fc nets ipynb

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1 Fully connected networks

In the previous notebook, you implemented a simple two-layer neural network class. However, this class is not modular. If you wanted to change the number of layers, you would need to write a new loss and gradient function. If you wanted to optimize the network with different optimizers, you'd need to write new training functions. If you wanted to incorporate regularizations, you'd have to modify the loss and gradient function.

Instead of having to modify functions each time, for the rest of the class, we'll work in a more modular framework where we define forward and backward layers that calculate losses and gradients respectively. Since the forward and backward layers share intermediate values that are useful for calculating both the loss and the gradient, we'll also have these function return "caches" which store useful intermediate values.

The goal is that through this modular design, we can build different sized neural networks for various applications.

In this HW #3, we'll define the basic architecture, and in HW #4, we'll build on this framework to implement different optimizers and regularizations (like BatchNorm and Dropout).

1.1 Modular layers

This notebook will build modular layers in the following manner. First, there will be a forward pass for a given layer with inputs (x) and return the output of that layer (out) as well as cached variables (cache) that will be used to calculate the gradient in the backward pass.

def layer_forward(x, w):

```
""" Receive inputs x and weights w """
# Do some computations ...
z = # ... some intermediate value
# Do some more computations ...
out = # the output

cache = (x, w, z, out) # Values we need to compute gradients
return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
      Receive derivative of loss with respect to outputs and cache,
      and compute derivative with respect to inputs.
      11 11 11
      # Unpack cache values
      x, w, z, out = cache
      # Use values in cache to compute derivatives
      dx = # Derivative of loss with respect to x
      dw = # Derivative of loss with respect to w
      return dx, dw
[]: ## Import and setups
     import time
     import numpy as np
     import matplotlib.pyplot as plt
     from nndl.fc_net import *
     from utils.data_utils import get_CIFAR10_data
     from utils.gradient_check import eval_numerical_gradient,_
      ⇒eval_numerical_gradient_array
     from utils.solver import Solver
     %matplotlib inline
     plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
     plt.rcParams['image.interpolation'] = 'nearest'
     plt.rcParams['image.cmap'] = 'gray'
     # for auto-reloading external modules
     # see http://stackoverflow.com/questions/1907993/
      \rightarrow autoreload-of-modules-in-ipython
     %load ext autoreload
     %autoreload 2
     def rel_error(x, y):
       """ returns relative error """
       return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
[]: # Load the (preprocessed) CIFAR10 data.
     data = get_CIFAR10_data()
     for k in data.keys():
       print('{}: {} '.format(k, data[k].shape))
    X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
```

```
y_val: (1000,)
X_test: (1000, 3, 32, 32)
y_test: (1000,)
```

1.2 Linear layers

In this section, we'll implement the forward and backward pass for the linear layers.

The linear layer forward pass is the function affine_forward in nndl/layers.py and the backward pass is affine_backward.

After you have implemented these, test your implementation by running the cell below.

1.2.1 Affine layer forward pass

Implement affine_forward and then test your code by running the following cell.

```
[]: # Test the affine forward function
     num_inputs = 2
     input\_shape = (4, 5, 6)
     output_dim = 3
     input_size = num_inputs * np.prod(input_shape)
     weight_size = output_dim * np.prod(input_shape)
     x = np.linspace(-0.1, 0.5, num=input_size).reshape(num_inputs, *input_shape)
     w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_shape),_
      →output_dim)
     b = np.linspace(-0.3, 0.1, num=output_dim)
     out, _ = affine_forward(x, w, b)
     correct_out = np.array([[ 1.49834967, 1.70660132, 1.91485297],
                             [ 3.25553199, 3.5141327, 3.77273342]])
     # Compare your output with ours. The error should be around 1e-9.
     print('Testing affine_forward function:')
     print('difference: {}'.format(rel_error(out, correct_out)))
```

Testing affine_forward function: difference: 9.7698500479884e-10

1.2.2 Affine layer backward pass

Implement affine backward and then test your code by running the following cell.

```
[]: # Test the affine_backward function

x = np.random.randn(10, 2, 3)
w = np.random.randn(6, 5)
```

```
b = np.random.randn(5)
dout = np.random.randn(10, 5)

dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0], x,u dout)

dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0], w,u dout)

db_num = eval_numerical_gradient_array(lambda b: affine_forward(x, w, b)[0], b,u dout)

_, cache = affine_forward(x, w, b)

dx, dw, db = affine_backward(dout, cache)

# The error should be around 1e-10

print('Testing affine_backward function:')

print('dx error: {}'.format(rel_error(dx_num, dx)))

print('dw error: {}'.format(rel_error(dw_num, dw)))

print('db error: {}'.format(rel_error(db_num, db)))
```

Testing affine_backward function: dx error: 8.845861628974646e-10

dw error: 4.405537926313691e-10 db error: 1.531984065068008e-11

1.3 Activation layers

In this section you'll implement the ReLU activation.

1.3.1 ReLU forward pass

Implement the relu_forward function in nndl/layers.py and then test your code by running the following cell.

Testing relu_forward function: difference: 4.999999798022158e-08

1.3.2 ReLU backward pass

Implement the relu_backward function in nndl/layers.py and then test your code by running the following cell.

```
[]: x = np.random.randn(10, 10)
dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be around 1e-12
print('Testing relu_backward function:')
print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Testing relu_backward function: dx error: 3.2756144884343895e-12

1.4 Combining the affine and ReLU layers

Often times, an affine layer will be followed by a ReLU layer. So let's make one that puts them together. Layers that are combined are stored in nndl/layer utils.py.

1.4.1 Affine-ReLU layers

We've implemented affine_relu_forward() and affine_relu_backward in nndl/layer_utils.py. Take a look at them to make sure you understand what's going on. Then run the following cell to ensure its implemented correctly.

```
[]: from nndl.layer_utils import affine_relu_forward, affine_relu_backward

x = np.random.randn(2, 3, 4)
w = np.random.randn(12, 10)
b = np.random.randn(10)
dout = np.random.randn(2, 10)

out, cache = affine_relu_forward(x, w, b)
dx, dw, db = affine_relu_backward(dout, cache)

dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w, b))[0], x, dout)
dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w, b))[0], w, dout)
db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w, b))[0], b, dout)

print('Testing affine_relu_forward and affine_relu_backward:')
```

```
print('dx error: {}'.format(rel_error(dx_num, dx)))
print('dw error: {}'.format(rel_error(dw_num, dw)))
print('db error: {}'.format(rel_error(db_num, db)))
```

Testing affine_relu_forward and affine_relu_backward:

dx error: 1.0361713691913885e-10 dw error: 1.3235761825149517e-10 db error: 3.2756031511796114e-12

1.5 Softmax loss

You've already implemented it, so we have written it in layers.py. The following code will ensure they are working correctly.

Testing softmax_loss: loss: 2.3024541667232965 dx error: 8.740178208266035e-09

1.6 Implementation of a two-layer NN

In nndl/fc_net.py, implement the class TwoLayerNet which uses the layers you made here. When you have finished, the following cell will test your implementation.

```
[]: N, D, H, C = 3, 5, 50, 7
X = np.random.randn(N, D)
y = np.random.randint(C, size=N)

std = 1e-2
model = TwoLayerNet(input_dim=D, hidden_dims=H, num_classes=C, weight_scale=std)

print('Testing initialization ... ')
W1_std = abs(model.params['W1'].std() - std)
```

```
b1 = model.params['b1']
W2_std = abs(model.params['W2'].std() - std)
b2 = model.params['b2']
assert W1_std < std / 10, 'First layer weights do not seem right'
assert np.all(b1 == 0), 'First layer biases do not seem right'
assert W2_std < std / 10, 'Second layer weights do not seem right'</pre>
assert np.all(b2 == 0), 'Second layer biases do not seem right'
print('Testing test-time forward pass ... ')
model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
scores = model.loss(X)
correct_scores = np.asarray(
  [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.
 →33206765, 16.09215096],
   [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.
 →49994135, 16.18839143],
   [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.
 →66781506, 16.2846319 ]])
scores diff = np.abs(scores - correct scores).sum()
assert scores_diff < 1e-6, 'Problem with test-time forward pass'
print('Testing training loss (no regularization)')
y = np.asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct loss = 3.4702243556
assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time loss'
model.reg = 1.0
loss, grads = model.loss(X, y)
correct_loss = 26.5948426952
assert abs(loss - correct_loss) < 1e-10, 'Problem with regularization loss'</pre>
for reg in [0.0, 0.7]:
 print('Running numeric gradient check with reg = {}'.format(reg))
 model.reg = reg
 loss, grads = model.loss(X, y)
 for name in sorted(grads):
   f = lambda _: model.loss(X, y)[0]
   grad_num = eval_numerical_gradient(f, model.params[name], verbose=False)
   print('{} relative error: {}'.format(name, rel_error(grad_num,_
 ⇔grads[name])))
```

```
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.2236151215593397e-08
W2 relative error: 3.3429539606923665e-10
b1 relative error: 4.7288944058018464e-09
b2 relative error: 4.3291285233961314e-10
Running numeric gradient check with reg = 0.7
W1 relative error: 3.1196421170137957e-07
W2 relative error: 7.976669724128995e-08
b1 relative error: 1.3467621663681023e-08
b2 relative error: 7.759087852670534e-10
b2 relative error: 7.759087852670534e-10
```

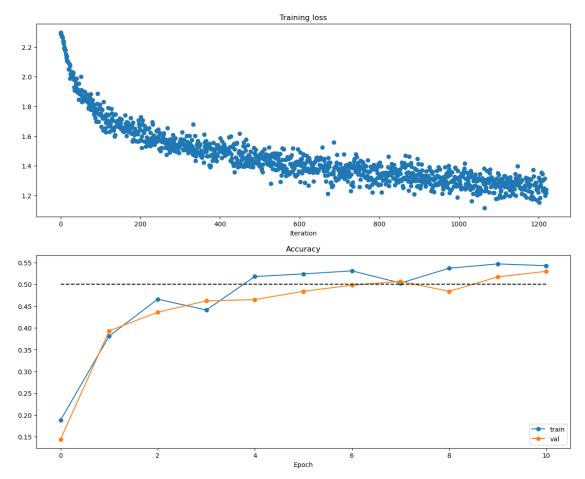
1.7 Solver

We will now use the utils Solver class to train these networks. Familiarize yourself with the API in utils/solver.py. After you have done so, declare an instance of a TwoLayerNet with 200 units and then train it with the Solver. Choose parameters so that your validation accuracy is at least 50%.

```
[]: model = TwoLayerNet()
    solver = None
    # YOUR CODE HERE:
      Declare an instance of a TwoLayerNet and then train
    # it with the Solver. Choose hyperparameters so that your validation
    # accuracy is at least 50%. We won't have you optimize this further
        since you did it in the previous notebook.
    # ----- #
    model = TwoLayerNet(hidden_dims = 200)
    X_train, y_train = data['X_train'], data['y_train']
    X_val, y_val = data['X_val'], data['y_val']
    X_test, y_test = data['X_test'], data['y_test']
    best_lr = 0.001
    best_bat_size = 400
    best num ite = 2000
    best_reg = 0.3
    mydata = {
          'X_train': X_train, # training data
          'y_train': y_train,# training labels
          'X_val': X_val, # validation data
          'y val': y val# validation labels
    # model = TwoLayerNet(hidden_size=100, req=best_req)
```

```
solver = Solver(model, mydata,
                       update_rule='sgd',
                       optim_config={
                         'learning_rate': best_lr,
                       },
                       lr_decay=0.95,
                       num_epochs=10, batch_size=best_bat_size,
                       print_every=100)
    solver.train()
    pass
    # ----- #
    # END YOUR CODE HERE
    (Iteration 1 / 1220) loss: 2.298761
    (Epoch 0 / 10) train acc: 0.188000; val acc: 0.144000
    (Iteration 101 / 1220) loss: 1.786055
    (Epoch 1 / 10) train acc: 0.381000; val acc: 0.393000
    (Iteration 201 / 1220) loss: 1.573889
    (Epoch 2 / 10) train acc: 0.466000; val acc: 0.436000
    (Iteration 301 / 1220) loss: 1.546084
    (Epoch 3 / 10) train acc: 0.441000; val_acc: 0.462000
    (Iteration 401 / 1220) loss: 1.510700
    (Epoch 4 / 10) train acc: 0.518000; val_acc: 0.465000
    (Iteration 501 / 1220) loss: 1.478797
    (Iteration 601 / 1220) loss: 1.429531
    (Epoch 5 / 10) train acc: 0.524000; val acc: 0.484000
    (Iteration 701 / 1220) loss: 1.339706
    (Epoch 6 / 10) train acc: 0.531000; val acc: 0.498000
    (Iteration 801 / 1220) loss: 1.340428
    (Epoch 7 / 10) train acc: 0.503000; val_acc: 0.507000
    (Iteration 901 / 1220) loss: 1.297518
    (Epoch 8 / 10) train acc: 0.537000; val_acc: 0.484000
    (Iteration 1001 / 1220) loss: 1.311881
    (Epoch 9 / 10) train acc: 0.547000; val_acc: 0.517000
    (Iteration 1101 / 1220) loss: 1.339683
    (Iteration 1201 / 1220) loss: 1.318799
    (Epoch 10 / 10) train acc: 0.543000; val_acc: 0.530000
[]: # Run this cell to visualize training loss and train / val accuracy
    plt.subplot(2, 1, 1)
    plt.title('Training loss')
    plt.plot(solver.loss_history, 'o')
    plt.xlabel('Iteration')
```

```
plt.subplot(2, 1, 2)
plt.title('Accuracy')
plt.plot(solver.train_acc_history, '-o', label='train')
plt.plot(solver.val_acc_history, '-o', label='val')
plt.plot([0.5] * len(solver.val_acc_history), 'k--')
plt.xlabel('Epoch')
plt.legend(loc='lower right')
plt.gcf().set_size_inches(15, 12)
plt.show()
```



1.8 Multilayer Neural Network

Now, we implement a multi-layer neural network.

Read through the FullyConnectedNet class in the file nndl/fc_net.py.

Implement the initialization, the forward pass, and the backward pass. There will be lines for batchnorm and dropout layers and caches; ignore these all for now. That'll be in HW #4.

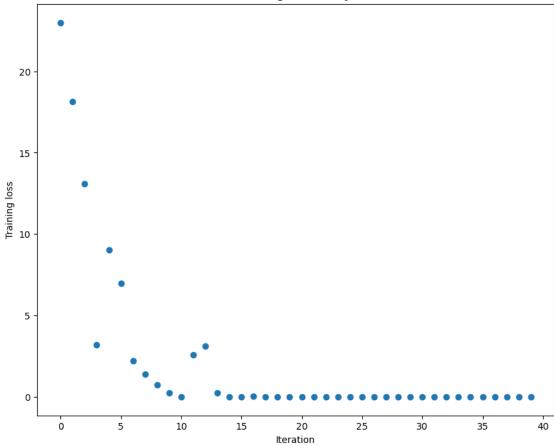
```
[]: N, D, H1, H2, C = 2, 15, 20, 30, 10
     X = np.random.randn(N, D)
     y = np.random.randint(C, size=(N,))
     for reg in [0, 3.14]:
       print('Running check with reg = {}'.format(reg))
       model = FullyConnectedNet([H1, H2], input_dim=D, num_classes=C,
                                 reg=reg, weight_scale=5e-2, dtype=np.float64)
       loss, grads = model.loss(X, y)
       print('Initial loss: {}'.format(loss))
       for name in sorted(grads):
         f = lambda _: model.loss(X, y)[0]
         grad_num = eval_numerical_gradient(f, model.params[name], verbose=False,_
      \rightarrowh=1e-5)
         print('{} relative error: {}'.format(name, rel_error(grad_num,__

¬grads[name])))
    Running check with reg = 0
    Initial loss: 2.2386625318598483
    W1 relative error: 4.591955823949023e-08
    W2 relative error: 1.1142544919980604e-07
    W3 relative error: 8.727606850444996e-08
    b1 relative error: 1.5861303017086138e-09
    b2 relative error: 3.470836247759264e-10
    b3 relative error: 9.392121566378062e-11
    Running check with reg = 3.14
    Initial loss: 509.957466505932
    W1 relative error: 4.957414338464139e-07
    W2 relative error: 8.487616752528423e-06
    W3 relative error: 3.0690488903966404e-07
    b1 relative error: 7.902554834430548e-08
    b2 relative error: 7.77362582871271e-08
    b3 relative error: 1.3738787948178761e-08
[]: # Use the three layer neural network to overfit a small dataset.
     num_train = 50
     small data = {
       'X_train': data['X_train'][:num_train],
      'y_train': data['y_train'][:num_train],
       'X_val': data['X_val'],
       'y_val': data['y_val'],
     }
```

```
#### !!!!!!
# Play around with the weight scale and learning rate so that you can overfit au
 ⇔small dataset.
# Your training accuracy should be 1.0 to receive full credit on this part.
weight scale = 1e-2
learning rate = 1e-4
model = FullyConnectedNet([100, 100],
              weight_scale=weight_scale, dtype=np.float64)
solver = Solver(model, small_data,
                print_every=10, num_epochs=20, batch_size=25,
                update_rule='sgd',
                optim_config={
                   'learning_rate': learning_rate,
solver.train()
plt.plot(solver.loss history, 'o')
plt.title('Training loss history')
plt.xlabel('Iteration')
plt.ylabel('Training loss')
plt.show()
(Iteration 1 / 40) loss: 22.997194
(Epoch 0 / 20) train acc: 0.300000; val acc: 0.130000
(Epoch 1 / 20) train acc: 0.500000; val acc: 0.127000
(Epoch 2 / 20) train acc: 0.580000; val_acc: 0.130000
(Epoch 3 / 20) train acc: 0.760000; val_acc: 0.138000
(Epoch 4 / 20) train acc: 0.920000; val_acc: 0.163000
(Epoch 5 / 20) train acc: 0.940000; val_acc: 0.187000
(Iteration 11 / 40) loss: 0.000828
(Epoch 6 / 20) train acc: 0.880000; val_acc: 0.158000
(Epoch 7 / 20) train acc: 0.980000; val_acc: 0.179000
(Epoch 8 / 20) train acc: 0.980000; val_acc: 0.178000
(Epoch 9 / 20) train acc: 1.000000; val_acc: 0.176000
(Epoch 10 / 20) train acc: 1.000000; val_acc: 0.177000
(Iteration 21 / 40) loss: 0.002572
(Epoch 11 / 20) train acc: 1.000000; val_acc: 0.176000
(Epoch 12 / 20) train acc: 1.000000; val acc: 0.176000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.176000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.176000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.176000
(Iteration 31 / 40) loss: 0.001593
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.178000
(Epoch 17 / 20) train acc: 1.000000; val_acc: 0.177000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.178000
```

(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.178000 (Epoch 20 / 20) train acc: 1.000000; val_acc: 0.178000





[]: