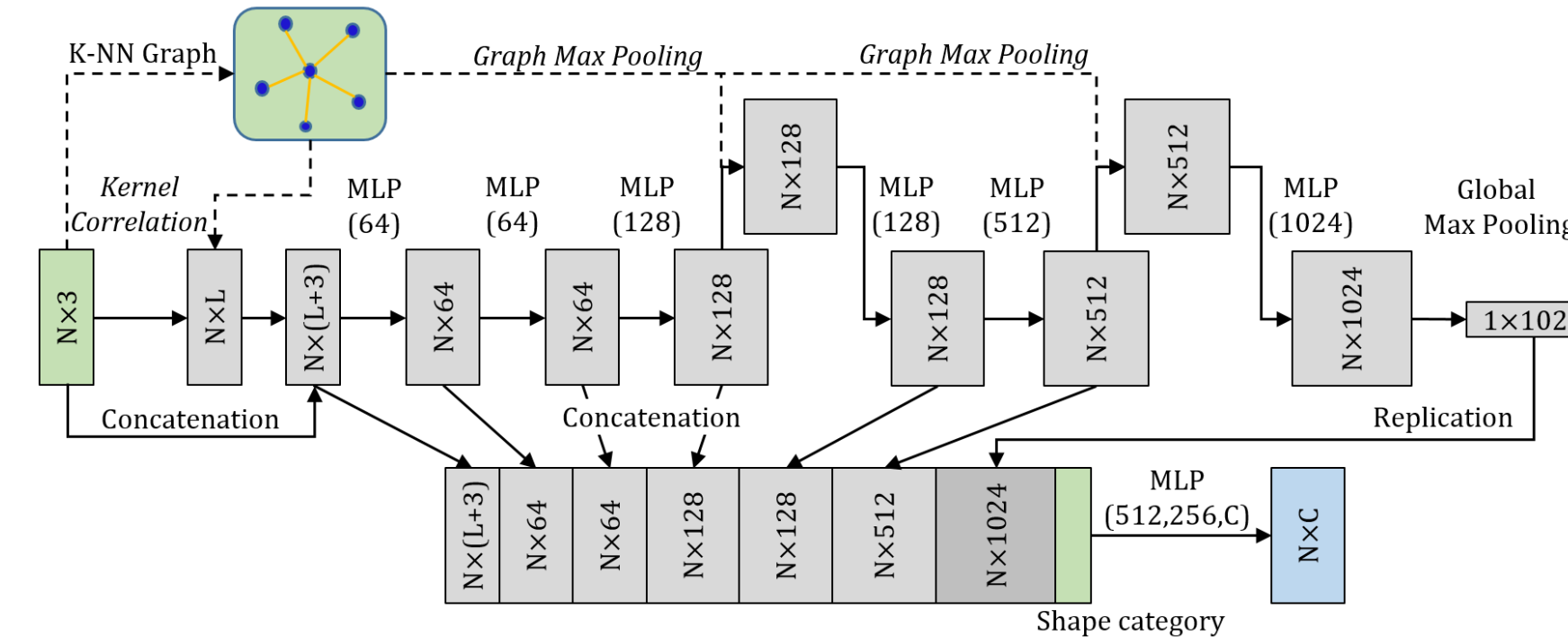
We used Kernel Correlation to capture local geometric structures.

$$KC(\kappa, x_i) = \frac{1}{|N(i)|} \sum_{m=1}^M \sum_{n \in N(i)} K_{\sigma}(\kappa_m, x_n - x_i),$$

$$K_{\sigma}(\kappa, \delta) = e^{\left(-\frac{\|\kappa - \delta\|}{2\sigma^2}\right)},$$

where  $N(i)$  indicates neighbors of  $x_i$ .

### Segmentation Network



### 2. Robust Features by Local Aggregation

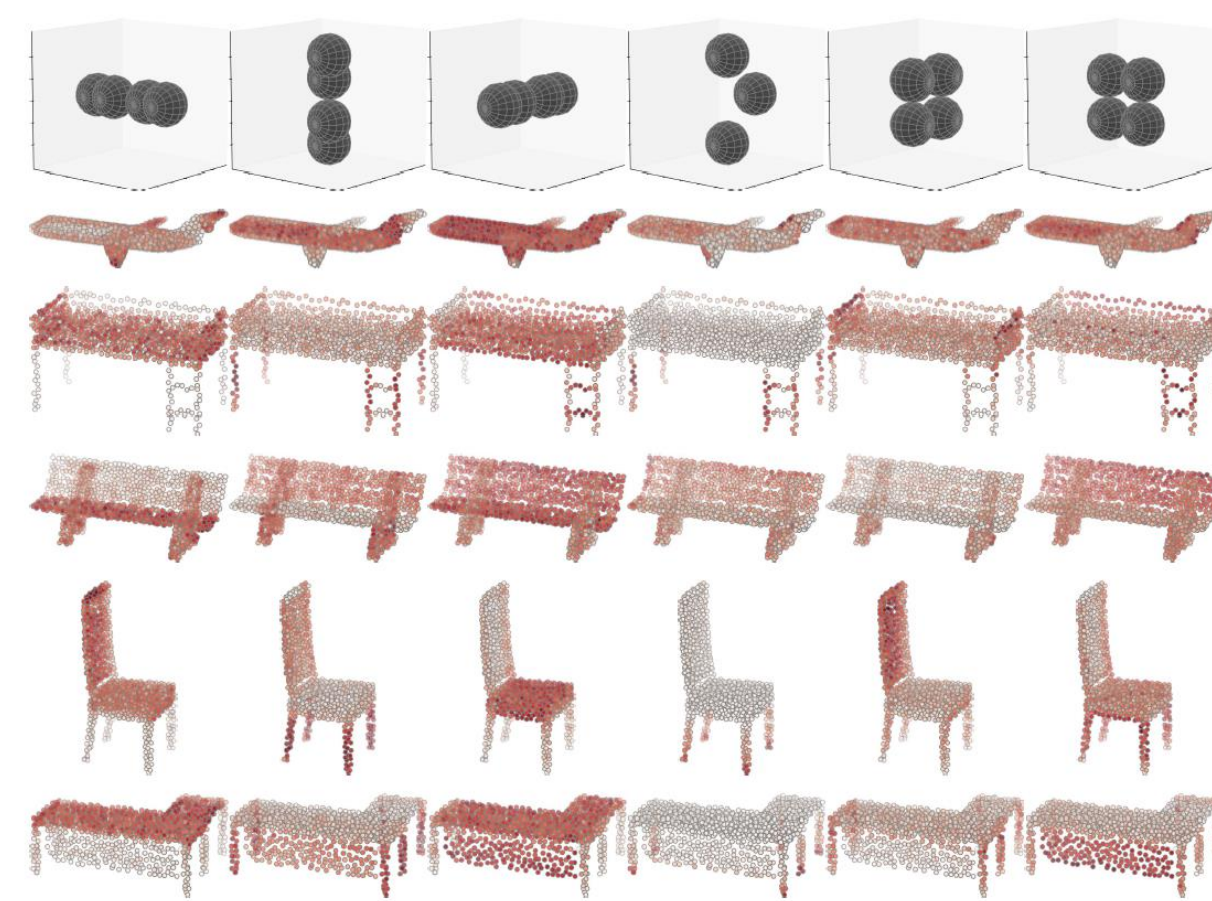
We used graph max pooling to each point within its neighborhood to improve feature robustness against noises.

$$Y(i, k) = \max_{n \in N(i)} X(n, k),$$

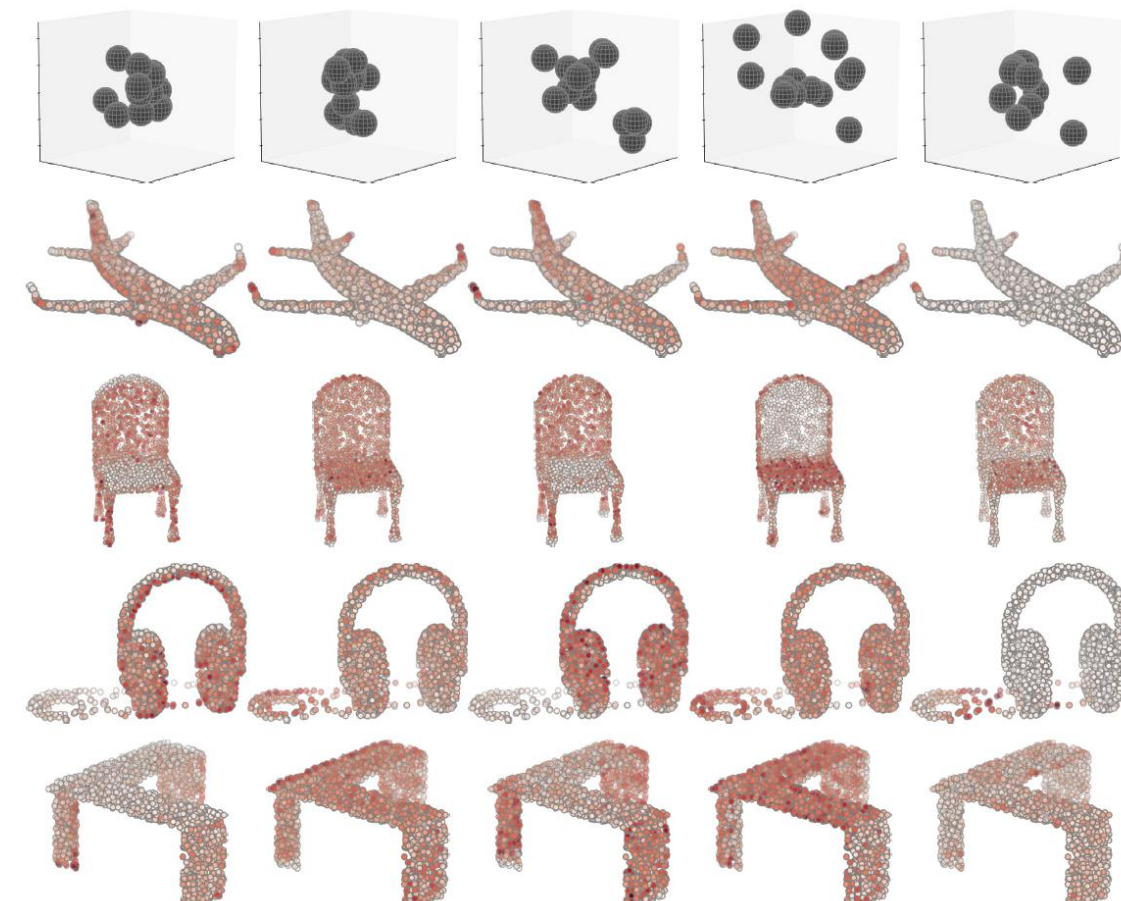
where  $Y \in R^{N \times K}$  and  $X \in R^{N \times K}$ .

## Visualization

### Handcrafted Kernels & Responses



### Learned Kernels & Responses



### ShapeNet Part Segmentation

GT	PointNet	Ours	GT	PointNet	Ours	GT	PointNet	Ours
	42.3%	96.8%		69.6%	83.1%		59.3%	72.1%
	68.5%	82.3%		70.8%	83.8%		61.4%	79.0%
	76.5%	78.3%		59.5%	66.9%		63.5%	82.8%
	48.4%	93.6%		55.8%	90.6%		84.6%	94.9%
	88.8%	96.8%		64.0%	67.9%		84.1%	91.5%
	48.7%	57.9%		89.9%	92.8%		59.2%	93.4%
	58.2%	65.4%		63.2%	68.8%		82.7%	90.4%
	68.5%	74.0%		90.8%	93.2%		39.8%	59.1%
	77.2%	91.6%		69.4%	94.3%		40.2%	53.9%

## Experimental Results

### 2D Digit Classification

Method	Accuracy (%)
LeNet5 [21]	99.2
PointNet (vanilla) [29]	98.7
PointNet [29]	99.2
PointNet++ [31]	<b>99.5</b>
KCNet (ours)	99.3

Table 1:  
Non-zero pixels in images from MNIST are converted to 2D point clouds.

### 3D Shape Classification

Method	MN10	MN40
MVCNN [36]	-	90.1
VRN Ensemble [2]	<b>97.1</b>	<b>95.5</b>
ECC [34]	90.0	83.2
PointNet (vanilla) [29]	-	87.2
PointNet [29]	-	89.2
PointNet++ [31]	-	90.7
Kd-Net(depth 10) [20]	93.3	90.6
Kd-Net(depth 15) [20]	94.0	91.8
KCNet (ours)	94.4	91.0

Table 2:  
Results on ModelNet.

### 3D Part Segmentation

	Cat. mIoU	Ins. mIoU	aero	bag	cap	car	chair	ear phone	guitar	knife	lamp	laptop	motor	mug	pistol	rocket	skate board	table
# shapes			2690	76	55	898	3758	69	787	392	1547	451	202	184	283	66	152	5271
PointNet	80.4	83.7	<b>83.4</b>	78.7	82.5	74.9	89.6	73.0	<b>91.5</b>	85.9	80.8	95.3	65.2	93.0	81.2	57.9	72.8	80.6
PointNet++	81.9	<b>85.1</b>	82.4	79.0	<b>87.7</b>	77.3	<b>90.8</b>	71.8	91.0	85.9	83.7	95.3	<b>71.6</b>	94.1	81.3	58.7	<b>76.4</b>	<b>82.6</b>
Kd-Net	77.4	82.3	80.1	74.6	74.3	70.3	88.6	73.5	90.2	<b>87.2</b>	81.0	94.9	57.4	86.7	78.1	51.8	69.9	80.3
KCNet (ours)	<b>82.2</b>	84.7	82.8	<b>81.5</b>	86.4	<b>77.6</b>	90.3	<b>76.8</b>	91.0	<b>87.2</b>	<b>84.5</b>	<b>95.5</b>	69.2	<b>94.4</b>	<b>81.6</b>	<b>60.1</b>	75.2	81.3

Table 3: Part segmentation on ShapeNet. Average mIoU over instances (Ins.) and categories (Cat.) are reported.

## Analysis Experiments

### Robustness Test

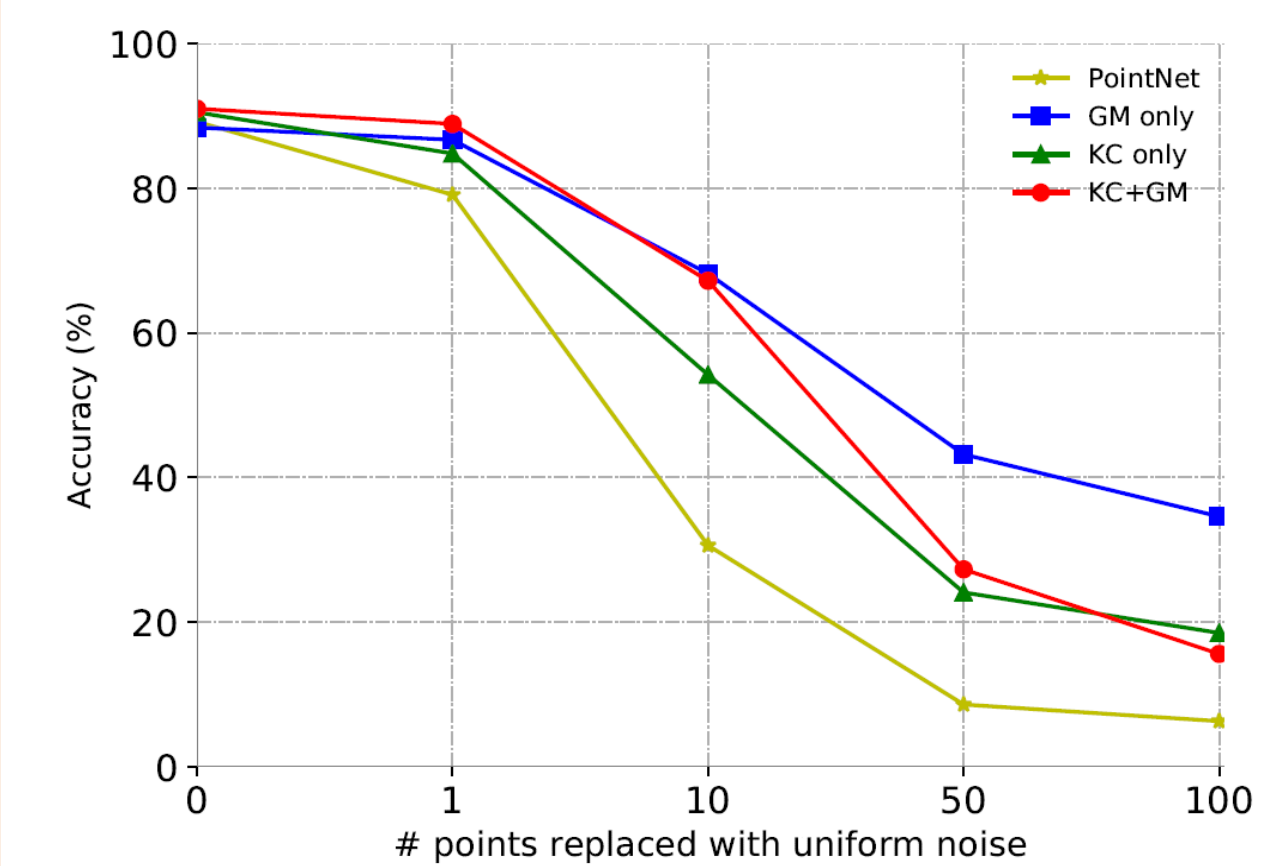


Figure 1: #points replaced with uniform noise between [-1,1].  
GM only: graph max pooling only.  
KC only: kernel correlation only.  
KC+GM: both.

### Ablation Study

Effectiveness of Kernel Correlation	Accuracy (%)
Normal	88.4
Kernel correlation	<b>90.5</b>
Symmetric Functions	Accuracy (%)
Graph average pooling	88.0
Graph max pooling	<b>88.6</b>
Effectiveness of Local Structures	Accuracy (%)
Baseline: PointNet (vanilla)	87.2
Kernel correlation (geometric)	90.5
Graph max pooling (feature)	88.6
Both	<b>91.0</b>

### Model Size & Time

Method	#params (M)	Fwd. time (ms)
PointNet(vanilla) [31]	<b>0.8</b>	<b>11.6</b>
PointNet [31]	3.5	25.3
PointNet++(MSG) [31]	1.0	163.2
Kd-Net (depth 10)	2.0	-
KCNet (M = 16)	0.9	18.5
KCNet (M = 3)	0.9	12.0

### Hyper-parameters

L	Acc. (%)	M	Acc. (%)	$\sigma$	Acc. (%)
16	90.7	3	90.9	1e-3	90.0
<b>32</b>	<b>91.0</b>	8	90.4	<b>5e-3</b>	<b>91.0</b>
48	91.0	<b>16</b>	<b>91.0</b>	1e-2	90.4