Modeling V

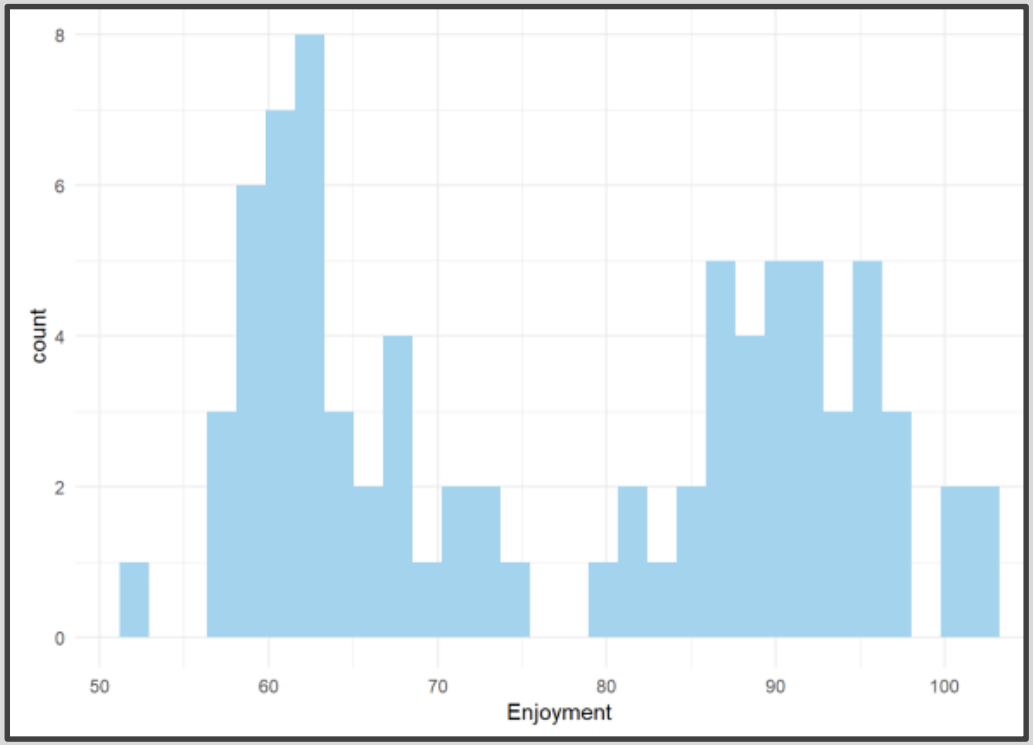
Introduction

- Fiercely Read Chapter 18 (R4DS)
- Previously: Numeric Variables
- New Focus
  - Categorical Predictor Variables
  - Interaction Effects
- Different Categorical Variables
  - Principled
  - Arbitrary
- Understand Using Multiple Datasets and Visualizations

Example 1

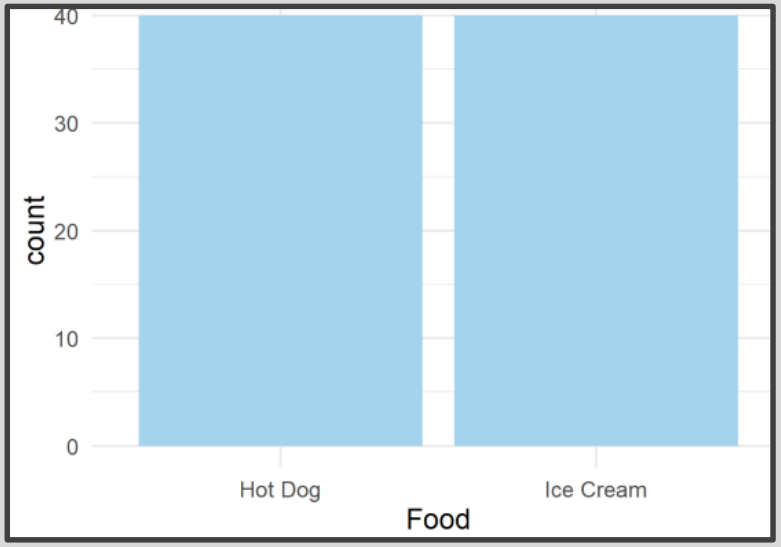
- Data Overview
  - Enjoyment (E)
  - Food (F)
  - Condiment (C)
  - 80 Observations

- Enjoyment Visualized

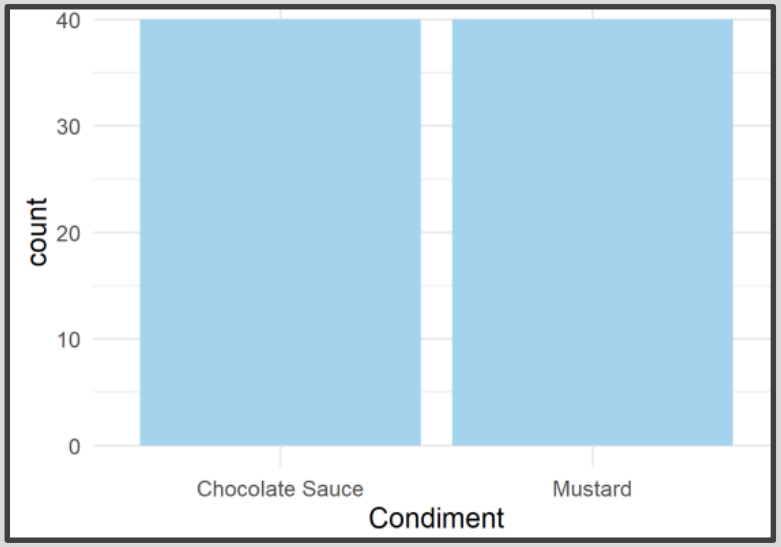


Example 1

- Food Visualized



- Condiment Visualized



Example 1

- Question of Interest

Can We Predict a Person's Culinary Enjoyment if…

We Serve Them a Particular Item:

- *Hot Dog*
- *Ice Cream*

With a Particular Condiment

- *Mustard*
- *Chocolate Sauce*

?

Example 1

- Regressing E on F

```
EvsF.Model=lm(Enjoyment~Food,data=CONDIMENT)
tidy(EvsF.Model)
```

```
## # A tibble: 2 x 5
##   term          estimate std.error statistic  p.value
##   <chr>            <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)      77.5       2.39    32.4    5.82e-47
## 2 FoodIce Cream    -0.283     3.39    -0.0835 9.34e- 1
```

- $\hat{E} = 77.5 - 0.283F$

- Questions:
  - What Does 77.5 Represent?
  - What About -0.283?

Example 1

- What is R Doing?

```
CONDIMENT$Food[1:6]
```

```
## [1] "Hot Dog" "Hot Dog" "Hot Dog" "Hot Dog
" "Hot Dog" "Hot Dog"
```

```
head(model_matrix(CONDIMENT, Enjoyment~Food))
```

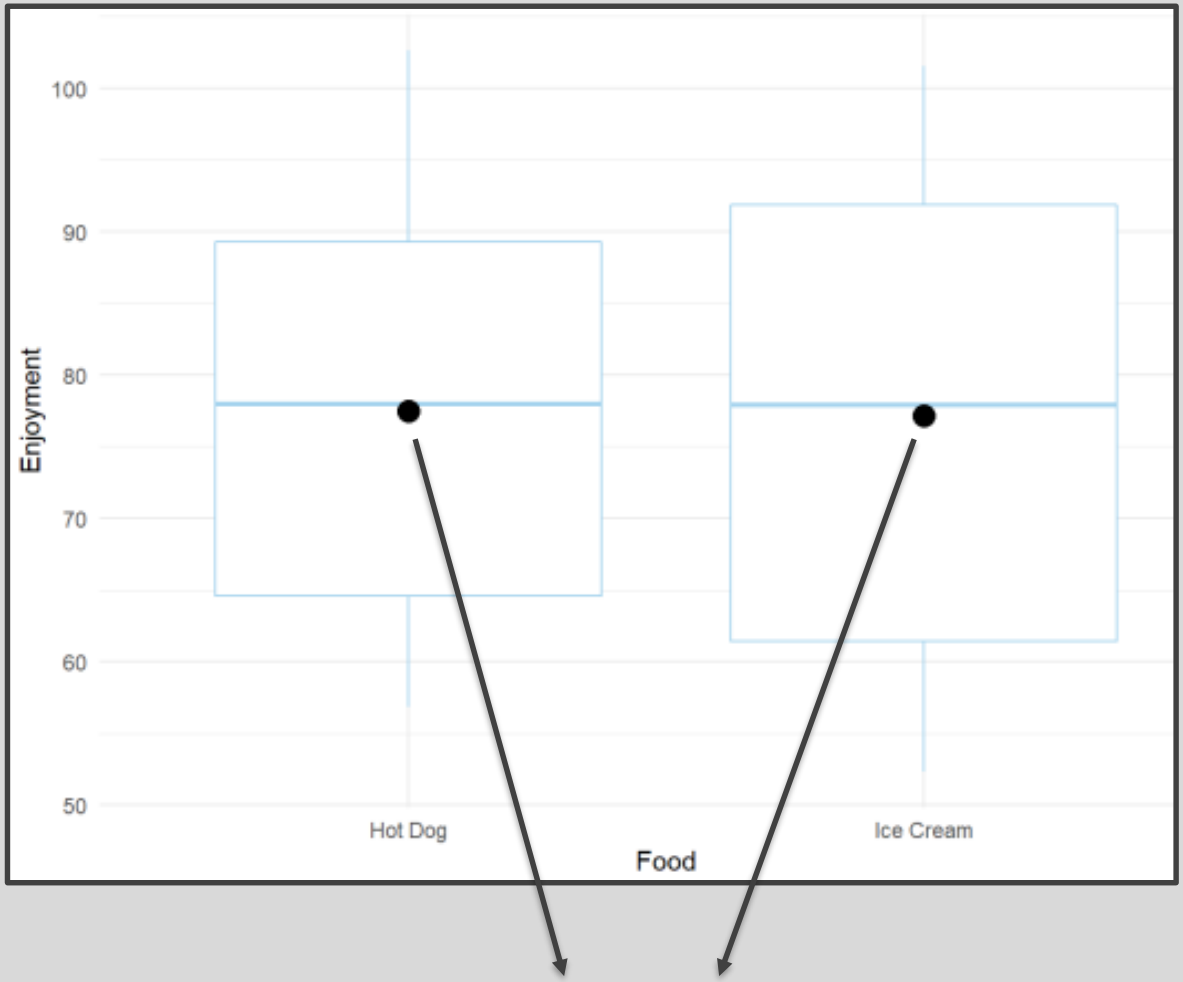
```
## # A tibble: 6 x 2
##   `(Intercept)` `FoodIce Cream`
##           <dbl>           <dbl>
## 1             1               0
## 2             1               0
## 3             1               0
## 4             1               0
## 5             1               0
## 6             1               0
```

Example 1

- Regressing E on F
  - $\hat{E} = 77.5 - 0.283F$
  - $F = \begin{cases} 0 & if\ Hot\ Dog \\ 1 & if\ Ice\ Cream \end{cases}$
  - If You Eat a Hot Dog,
    $\hat{E} = 77.5 - 0.283(0) = 77.5$
  - If You Eat Ice Cream,
    $\hat{E} = 77.5 - 0.283(1) = 77.217$
  - P-value = 0.934 for the Parameter Estimated by 0.283 (Not Statistically Significant)

Example 1

- Understanding This Visually



Predicted Values Under Model

Example 1

- Regressing E on C

```
EvsC.Model=lm(Enjoyment~Condiment,data=CONDIMENT)
tidy(EvsC.Model)
```

```
## # A tibble: 2 x 5
##   term             estimate std.error statistic  p.value
##   <chr>               <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)         79.2       2.38      33.3  6.67e-48
## 2 CondimentMustard    -3.73      3.36      -1.11 2.71e- 1
```

Significant: P-value < 0.05

Not Significant: P-value > 0.05

Example 1

- Regressing E on C + F

```
EvsCF.Model=lm(Enjoyment~Food+Condiment,data=CONDIMENT)
tidy(EvsCF.Model)
```

```
## # A tibble: 3 x 5
##   term             estimate std.error statistic  p.value
##   <chr>               <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)        79.3       2.93    27.1     4.07e-41
## 2 FoodIce Cream      -0.283     3.38    -0.0836  9.34e- 1
## 3 CondimentMustard   -3.73      3.38    -1.10    2.74e- 1
```

- $\hat{E} = 79.3 - 0.283F - 3.73C$
- $F = \begin{cases} 0 & if\ Hot\ Dog \\ 1 & if\ Ice\ Cream \end{cases}$
- $C = \begin{cases} 0 & if\ Chocolate\ Sauce \\ 1 & if\ Mustard \end{cases}$
- What does 79.3 Represent?

Example 1

- Obtaining Predicted Values

```
GRID=CONDIMENT %>%
      data_grid(
        Food=unique(Food),
        Condiment=unique(Condiment)
      )
print(GRID)
```

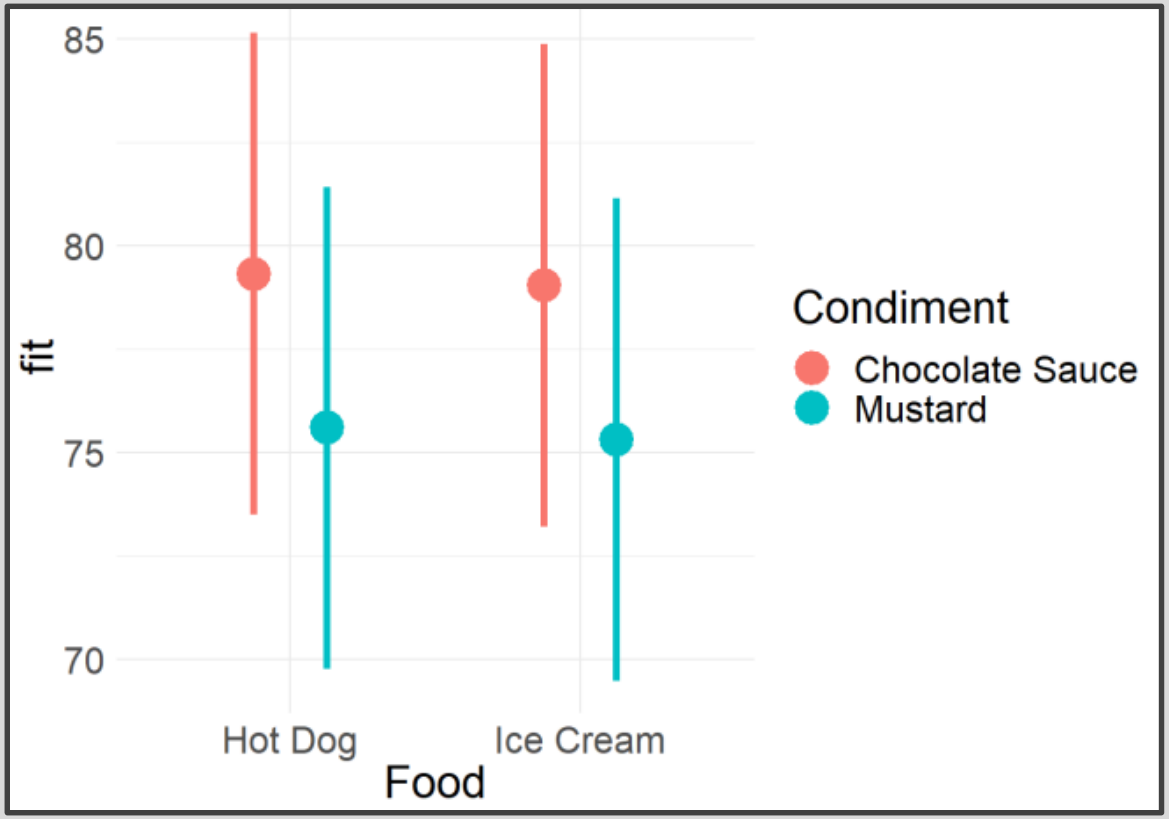
```
## # A tibble: 4 x 2
##   Food      Condiment
##   <chr>     <chr>
## 1 Hot Dog   Chocolate Sauce
## 2 Hot Dog   Mustard
## 3 Ice Cream Chocolate Sauce
## 4 Ice Cream Mustard
```

```
GRID2=cbind(GRID,predict(EvsCF.Model,
                         newdata=GRID,
                         interval="confidence"))
print(GRID2)
```

```
##         Food       Condiment      fit      lwr      upr
## 1    Hot Dog Chocolate Sauce 79.32368 73.49373 85.15363
## 2    Hot Dog         Mustard 75.59862 69.76867 81.42857
## 3 Ice Cream Chocolate Sauce 79.04103 73.21108 84.87098
## 4 Ice Cream         Mustard 75.31598 69.48603 81.14593
```

Example 1

- Understanding This Visually



Notice the Overlap

Example 1

- Interaction Effect

```
EvFC.Full.Model=lm(Enjoyment~Food+Condiment+Food*Condiment,data=CONDIMENT)
tidy(EvFC.Full.Model)
```

```
## # A tibble: 4 x 5
##   term                          estimate std.error statistic  p.value
##   <chr>                            <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)                       65.3      1.12      58.3 7.18e-65
## 2 FoodIce Cream                     27.7      1.58      17.5 2.11e-28
## 3 CondimentMustard                  24.3      1.58      15.3 5.58e-25
## 4 FoodIce Cream:CondimentMustard   -56.0      2.24     -25.0 1.95e-38
```

```
## # A tibble: 6 x 2
##   Food     Condiment
##   <chr>    <chr>
## 1 Hot Dog  Mustard
## 2 Hot Dog  Mustard
## 3 Hot Dog  Mustard
## 4 Hot Dog  Mustard
## 5 Hot Dog  Mustard
## 6 Hot Dog  Mustard
```

```
## # A tibble: 6 x 4
##     Int     F     C    FC
##   <dbl> <dbl> <dbl> <dbl>
## 1     1     0     1     0
## 2     1     0     1     0
## 3     1     0     1     0
## 4     1     0     1     0
## 5     1     0     1     0
## 6     1     0     1     0
```

Example 1

- Full Model:

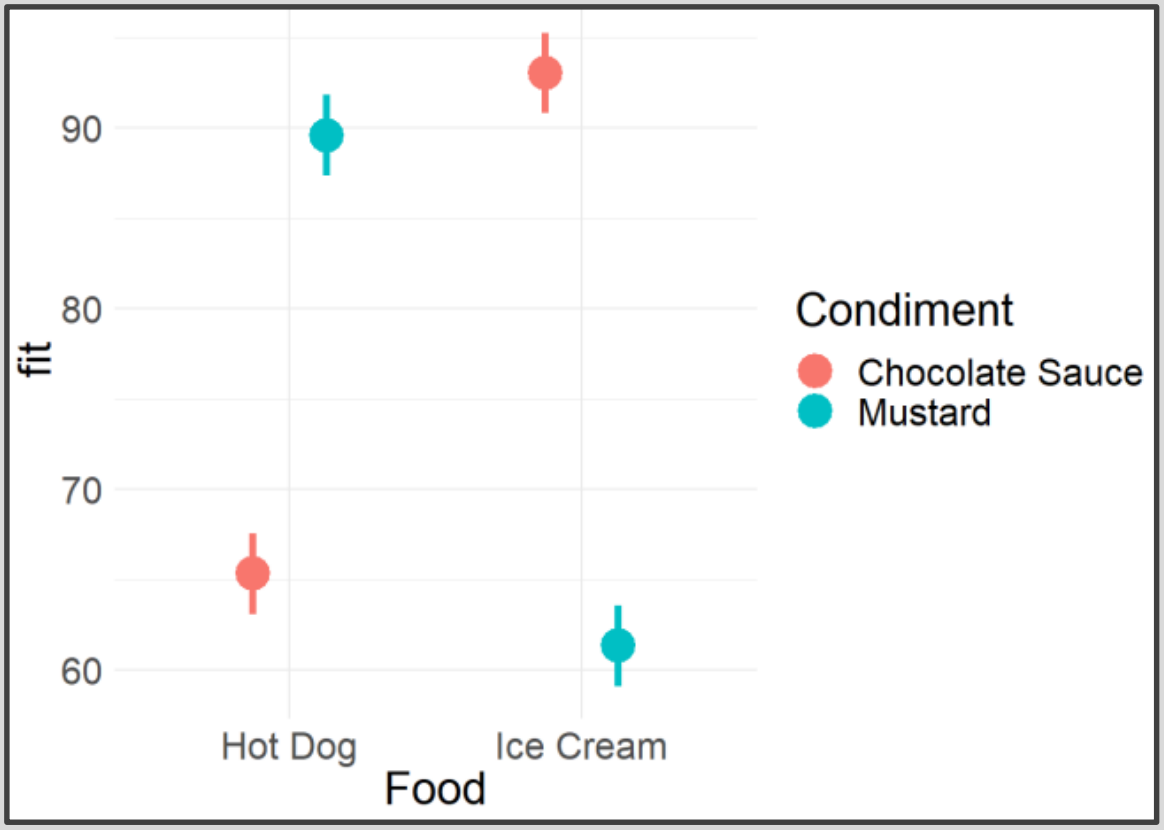
$$\hat{E} = 65.32 + 27.73F + 24.29C - 56.03FC$$

- $F = \begin{cases} 0 & if\ Hot\ Dog \\ 1 & if\ Ice\ Cream \end{cases}$
- $C = \begin{cases} 0 & if\ Chocolate\ Sauce \\ 1 & if\ Mustard \end{cases}$
- $FC = \begin{cases} 0 & otherwise \\ 1 & if\ Ice\ Cream\ and\ Mustard \end{cases}$

- What Does Each Parameter Estimate Represent?
  - 65.32?
  - 27.73?
  - 24.29?
  - -56.03?

Example 1

- Understanding This Visually
  - What Is Different?



Example 1

- Summary
  - Analysis of Variance (ANOVA)
  - Numerical Response Variable
  - Categorical Explanatory Variables
  - Purpose:
    - Generalize t-test
    - Estimate Difference in Means Between Groups
  - Experimental Designs

Example 2

- Data Overview
  - Popular Built-in Data `> iris`
    - Sepal.Width (W)
    - Sepal.Length (L)
    - Species (S)
    - 150 Observations

```
IRIS=iris[,c(1,2,5)]
names(IRIS)=c("L","W","S")
head(IRIS)
```

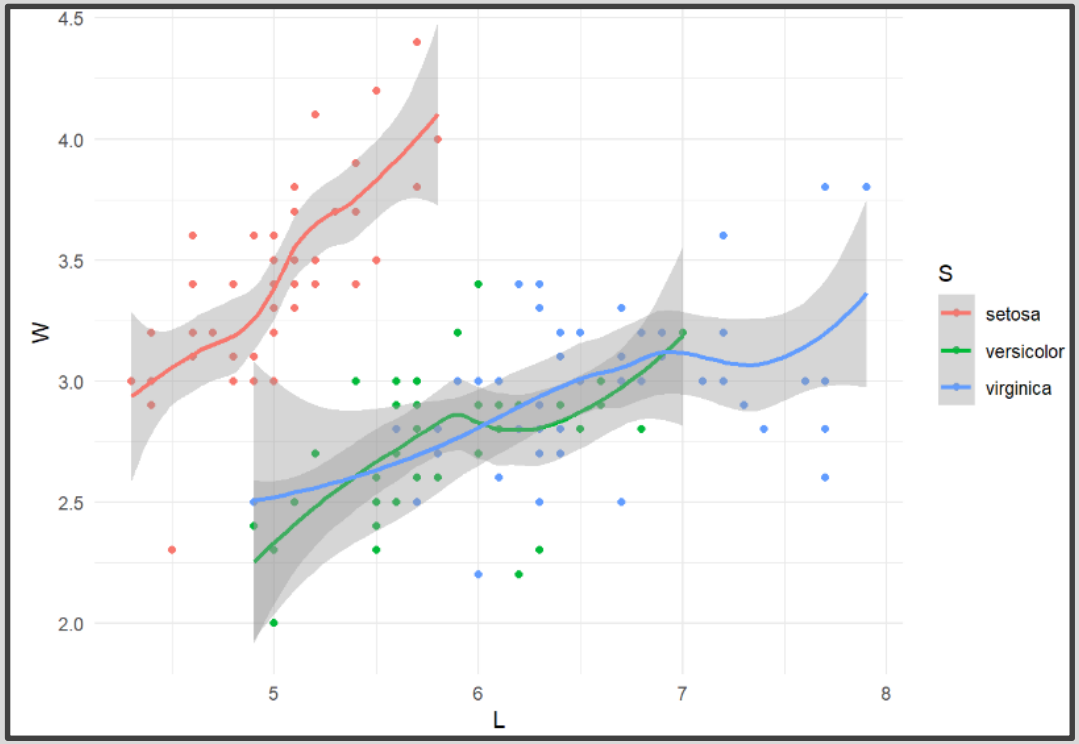
```
##     L   W       S
## 1 5.1 3.5 setosa
## 2 4.9 3.0 setosa
## 3 4.7 3.2 setosa
## 4 4.6 3.1 setosa
## 5 5.0 3.6 setosa
## 6 5.4 3.9 setosa
```

Example 2

- Question of Interest

Can We Explain the Variation in Sepal Width Using Sepal Length and Species (setosa,versicolor,virginica)?

- Visual of Relationship



Example 2

- Multiple Models

```
model1=lm(W~L,IRIS)
tidy(model1)
```

```
## # A tibble: 2 x 5
##   term        estimate std.error statistic  p.value
##   <chr>          <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)   3.42      0.254      13.5  1.55e-27
## 2 L            -0.0619    0.0430     -1.44 1.52e- 1
```

```
model2=lm(W~L+S,IRIS)
tidy(model2)
```

```
## # A tibble: 4 x 5
##   term        estimate std.error statistic  p.value
##   <chr>          <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)    1.68      0.235      7.12 4.46e-11
## 2 L              0.350     0.0463     7.56 4.19e-12
## 3 Sversicolor   -0.983     0.0721   -13.6  7.62e-28
## 4 Svirginica    -1.01      0.0933   -10.8  2.41e-20
```

```
model3=lm(W~L+S+L*S,IRIS)
tidy(model3)
```

```
## # A tibble: 6 x 5
##   term          estimate std.error statistic  p.value
##   <chr>            <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)     -0.569     0.554     -1.03 3.06e- 1
## 2 L                0.799     0.110      7.23 2.55e-11
## 3 Sversicolor      1.44      0.713      2.02 4.51e- 2
## 4 Svirginica       2.02      0.686      2.94 3.85e- 3
## 5 L:Sversicolor   -0.479     0.134     -3.58 4.65e- 4
## 6 L:Svirginica    -0.567     0.126     -4.49 1.45e- 5
```

Example 2

- Gathering Predictions

```
IRIS %>%
  gather_predictions(model1,model2,model3)%>%
  glimpse()
```

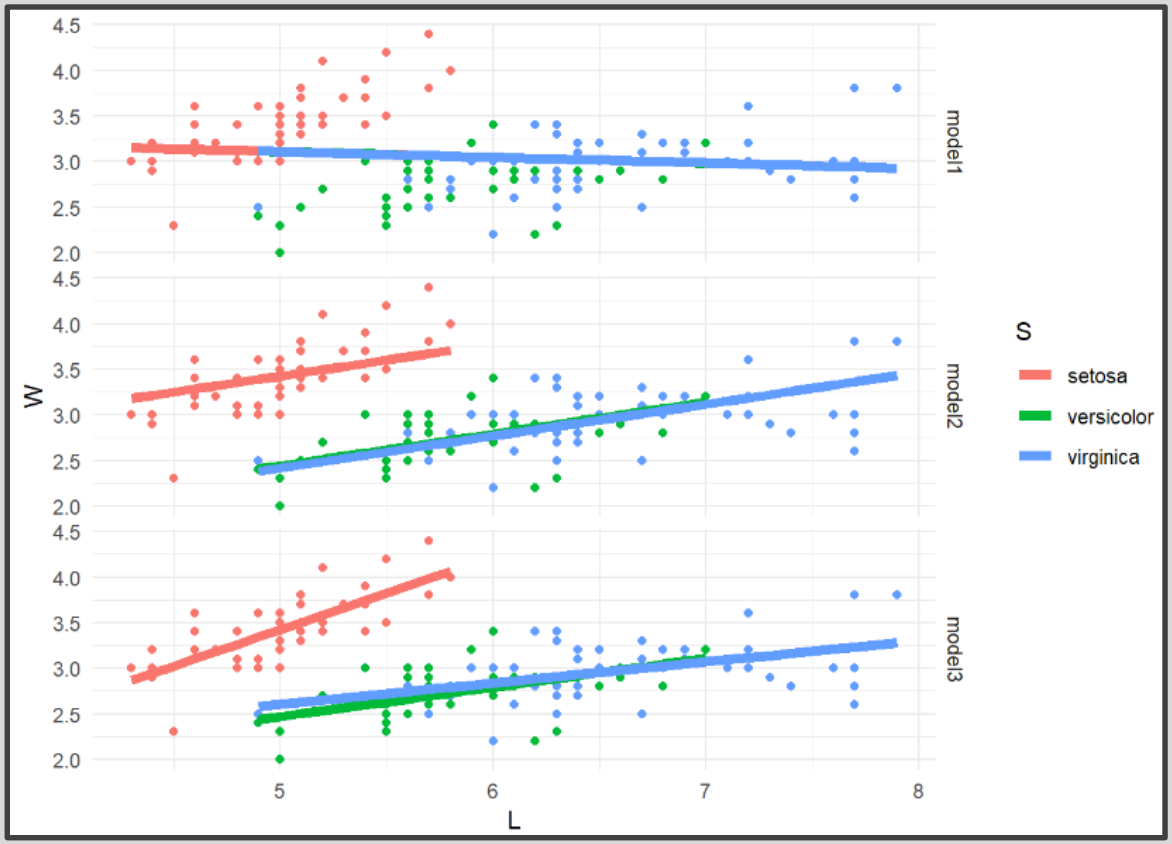
```
## Observations: 450
## Variables: 5
## $ model <chr> "model1", "model1", "model1", "model1", "model1", "model...
## $ L     <dbl> 5.1, 4.9, 4.7, 4.6, 5.0, 5.4, 4.6, 5.0, 4.4, 4.9, 5.4, 4...
## $ W     <dbl> 3.5, 3.0, 3.2, 3.1, 3.6, 3.9, 3.4, 3.4, 2.9, 3.1, 3.7, 3...
## $ S     <fct> setosa, setosa, setosa, setosa, setosa, setosa, setosa, ...
## $ pred  <dbl> 3.103334, 3.115711, 3.128088, 3.134277, 3.109523, 3.0847...
```

150 Predictions for 3 Models

- Variable Named “model”
- Allows Us To Quickly Create Graphics That Compare Models

Example 2

- Visualizing Models



Example 2

- Full Model Matrix

(Intercept) <dbl>	L <dbl>	Sversicolor <dbl>	Svirginica <dbl>	L:Sversicolor <dbl>	L:Svirginica <dbl>
1	5.1	0	0	0.0	0.0
1	4.9	0	0	0.0	0.0
1	4.7	0	0	0.0	0.0
1	4.6	0	0	0.0	0.0
1	5.0	0	0	0.0	0.0
1	5.4	0	0	0.0	0.0
1	4.6	0	0	0.0	0.0
1	5.0	0	0	0.0	0.0
1	4.4	0	0	0.0	0.0
1	4.9	0	0	0.0	0.0

- Full Model Estimated

```
## # A tibble: 6 x 5
##   term          estimate std.error statistic  p.value
##   <chr>            <dbl>     <dbl>     <dbl>    <dbl>
## 1 (Intercept)     -0.569     0.554     -1.03 3.06e- 1
## 2 L                0.799     0.110      7.23 2.55e-11
## 3 Sversicolor      1.44      0.713      2.02 4.51e- 2
## 4 Svirginica       2.02      0.686      2.94 3.85e- 3
## 5 L:Sversicolor   -0.479     0.134     -3.58 4.65e- 4
## 6 L:Svirginica    -0.567     0.126     -4.49 1.45e- 5
```

Adjustment In Mean

Adjustment In Slope

Example 2

- Summary
  - Analysis of Covariance (ANCOVA)
  - Numerical Response Variable
  - Categorical & Numerical Explanatory Variables

Closing

Disperse and Make Reasonable Decisions