CS303E: Elements of Computers and Programming Functions

Dr. Bill Young
Department of Computer Science
University of Texas at Austin

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We've seen lots of system-defined functions; now it's time to define our own.

General form:

Function

def functionName(list of parameters): # header
 statement(s) # body

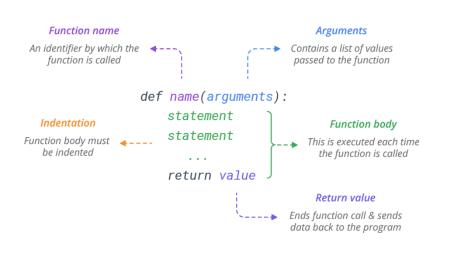
Meaning: a function definition defines a block of code that performs a specific task. It can reference any of the variables in the list of parameters. It may or may not return a value.

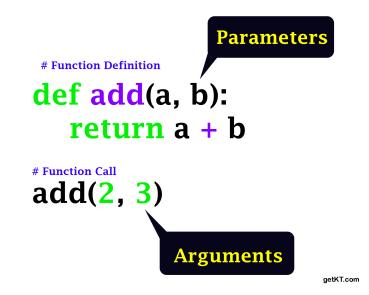
The parameters are **formal parameters**; they stand for arguments passed to the function later.

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Calling a Function





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Function Example

Suppose you want to sum the integers 1 to n.

In file functionExamples.py:

Notice this defines a *function* to perform the task, but *doesn't* actually perform the task. We still have to call/invoke the function with specific arguments.

```
>>> from functionExamples import *
>>> sumToN( 10 )
55
>>> sumToN( 1000 )
500500
>>> sumToN(1000000)
500005000000
```

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Functions

Functional Abstraction

Once we've defined sumToN, we can use it almost as if were a primitive in the language without worry about the details of the definition.

We need to know what it does, but don't care anymore how it does it!

This is called **information hiding** or **functional abstraction**.

Some Observations

Here n is a *formal parameter*. It is used in the definition as a place holder for an *actual parameter* (e.g., 10 or 1000) in any specific call.

sumToN(n) returns an int value, meaning that a call to sumToN can be used anyplace an int expression can be used.

```
>>> print( sumToN( 50 ) )
1275
>>> ans = sumToN( 30 )
>>> print( ans )
465
>>> print( "Even" if sumToN(3) % 2 == 0 else "Odd" )
Even
```

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Functions

Another Way to Add Integers 1 to N

Suppose later we discover that we could have coded sumToN more efficiently (as discovered by the 8-year old C.F. Gauss in 1785):

```
def sumToN( n ):
    """ Sum the integers from 1 to n. """
    return ( n * (n+1) ) // 2
```

Because we defined sumToN as a function, we can just swap in this definition without changing any other code. If we'd done the implementation in-line, we'd have had to go find every instance and change it.

```
>>> sumToN(10)
55
>>> sumToN( 10000000000 )
500000000000050000000000
```

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Function

When you execute a return statement, you return to the calling environment. You may or may not return a value.

General forms:

```
return
return expression
```

A return that doesn't return a value actually returns the constant None.

Every function has an *implicit* return at the end.

```
def printTest ( x ):
 print( x )
```

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About return

```
> python returnExamples.py
Enter an integer or 0 to exit: 7
The square of 7 is: 49
Enter an integer or 0 to exit: -12
The square of -12 is: 144
Enter an integer or 0 to exit: 0
```

A function that "doesn't return a value" actually returns the constant None

In file returnExamples.py:

```
def printSquares():
    """ Compute and print squares until 0 is entered
       by the user. """
   while True:
       num = int(input("Enter an integer or 0 to exit: "))
       if ( num != 0 ):
                              # "if num:" works
            print( "The square of", num, "is:", num ** 2 )
       else:
           return
                                # no value is returned
printSquares()
```

This doesn't return a value, but accomplishes it's function by the "side effect" of printing.

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Some More Function Examples

Suppose we want to multiply the integers from 1 to n:

```
def multToN( n ):
    """ Compute the product of the numbers from 1 to n. """
                             # identity element for *
   prod = 1
   for i in range(1, n+1):
        prod *= i
   return prod
```

Convert fahrenheit to celsius:

```
def fahrToCelsius( f ):
""" Convert fahrenheit temperature value to celsius
    using formula: C = 5/9(F-32). """
    return 5 / 9 * ( f - 32 )
```

Or celsius to fahrenheit:

```
def celsiusToFahr( c ):
    """ Convert celsius temperature value to fahrenheit
        using formula: F = 9/5 * C + 32. """
   return 9 / 5 * c + 32
```

Fahr to Celsius Table

In slideset 1, we showed the C version of a program to print a table of Fahrenheit to Celsius values. Here's a Python version:

In file FahrToCelsius.py:

```
from functionExamples import fahrToCelsius
def printFahrToCelsius():
    """ Print table fahrenheit to celsius for temp
       in [0, 20, 40, ... 300]."""
   lower = 0
   upper = 300
   step = 20
   print("Fahr\tCelsius")
   for fahr in range( lower, upper + 1, step ):
        # Use an already defined function.
       celsius = fahrToCelsius( fahr )
        print( format( fahr, "3d"), "\t", \
               format( celsius, "6.2f") )
                  # not actually necessary
printFahrToCelsius()
```

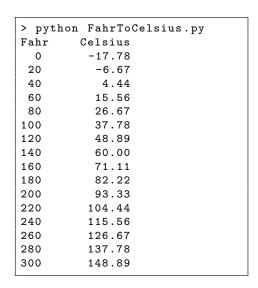
Notice that printFahrToCelsius doesn't return a value.

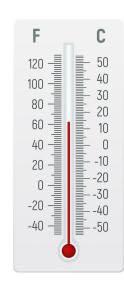
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Let's Take a Break



Running the Temperature Program





Exercise: Do a similar problem converting Celsius to Fahrenheit.

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A Bigger Example: Print First 100 Primes

Suppose you want to print out a table of the first 100 primes, 10 per line.

You could sit down and write this program from scratch, without using functions. But it would be a complicated mess (see section 5.8).

Better to use functional abstraction: find parts of the algorithm that can be coded separately and "packaged" as functions.

2	3	5	7	11	13	17	19	23	29
31	37	41	43	47	53	59	61	67	71
73	79	83	89	97	101	103	107	109	113
127	131	137	139	149	151	157	163	167	173
179	181	191	193	197	199	211	223	227	229
233	239	241	251	257	263	269	271	277	281
283	293	307	311	313	317	331	337	347	349
353	359	367	373	379	383	389	397	401	409
419	421	431	433	439	443	449	457	461	463
467	479	487	491	499	503	509	521	523	541

Top Down Development

Here's some Python-like pseudocode to print 100 primes:

```
def print100Primes():
    primeCount = 0
    num = 0
    while (primeCount < 100):
        if (we've already printed 10 on the current line):
            go to a new line
        nextPrime = ( the next prime > num )
        print nextPrime on the current line
        num = nextPrime
        primeCount += 1
```

Note that most of this is just straightforward Python programming! The only "new" part is how to find the next prime. So we'll make that a *function*.

So let's assume we can define a function:

```
def findNextPrime( num ):
    """ Return the first prime greater than
        num. """
    < body >
```

in such a way that it returns the first prime larger than num.

Is that even possible? Is there always a "next" prime larger than num?

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Top Down Development

Value of Functional Abstraction

So let's assume we can define a function:

```
def findNextPrime( num ):
    """ Return the first prime greater than
        num. """
    < body >
```

in such a way that it returns the first prime larger than num.

Is that even possible? Is there always a "next" prime larger than num?

Yes! There are an infinite number of primes. So if we keep testing successive numbers starting at num + 1, we'll eventually find the next prime. That may not be the most efficient way!

Notice we're following a "divide and conquer" approach: Reduce the solution of our bigger problem into one or more subproblems which we can tackle independently.

It's also an instance of "information hiding." We don't want to think about how to find the next prime, while we're worrying about printing 100 primes. Put that off!



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Looking Ahead

Now solve the original problem, assuming we can write findNextPrime.

In file IsPrime3.py:

```
def print100Primes ():
  """ Print a table of the first 100 primes,
      10 primes per line. """
  primeCount = 0
                               # primes we've found
  onLine = 0
                               # primes printed on line
                               # need next prime > num
  num = 0
  while (primeCount < 100):</pre>
     # Stay on current line?
     if ( onLine >= 10 ):
        print()
        onLine = 0
     # This is the only thing left to define:
     nextPrime = findNextPrime( num )
     num = nextPrime
      primeCount += 1
     print( format( nextPrime, "3d"), end = " " )
     onLine += 1
  print()
```

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How to Find the Next Prime

The next prime (> num) can be found as indicated in the following pseudocode:

```
def findNextPrime( num ):
    if num < 2:
       return 2 as the answer
    else:
       guess = num + 1
       while ( guess is not prime )
           guess += 1
       return guess as the answer
```

Again we solved one problem by assuming the solution to another problem: deciding whether a number is prime.

Can you think of ways to improve this algorithm?

Here's what the output should look like.

```
>>> from IsPrime3 import print100Primes
>>> print100Primes()
             7 11 13 17 19
                                23 29
           43 47 53
    37 41
                       59 61
    79 83 89 97 101 103 107 109 113
127 131 137 139 149 151 157 163 167 173
179 181 191 193 197 199 211 223 227 229
233 239 241 251 257 263 269 271 277 281
283 293 307 311 313 317 331 337 347 349
353 359 367 373 379 383 389 397 401 409
419 421 431 433 439 443 449 457 461 463
467 479 487 491 499 503 509 521 523 541
```

Of course, we couldn't do this if we really hadn't defined findNextPrime. So let's see what that looks like.

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Here's the Implementation

Note that we're assuming we can write:

```
def isPrime( num ):
    """ Boolean test for primality. """
    < body >
```

```
def findNextPrime( num ):
   """ Find the first prime > num. """
   if ( num < 2 ):</pre>
      return 2
   guess = num + 1
   while ( not isPrime( guess ) ):
      guess += 1
   return guess
```

This works (assuming we can define isPrime), but it's pretty inefficient. How could you fix it?

When looking for the next prime, we don't have to test every number, just the odd numbers (after 2).

```
def findNextPrime ( num ):
  """ Find the first prime > num. """
  if ( num < 2 ):</pre>
     return 2
  # If (num >= 2 and num is even), the
  # next prime after num is at least
  \# (num - 1) + 2, which is odd.
  if (num % 2 == 0):
     num -= 1
  guess = num + 2
  while ( not isPrime( guess )):
      guess += 2
  return guess
```

Now all that remains is to write isPrime.

We already solved a version of this in slideset 5. Let's rewrite that code as a Boolean-valued function:

```
def isPrime( num ):
   """ Test whether num is prime. """
   # Deal with evens and numbers < 2.
   if (num < 2 or num % 2 == 0 ):
      return ( num == 2 )
   # See if there are any odd divisors
   # up to the square root of num.
   divisor = 3
   while (divisor <= math.sqrt( num )):</pre>
      if ( num % divisor == 0 ):
         return False
      else:
         divisor += 2
   return True
```

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Testing Our Code

```
>>> from IsPrime3 import findNextPrime, isPrime
>>> findNextPrime( -10 )
>>> findNextPrime( 2 )
>>> findNextPrime( 1000 )
1009
>>> findNextPrime( 100000000 )
100000007
>>> isPrime( 10000007 )
>>> isPrime( 1001 )
False
>>> isPrime( 1003 )
False
>>> isPrime( 1007 )
>>> isPrime( 1009 )
True
```

One More Example

Suppose we want to find and print k primes, starting from a given number:

In file IsPrime3.py:

```
def findKPrimesStartingFrom ( k, num ):
   """ Find the next k primes bigger than num. """
   if (k < 1):
      print( "You asked for zero primes!" )
   else:
      for i in range( k ):
         nextPrime = findNextPrime( num )
         print( nextPrime, end=" " )
         num = nextPrime
      print()
```

Notice that we can use functions we've defined such as findNextPrime and isPrime (almost) as if they were Python primitives.

```
>>> from IsPrime3 import findKPrimesStartingFrom
>>> findKPrimesStartingFrom( -10, 100000000 )
You asked for zero primes!
>>> findKPrimesStartingFrom( 5, -10 )
2 3 5 7 11
>>> findKPrimesStartingFrom( 10, 100000000 )
100000007 100000037 100000039 100000049 100000073 100000081
100000123 100000127 100000193 100000213
```

Functions can return a value or not. A function that doesn't return a value is sometimes called a **procedure**.

Of the functions defined earlier:

- sumToInt, multToN, findNextPrime all return int values
- farhToCelsius and celsiusToFahr return float values
- isPrime returns a bool value
- printSquares, printFahrToCelsius, print100Primes, and findKPrimesStartingFrom don't return a value (return None).

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Let's Take a Break

Positional Arguments



This function has four formal parameters:

```
def functionName ( x1, x2, x3, x4 ):
     < body >
```

Any call to this function should have exactly four actual arguments, which are matched to the corresponding formal parameters:

```
functionName( 9, 12, -3, 10 )
functionName( 'a', 'b', 'c', 'd' )
functionName( 2, "xyz", 2.5, [3, 4, 5] )
```

This is called using **positional** arguments.

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It is also possible to use the formal parameters as keywords.

```
def functionName ( x1, x2, x3, x4 ):
   functionBody
```

These two calls are equivalent:

```
functionName('a', 'b', 'c', 'd')
functionName(x3 = 'c', x1 = 'a', x2 = 'b', x4 = 'd')
```

You can list the keyword arguments in any order, but all must still be specified.

You can mix keyword and positional arguments, but *must* have positional arguments first in order.

```
def functionName ( x1, x2, x3, x4 ):
    functionBody

functionName( 'a', 'b', x4 = 'd', x3 = 'c' ) # OK
functionName( x2 = 'b', x1 = 'a', 'c', 'd' ) # illegal
```

Why do you think they make this rule?

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Default Parameters

You can also specify **default arguments** for a function. If you don't specify a corresponding actual argument, the default is used.

Using Defaults

```
> python RectangleArea.py
width:
               height: 2
                                area: 2
width: 4
               height:
                                area: 10.0
                        2.5
               height:
width:
                                area: 15
       1.2
               height:
width:
                                area: 2.4
               height:
width: 1
                         6.2
                                area: 6.2
```

Notice that you can mix default and non-default arguments, but must define the non-default arguments first.

```
def email (address, message = ""):
```

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All values in Python are objects, including numbers, strings, etc.

When you pass an argument to a function, you're actually passing a **reference** to the object, not the object itself.

There are two kinds of objects in Python:

mutable: you can change them in your program.

immutable: you can't change them in your program.

If you pass a reference to a mutable object, it can be changed by your function. If you pass a reference to an immutable object, it can't be changed by your function.

Туре	Description	Syntax example			
int	An immutable fixed precision number of	42			
	unlimited magnitude				
float	An immutable floating point number	3.1415927			
	(system-defined precision)				
str	An immutable sequence of characters.	'Wikipedia'			
		"Wikipedia"			
		"""Spanning			
		multiple lines"""			
bool	An immutable truth value	True, False			
tuple	Immutable, can contain mixed types	(4.0, 'string', True)			
bytes	An immutable sequence of bytes	b'Some ASCII'			
		b"Some ASCII"			
list	Mutable, can contain mixed types	[4.0, 'string', True]			
set	Mutable, unordered, no duplicates	{4.0, 'string', True}			
dict	A mutable group of key and value pairs	{'key1': 1.0, 3: False}			

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Passing an Immutable Object

Consider the following code:

```
def increment (x):
    x += 1
    print( "Within the call x is: ", x )

x = 3
print( "Before the call x is: ", x )
increment( x )
print( "After the call x is: ", x )

def revList (lst):
    lst.reverse()
    print( "Within the call lst is: ", lst )

lst = [1, 2, 3]
print( "Before the call lst is: ", lst )
revList( lst )
print( "After the call lst is: ", lst )
```

Passing an Immutable and Mutable Objects

Invoking this code:

```
>python Test.py
Before the call x is: 3
Within the call x is: 4
After the call x is: 3
Before the call lst is: [1, 2, 3]
Within the call lst is: [3, 2, 1]
After the call lst is: [3, 2, 1]
```

Notice that the immutable integer parameter to increment was unchanged, while the mutable list parameter to revList was changed.

Variables defined in a Python program have an associated **scope**, meaning the portion of the program in which they are defined.

A global variable is defined outside of a function and is visible after it is defined. Use of global variables is generally considered bad programming practice.

A **local variable** is defined within a function and is visible from the definition until the end of the function.

A local definition overrides a global definition.

A local definition (locally) overrides the global definition.

```
# x is global
x = 1
def func():
   x = 2
                     # this x is local
  print( x )
                     # will print 2
func()
print(x)
                     # will print 1
```

Running the program:

```
> python funcy.py
2
1
```

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Global Variables

```
callCount = 0
                     # global variable
def caller ():
  global callCount # needed to access
  callCount += 1
caller()
print( "callCount = ", callCount )
caller()
print( "callCount = ", callCount )
caller()
print( "callCount = ", callCount )
```

```
> python Test.py
callCount = 1
callCount = 2
callCount = 3
```

What would happen if you took out the line containing global?

Returning Multiple Values

The Python return statement can also return multiple values. In fact it returns a tuple of values.

```
def multipleValues ( x, y ):
 return x + 1, y + 1
print( "Values returned are: ", multipleValues ( 4, 5.2 ))
x1, x2 = multipleValues(4, 5.2)
print( "x1: ", x1, "\tx2: ", x2 )
```

```
Values returned are: (5, 6.2)
x1: 5 x2: 6.2
```

You can operate on this using tuple functions, which we'll cover later in the semester, or assign them to variables.