

Modeling IV

Introduction



Instructions

- Download Tutorial 13 Zip
- Unzip Folder
- Required Packages
 - library(tidyverse)
 - library(modelr)
 - library(purrr)
 - library(broom)
- Open .Rmd File and Knit

Discussion



- Problems With Current Approach
 - Same Model For All Locations
 - Not All Locations Used in Train
 - Not All Locations Used in Test
 - Residuals Indicate that Model Can Be Improved
 - Not Helpful for Forecasting
 - Ambiguous Results: No Clear Winner



Previously

- Split Data in Train and Test
 - Train (28 Rivers)
 - Test (3 Rivers)
- Purpose
 - Estimate Out-of-Sample Error
 - Pick Best Model Based on This Estimate
 - Combat Overfitting
 - Robustification
- Goal: Find the Simplest Model that Adequately Predicts



Current Issues

- Decision on Final Model Heavily
 Influenced by the Test Data
- Loss of Data in Model Fitting
- Not Appropriate in Small Datasets
- Cross Validation Idea
 - Split Data Into Many Groups
 - Each Group Acts as a Test Set
 - All Data is Used in Both Model Fitting and Model Testing
 - Help: Chapter 5 (ISLR)



- Tidyverse Concepts
 - Chapter 20 (R4DS)
 - List-Columns
 - Columns in Data Frames or Tibbles Can Be Lists
 - What this Means
 - Column of Tables
 - Column of Models
 - Column of Functions
 - Functions
 - nest(): Converts Rows of a Data Frame into a List
 - unnest(): What do You Think It Does?



Run Chunk 1

- Observe the Output
- Column of Tibbles
- Run Chunk 2
 - Imagine We Wanted to Split
 - Test: Data For Location 103
 - Train: All Remaining Data
 - Use of filter() and unnest()
 - First Glimpse -> 365 x 8
 - Second Glimpse -> 10,972 x 8



Chunk 3

- Run Each Line
- What is Happening?
- Use View() on DATA2 and Scan Through the Data
- What do You Notice?

Chunk 4

- Create a Loop that Repeats this Process for Each Location
- Each Location Is a Test Set
- Predictions Saved are All Outof-Sample
- Run Chunk 4 to Test Your Code



Chunk 4 (Continued)

```
DATA2=DATA
DATA2$linpred=NA
for(k in unique(DATA2$L)){
 TEST = NEST.DATA %>% filter(L==k) %>%
unnest()
 TRAIN = NEST.DATA %>% filter(L!=k) %>%
unnest()
 linmod=lm(W~A, data=TRAIN)
 linmodpred=predict(linmod,newdata=TEST)
 DATA2$linpred[which(DATA2$L==k)]=linmodpred
```



Chunk 5

- In Our Data, We Have:
 - Actual Water Temperatures
 - Out-of-Sample Predicted Water Temperatures
- Create RMSE.func() With Two Arguments
 - actual= vector of actual water temperatures
 - predict=vector of predicted water temperatures
- Use This Function on the Two Columns in DATA2 for RMSE
 - actual=W
 - predict=linpred



Chunk 5 (Continued)



RMSE.func(actual=DATA2\$W,predict=DATA2\$linpred)
[] 3.147084

Intermission



Current

- Using the Natural Grouping of Data for 31-Fold Cross
 Validation
- Only Fit One Linear Model
- Should Use Cross-Validation for Multiple Different Models and Compare Cross-Validated RMSE

Next

- Randomly Assign Observations to *K*-Folds
- CV Function: crossv_kfold(K)



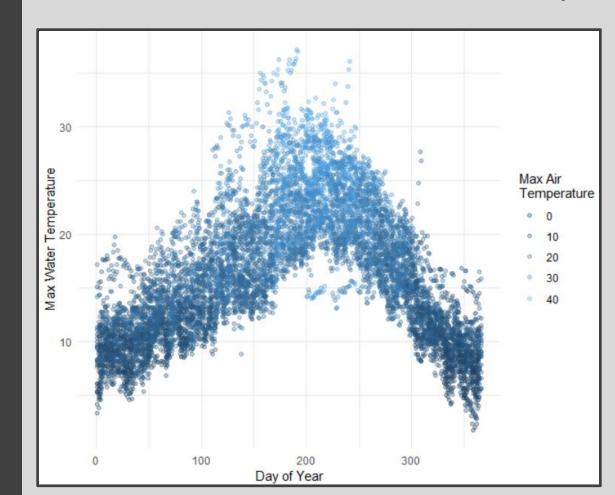
- Overview (*K*=10)
 - Randomly Split Observations Into K Groups
 - Each Fold Acts as a Test Set
 - If Each Fold Contains
 Approximately the Same # of Observations,





Run Chunk 1

- Variables (Julian Day)
- Clear Non-Linear Relationship





General Polynomial Model

$$W = a + \sum_{i=1}^{I} b_i A^i + \sum_{j=1}^{J} c_j D^j + \varepsilon$$

- Perform K-Fold CV to Estimate
 Out-of-Sample RMSE for
 Choices of *I=4* and *J=3*
- Ultimate Goal is To Select Best I and J



Run Chunk 2

- Fit Model with *I=4* and *J=3*
- Functions from broom Package
 - tidy()
 - glance()
- Used For Previewing Data

```
tidy(polymodel)
A tibble: 8 x 5
                     estimate std.error statistic
                                                  p.value
term
                        <db7>
                                 <db1>
                                            <db7>
                                                     < db.7 >
<chr>>
(Intercept)
                       16.2
                                0.0273
                                          595.
                                                 0.
poly(A, 4)1
                       328.
                                4.36
                                           75.3
poly(A, 4)2
                                2.80
                                           17.5
                       49.0
                                                 1.62e-67
poly(A, 4)3
                        2.85
                                2.78
                                            1.02 3.06e- 1
                                2.72
                       -3.62
                                           -1.33 1.84e- 1
poly(A, 4)4
                     46.0
                                2.78
poly(JULIAN_DAY, 3)1
                                           16.6 8.85e-61
                                          -52.5
poly(JULIAN_DAY, 3)2 -226.
                                4.31
poly(JULIAN_DAY, 3)3
                                          -20.5 8.66e-92
                      -59.3
                                2.89
```

```
      glance(polymodel)

      A tibble: 1 x 11

      r.squared adj.r.squared sigma statistic p.value
      df logLik
      AIC
      BIC

      <db7>
      <db7</td>
      <db7>
      <db7</td>
      <db7</td>
```



- Run Chunk 3
 - Divide Data into 10 Folds
 - Use crossv_kfold() Function
 - Variables are Lists of Train and Test Sets
 - For Each Row, We Want to Fit on Train and Predict on Test

```
head(DATA3)
A tibble: 6 x 3

train test .id

resample> 
resample> 
resample> 01

resample> 
resample> 02

resample> 
resample> 03

resample> 
resample> 04

resample> 
resample> 05

resample> 
resample> 06
```



Run Chunk 4

- Create Function to Fit Models
- Apply Function to All Train Sets Using purrr:map() Function

```
DATA4=DATA3 %>%
   mutate(tr.model=map(train,train.model.func,i=i,j=j))
head(DATA4)
A tibble: 6 x 4
train
                .id
                    tr.model
     test
                <chr> <chr>> <ist>
      <1ist>
<1ist>
<S3: resample> <S3: resample> 01
                   <S3: 1m>
<S3: resample> <S3: resample> 04 <S3: lm>
```

- Functions from purrr Package
 - map() Loop Over Train
 - map2() Loop Over Fitted Models and Test



Run Chunk 5

- purrr:map2() Iterates FunctionOver Two Arguments
- For Every Test Set and Trained Model, We Use augment() to Get Predictions

```
DATA4.PREDICT = DATA4 %>%
          mutate(predict=map2(test,tr.model,~augment(.y,newdata=.x))) %>%
          select(predict) %>%
          unnest()
head(DATA4.PREDICT)
A tibble: 6 x 10
                                                         l.fitted
JULIAN DAY
                                                     DAY
                                                                  .se.fit
                         < db 1 >
     <int> <int> <int>
                                :db 1>
                                     <int> <int> <int>
                                                           < db 7 >
                                                                    < db 1 >
                                 5.1
                                                            7.27
            2003
                    103
                                                                   0.138
                                6.2
            2003
                    103
                                                            7.67
                                                                   0.119
                              14
            2003
                    103
                                                           10.4
                                                                  0.0744
                    103
            2003
                          9.5
                                                            9.14
                                                                   0.0803
                              11.4
                         12.5
                                         47
                                                     16
            2003
                    103
                                                           10.5
                                                                   0.0621
            2003
                    103
                         10.7
                                                           11.5
                                                                   0.0548
```

Next, Compare Fitted With Actual Using RMSE.func()

RMSE.func(actual=DATA4.PREDICT\$W,predict=DATA4.PREDICT\$.fitted)
[] 2.709727

Look Ahead



- What We Have Done
 - Specify I and J
 - Use 10-Fold Cross Validation to Estimate Out-of-Sample RMSE
- How We Should Use This
 - Choose Max / and Max J (Example: 10)
 - Initiate 10 x 10 Matrix of NA
 - Loop Through All i and j to Capture Out-of-Sample RMSE
 - Create a Tile Plot that Visualizes the RMSE for Each Combination of i and j
 - Choose Best i and j

Closing



Disperse and Make Reasonable Decisions