

EDDA Group 29 Assignment 2

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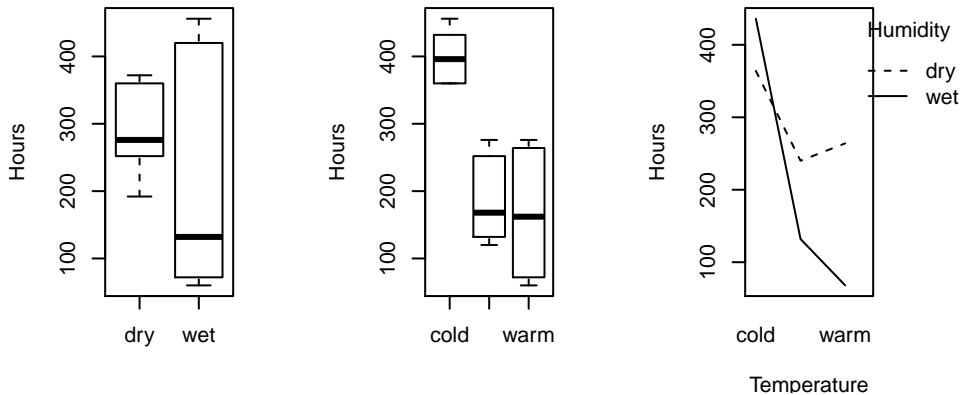
An overview of the R code is shown in the Appendix on page 13.

Exercise 1

a) A randomized design with two categorical factors, with (1) the first factor having three categorical levels, (2) the second factor having two levels and (3) having three samples for each unique category, can be produced with the following R code:

```
I=3; J=2; N=3
rbind(rep(1:I,each=N*J),rep(1:J,N*I),sample(1:(N*I*J)))
```

b) The boxplot and interaction plot below confirms our intuition: (1) a cold environment causes a much slower decay, (2) wet bread has a much wider distribution (variance), (3) on average dry bread decays slower than wet bread, however, (4) wet and cold (frozen) bread has the slowest decay. From the non-parallel lines in the interaction plot and the wide distribution of the wet sample, we conclude that the (wet) humidity amplifies the effect of the temperature and it can thus be explained by the strong interaction between the two factors (opposed to the errors in the measurement).



c) We have three null hypotheses: (1) H_0 : there is no main effect of first factor (humidity), (2) H_0 : there is no main effect of second factor (environment) and (3) H_0 : there is no interactions between the two factors. From the two-way ANOVA result below, we reject all null hypotheses. This means that both factors have a main effect on the decay time of bread, and the factors have an interaction effect.

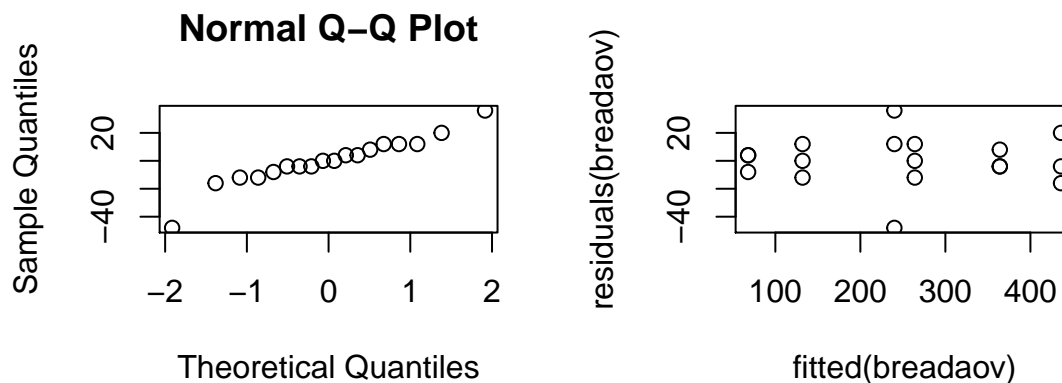
```
## Analysis of Variance Table
##
## Response: hours
##
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)
## humidity	1	26912	26912	62.296	4.316e-06 ***
## environment	2	201904	100952	233.685	2.461e-10 ***
## humidity:environment	2	55984	27992	64.796	3.705e-07 ***

```
## Residuals          12    5184    432
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

d) According to the means of squares, on average the environment has the largest effect on the decay. However, this can not easily be concluded as it is being compared to one base (the first category), instead of a more comprehensive analysis. A different method could be to look at the distribution (mean and sd) of the two factors and simply use a two sample t-test to determine which factor has the slower decay and how significant.

e) The first requirement is that for each unique category, there should be at least 2 samples, which is the case. Then, the most important requirement is that the data among the factors should approximately have equal variances. This has been tested in b) and the conclusion was that they approximately were the same. A different test we can do after the ANOVA test, is check whether the error is normally distributed, which can be expected from a random variable. In the QQ-plot, it can be seen that the residuals are approximately normally distributed. In the fitted residuals plot, it can be seen that the spread is approximately horizontally symmetric among the fitted values, however, there are 2 outliers in the middle.

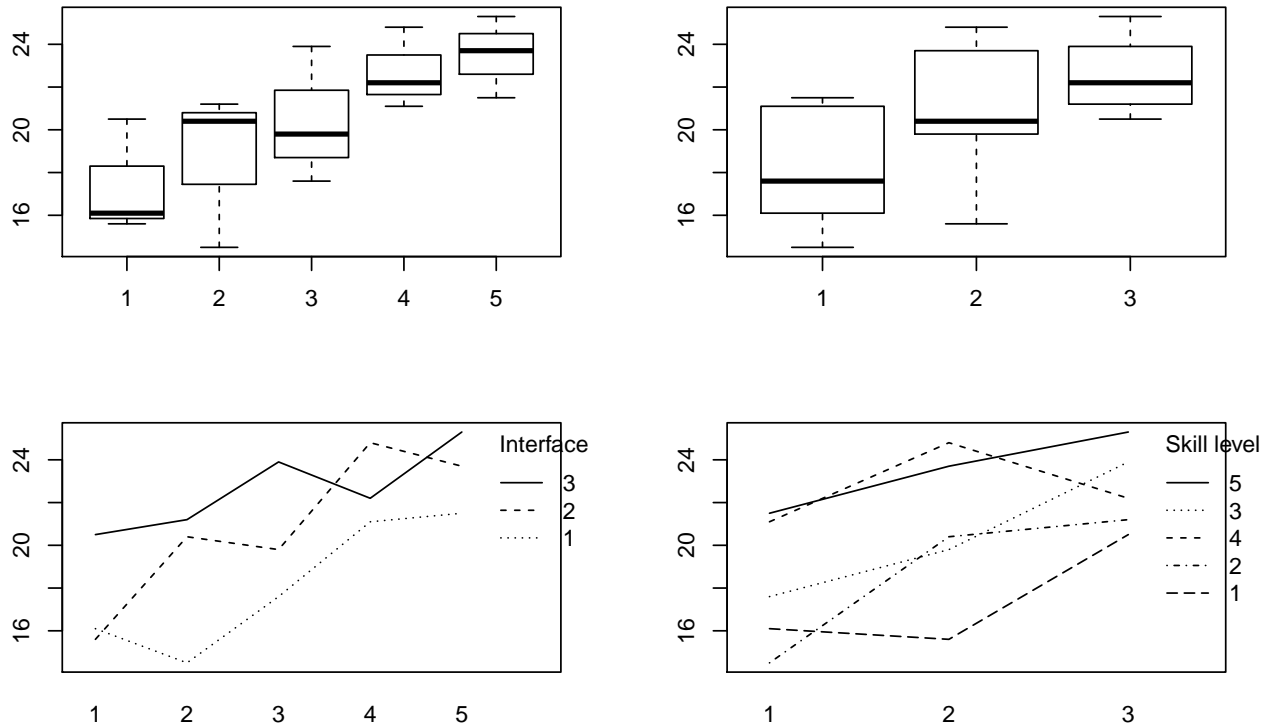


Exercise 2

a) The following code generates a random block design with five blocks, a factor with three levels and one sample per unique category.

```
B=5;
if1 = sample(1:5)
if2 = sample(6:10)
if3 = sample(11:15)
for (i in 1:B) print(c(if1[i], if2[i], if3[i]))
```

b) The boxplots below suggest that indeed the skill level and the interfaces matter for the search time. We see that skill level 1 and interface 1 are the fastest. From the interaction plots below, we observe clear interaction effects. Overall, the factors have the same pattern, namely, all lines start in the lower left corner and end towards the upper right corner. However, they are not perfectly parallel, this can be explained by the small sample sizes which cause local irregularities. Thus, we conclude that there is no interaction between the two factors.



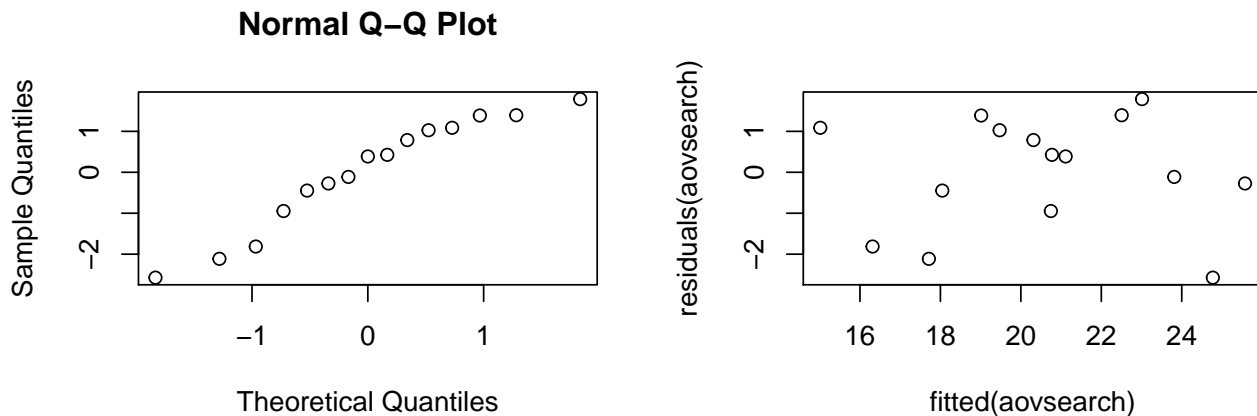
c) H_0 : search time is the same for all interfaces. From the ANOVA results below, it can be concluded that H_0 is rejected. This means that the search time is not the same for all interfaces. Furthermore, we can estimate the time it takes for a user with skill level 3 to find a product using interface 2 by looking at the summary table and adding the coefficients of these two categories to the intercept. In this case, that would be $15.015 + 3.033 + 2.7 = 20.748$.

```
## Analysis of Variance Table
##
## Response: time
##           Df Sum Sq Mean Sq F value    Pr(>F)
## interface  2  50.465  25.2327   7.8237 0.01310 *
## skill      4  80.051  20.0127   6.2052 0.01421 *
## Residuals  8   25.801   3.2252
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

##
## Call:
## lm(formula = time ~ interface + skill, data = search)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.5733 -0.6967  0.3867  1.0567  1.7867
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   15.013      1.227   12.238 1.85e-06 ***
## interface2     2.700      1.136    2.377  0.04474 *
## interface3     4.460      1.136    3.927  0.00438 **
## skill2         1.300      1.466    0.887  0.40118
## skill3         3.033      1.466    2.069  0.07238 .
##
```

```
## skill4      5.300      1.466      3.614  0.00684 **
## skill5      6.100      1.466      4.160  0.00316 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.796 on 8 degrees of freedom
## Multiple R-squared:  0.8349, Adjusted R-squared:  0.7111
## F-statistic: 6.745 on 6 and 8 DF,  p-value: 0.008395
```

d) The QQ-plot of the residuals below looks normally distributed, which is good. The fitted residuals do not depict any outliers.



e) The result of the Friedman test is the same as the ANOVA test: we reject the H_0 mentioned before, thus, there is a difference in search times.

```
##
## Friedman rank sum test
##
## data:  search$time, search$interface and search$skill
## Friedman chi-squared = 6.4, df = 2, p-value = 0.04076
```

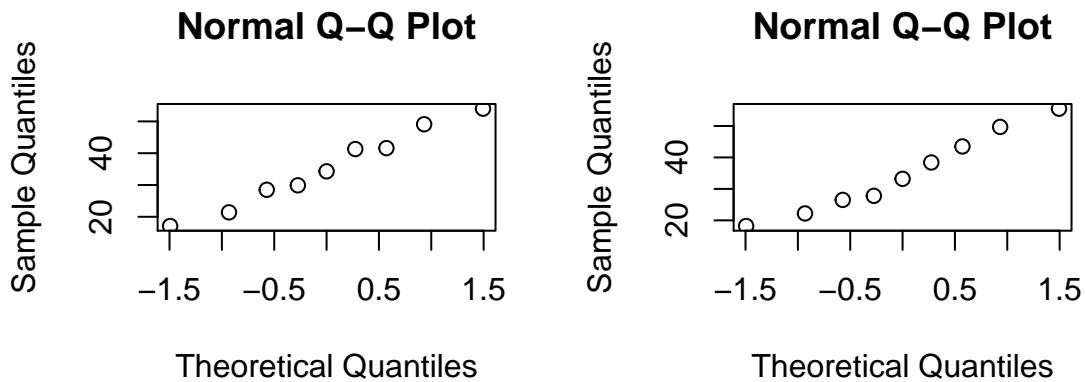
f) The one-way ANOVA returns no significant difference in the search time between the interfaces. This result is not very useful, because (1) we removed a lot of information from the model and (2) the model now assumes that the block is a random selection of all available blocks, which is not the case because the blocks were fixed/predetermined.

```
## Analysis of Variance Table
##
## Response: time
##          Df Sum Sq Mean Sq F value Pr(>F)
## interface  2  50.465   25.233   2.8605 0.09642 .
## Residuals 12 105.852    8.821
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Exercise 3

a) First, we evaluate normality of the dataset. From the QQ-plots below, we conclude that both treatment samples are normally distributed. There are three hypotheses: (1) H_0 (id) : there is no difference in milk production between cows, (2) H_0 (per) : there is no difference in milk production in different periods and (3) H_0 (treatment) : there

is no difference in milk production with different treatment. From the ANOVA results below, we can conclude that within-cow variation (see variable “id”) the milk production differs. Because the p-value for id is less than the significance level of 0.05, therefore, the first H_0 is rejected. Furthermore, from the summary, we can conclude that most of the cows (except id4) are different from the cow with id1. Afterwards, we could see p-value for per is less than 0.05, so we reject the second H_0 which means that whether a cow is going through the first period or second seems to make a difference. Furthermore, as the p-value of treatment is equal to 0.51654, we do not reject the third H_0 . This means that treatment A does not significantly differ from treatment B. This could be seen from the second table (treatment B). In conclusion, the type of feedingstuffs doesn’t influence the milk production. And the summary below indicates that there is no significant difference in milk production.



```
## Analysis of Variance Table
##
## Response: milk
##      Df Sum Sq Mean Sq F value    Pr(>F)
## id      8 2467.47  308.434  124.4832 7.494e-07 ***
## per      1   24.50   24.500    9.8881  0.01628 *
## treatment 1    1.16    1.156    0.4666  0.51654
## Residuals 7   17.34    2.478
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

##
## Call:
## lm(formula = milk ~ id + per + treatment, data = cow)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.2600 -0.4375  0.0000  0.4375  2.2600
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   30.3000     1.2444   24.349 5.02e-08 ***
## id2            23.0000     1.5741   14.612 1.68e-06 ***
## id3            11.1500     1.5741    7.084 0.000196 ***
## id4            -1.3500     1.5741   -0.858 0.419480
## id5            -7.0500     1.5741   -4.479 0.002870 **
## id6            23.4500     1.5741   14.898 1.47e-06 ***
## id7            13.5500     1.5741    8.608 5.69e-05 ***
## id8             4.9000     1.5741    3.113 0.017011 *
## id9           -11.2000     1.5741   -7.115 0.000191 ***
```

```
## per2          -2.3900      0.7466  -3.201 0.015046 *
## treatmentB   -0.5100      0.7466  -0.683 0.516536
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.574 on 7 degrees of freedom
## Multiple R-squared:  0.9931, Adjusted R-squared:  0.9832
## F-statistic: 100.6 on 10 and 7 DF,  p-value: 1.349e-06
```

b) In this exercise, we model the cows effect as a random effect by using the function lmer.

```
## Loading required package: Matrix

## Linear mixed model fit by maximum likelihood ['lmerMod']
## Formula: milk ~ treatment + order + per + (1 | id)
## Data: cow
##
##      AIC      BIC   logLik deviance df.resid
##  119.3   124.7   -53.7   107.3      12
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -1.53112 -0.37104  0.02686  0.26748  1.72489
##
## Random effects:
## Groups   Name      Variance Std.Dev.
## id       (Intercept) 133.145  11.539
## Residual                1.927   1.388
## Number of obs: 18, groups: id, 9
##
## Fixed effects:
##              Estimate Std. Error t value
## (Intercept)  38.5000     5.8110   6.625
## treatmentB   -0.5100     0.6585  -0.775
## orderBA      -3.4700     7.7685  -0.447
## per2         -2.3900     0.6585  -3.630
##
## Correlation of Fixed Effects:
##              (Intr) trtmnB ordrBA
## treatmentB -0.063
## orderBA    -0.743  0.000
## per2       -0.063  0.111  0.000
```

Based on the three p-values below, first we do not reject H_0 for treatment. This means that treatment is not important. Secondly, we do not reject H_0 for order. Therefore, the order of treatment AB is not important. Finally we reject H_0 for per, which means whether a cow is going through the first treatment or second is important. The results are the same as the result in a).

```
## Data: cow
## Models:
## cowlmerTreatment: milk ~ order + per + (1 | id)
## cowlmer: milk ~ treatment + order + per + (1 | id)
##              Df      AIC      BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## cowlmerTreatment  5 117.89 122.34 -53.946   107.89
## cowlmer           6 119.31 124.65 -53.656   107.31 0.5807    1    0.446
```

```
## Data: cow
## Models:
## cowlmerOrder: milk ~ treatment + per + (1 | id)
## cowlmer: milk ~ treatment + order + per + (1 | id)
##           Df      AIC      BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## cowlmerOrder  5 117.51 121.96 -53.755   107.51
## cowlmer       6 119.31 124.65 -53.656   107.31 0.1973      1    0.6569

## Data: cow
## Models:
## cowlmerPer: milk ~ treatment + order + (1 | id)
## cowlmer: milk ~ treatment + order + per + (1 | id)
##           Df      AIC      BIC logLik deviance Chisq Chi Df Pr(>Chisq)
## cowlmerPer   5 125.43 129.88 -57.714   115.43
## cowlmer      6 119.31 124.65 -53.656   107.31 8.1151      1    0.00439 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

c) From the p-value below we do not reject H_0 for treatment. This means the treatment is not important. From previous analysis, the same conclusion was reached. Given the design, it is inappropriate to use the paired t-test. Since the previous analysis shows that factors such as per have a significant effect on the milk production, it might be unwise to ignore such factors.

```
##
## Paired t-test
##
## data:  milk[treatment == "A"] and milk[treatment == "B"]
## t = 0.22437, df = 8, p-value = 0.8281
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -2.267910  2.756799
## sample estimates:
## mean of the differences
##           0.2444444
```

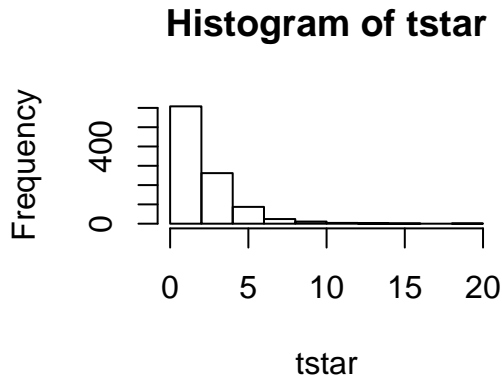
Exercise 4

a) We created a data frame that contains two columns: nausea and medicine. For patients who suffer from nausea, the variable nausea is set to 1. For patients who do not suffer from nausea, the variable is set to 0. We validated that the newly constructed data frame is similar to the dataset by comparing the output of the xtabs function to the original data.

```
##           nausea
## medicine      0    1
## Chlorpromazine 100 52
## Pentobarbital (100mg) 32 35
## Pentobarbital (150mg) 48 37
```

b) We perform a permutation test to test H_0 : the medicines work equally well against nausea. To perform this test, we create 1000 random samples (permutations) of the medication data in which the order varies. We match these permutations of the medication data to the ordered nausea data and calculate the chi-square test statistic. The results of the test statistics of the permutations are shown in the histogram below. The result of the chi-square test statistic of the original data is 6.63. We observe that this value deviates from most values in the histogram. To confirm this, we calculated that the p-value is equal to 0.029. The p-value is smaller than the significance level

of 0.05, therefore, H_0 is rejected and we can conclude that the different medicines do not work equally well against nausea.

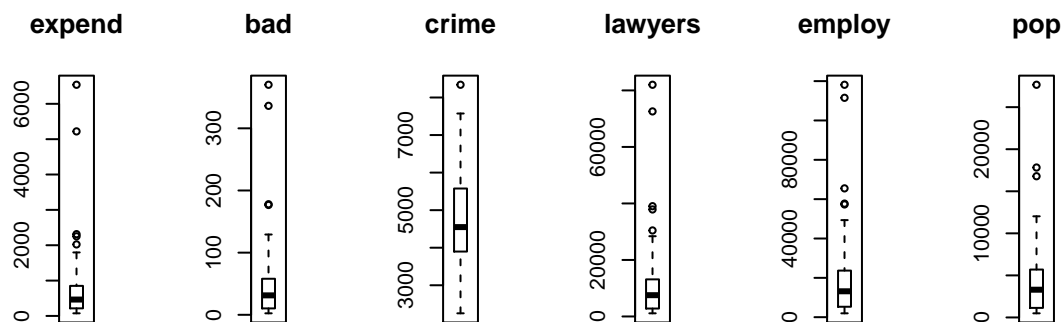
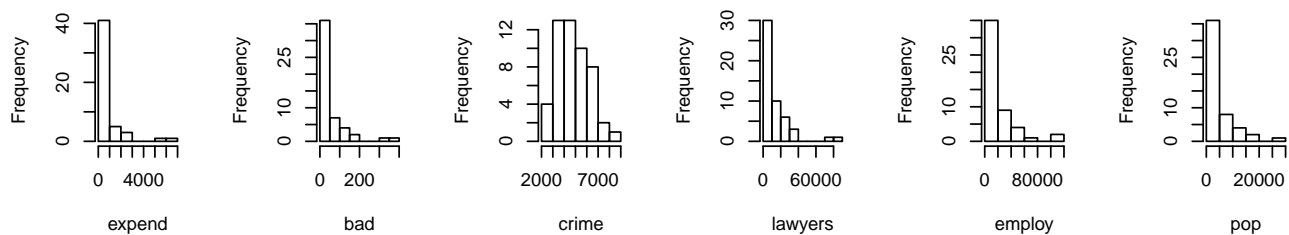
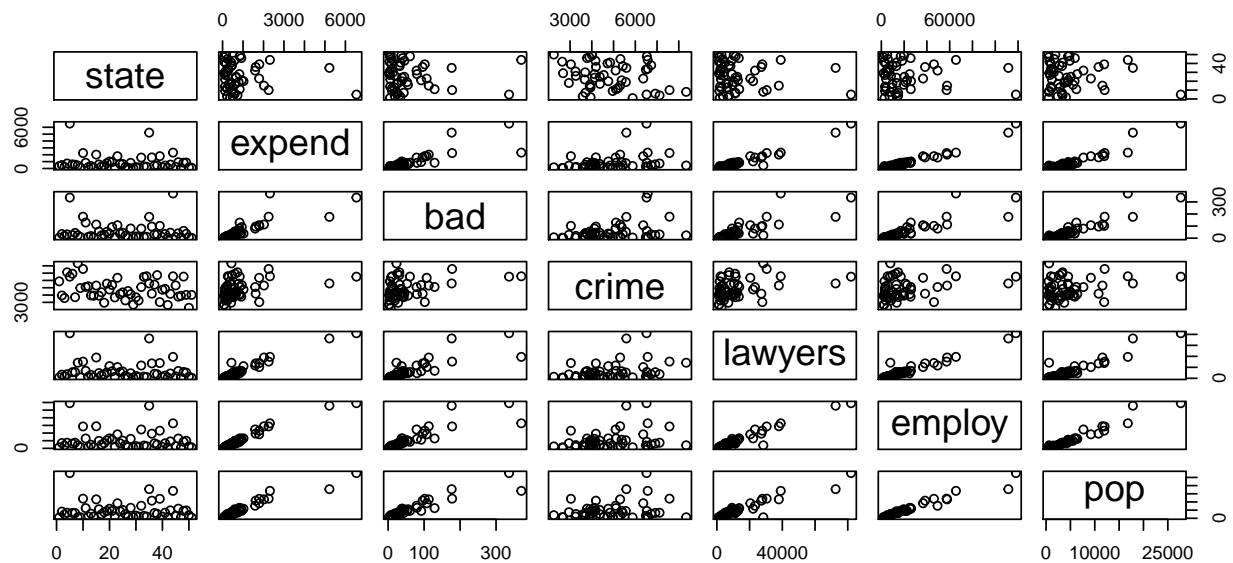


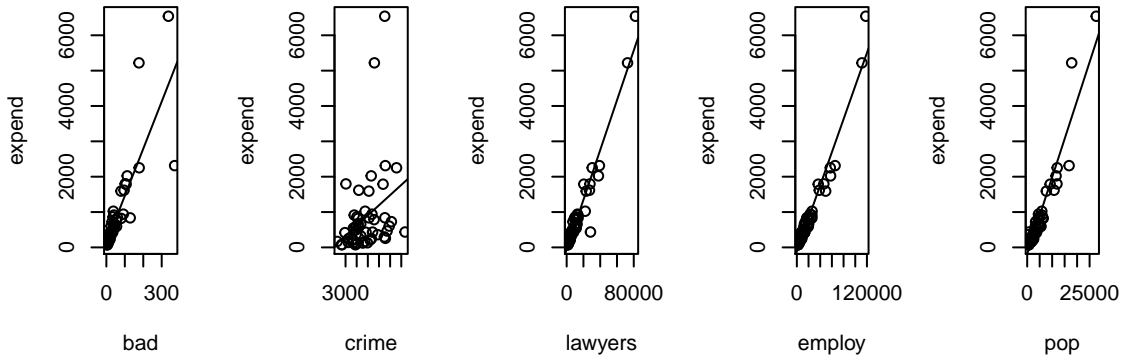
c) When performing the chi-squared test, we observe that the p-value is equal to 0.03643. This is smaller than the significance level of 0.05, therefore, H_0 (the medicines work equally well against nausea) is rejected. This is a similar outcome to the permutation test, however, the p-values do differ. The values lie close to each other as both tests are valid in this situation and compare the proportion of expected outcomes (when assuming no dependence) to the actual outcome. The difference can be explained by the different way of calculating the p-value. Using the permutation test, the p-value is calculated by calculating the number of times that the test statistics of the permuted data is smaller than the test statistic of the original data. Using the chi-squared test, the p-value is calculated by comparing the proportion of rows and columns of independent data to the proportion of rows and columns of the actual data.

```
##
## Pearson's Chi-squared test
##
## data:  xtabs(~patientdata$medicine + patientdata$nausea)
## X-squared = 6.6248, df = 2, p-value = 0.03643
```

Exercise 5

a) First, we make a graphical summary of the data by plotting each variable against the others in scatterplots. Looking at the plots, we observe that `expend`, `lawyers`, `employ` and `pop` all approximate a linear relationship with each other. Furthermore, `state` and `crime` have nonlinear relationships with all the other variables. Lastly, the variable `bad` can be argued to have a weak linear relationship with the variables `expend`, `lawyers`, `employ` and `pop`. Thereafter, we constructed histograms of the numerical data. Looking at the histograms, it is interesting to see that almost all variables (`expend`, `bad`, `lawyers`, `employ` and `pop`) follow a similar pattern, namely, the lowest value appears frequently and as the value increases, the frequency decreases steeply. Except for a few outliers of frequently occurring high values. In contrast, the variable `crime` shows a different pattern. Namely, the values in the middle occur also relatively frequently. But the rule: as the value increases, the frequency decreases, applies as well. Afterwards, we constructed boxplots of the data. Again, we observe a similar pattern of all variables except the variable `crime`. `Crime` is more evenly distributed and contains fewer outliers. The other variables are skewed towards the lower values combined with outlying higher values. To explore these outliers further and in order to build an intuition of the linear relationship between the response variable (`expand`) and the explanatory variables, we zoomed in on the relevant scatter plots that were presented above. From these plots, we observe a strong linear relationship between the response variable `expend` and the variables: `bad`, `lawyers`, `employ` and `pop`. When plotting the simple regression models in these scatterplots, we observe that the outliers follow the linear pattern.





A potential point is an outlier in an explanatory variable. The effect can be studied by fitting the model with and without the potential point. If the estimated parameters change drastically when removing the potential point, the observation is called an influence point. Using the Cook's formula, the distance of an observation on the predictions can be calculated. Whenever the Cook's distance for an observation approximates or is larger than 1, the observation can be considered to be an influence point. As we have not constructed a model yet, we analyse the potential and influence points of our chosen model in c). Another relevant concept is collinearity. This is the problem of linear relations between explanatory variables. Collinearity can be detected by a straight line in a scatter plot or by calculating the correlation coefficient. Looking at the scatter plots of the data, we suspect collinearity between the variables bad, lawyers, employ and pop. We confirm this by calculating the correlation coefficients of all possible variable combinations. Looking at the output below, we observe that all the combinations of the variables lawyers, employ and pop have a correlation coefficient above 93. Thus, we conclude that these variables have a collinear relation. The variable bad has a weaker collinear relation with the variables lawyers, employ and pop, namely, ranging from 0.83 to 0.93. Lastly, the variable crime has no collinear relation with any of the other variables. When collinearity is detected among variables, we should avoid having both explanatory variables in the model.

```
##          bad crime lawyers employ  pop
## bad      1.00  0.37    0.83   0.87 0.92
## crime    0.37  1.00    0.38   0.31 0.28
## lawyers  0.83  0.38    1.00   0.97 0.93
## employ   0.87  0.31    0.97   1.00 0.97
## pop      0.92  0.28    0.93   0.97 1.00
```

b) To fit a linear regression model to the data, first, we start with the step-up method. Using this method, we start by fitting all possible simple linear regression models and calculate the determination coefficient (R^2). The results are shown in the table below (Round 1). Looking at this table, we observe that employ has the largest value of R^2 (0.954) and is thus selected. Therefore, we add the remaining variables to construct a model with the variable employ. The results are shown in the table below (Round 2). We observe that the model that is constructed using the variables employ and lawyers has the highest value of R^2 (0.9632). This value is also higher than the R^2 value of the previous model (0.954) and is significant (the p-values are smaller than the significance level of 0.05). For this reason, we extend the model with the remaining variables. The results are shown in the table below (Round 3). The table constructed using the variables employ, lawyers and bad has the highest value of R^2 (0.9639). However, the result is insignificant (p-value is equal to 0.34496), therefore, the method stops. The resulting model (expend \sim lawyers + employ) is $\text{expend} = -1.107e^{+02} + 2.686e^{-02} * \text{lawyers} + 2.971e^{-02} * \text{employ} + \text{error}$.

Round 1

Explanatory Variable	bad	crime	lawyers	employ	pop
Multiple R-squared	0.6964	0.1119	0.9373	0.954	0.9073

Round 2				
Explantory Variables	employ + bad	employ + crime	employ + lawyers	employ + pop
Multiple R-squared	0.9551	0.9551	0.9632	0.9543

Round 3

Explantory Variables	employ + lawyers + bad	employ + lawyers + crime	employ + lawyers + pop
Multiple R-squared	0.9639	0.9632	0.9637

Second, we use the step-down method. This method starts with fitting all explanatory variables in the so-called full model. In each iteration, one explanatory variable is removed. In Round 1, we observe that the variable crime has the highest p-value, $0.25534 > 0.05$, therefore, the variable crime will be removed. In Round 2, pop has the highest p-value, $0.06012 > 0.05$, therefore, the variable pop will be removed. In Round 3, bad has the highest p-value, $0.34496 > 0.05$, therefore, the variable bad will be removed. In Round 4, lawyers has the highest p-value, $0.00113 < 0.05$, therefore, the variable will not be removed and the method stops. This results in the model $\text{expend} = -1.107e^{+02} + 2.686e^{-02} * \text{lawyers} + 2.971e^{-02} * \text{employ} + \text{error}$. The step-up and step-down model resulted in the same model. Note that the explanatory variables in this model are linearly correlated, this is bad practise for a regression model. If the step-up and step-down resulted in different models, the one with the highest value of R^2 , the lowest number of explanatory variables and no collinear variables would be preferred.

Round 1	expend ~ bad +	crime +	lawyers +	employ +	pop
Explantory Variable	bad	crime	lawyers	employ	pop
p-value	0.02719	0.25534	0.00592	0.00354	0.03184

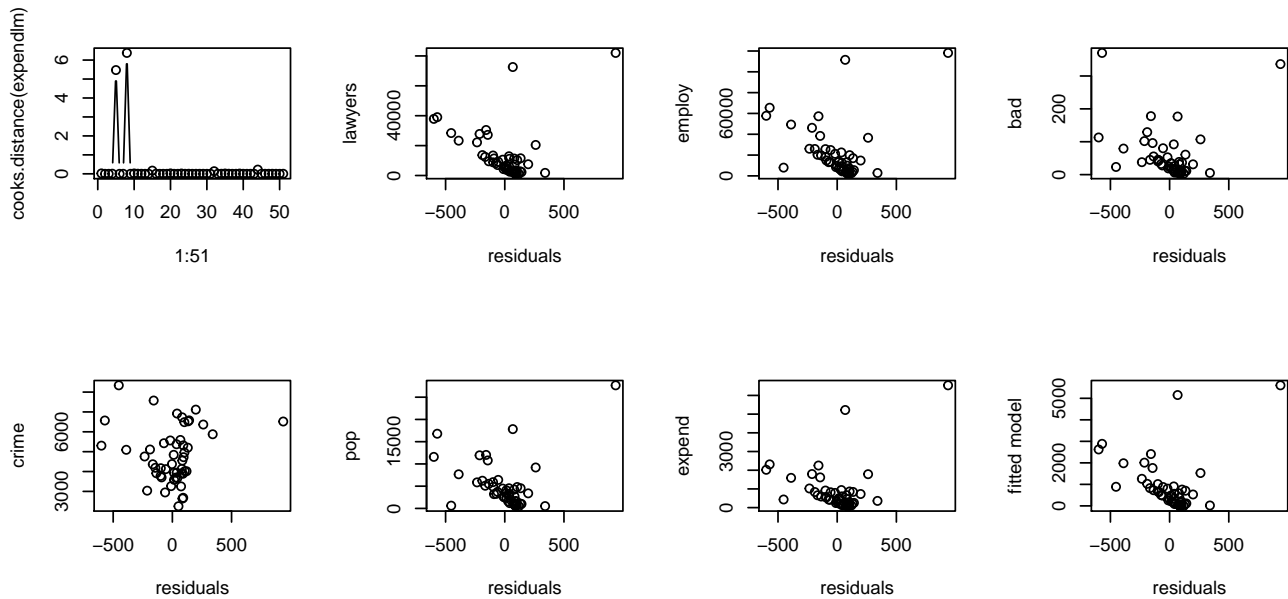
Round 2	expend ~ bad +	lawyers +	employ +	pop
Explantory Variable	bad	lawyers	employ	pop
p-value	0.05402	0.00106	0.00380	0.06012

Round 3	expend ~ bad +	lawyers +	employ
Explantory Variable	bad	lawyers	employ
p-value	0.34496	0.00147	$1.2e^{-06}$

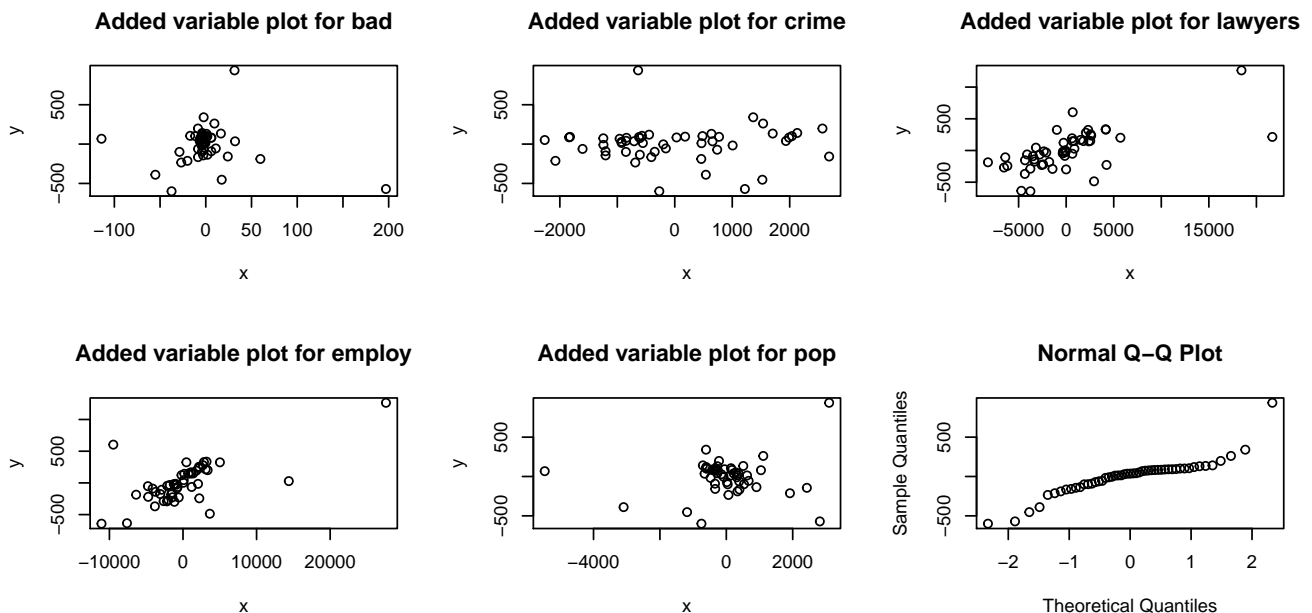
Round 4	expend ~ lawyers +	employ
Explantory Variables	lawyers	employ
p-value	0.00113	$4.89e^{-07}$

c) Coming back to question a), we investigate the potential and influence points of the model ($\text{expend} \sim \text{lawyers} + \text{employ}$). When ordering the residuals of the model, we observe the presence of outliers. Thus, we test if these potential points are influence points using the Cook's distance. We calculate that the data on the 5th and 8th position have a Cook's distance larger than 1. This is also visible from the plot of the Cook's distances. Hence, we conclude that the data on position 5 and 8 are influence points. Now, we check the model assumptions (linearity of the relation and normality of the errors) using both graphical and numerical tools. First, we construct the scatter plot of the residuals against each explanatory variable that is in the model (lawyers and employ) seperately. We observe a cluster around zero and relatively little spread, except for two outliers. Second, we construct the scatter plots of the residuals against each explanatory variable that is not in the model (bad, crime and pop) seperatly. The outputs of bad and pop have a similar pattern as the previous plots. This can be explained by the fact that

these variables are all collinear (see a). Except for the variable crime, this plot shows more spread. When looking at the patterns, we do not observe a linear relation and therefore should not include more variables into the model. Third, we construct the scatter plot of the residuals against the response variable (expend) and the fitted model. We observe little spread as in both plots there is a cluster around zero except the two reoccurring outliers.



Afterwards, we construct the added variable plots. In these plots, the residuals of the explanatory variables are plotted against the residuals of the model without that specific variable. This shows the effect of adding an explanatory variable to the model. Looking at the figure, we observe that the added variable plots for bad, lawyers, employ and pop are clustered around zero, again, with the exception of two outliers. The added variable plot for crime shows more spread. Lastly, we check the normality assumption by constructing a normal QQ-plot. We cannot assume normality as the QQ-plot does not approximate a straight line, this means that the model is invalid. In conclusion, the model is flawed. First of all, the explanatory variables lawyers and employ are collinear. Second, the scatter plots of the residuals show little spread and are clustered around zero. Lastly, the residuals are not normally distributed. Therefore, in a next iteration the model should be adjusted.



Appendix: R code

```
# --- Exercise 1 --- #
#A
I=3; J=2; N=3
rbind(rep(1:I,each=N*J),rep(1:J,N*I),sample(1:(N*I*J)))
#B
bread = read.table("bread.txt", header = TRUE)
par(mfrow=c(1,3))
boxplot(hours ~ humidity, data = bread, ylab = "Hours")
boxplot(hours ~ environment, data = bread, ylab = "Hours")
interaction.plot(bread$environment, bread$humidity, bread$hours, xlab = "Temperature",
  ylab = "Hours", trace.label = "Humidity")
#C
breadaov=lm(hours~humidity*environment, data = bread);
anova(breadaov)
#E
par(mfrow=c(1,2))
qqnorm(residuals(breadaov))
plot(fitted(breadaov),residuals(breadaov))

# --- Exercise 2 --- #
#A
B=5;
if1 = sample(1:5)
if2 = sample(6:10)
if3 = sample(11:15)
for (i in 1:B) print(c(if1[i], if2[i], if3[i]))
#B
search = read.table("search.txt", header = TRUE)
par(mfrow=c(2,2))
boxplot(time~skill, data=search)
boxplot(time~interface, data=search)
interaction.plot(search$skill,search$interface, search$time, xlab = "Skill level",
  ylab = "Time", trace.label = "Interface")
interaction.plot(search$interface,search$skill, search$time, xlab = "Interface",
  ylab = "Time", trace.label = "Skill level")
#C
search$skill = factor(search$skill)
search$interface = factor(search$interface)
aovsearch=lm(time~interface+skill, data=search)
anova(aovsearch)
summary(aovsearch)
#D
par(mfrow=c(1,2))
qqnorm(residuals(aovsearch))
plot(fitted(aovsearch),residuals(aovsearch))
#E
friedman.test(search$time,search$interface,search$skill)
#F
aovsearch2=lm(time~interface, data=search)
anova(aovsearch2)

# --- Exercise 3 --- #
# A
cow = read.table("cow.txt", header = TRUE);
```

```

mm = subset(cow, treatment=="A")["milk"]
sf = subset(cow, treatment=="B")["milk"]
mm1 = as.numeric(unlist(mm))
sf1 = as.numeric(unlist(sf))
par(mfrow=c(1,2))
qqnorm(mm1); qqnorm(sf1)
cow$id = factor(cow$id); cow$per = factor(cow$per)
cowanova = lm(milk~id+per+treatment,data = cow)
anova(cowanova)
summary(cowanova)
# B
library(lme4)
cow$order=factor(cow$order)
cowlmer = lmer(milk~treatment+order+per+(1|id), data=cow, REML = FALSE)
summary(cowlmer)
cowlmerTreatment = lmer(milk~order+per+(1|id), data=cow, REML = FALSE)
anova(cowlmerTreatment, cowlmer)
cowlmerOrder = lmer(milk~treatment+per+(1|id), data=cow, REML = FALSE)
anova(cowlmerOrder, cowlmer)
cowlmerPer = lmer(milk~treatment+order+(1|id), data=cow, REML = FALSE)
anova(cowlmerPer, cowlmer)
# C
attach(cow);t.test(milk[treatment=="A"],milk[treatment=="B"],paired=TRUE)

# --- Exercise 4 --- #
# A
data=read.table("nauseatable.txt",header=TRUE)
nausea=c(rep(0,times=100),rep(1,times=52),rep(0,times=32),rep(1,times=35),rep(0,times=48),
  rep(1,times=37))
medicine=c(rep("Chlorpromazine",times=152),rep("Pentobarbital (100mg)",times=67),
  rep("Pentobarbital (150mg)",times=85))
patientdata=data.frame(nausea,medicine)
xtabs(~medicine+nausea,data=patientdata)
#B
medication=factor(patientdata$medicine)
B=1000;tstar=numeric(B)
for (i in 1:B) {
  patientstar=sample(medication) # permute medicine lables
  tstar[i] = chisq.test(xtabs(~patientstar+patientdata$nausea))[[1]] }
hist(tstar)
test_statistic=chisq.test(xtabs(~patientdata$medicine+patientdata$nausea))[[1]]
pl=sum(tstar<test_statistic)/B;pl
pr=sum(tstar>test_statistic)/B;pr
#C
chisq.test(xtabs(~patientdata$medicine+patientdata$nausea))

# --- Exercise 5 --- #
#A
data=read.table(file="expensescrime.txt",header=TRUE);plot(data)
par(mfrow=c(1,ncol(data)-1)) # minus the state column
for (i in 2:ncol(data)) hist(data[,i],xlab=names(data)[i],main=NULL)
par(mfrow=c(1,ncol(data)-1)) # minus the state column
for (i in 2:ncol(data)) boxplot(data[,i],main=names(data)[i])
par(mfrow=c(1,5))
plot(data$bad, data$expend,xlab="bad",ylab="expend")
abline(lm(expend ~ bad, data=data))

```

```

plot(data$crime, data$expend,xlab="crime",ylab="expend")
abline(lm(expend ~ crime, data=data))
plot(data$lawyers, data$expend,xlab="lawyers",ylab="expend")
abline(lm(expend ~ lawyers, data=data))
plot(data$employ, data$expend,xlab="employ",ylab="expend")
abline(lm(expend ~ employ, data=data))
plot(data$pop, data$expend,xlab="pop",ylab="expend")
abline(lm(expend ~ pop, data=data))
round(cor(data[,3:7]),2) # exclude state and expend
#B
summary(lm(expend~bad,data=data))
summary(lm(expend~crime,data=data))
summary(lm(expend~lawyers,data=data))
summary(lm(expend~employ,data=data))
summary(lm(expend~pop,data=data))
summary(lm(expend~employ+bad,data=data))
summary(lm(expend~employ+crime,data=data))
summary(lm(expend~employ+lawyers,data=data))
summary(lm(expend~employ+pop,data=data))
summary(lm(expend~employ+lawyers+bad,data=data))
summary(lm(expend~employ+lawyers+crime,data=data))
summary(lm(expend~employ+lawyers+pop,data=data))
summary(lm(expend~bad+crime+lawyers+employ+pop,data=data))
summary(lm(expend~bad+lawyers+employ+pop,data=data))
summary(lm(expend~bad+lawyers+employ,data=data))
summary(lm(expend~lawyers+employ, data=data))
#C
expendlm = lm(expend~lawyers+employ,data=data)
round(residuals(expendlm),2);order(abs(residuals(expendlm)))
round(cooks.distance(expendlm),2)
par(mfrow=c(2,4))
plot(1:51,cooks.distance(expendlm),type="b")
plot(residuals(expendlm),data[,5],xlab="residuals",ylab="lawyers")
plot(residuals(expendlm),data[,6],xlab="residuals",ylab="employ")
plot(residuals(expendlm),data[,3],xlab="residuals",ylab="bad")
plot(residuals(expendlm),data[,4],xlab="residuals",ylab="crime")
plot(residuals(expendlm),data[,7],xlab="residuals",ylab="pop")
plot(residuals(expendlm),data[,2],xlab="residuals",ylab="expend")
plot(residuals(expendlm),fitted(expendlm),xlab="residuals",ylab="fitted model")
par(mfrow=c(2,3))
x = residuals(lm(bad~employ+lawyers,data=data))
y = residuals(lm(expend~employ+lawyers,data=data))
plot(x,y,main="Added variable plot for bad")
x = residuals(lm(crime~employ+lawyers,data=data))
y = residuals(lm(expend~employ+lawyers,data=data))
plot(x,y,main="Added variable plot for crime")
x = residuals(lm(lawyers~pop+crime+bad,data=data))
y = residuals(lm(expend~pop+crime+bad,data=data))
plot(x,y,main="Added variable plot for lawyers")
x = residuals(lm(employ~pop+crime+bad,data=data))
y = residuals(lm(expend~pop+crime+bad,data=data))
plot(x,y,main="Added variable plot for employ")
x = residuals(lm(pop~employ+lawyers,data=data))
y = residuals(lm(expend~employ+lawyers,data=data))
plot(x,y,main="Added variable plot for pop")
qqnorm(residuals(expendlm))

```