

VE230: Electromagnetics I

Homework V

Due: July 3, 11.59pm

P.5-6 Lightning strikes a lossy dielectric sphere— $\epsilon = 1.2\epsilon_0$, $\sigma = 10 \text{ (S/m)}$ —of radius 0.1 (m) at time $t = 0$, depositing uniformly in the sphere a total charge 1 (mC) . Determine, for all t ,

- a) the electric field intensity both inside and outside the sphere,
- b) the current density in the sphere.

P.5-8 A d-c voltage of 6 (V) applied to the ends of 1 (km) of a conducting wire of 0.5 (mm) radius results in a current of $1/6 \text{ (A)}$. Find

- a) the conductivity of the wire,
- b) the electric field intensity in the wire,
- c) the power dissipated in the wire,
- d) the electron drift velocity, assuming electron mobility in the wire to be $1.4 \times 10^{-3} \text{ (m}^2/\text{V}\cdot\text{s)}$

P.5-10 The space between two parallel conducting plates each having an area S is filled with an inhomogeneous ohmic medium whose conductivity varies linearly from σ_1 at one plate ($y = 0$) to σ_2 at the other plate ($y = d$). A d-c voltage V_0 is applied across the plates as in Fig.5-11. Determine

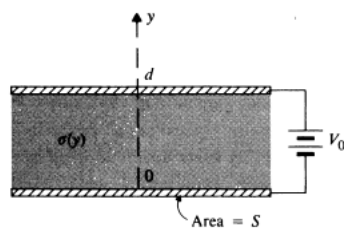


FIGURE 5-11
Inhomogeneous ohmic medium with conductivity $\sigma(y)$ (Problem P.5-10).

- a) the total resistance between the plates,
- b) the surface charge densities on the plates,
- c) the volume charge density and the total amount of charge between the plates.

P.5-22 Assume a rectangular conducting sheet of conductivity σ , width a , and height b . A potential difference V_0 is applied to the side edges, as shown in Fig.5-14. Find

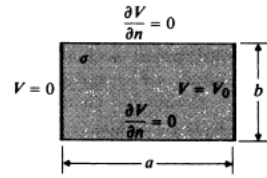


FIGURE 5-14
A conducting sheet (Problem P.5-22).

- a) the potential distribution,
- b) the current density everywhere within the sheet. (*Hint:* Solve Laplace's equation in Cartesian coordinates subject to appropriate boundary conditions.)