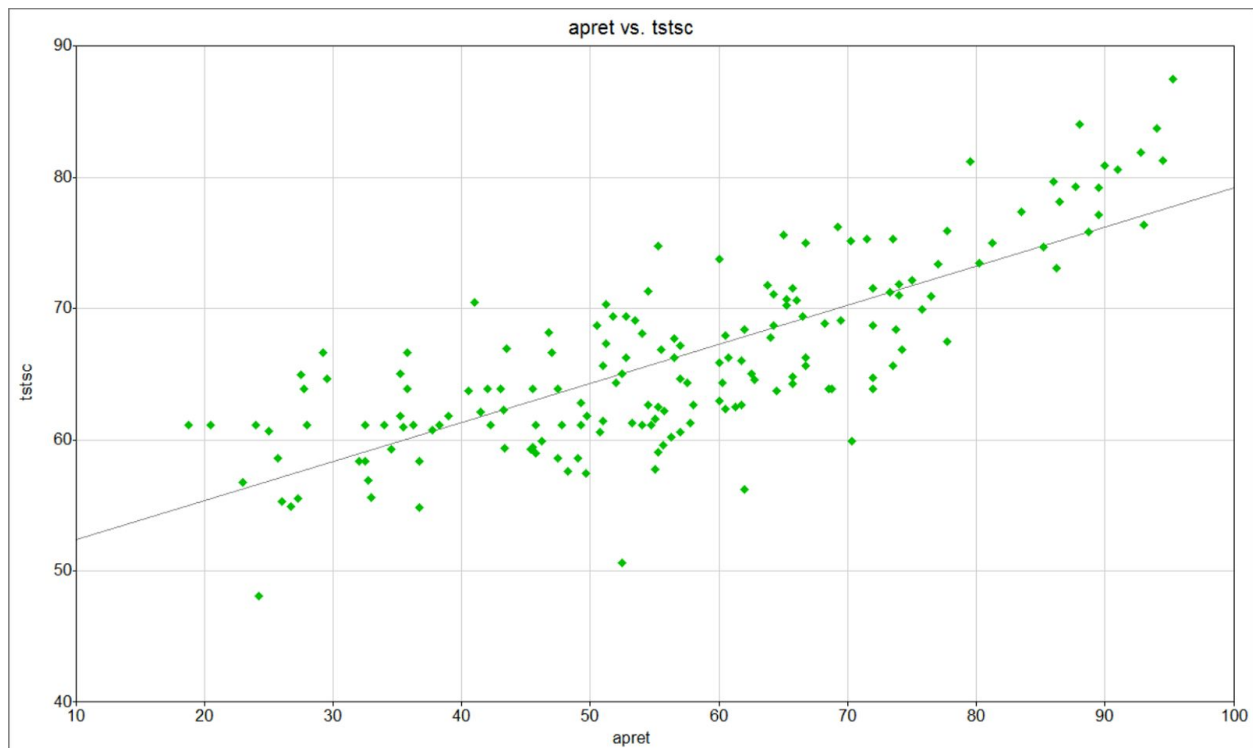


Assignment 5: Causal Relationship Discovery

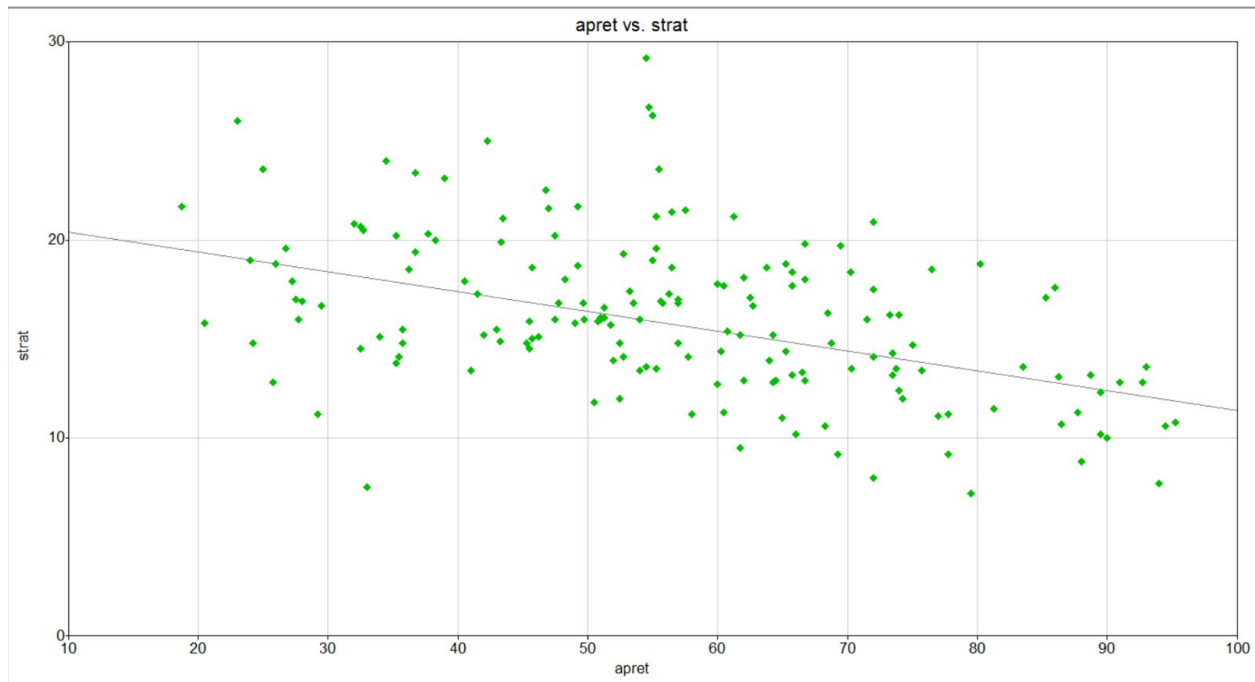
Zhaoyan Ai (zha4), Ja-jan Hsu (jah247), Leilei Liu (lel74)

In the article, the two authors tried to find out the reasons for low freshman retention rate in US colleges. One apparently robust finding in this article is that student retention is directly related to the average test scores and high school class standing of the incoming freshmen.

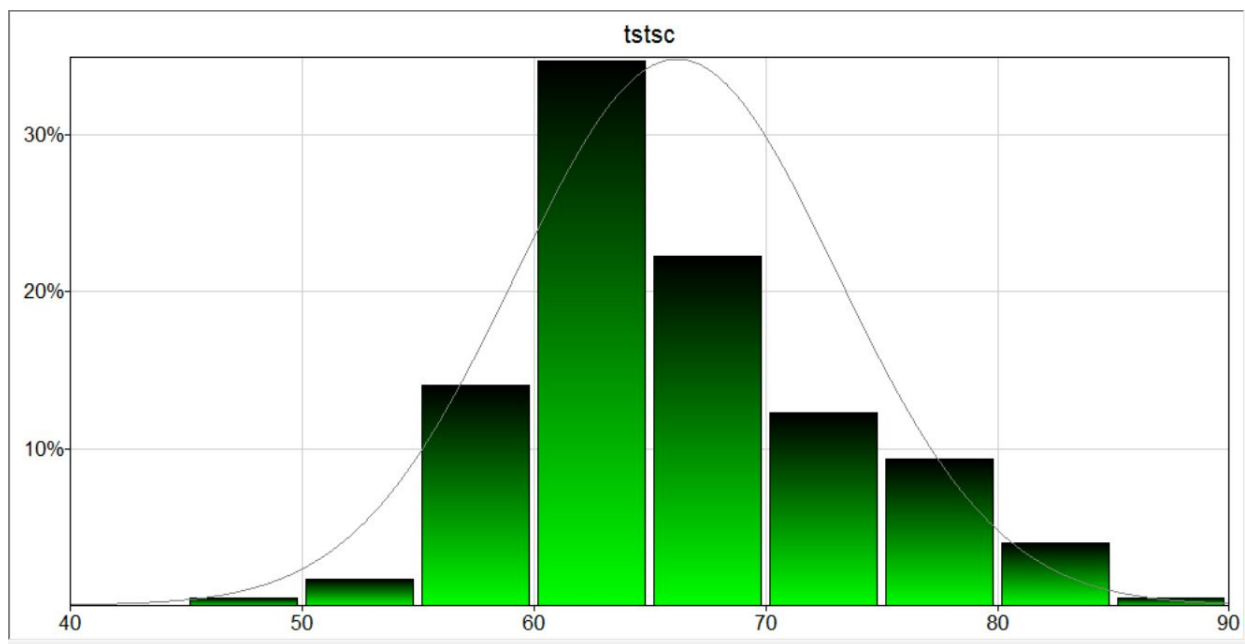
As we can see from the directed acyclic graph (DAG), both *tstsc* (test score) and *strat* (student teacher ratio) are parents of *apret* (average retention rate). Here we first plotted *apret* vs. *tstsc* and it is obvious that there is a linear relationship between *apret* and *tstsc*, though this relationship is not very strong.

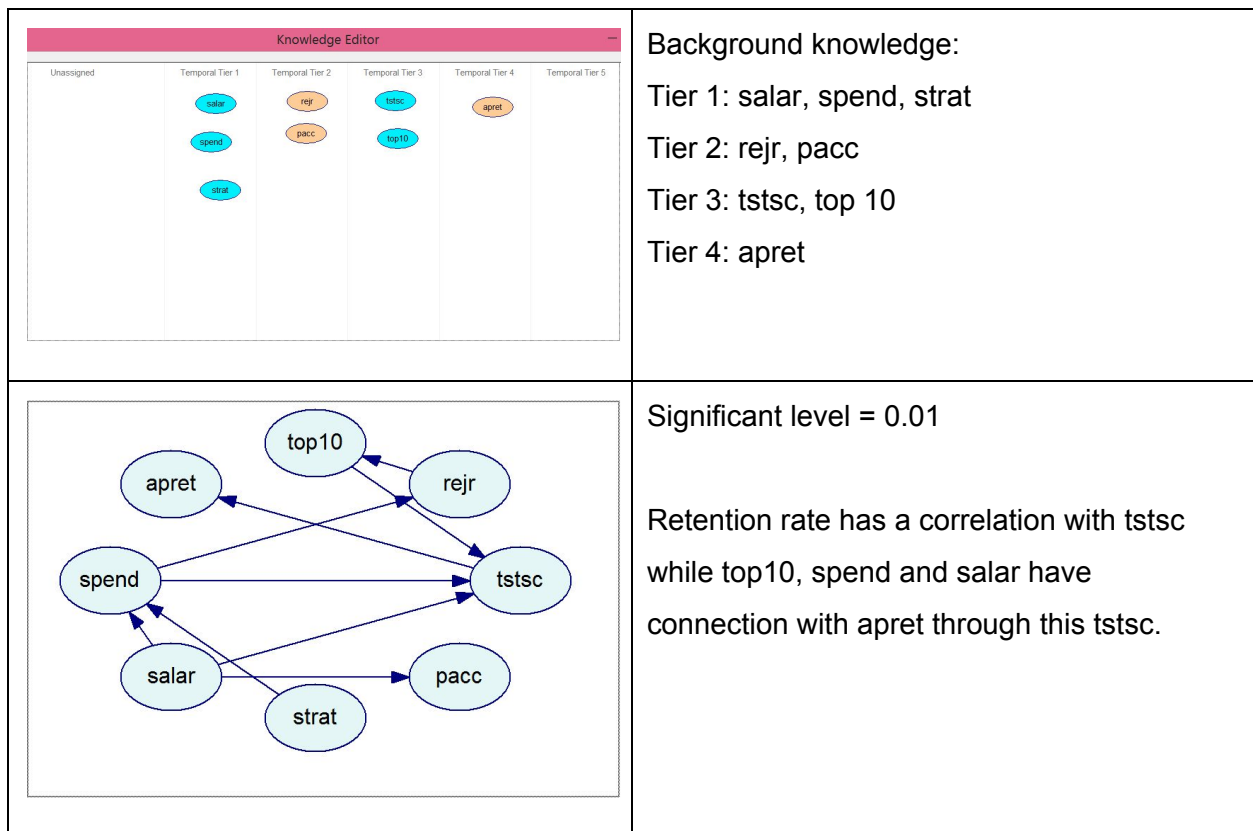
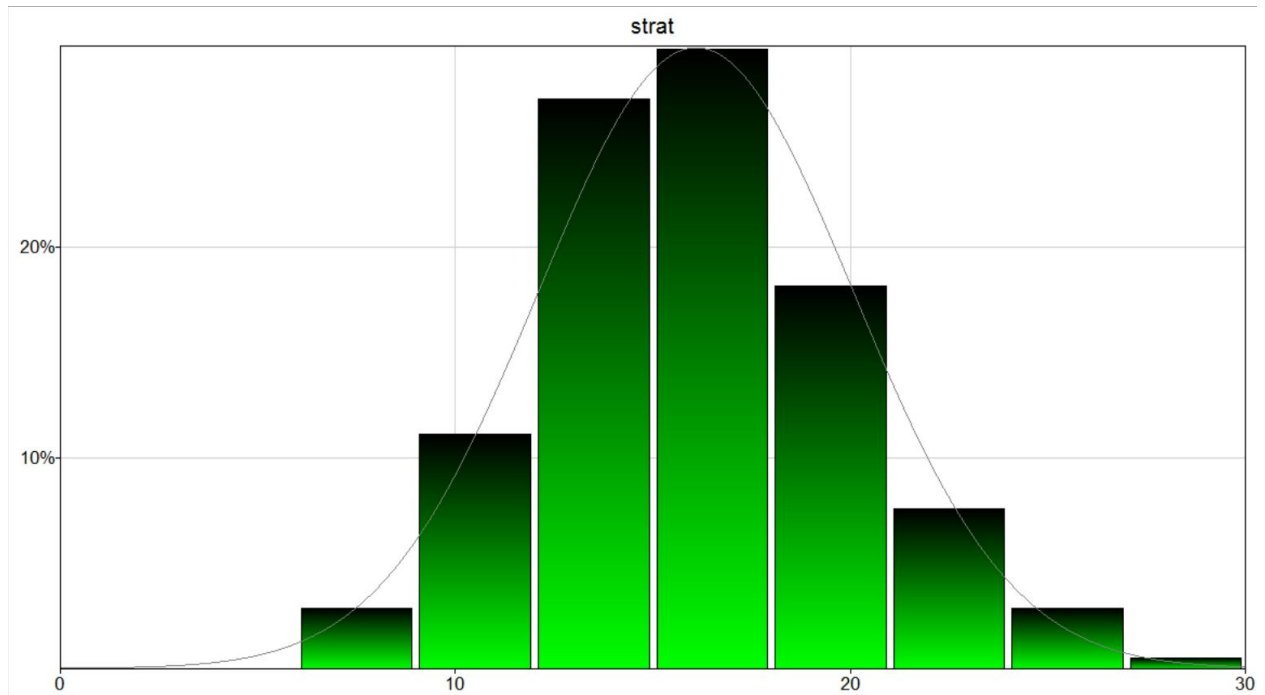


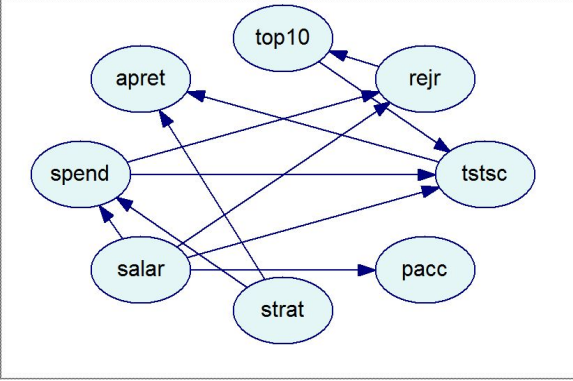
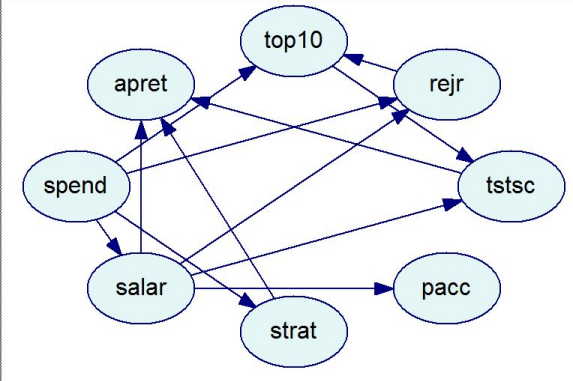
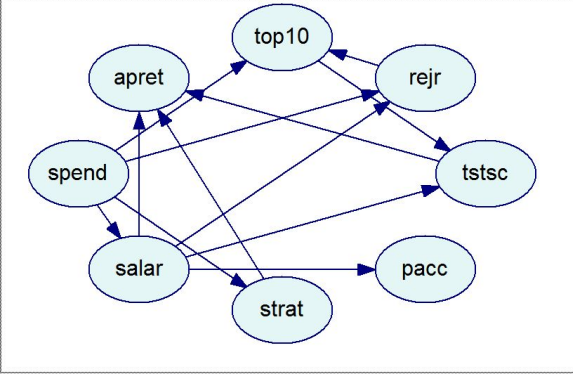
There also seems to be a linear relationship between *apret* and *strat* as illustrated by the plot, this relationship is not as strong as that of *apret* vs. *tstsc*.



Further investigation into the distribution of tstsc and strat led to the observation that tstsc is slightly skewed-right while strat appears to more normal distributed. (Normal fit is displayed in both histograms)





	<p>Significant level = 0.05</p> <p>Retention rate has a correlation with tstsc and strat while top10, spend and salar have connection with apret through these two attributes.</p>
	<p>Significant level = 0.1</p> <p>Retention rate has a correlation with tstsc, salar and strat while only spend and top 10 have connection with apret through salar/tstsc.</p>
	<p>Significant level = 0.15</p> <p>Retention rate has a correlation with tstsc, salar and strat while only spend and top 10 have connection with apret through salar/tstsc.</p>

From the four graph, we can conclude that as the significant level increases, apret has more and more parent nodes. When significant level is only 0.01, tstsc is the only possible cause of apret while as significant level increases to 0.05 and 0.1, strat and salar comes into play. We might infer that tstsc has a stronger relationship with apret than strat and then salar. No matter what the significant level is, top10 is always leading to tstsc, so we may infer that top10 is a non-negligible influencing factor.