ECE 4110/5110

Wednesday, 09/13/23

Handout 8

## Lecture 7: The Poisson Processes

Dr. Kevin Tang

## Related Reading

Bertsekas and Tsitsiklis Section 6.2

## **Definition and Properties**

$$P(k,\tau) = \frac{\lambda^k \tau^k}{k!} e^{-\lambda \tau} \tag{1}$$

Nonoverlapping time sets are independent.

The interarrival time distribution is memoryless.

## Interarrival Time Is Exponentially Distributed

$$f_T(t) = \lambda e^{-\lambda t} \tag{2}$$

The kth Arrival Time Follows Erlang Distribution

$$f_{Y_k}(y) = \frac{\lambda^k y^{k-1} e^{-\lambda y}}{(k-1)!} \tag{3}$$

Splitting and merging of Poisson processes result in Poisson processes