

Quiz 5

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1. (a)

$$\begin{aligned}
 V_0 &= \oint_C (\mathbf{u} \times \mathbf{B}) \cdot d\mathbf{l} \\
 &= \int_2^{1'} (\hat{x}u \times \hat{z}B_0) \cdot (\hat{y}dl) \\
 &= -u \cdot B_0 h \quad (V)
 \end{aligned}$$

$$(b) \quad P = I'R \quad , \quad I = \frac{V_0}{R} = \frac{-uB_0h}{R} \Rightarrow P = \frac{u^2 B_0^2 h^2}{R} \quad (W)$$

(c) The mechanic power: $P = F \cdot u$

$$\text{The magnetic force: } F = I \cdot \oint_C d\mathbf{l} \times \mathbf{B} = I \cdot \int_2^{1'} d\mathbf{l} \times \mathbf{B} = -\hat{x} I B_0 h$$

$$\text{since } I = -\frac{uB_0h}{R} \Rightarrow F = \hat{x} \cdot \frac{uB_0^2h^2}{R}$$

$$\Rightarrow P = F \cdot u = \frac{u^2 B_0^2 h^2}{R} \quad \text{which is the same as what calculated in (b)}$$

$$2. \quad ① \quad \nabla \times \mathbf{E}' = \eta \nabla \times \mathbf{H} = \eta \cdot j\omega \epsilon \mathbf{E} = -j\omega \mu \left(-\frac{\mathbf{E}}{\eta}\right) = -j\omega \mu \mathbf{H}'$$

$$② \quad \nabla \times \mathbf{H}' = -\frac{1}{\eta} \nabla \times \mathbf{E} = \frac{1}{\eta} j\omega \mu \mathbf{H} = j\omega \epsilon \eta \cdot \mathbf{H} = j\omega \epsilon \mathbf{E}'$$

$$③ \quad \nabla \cdot \mathbf{E}' = \eta \cdot \nabla \cdot \mathbf{H} = 0$$

$$④ \quad \nabla \cdot \mathbf{H} = -\frac{1}{\eta} \nabla \cdot \mathbf{E} = 0$$

Therefore, the four equations also holds for $(\mathbf{E}', \mathbf{H}')$ $\Rightarrow (\mathbf{E}', \mathbf{H}')$ is also the solution.