

Common Number Systems

System	Base	Symbols	Used by humans?	Used in computers?
Decimal	10	0, 1, ... 9	Yes	No
Binary	2	0, 1	No	Yes
Octal	8	0, 1, ... 7	No	No
Hexa-decimal	16	0, 1, ... 9, A, B, ... F	No	No

Quantities/Counting (1 of 3)

Decimal	Binary	Octal	Hexa- decimal
0	0	0	0
1	1	1	1
2	10	2	2
3	11	3	3
4	100	4	4
5	101	5	5
6	110	6	6
7	111	7	7

Quantities/Counting (2 of 3)

Decimal	Binary	Octal	Hexa- decimal
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	B
12	1100	14	C
13	1101	15	D
14	1110	16	E
15	1111	17	F

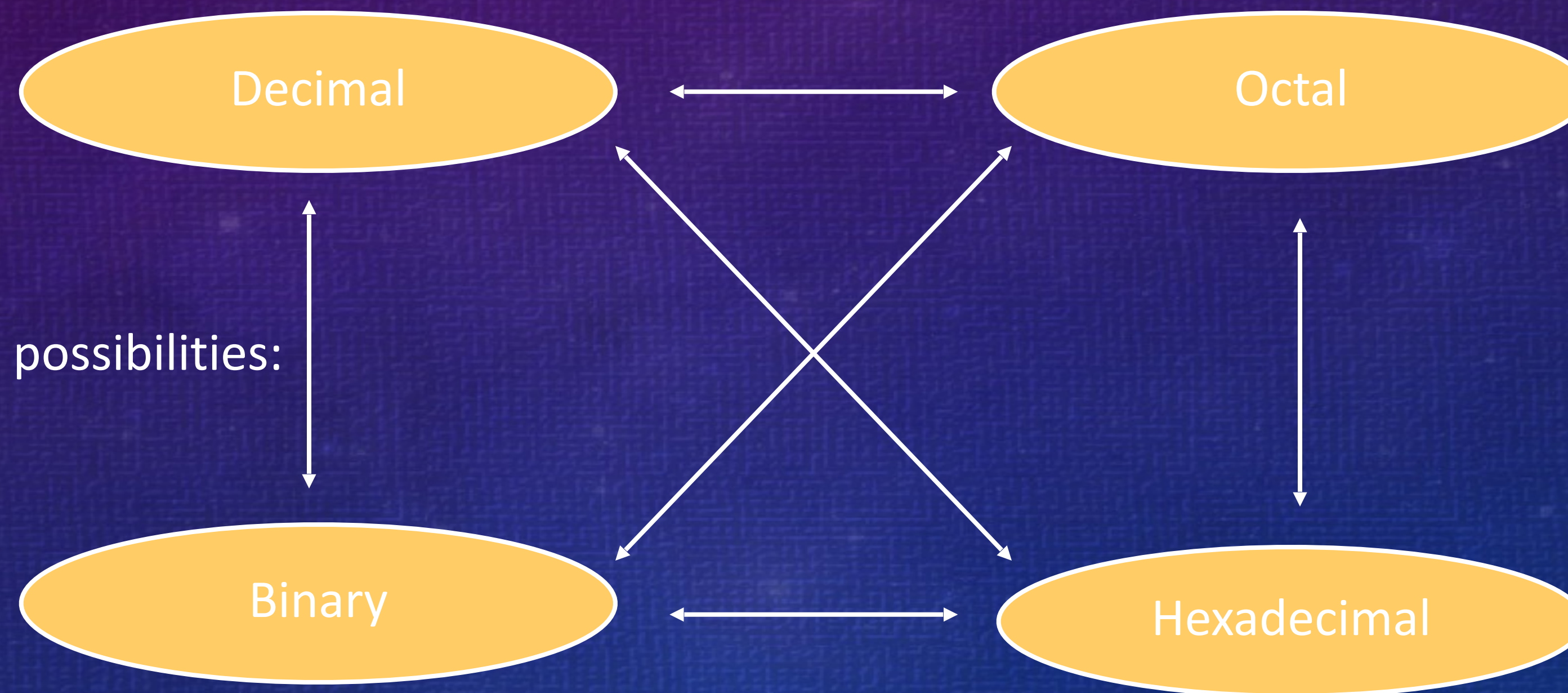
Quantities/Counting (3 of 3)

Decimal	Binary	Octal	Hexa- decimal
16	10000	20	10
17	10001	21	11
18	10010	22	12
19	10011	23	13
20	10100	24	14
21	10101	25	15
22	10110	26	16
23	10111	27	17

Etc.

Conversion Among Bases

- The possibilities:



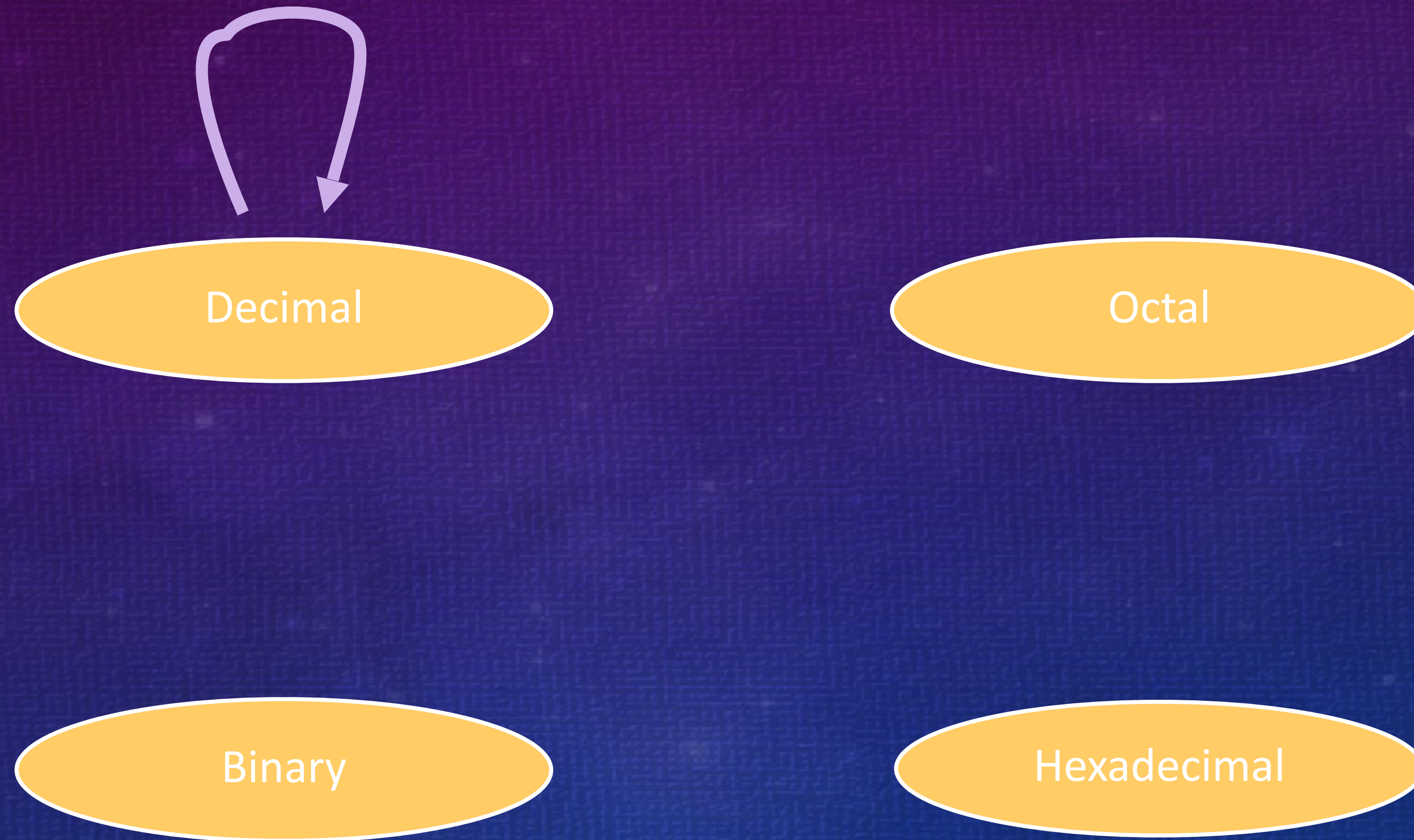
Quick Example

$$25_{10} = 11001_2 = 31_8 = 19_{16}$$



Base

Decimal to Decimal (just for fun)



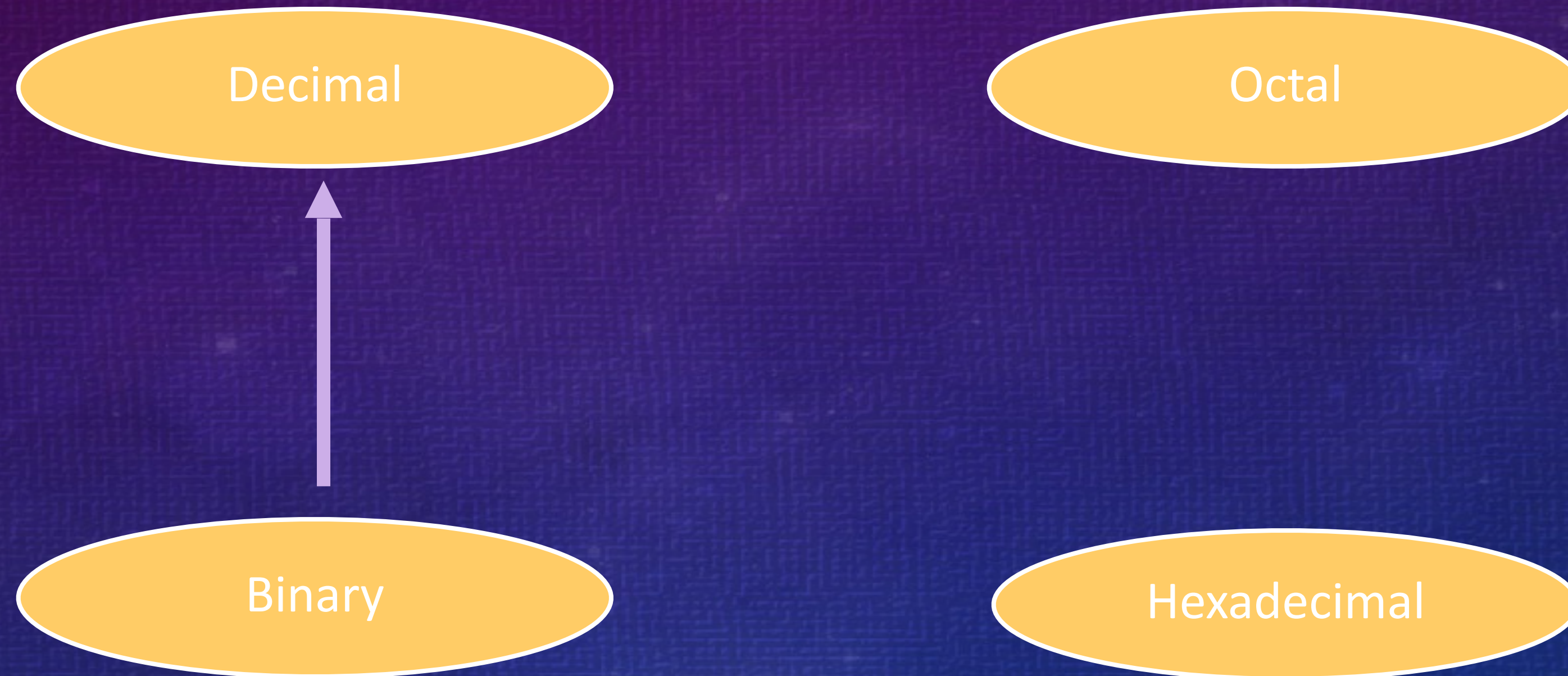
Next slide...

Weight

$$\begin{array}{rcll} 125_{10} \Rightarrow & 5 \times 10^0 & = & 5 \\ & 2 \times 10^1 & = & 20 \\ & 1 \times 10^2 & = & 100 \\ & & & 125 \end{array}$$

Base

Binary to Decimal



Binary to Decimal

- Technique
 - Multiply each bit by 2^n , where n is the “weight” of the bit
 - The weight is the position of the bit, starting from 0 on the right
 - Add the results

Example

Bit "0"

$101011_2 \Rightarrow$

$$1 \times 2^0 = 1$$

$$1 \times 2^1 = 2$$

$$0 \times 2^2 = 0$$

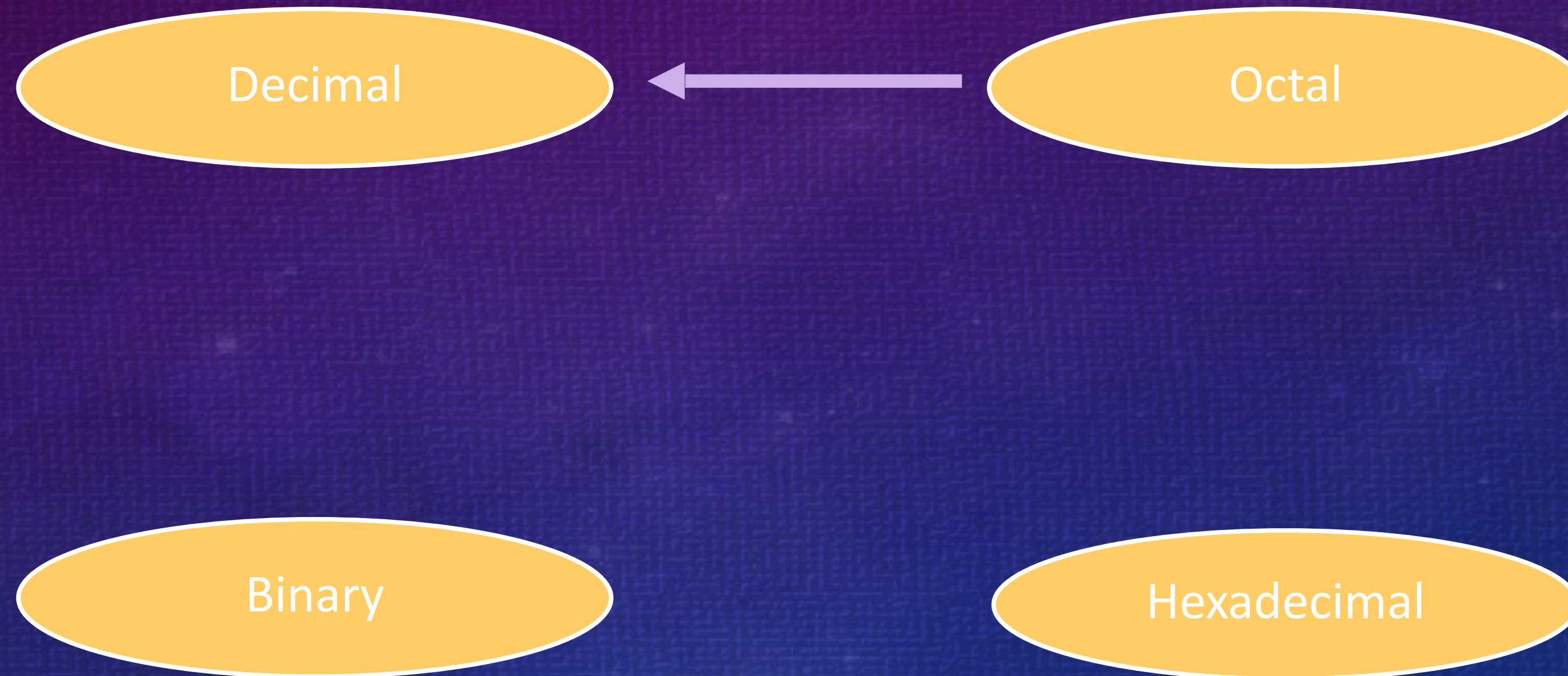
$$1 \times 2^3 = 8$$

$$0 \times 2^4 = 0$$

$$1 \times 2^5 = 32$$

43_{10}

Octal to Decimal



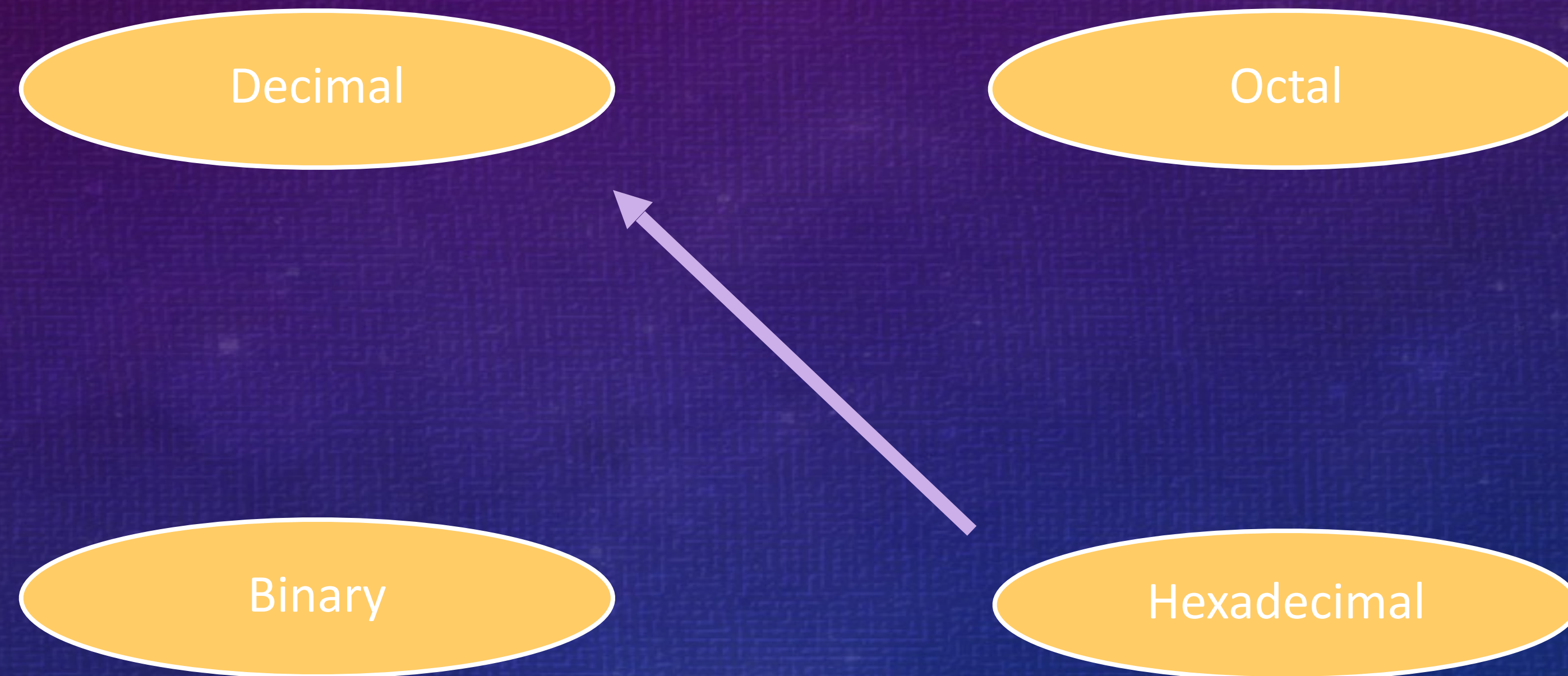
Octal to Decimal

- Technique
 - Multiply each bit by 8^n , where n is the “weight” of the bit
 - The weight is the position of the bit, starting from 0 on the right
 - Add the results

Example

$$\begin{aligned} 724_8 &\Rightarrow 4 \times 8^0 = 4 \\ &\quad 2 \times 8^1 = 16 \\ &\quad 7 \times 8^2 = 448 \\ &\quad 468_{10} \end{aligned}$$

Hexadecimal to Decimal



Hexadecimal to Decimal

- Technique
 - Multiply each bit by 16^n , where n is the “weight” of the bit
 - The weight is the position of the bit, starting from 0 on the right
 - Add the results

Example

$$\begin{aligned} \text{ABC}_{16} \Rightarrow & \quad \text{C} \times 16^0 = 12 \times 1 = 12 \\ & \quad \text{B} \times 16^1 = 11 \times 16 = 176 \\ & \quad \text{A} \times 16^2 = 10 \times 256 = 2560 \\ & \quad \quad \quad 2748_{10} \end{aligned}$$

Decimal to Binary

Decimal

Octal



Binary

Hexadecimal

Decimal to Binary

- Technique
 - Divide by two, keep track of the remainder
 - First remainder is bit 0 (LSB, least-significant bit)
 - Second remainder is bit 1
 - Etc.

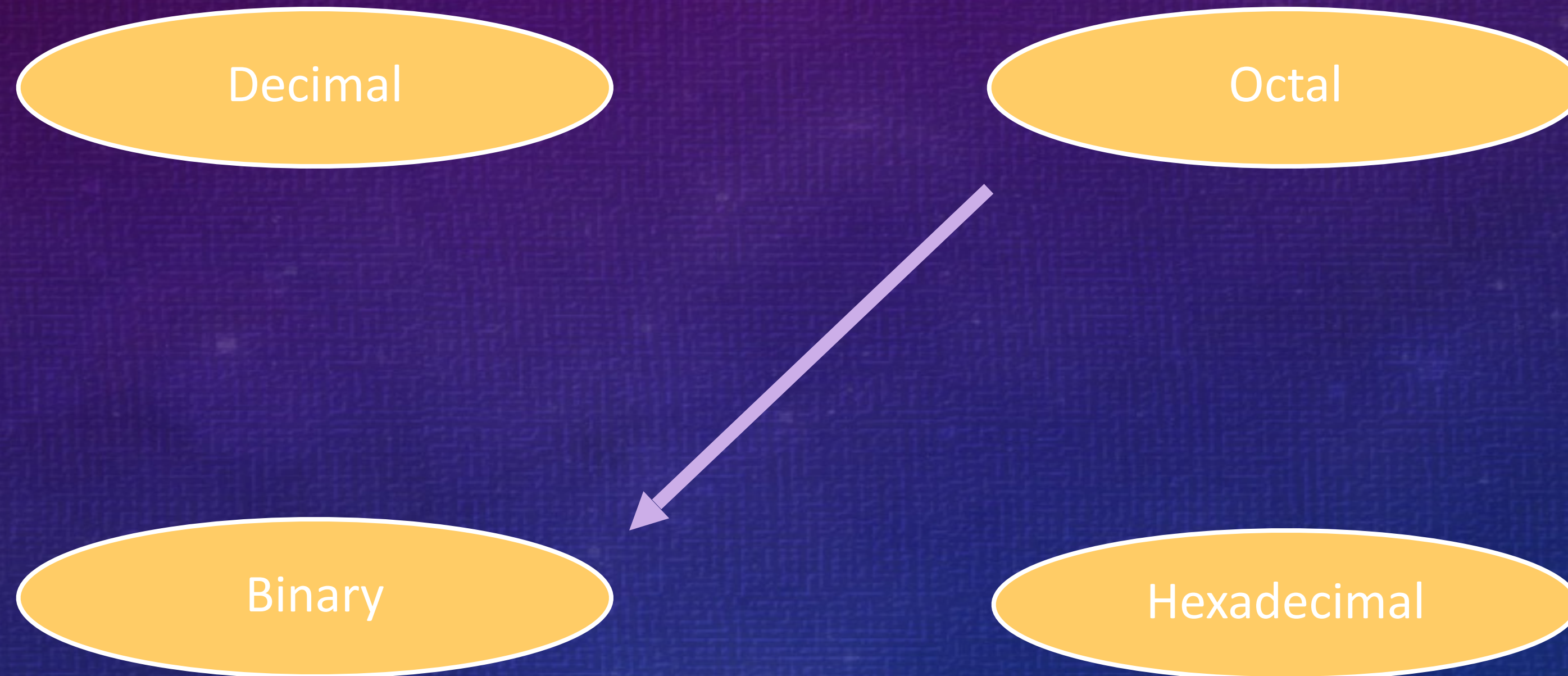
Example

$$125_{10} = ?_2$$

2		125	
2		62	1
2		31	0
2		15	1
2		7	1
2		3	1
2		1	1
		0	1


$$125_{10} = 1111101_2$$

Octal to Binary

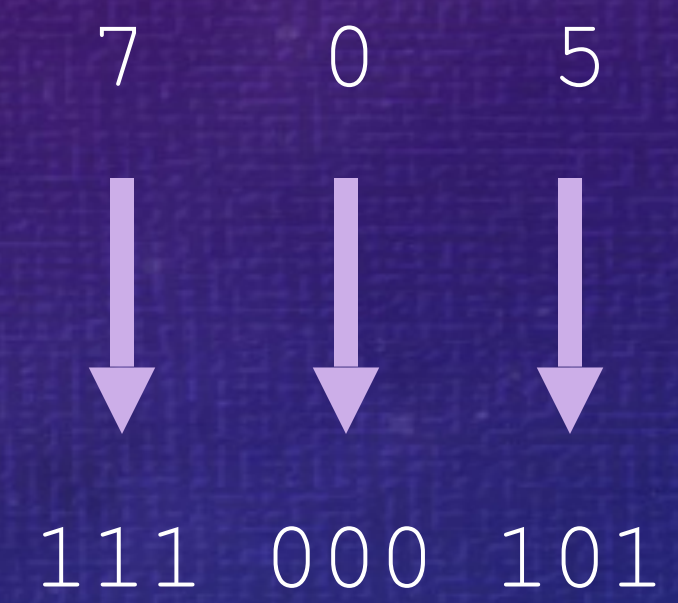


Octal to Binary

- Technique
 - Convert each octal digit to a 3-bit equivalent binary representation

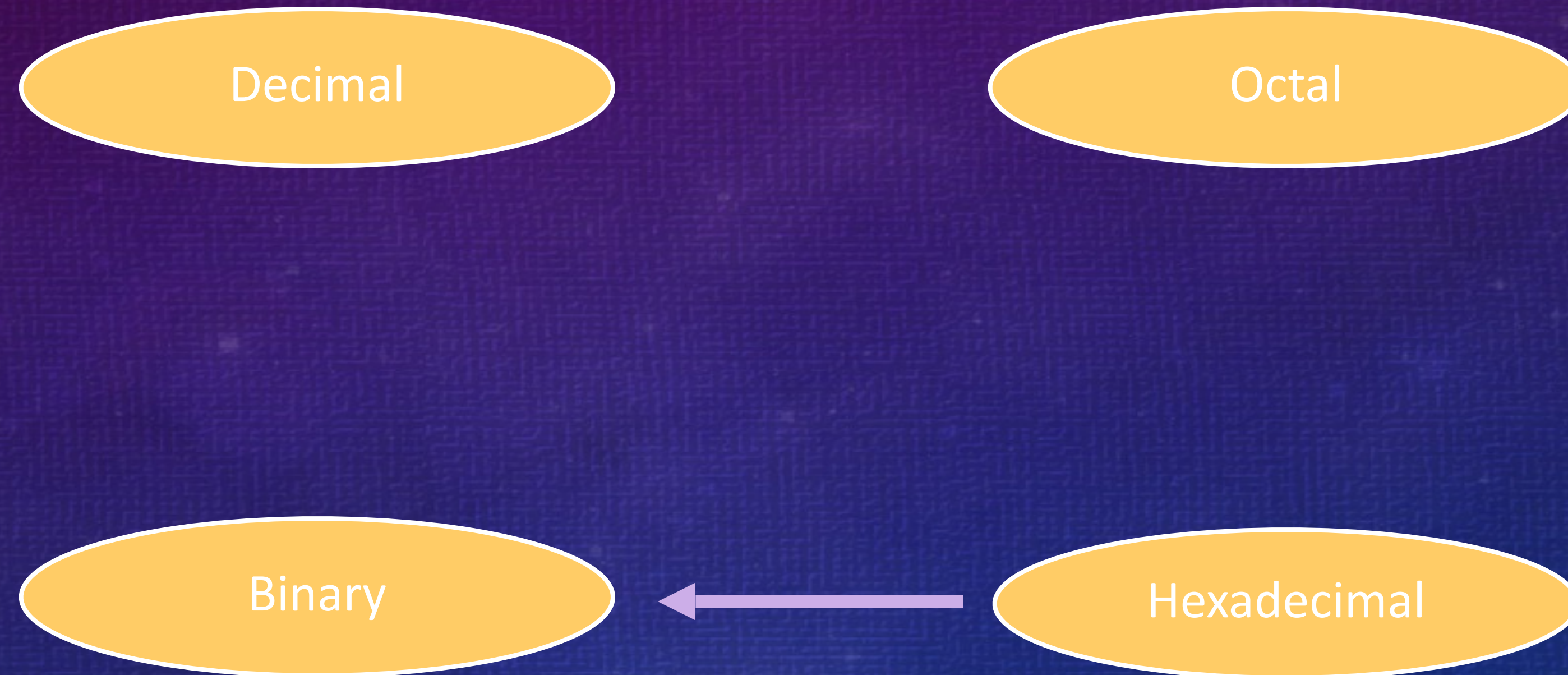
Example

$$705_8 = ?_2$$



$$705_8 = 111000101_2$$

Hexadecimal to Binary

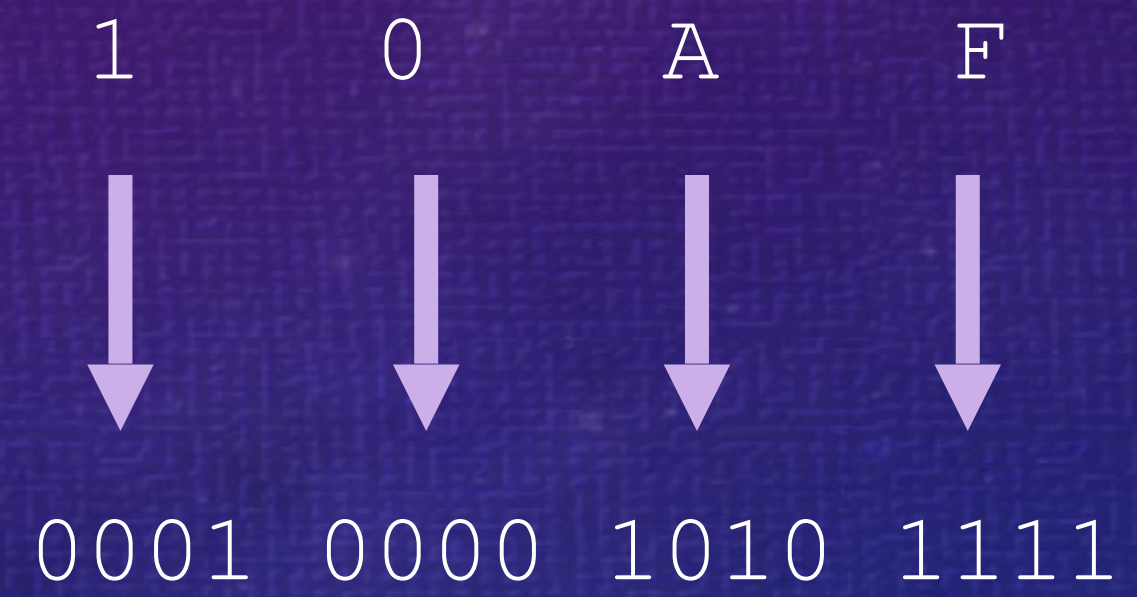


Hexadecimal to Binary

- Technique
 - Convert each hexadecimal digit to a 4-bit equivalent binary representation

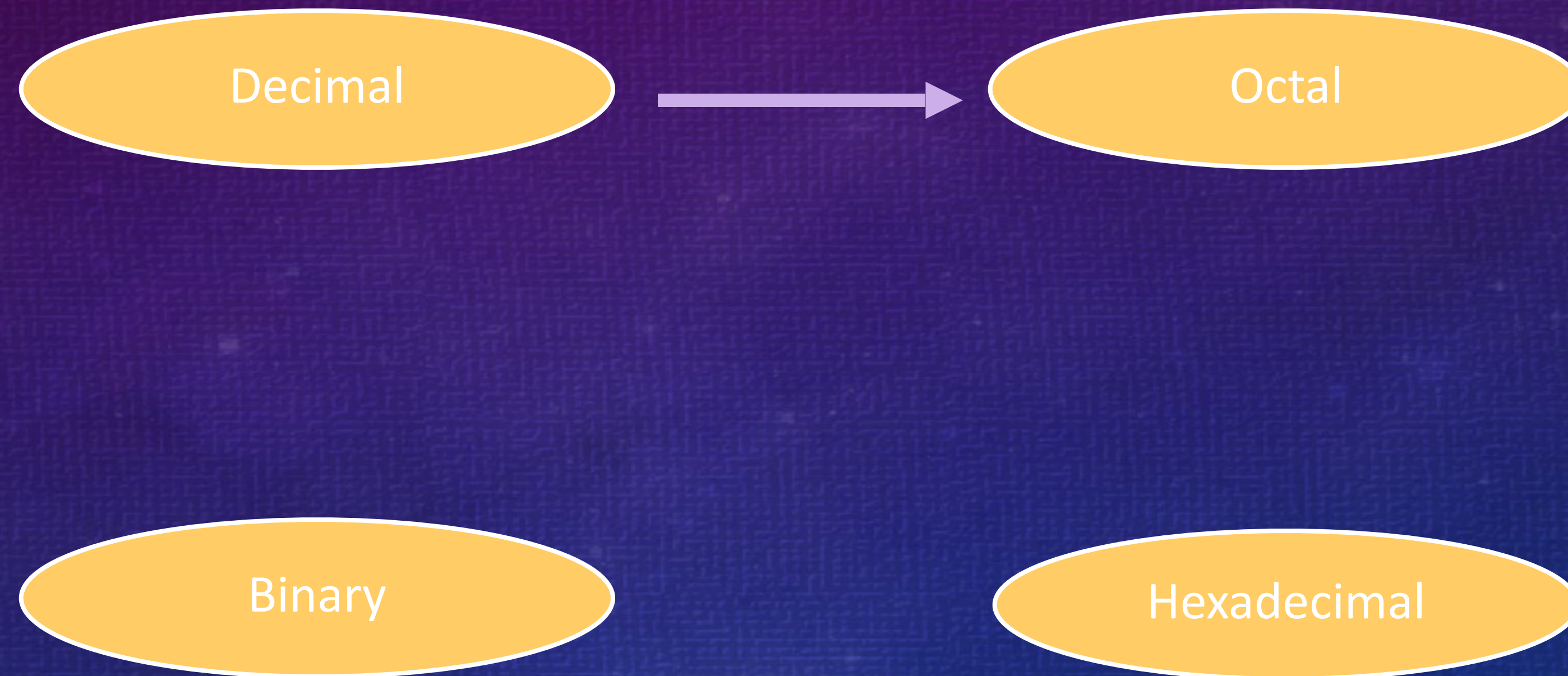
Example

$$10AF_{16} = ?_2$$



$$10AF_{16} = 0001000010101111_2$$

Decimal to Octal



Decimal to Octal

- Technique
 - Divide by 8
 - Keep track of the remainder

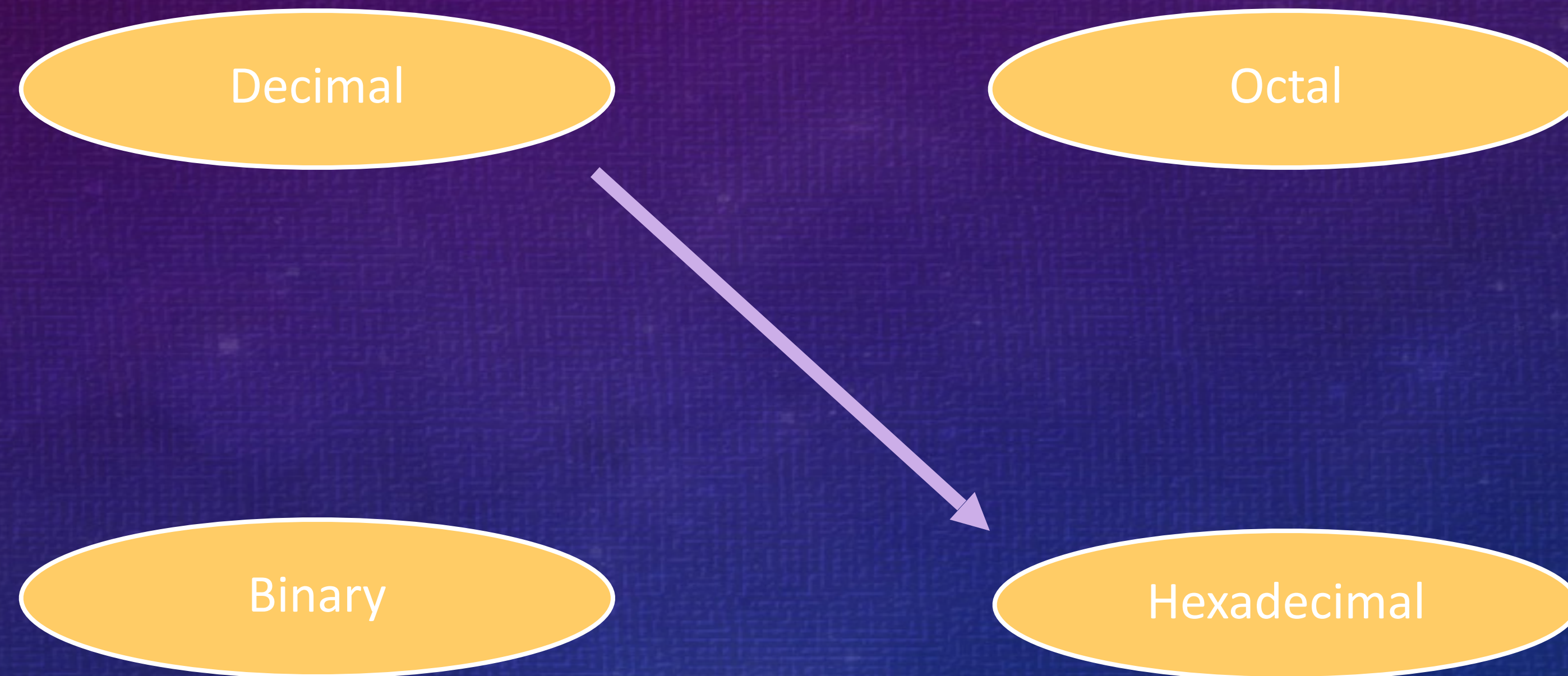
Example

$$1234_{10} = ?_8$$

8		1234	
		154	2
8			
		19	2
8			
		2	3
8			
		0	2


$$1234_{10} = 2322_8$$

Decimal to Hexadecimal




Decimal to Hexadecimal

- Technique
 - Divide by 16
 - Keep track of the remainder

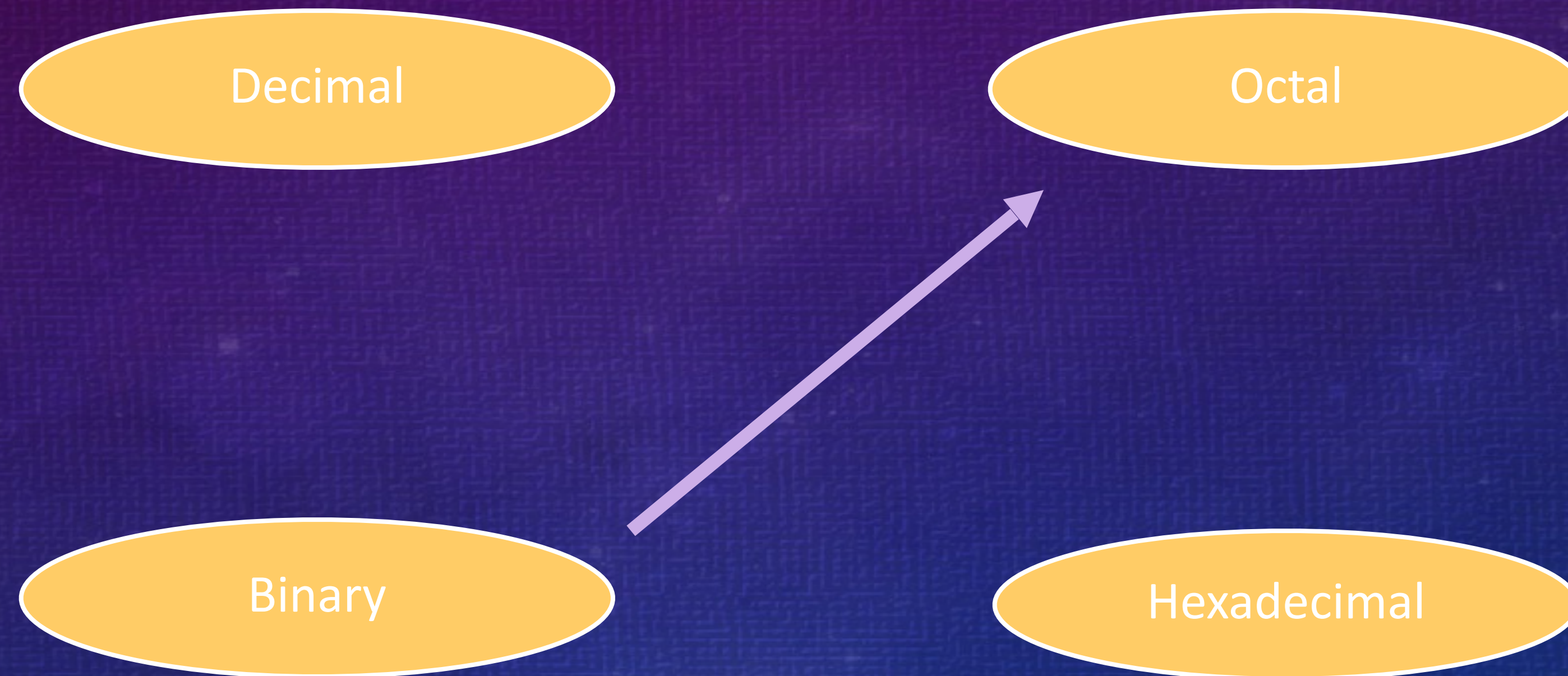
Example

$$1234_{10} = ?_{16}$$

16	1234	
16	77	2
16	4	13 = D
	0	4


$$1234_{10} = 4D2_{16}$$

Binary to Octal

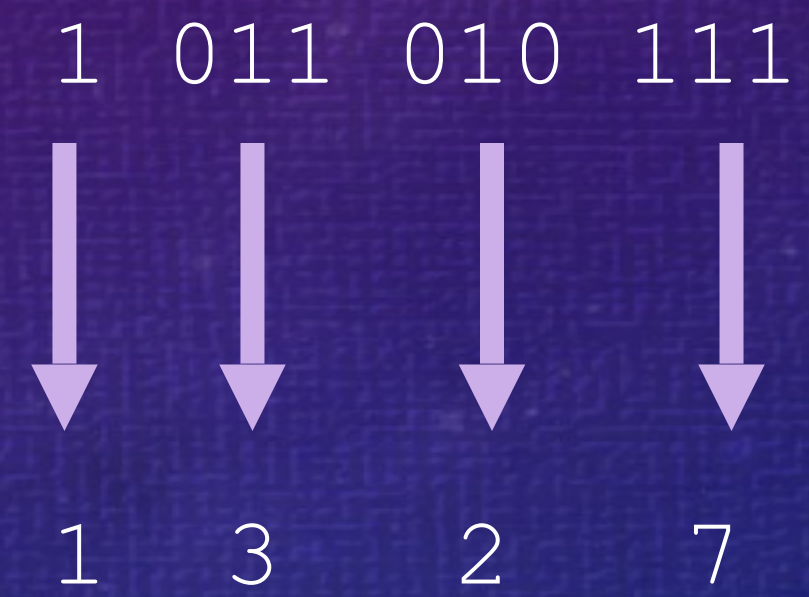


Binary to Octal

- Technique
 - Group bits in threes, starting on right
 - Convert to octal digits

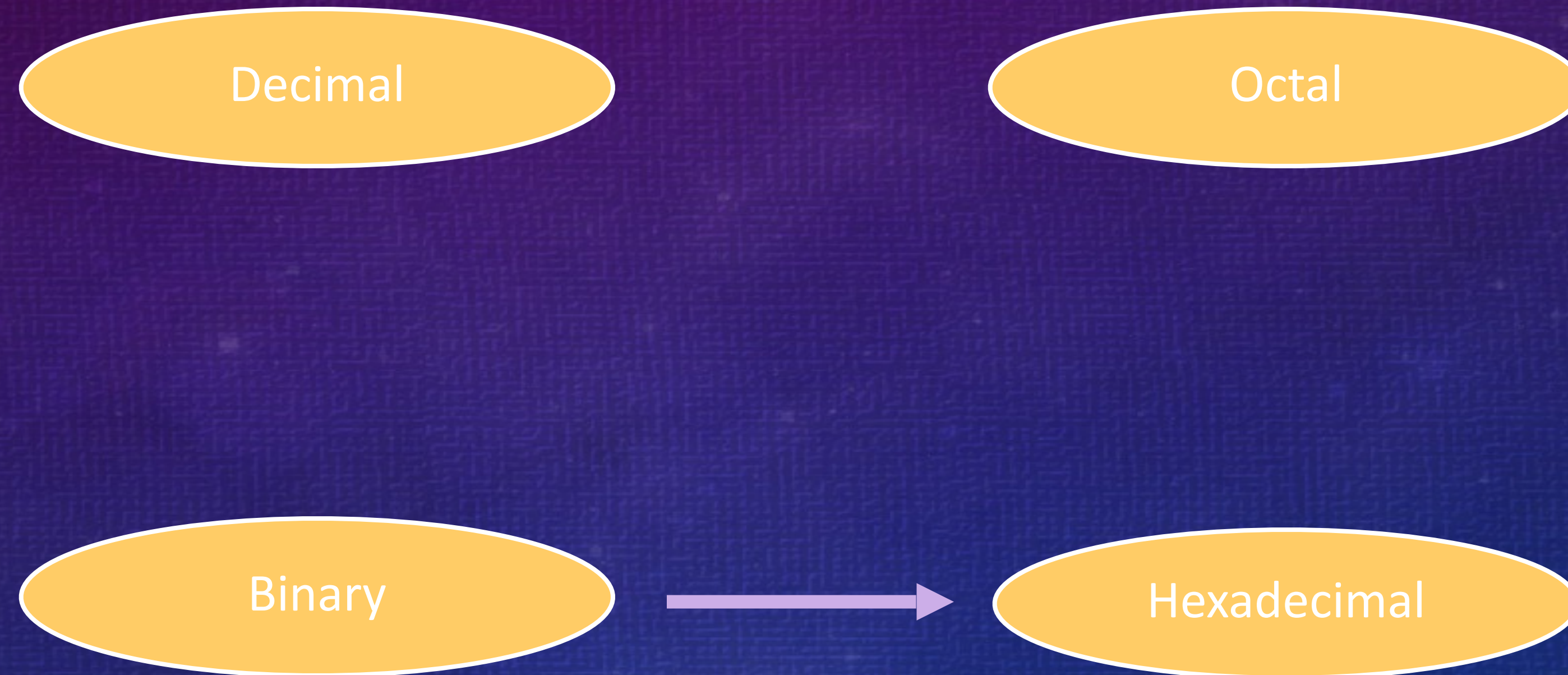
Example

$$1011010111_2 = ?_8$$



$$1011010111_2 = 1327_8$$

Binary to Hexadecimal



Binary to Hexadecimal

- Technique
 - Group bits in fours, starting on right
 - Convert to hexadecimal digits

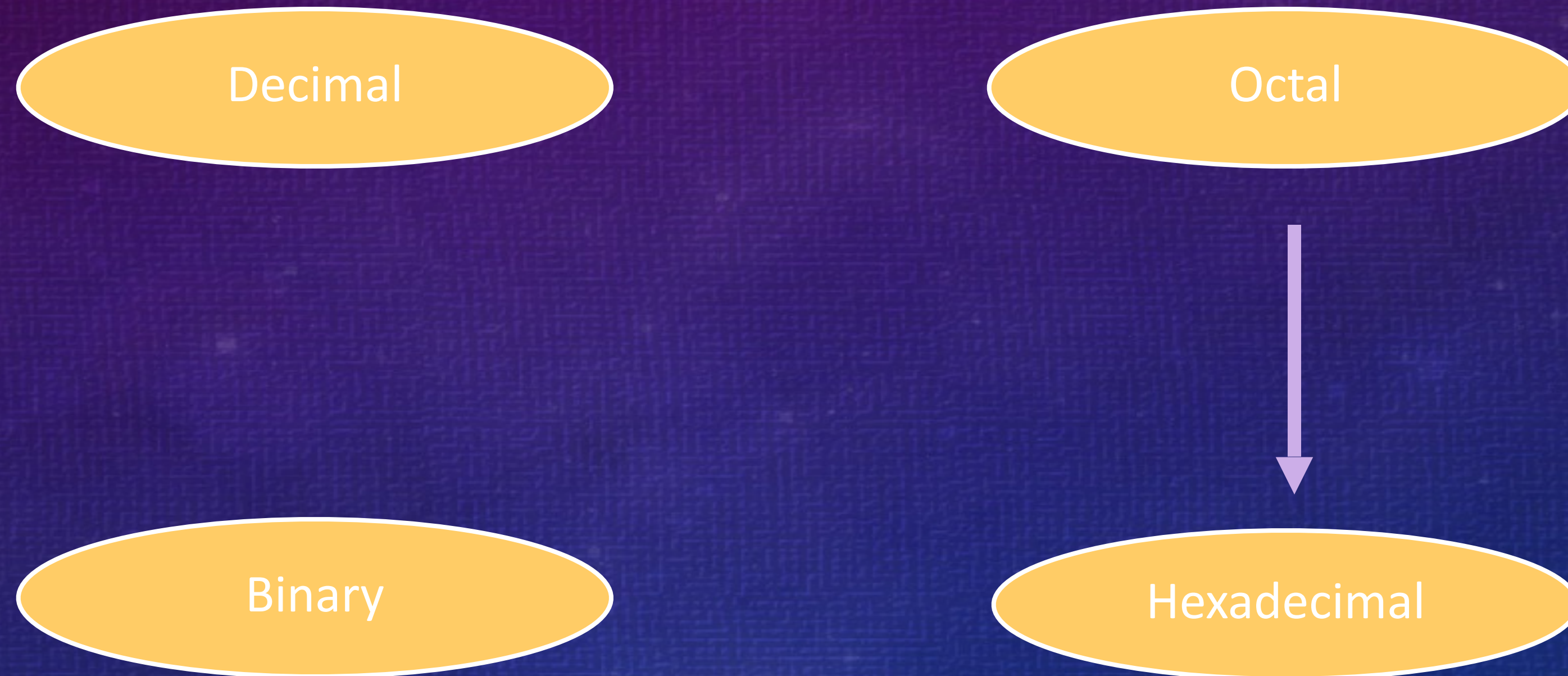
Example

$$1010111011_2 = ?_{16}$$

10	1011	1011
↓	↓	↓
2.	B	B

$$1010111011_2 = 2BB_{16}$$

Octal to Hexadecimal

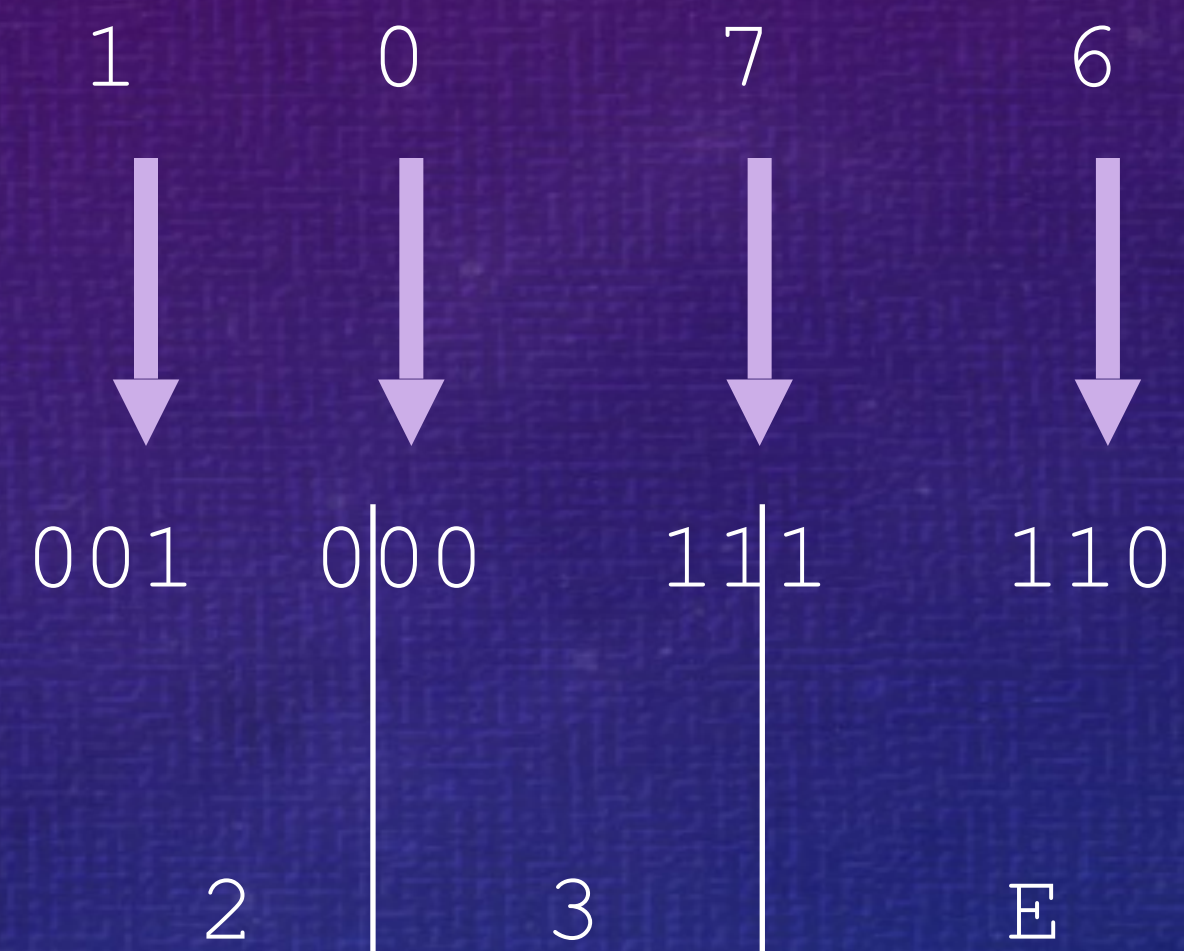


Octal to Hexadecimal

- Technique
 - Use binary as an intermediary

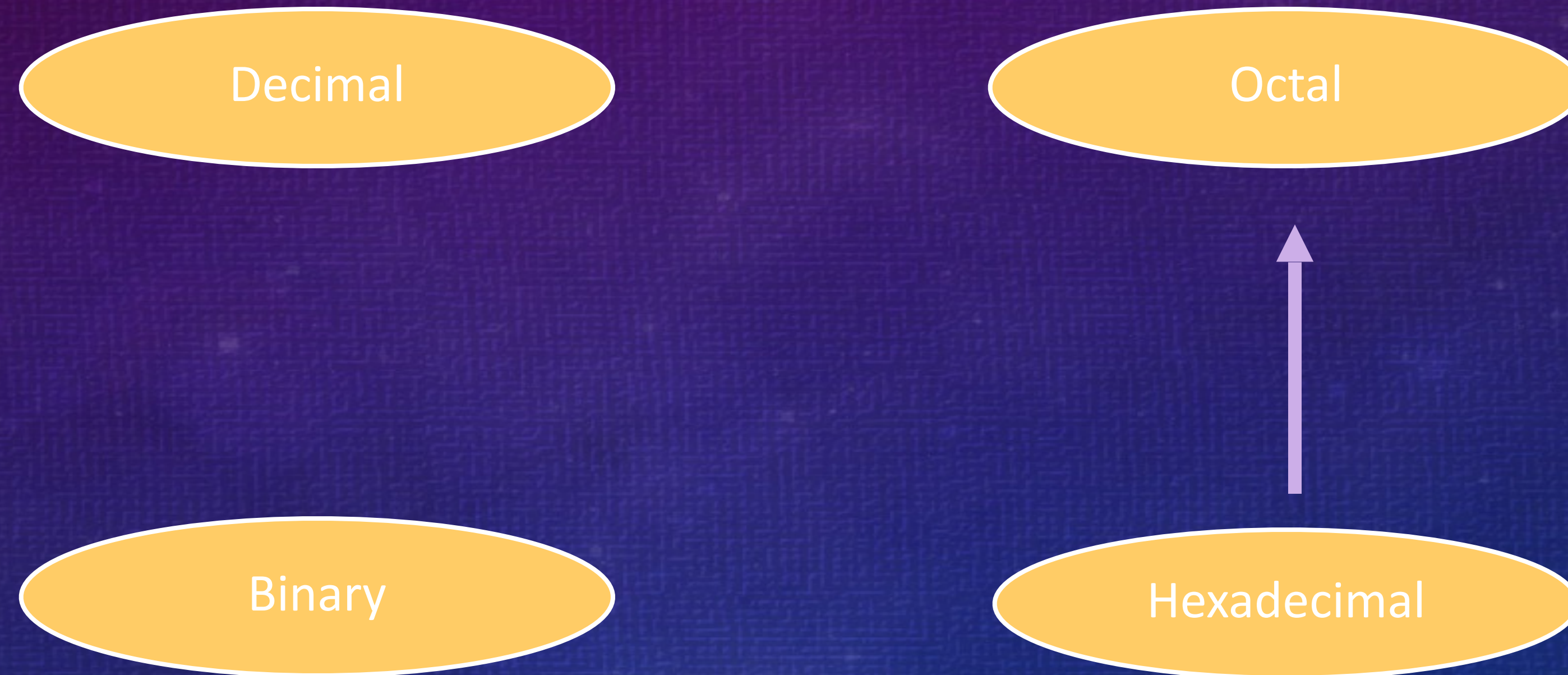
Example

$$1076_8 = ?_{16}$$



$$1076_8 = 23E_{16}$$

Hexadecimal to Octal

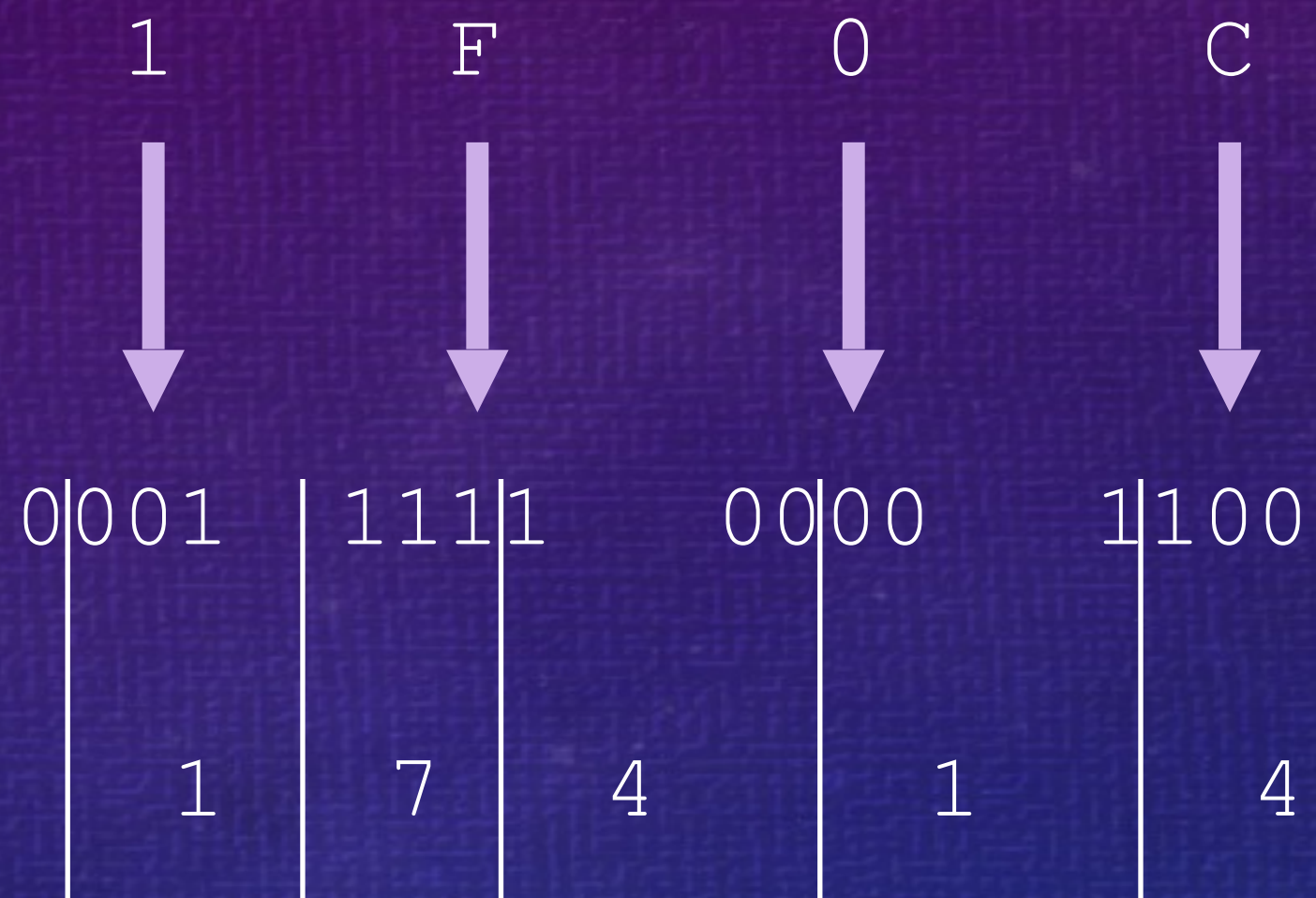


Hexadecimal to Octal

- Technique
 - Use binary as an intermediary

Example

$$1F0C_{16} = ?_8$$



$$1F0C_{16} = 17414_8$$

Exercise – Convert ...

Decimal	Binary	Octal	Hexa- decimal
33			
	1110101		
		703	
			1AF

Don't use a calculator!
