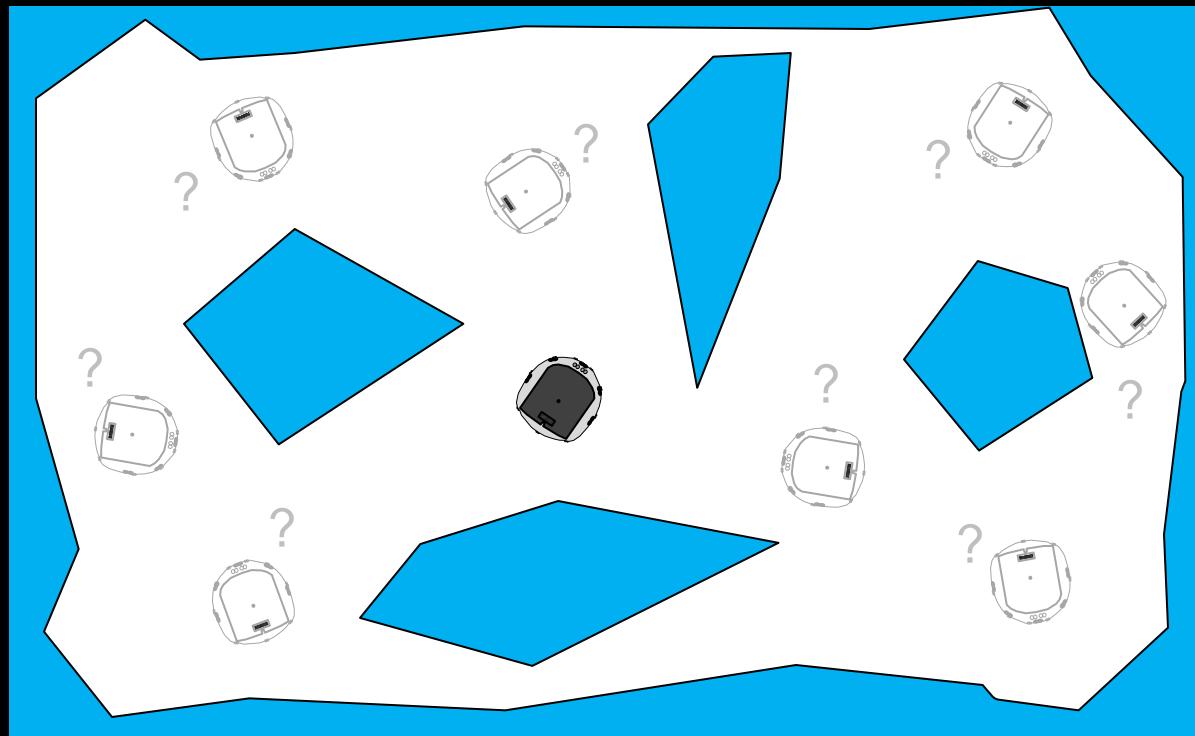


Localization

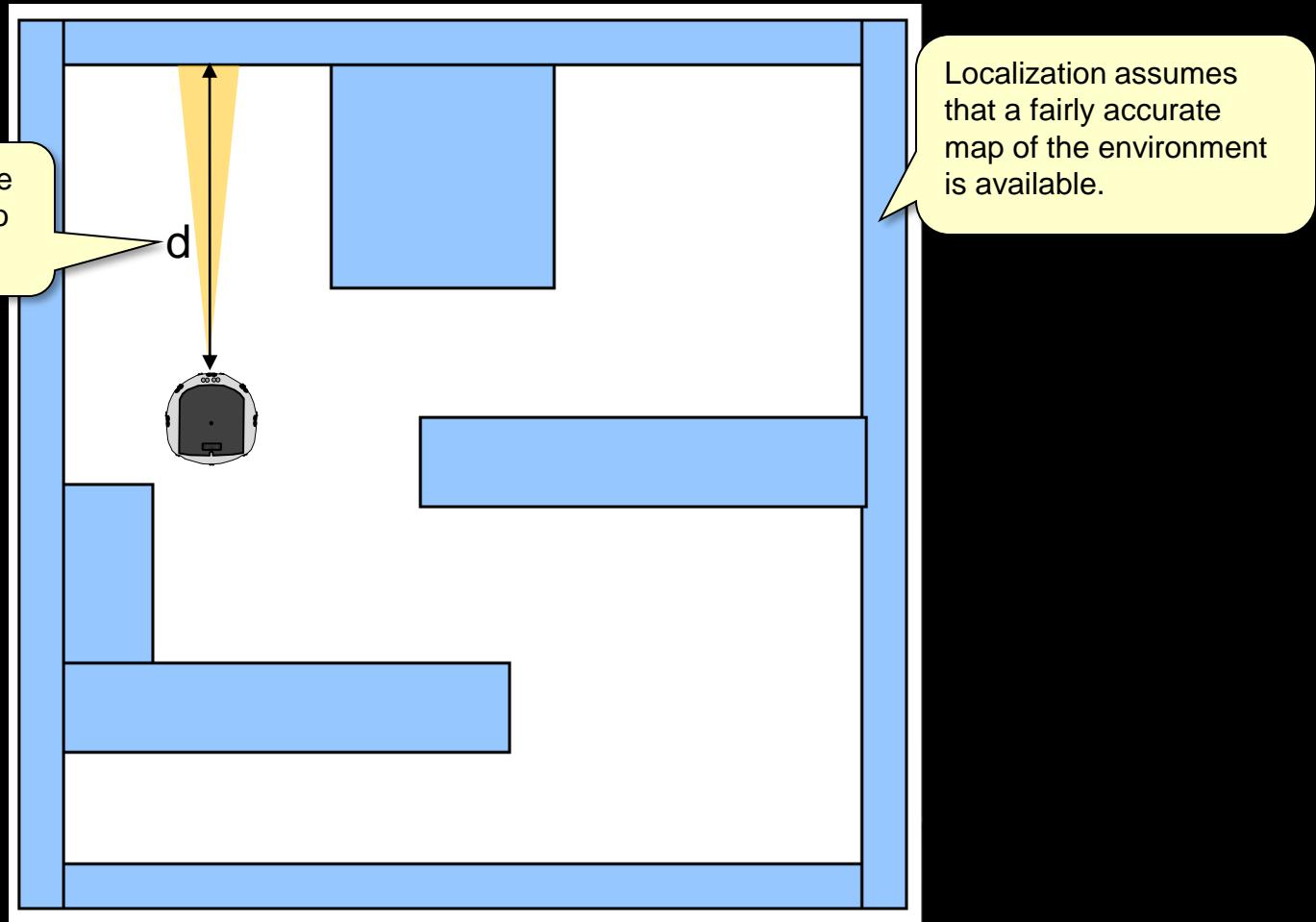
Localization

- Given a robot and a map, find the robot's pose (i.e., where the robot is and which direction it faces)
 - There are many algorithms ... we will look at Monte Carlo Estimation (a.k.a. Particle Filtering)



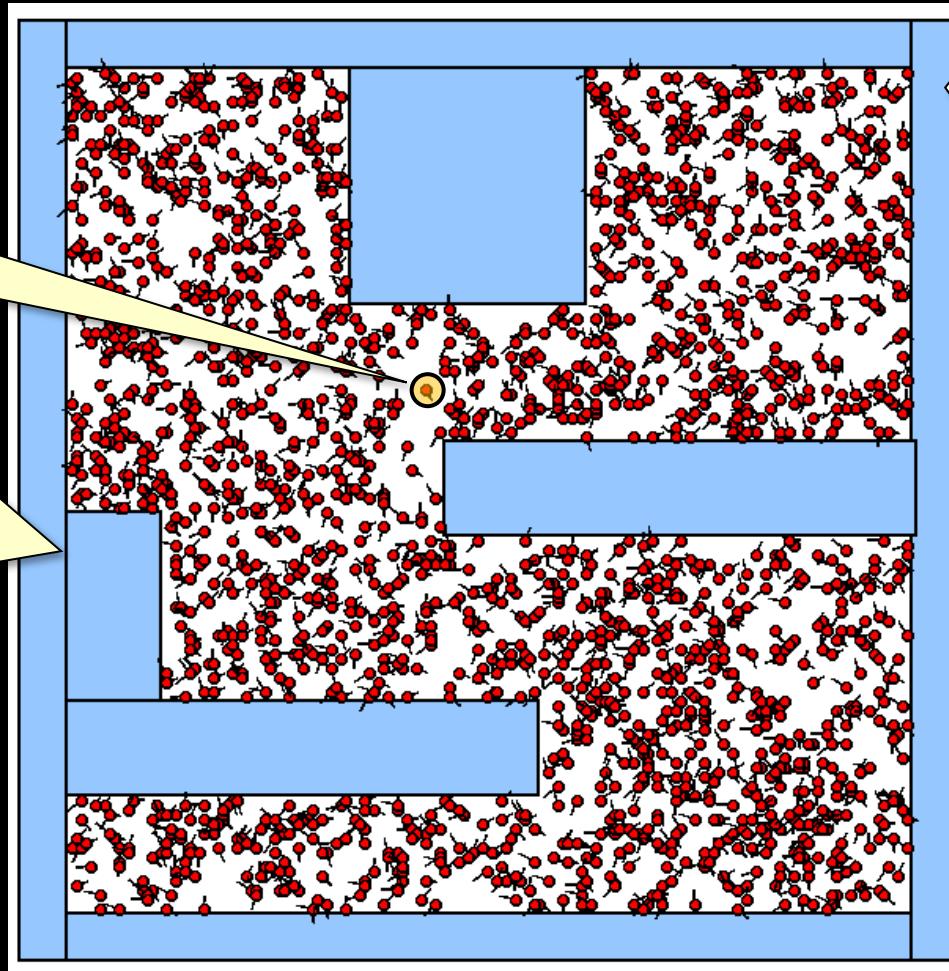
Monte Carlo Localization

- Assume robot is entirely enclosed within its environment at all times.



Monte Carlo Localization

- Start by computing a LOT (i.e., 2000 used here) of random poses as *initial estimates* of where the robot is.

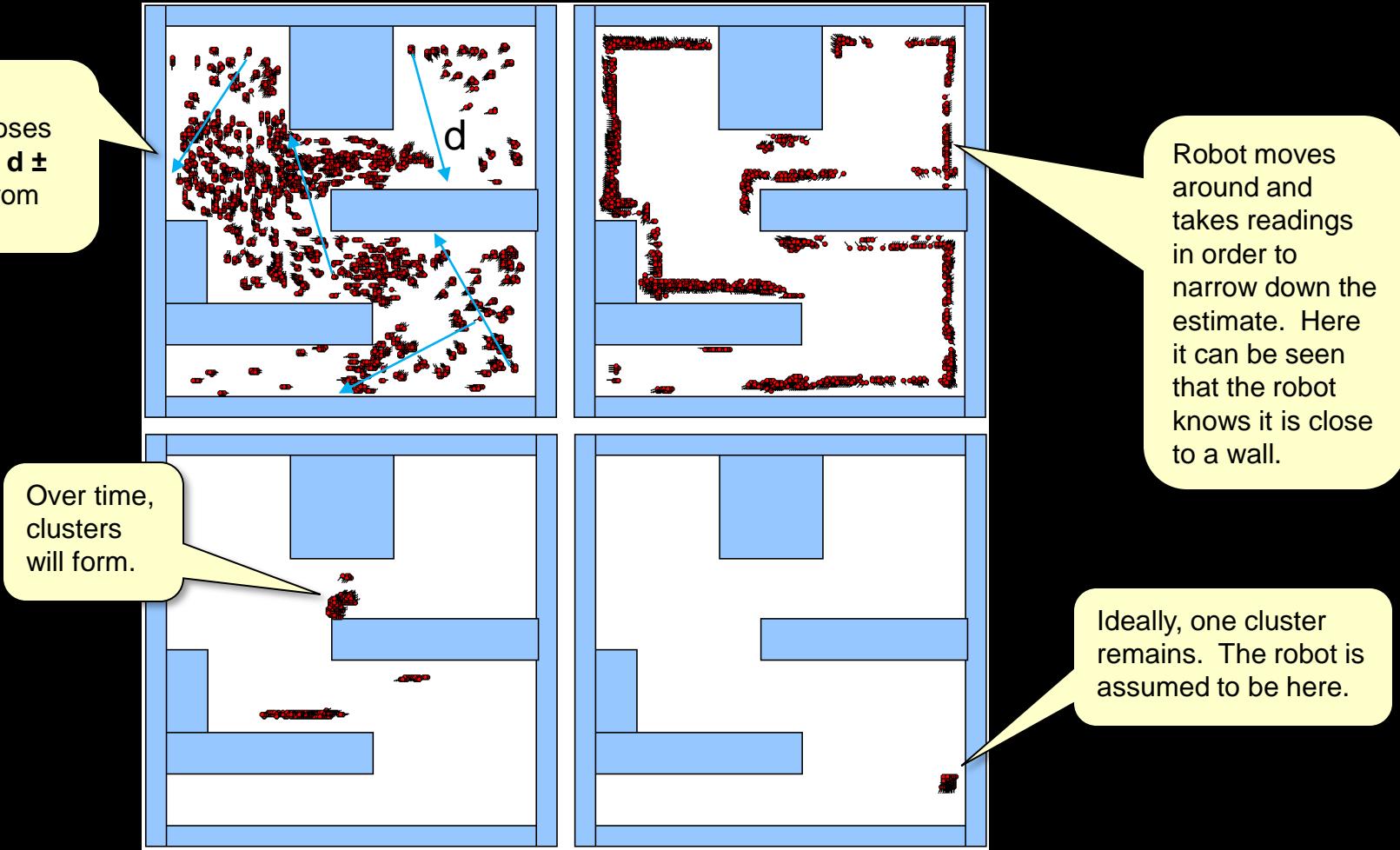


Need to check to ensure that no pose estimate lies **inside** of an obstacle, otherwise discard it.

Need to also check to ensure that no pose estimate lies outside of the boundary (just check against **minX**, **minY**, **maxX** and **maxY** of all obstacles).

Monte Carlo Localization

- As time goes on, many of these poses will be discarded and replaced by “better” estimates.



Monte Carlo Localization

- Algorithm is as follows:

```
1  FUNCTION Localize(ArrayList<Obstacle> obstacles, NUM_SAMPLES, %TOL)
2      currentEstimates = a list of NUM_SAMPLES randomly chosen poses
3      REPEAT {
4          message = getMessageFromRobot()
5          IF (message is a new distance reading) THEN
6              d = getDistanceReading()
7              estimateFromReading(currentEstimates, d, obstacles, NUM_SAMPLES, %TOL)
8          IF (message is a motion update from forward movement) THEN
9              distance = getDistanceMovedForward()
10             updateLocation(currentEstimates, distance, %TOL)
11         IF (message is a motion update from turning) THEN
12             angle = getAngleTurned()
13             updateOrientation(currentEstimates, angle, %TOL)
14     }
```

Wait until the robot sends some new information ...

Now re-compute the **currentEstimates** based on this latest distance reading.

If robot moved forward, move all estimates forward by that amount.

If robot turned, turn all estimates by that amount.

Monte Carlo Localization

- When a distance reading is obtained ... update estimates:

```
1  FUNCTION estimateFromReading(currentEstimates, d, obstacles, NUM_SAMPLES, %TOL)
2      goodEstimates = an empty list
3      FOR (each pose p in currentEstimates) DO
4          IF (isGoodEstimate(p, d, obstacles, %TOL)) THEN
5              Add p to goodEstimates if it is a valid pose
6      IF (goodEstimates is empty)
7          currentEstimates = reset to NUM_SAMPLES random poses
8      OTHERWISE
9          Call resetEstimates()
10         c = NUM_SAMPLES / number of poses in goodEstimates
11         Clear the currentEstimates list
12         Add c copies of each pose in goodEstimates to currentEstimates
```

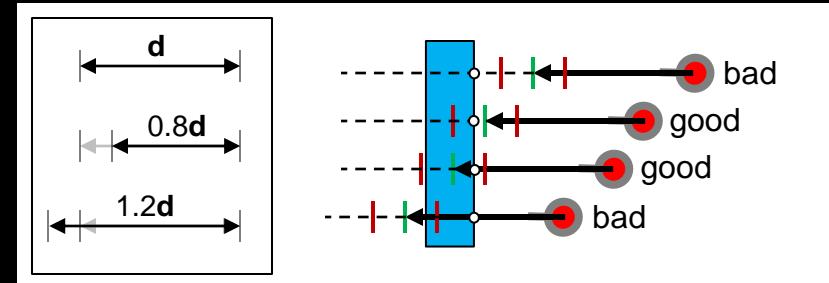
Go through the poses and keep only the “good” ones. Check also that it is valid (i.e., it does not lie within an obstacle).

Duplicate the good ones so that we always have a constant number of samples.

To make a copy, you need to call the constructor: `new Pose(p.x, p.y, p.angle)`

- How do we know if an estimate is “good” ?

- Check intersection with closest obstacle. If within reasonable error tolerance (e.g., 20%), then it is a good estimate.



Is the Estimate Good?

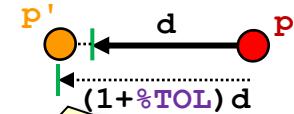
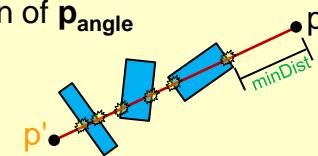
```

1  FUNCTION isGoodEstimate( $p$ ,  $d$ , obstacles, %TOL)
2      Compute point  $p'$  to be  $(p_x + (1+\%TOL) d \cdot \cos(p_{\text{angle}}), p_y + (1+\%TOL) d \cdot \sin(p_{\text{angle}}))$ 
3      minDist = infinity;
4      FOR (each obstacle obj in obstacles) DO
5          FOR (each edge e of obj) DO
6              IF ( $pp'$  intersects e) THEN
7                  q = intersection of  $pp'$  with e
8                  IF (q is not null)
9                      qDist = distance from  $p$  to q
10                 IF (qDist < minDist) THEN
11                     minDist = qDist
12                 IF (minDist is still infinity) THEN
13                     RETURN false
14
15                 IF (minDist > (1-%TOL)d AND minDist < (1+%TOL)d) THEN
16                     RETURN true
17
18                 RETURN false

```

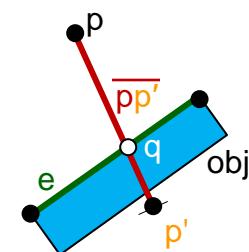
If no intersection, estimate is bad.

Minimum distance from (p_x, p_y) to an obstacle in the direction of p_{angle}



p' is %TOL further than d from (p_x, p_y) in direction of p_{angle}

Use the **distance** function in the Point class that takes another point's x, y coordinates as parameters.



Find distance to closest obstacle intersection point q among all obstacle edges.

If reading is within %TOL range, it is a good estimate.

Monte Carlo Localization

- Updating estimates when a robot moves forward ...

```
1  FUNCTION updateLocation(currentEstimates, d, %TOL)
2      FOR (each pose p in currentEstimates) DO
3          randomPercent = %TOL · (2R - 1)
4          px = px + d · (1 + randomPercent) · cos(pangle)
5          py = py + d · (1 + randomPercent) · sin(pangle)
```

Move forward by distance **d** cm plus a random amount from $-\%TOL$ to $+\%TOL$

R is a random number such that $0 \leq R < 1$.

The randomness is needed so as to allow the poses to vary slightly over time. This is crucial for the algorithm to work, otherwise it may never converge to a proper pose or may lose a good pose due to inaccurate robot movements.

Math.random() gives a random # in range from 0 to 0.9999999

- Updating estimates when a robot spins ...

```
1  FUNCTION updateOrientation(currentEstimates, angle, %TOL)
2      FOR (each pose p in currentEstimates) DO
3          randomPercent = %TOL · (2R - 1)
4          pangle = pangle + angle · (1 + randomPercent)
```

Turn by **angle** degrees plus a random amount from $-\%TOL$ to $+\%TOL$

Start the
Lab ...