



*Modeling III*

# Introduction



- Instructions
  - Download Tutorial 12 Zip
  - Unzip Folder
  - Required Packages
    - `library(tidyverse)`
    - `library(modelr)`
    - `library(xtable)`
  - Open .Rmd File and Knit
- Within R, Run all Code Chunks for Parts 1,2, and 3 (This was Covered in Tutorial 11)

## Part 4: Logistic Model



- Logistic Model

$$W = l + \frac{h}{1 + e^{a - bA}} + \varepsilon$$

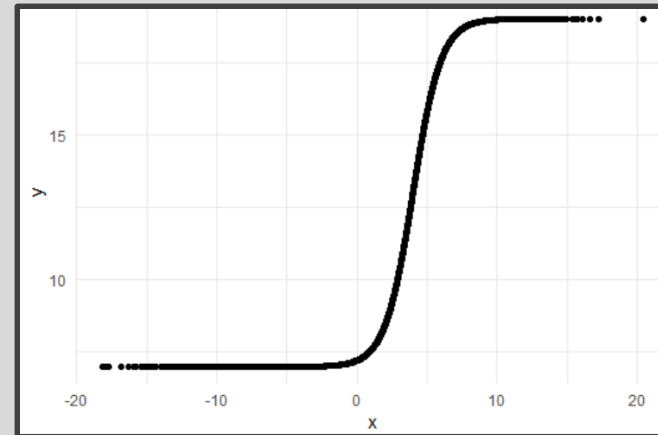
- “Smart” Model Based On Physical Relationship Between A and W
- Four Parameters
  - Controls the Shape of the Relationship
  - $l$  and  $h$
  - $a$  and  $b$
- What Shape Do You Think This Function Makes?
  - Idea: Precalculus

## Part 4: Logistic Model



- Run Chunk 1

- Plant that Seed
- Example Model



- Parameter Investigation
  - What Does 7 Represent?
  - What Does 12 Represent?
  - What Does 4 Represent?
  - What Does 1 Represent?

## Part 4: Logistic Model



- Run Chunk 2
  - Creation of Modeling Function
  - Creation of MSE Function Specific to this Model
- Run Chunk 3
  - Use `optim()` Function With Smart Starting Values Based on Understanding of The Model
  - Finds Estimates Based on Minimization of MSE

## Part 4: Logistic Model



- Run Chunk 4
  - Use Logistic Model Function and Estimated Parameters from `optim()` to Obtain
    - Predictions
    - Residuals

## Intermission

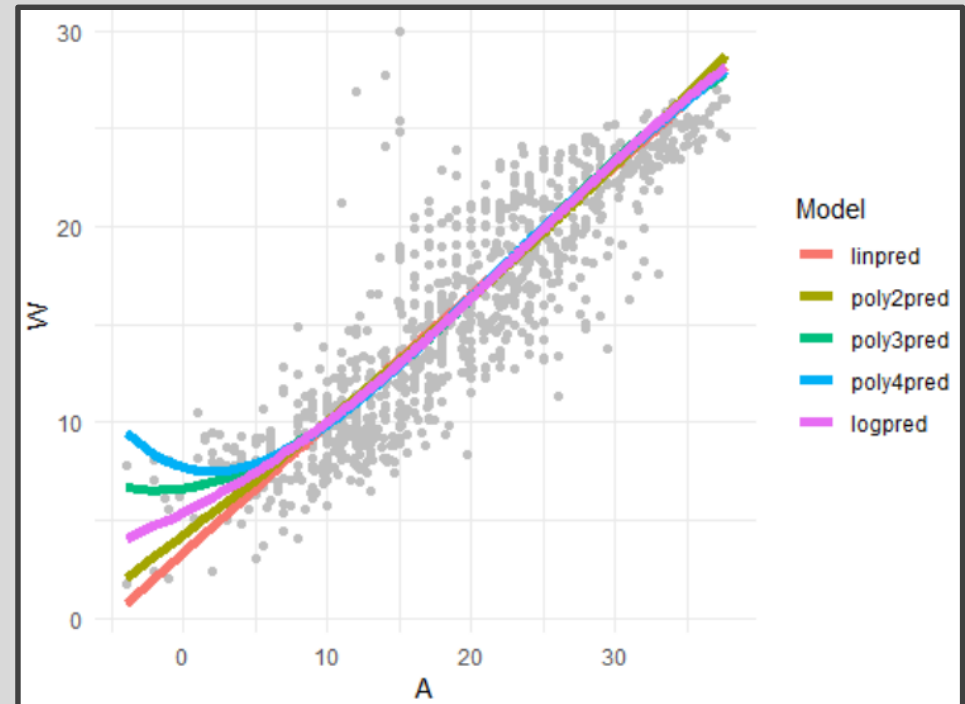


- Run Code Chunk
  - `save.image()` = Used to Save Workspace into .Rdata File
  - `load()` = Used to Load Workspace from .Rdata File
  - .Rdata = File Extension of R Workspace File (All Objects in Global Environment)

## Part 5: Evaluation by Visualization



- Run Chunk 1
  - Plots of Different Models
  - What Can We Say About the Different Models?



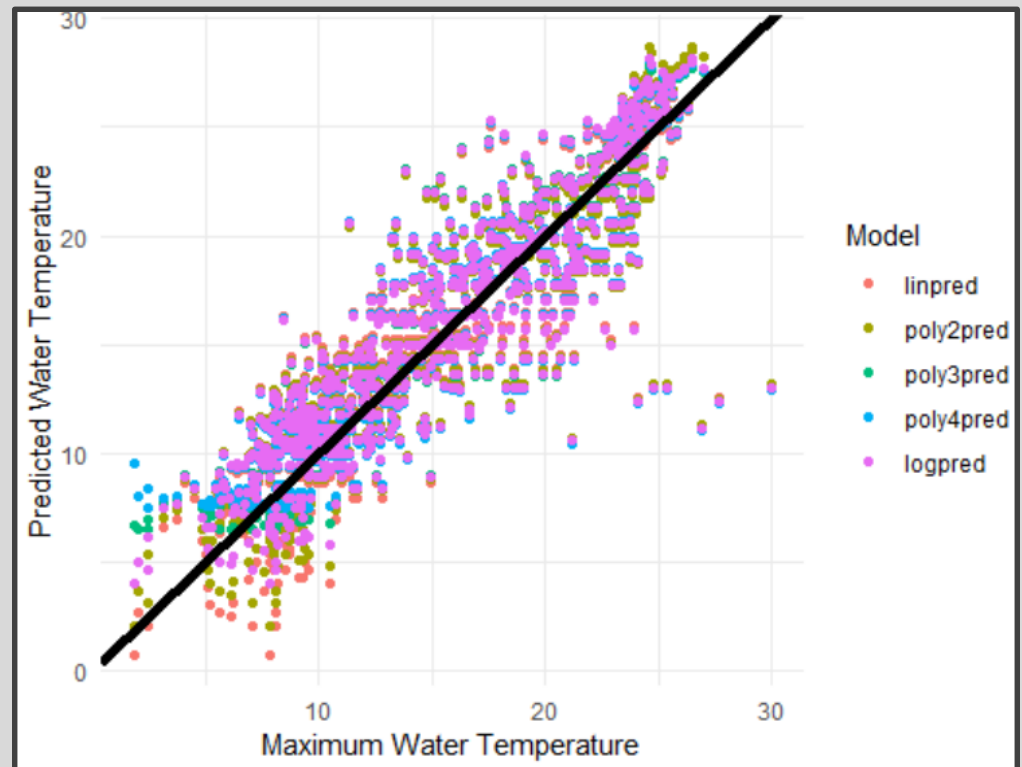
- Which Model Would You Use?



## Part 5: Evaluation by Visualization



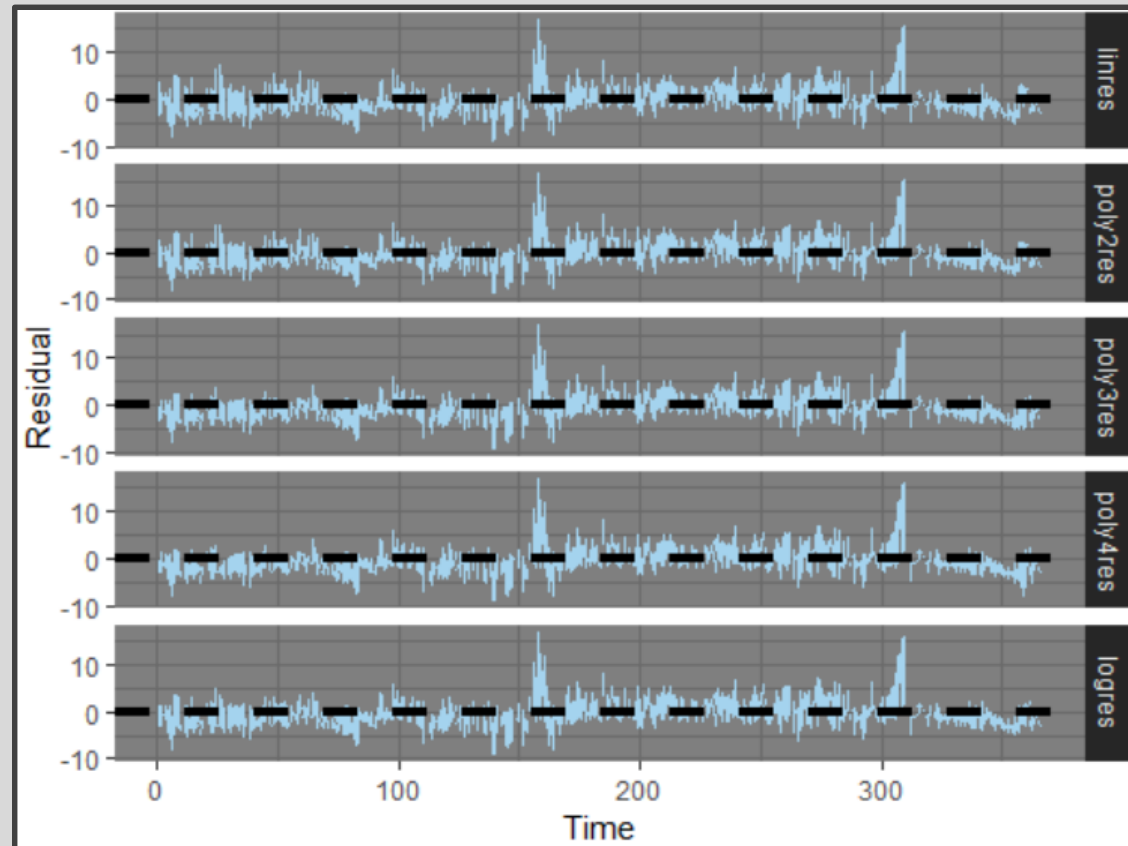
- Run Chunk 2
  - Comparing Predictions vs Actual Maximum Water Temperatures
  - Models Give Similar Predictions



## Part 5: Evaluation by Visualization



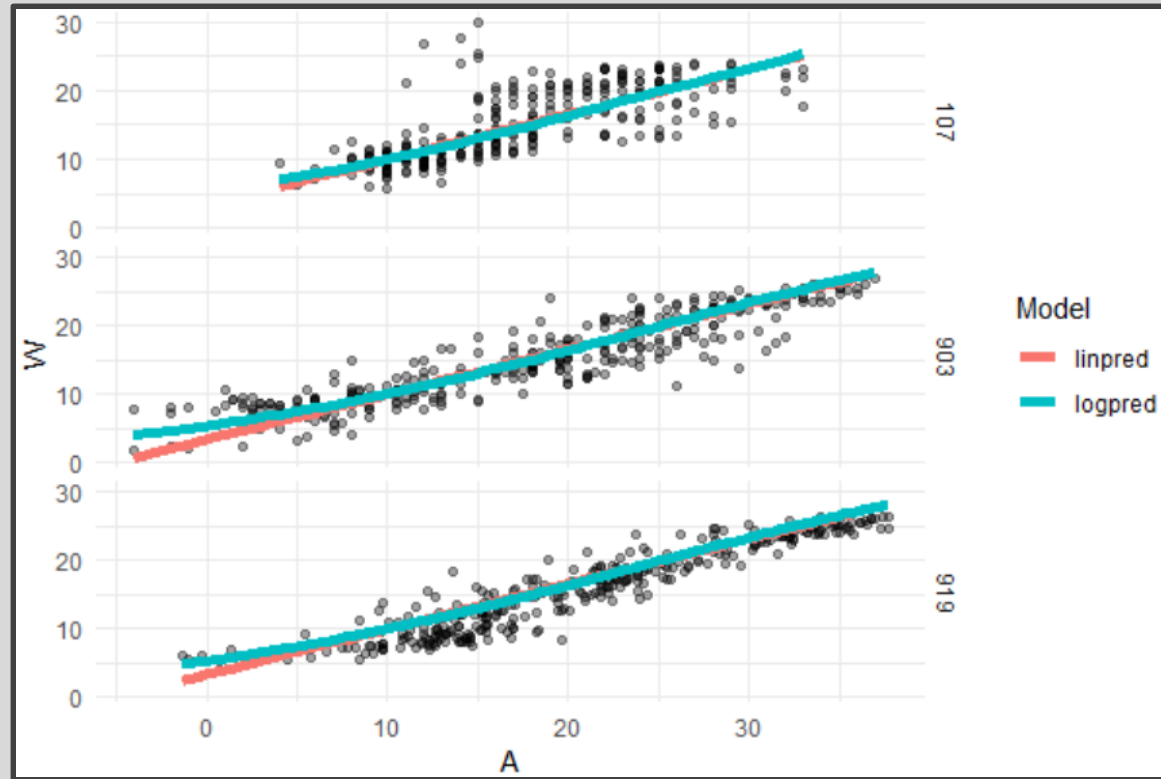
- Run Chunk 3
  - Shows Residuals Under the 4 Models Plotted Over Time
  - What is the Problem?



## Part 5: Evaluation by Visualization



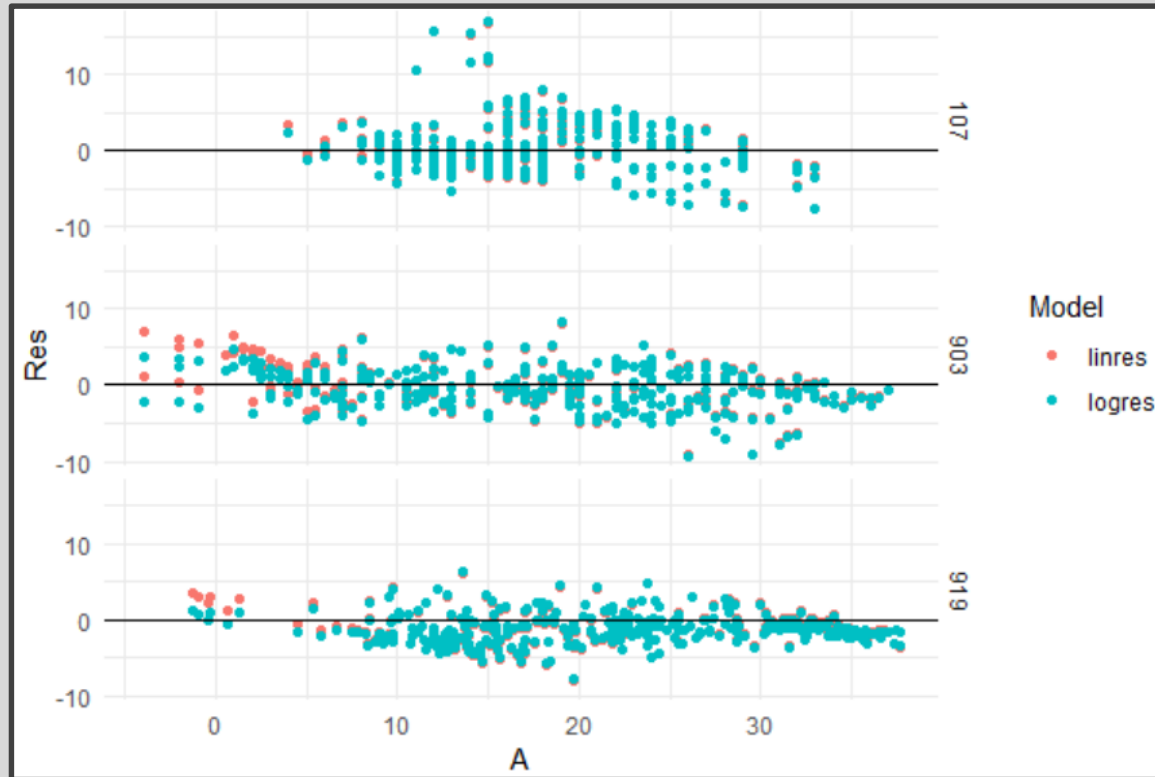
- Run Chunk 4
  - Evaluate Models For the Three Locations Separately



## Part 5: Evaluation by Visualization



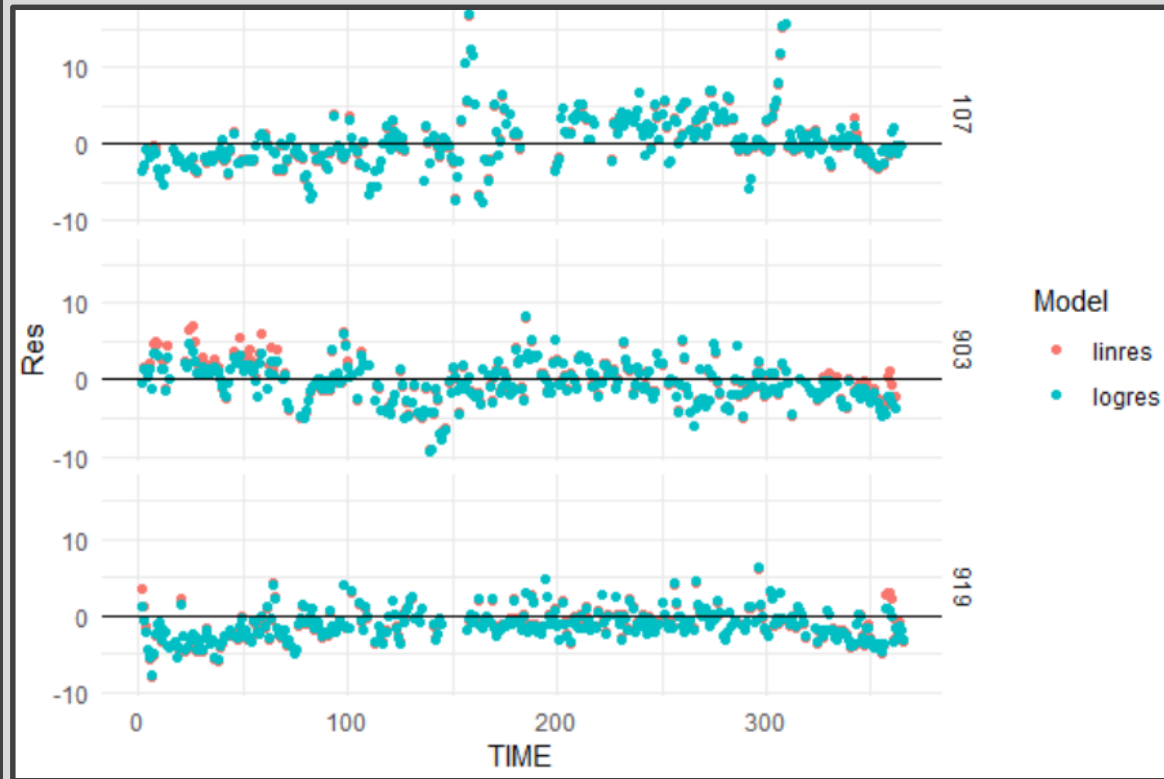
- Run Chunk 5
  - Evaluate Error For the Three Locations Separately (by A)



## Part 5: Evaluation by Visualization



- Run Chunk 6
  - Evaluate Error For the Three Locations Separately (by Time)



## Part 6: Evaluation by Numerical Summary



- Run Chunk 1

- Mean Bias

$$MB = \frac{1}{N} \sum \hat{\epsilon}_k$$

- Mean Absolute Error

$$MAE = \frac{1}{N} \sum |\hat{\epsilon}_k|$$

- Root Mean Squared Error

$$RMSE = \sqrt{\frac{1}{N} \sum \hat{\epsilon}_k^2}$$

- MB, MAE, and RMSE are in Degrees Celsius

## Part 6: Evaluation by Numerical Summary



- Summarizing Table
  - Evaluate MB, MAE, and RMSE on Test Data to Choose Best Model Going Forward
  - Sketch of Table We Want

| Model    | MB | MAE | RMSE |
|----------|----|-----|------|
| Linear   |    |     |      |
| Poly(2)  |    |     |      |
| Poly(3)  |    |     |      |
| Poly(4)  |    |     |      |
| Logistic |    |     |      |

- Before Writing Code, Have a Plan for the Output

## Part 6: Evaluation by Numerical Summary



- Chunk 2
  - Run Line-By-Line
  - Think About Ways to Quickly Apply All 3 Functions to All Residuals
- Run Chunk 3
  - Combine `rename()`, `gather()`, `group_by()`, and `summarize()`
- Chunk 4
  - Change `eval=F` to `eval=T` and Knit the File (What is Seen?)



Part 6:  
Evaluation by  
Numerical  
Summary



- My Results Based on My Seed

| Model    | MB     | MAE   | RMSE  |
|----------|--------|-------|-------|
| <fct>    | <dbl>  | <dbl> | <dbl> |
| Linear   | -0.350 | 2.18  | 2.87  |
| Poly(2)  | -0.387 | 2.17  | 2.86  |
| Poly(3)  | -0.466 | 2.11  | 2.82  |
| Poly(4)  | -0.492 | 2.10  | 2.83  |
| Logistic | -0.426 | 2.13  | 2.83  |

- When Results Are This Close,  
Always Consider the Most  
Simple Model

## Discussion



- Problems With The Approach
  - Same Model For All Locations
  - Not All Locations Used in Train
  - Not All Locations Used in Test
  - Residuals Indicate that Model Can Be Improved
  - All Models Have the Same Issue if Used for Predicting the Maximum Water Temperature Given the Maximum Air Temperature

Closing



Disperse  
and Make  
Reasonable  
Decisions