

1. Grammar given.

a. The given grammar isn't LL(1) because the CMD var has common prefix 'printf' for more than one rule.

b. The fixed grammar:

$$PROG \rightarrow TDEF\ BLK$$

$$TDEF \rightarrow 'var'\ 'is'\ 'type'\ ';' \ TDEF \mid \epsilon$$

$$BLK \rightarrow '\{'\ STL\ '\}'$$

$$STL \rightarrow CMD\ STL \mid \epsilon$$

$$CMD \rightarrow 'printf'\ P \mid 'var'\ '='\ 'num'\ ';' \mid BLK$$

$$P \rightarrow 'num'\ ';' \mid 'var'\ ';' \mid$$

c. Let's show that the fixed grammar is LL(1).

i. We'll start by building the FIRST table:

PROG	TDEF	BLK	STL	CMD	P
-	-	-	-	-	-
-	'var'	'{'	-	'printf', 'var', '{'	'num', 'var'
'var', '{'	'var'	'{'	'printf', 'var', '{'	'printf', 'var', '{'	'num', 'var'
'var', '{'	'var'	'{'	'printf', 'var', '{'	'printf', 'var', '{'	'num', 'var'

ii. Next we'll build the FOLLOW table:

PROG	TDEF	BLK	STL	CMD	P
\$	-	-	-	-	-
\$	'{'	-	'}'	'printf', 'var', '{', '}'	-
\$	'{'	-	'}'	'printf', 'var', '{', '}'	-

iii. And finally we'll calculate SELECT for each rule. For each variable, if the all SELECTs have no terminal in common then the grammar is LL(1):

$$SELECT(PROG \rightarrow TDEF\ BLK) = 'var'$$

$$SELECT(TDEF \rightarrow 'var'\ 'is'\ 'type'\ ';' \ TDEF) = 'var' \# SELECT(TDEF \rightarrow \epsilon) = '\{'$$

$$SELECT(BLK \rightarrow '\{'\ STL\ '\}') = '\{'$$

$$SELECT(STL \rightarrow CMD\ STL) = 'printf', 'var', '\{' \# SELECT(STL \rightarrow \epsilon) = '\}'$$

$$SELECT(CMD \rightarrow 'printf'\ P) = 'printf' \# SELECT('var'\ '='\ 'num'\ ';') = 'var' \# SELECT(BLK) = '\{'$$

$$SELECT(P \rightarrow 'num'\ ';') = 'num' \# SELECT('var'\ ';') = 'var'$$

d. Let's assign number to all rules:

- 1 $PROG \rightarrow TDEF\ BLK$
- 2 $TDEF \rightarrow 'var' 'is' 'type' ';' TDEF$
- 3 $TDEF \rightarrow \epsilon$
- 4 $BLK \rightarrow '\{ STL \}'$
- 5 $STL \rightarrow CMD\ STL$
- 6 $STL \rightarrow \epsilon$
- 7 $CMD \rightarrow 'printf' P$
- 8 $CMD \rightarrow 'var' '=' 'num' ';' '$
- 9 $CMD \rightarrow BLK$
- 10 $P \rightarrow 'num' ';' '$
- 11 $P \rightarrow 'var' ';' '$

	{	}	printf	var	num
PROG				1	
TDEF	3			2	
BLK	4				
STL	5	6	5	5	
CMD	9		7	8	
P				10	11

2. See the state machine description below.

- a. The given grammar is LR(1) because the parser described by the state machine below has no conflicts.

For each state we can easily decide weather we need to 'shift' or 'reduce'.

- b. However, the grammar is NOT LR(0). Let's look at State4: if the current token is 'm' than we may perform a 'shift-6' operation. But, bereft of a lookahead, we may also perform a 'reduce' operation with the rule $H \rightarrow k$.

- c. The same example is enough to show that the grammar is not SLR either. Because 'm' is clearly in FOLLOW(H), we would still want to perform the 'reduce' operation AND the 'shift' operation.

d.

	Operations Table				GOTO Table	
	m	k	d	\$	A	H
0		s5	s2		1	3
1				acc		
2		r4				
3		s5				
4	s6	r3				
5		s7	s8			9
6		s11	s2		13	12
7	r3					
8	r4					
9	s10					
10				r2		
11	s16					
12		s15				
13			s14			
14				r1		
15		s7	s8			19
16		s11			17	
17			s18			
18			r1			
19	s20					
20			r2			

Rules index: (0) $S \rightarrow A$

(1) $A \rightarrow kmAd$

(2) $A \rightarrow HkHm$

(3) $H \rightarrow k$

(4) $H \rightarrow d$

2. A list of states:

State0:

$S \rightarrow \bullet A, \$$
 $A \rightarrow \bullet kmAd, \$$
 $A \rightarrow \bullet HkHm, \$$
 $H \rightarrow \bullet k, k$
 $H \rightarrow \bullet d, k$

State1:

$S \rightarrow A \bullet, \$$

State2:

$H \rightarrow d \bullet, k$

State3:

$A \rightarrow H \bullet kHm, \$$

State4:

$A \rightarrow k \bullet mAd, \$$
 $H \rightarrow k \bullet, k$

State5:

$A \rightarrow Hk \bullet Hm, \$$
 $H \rightarrow \bullet k, m$
 $H \rightarrow \bullet d, m$

State6:

$A \rightarrow km \bullet Ad, \$$
 $A \rightarrow \bullet kmAd, d$
 $A \rightarrow \bullet HkHm, d$
 $H \rightarrow \bullet k, k$
 $H \rightarrow \bullet d, k$

State7:

$H \rightarrow k \bullet, m$

State8:

$H \rightarrow d \bullet, m$

State9:

$A \rightarrow HkH \bullet m, \$$

State10:

$A \rightarrow HkHm \bullet, \$$

State11:

$A \rightarrow k \bullet mAd, d$
 $H \rightarrow \bullet k, k$

State12:

$A \rightarrow H \bullet kHm, d$

State13:

$A \rightarrow kmA \bullet d, \$$

State14:

$A \rightarrow kmAd \bullet, \$$

State15:

$A \rightarrow Hk \bullet Hm, d$
 $H \rightarrow \bullet k, m$
 $H \rightarrow \bullet d, m$

State16:

$A \rightarrow km \bullet Ad, d$
 $A \rightarrow \bullet kmAd, d$
 $A \rightarrow \bullet HkHm, d$
 $H \rightarrow \bullet k, k$
 $H \rightarrow \bullet d, k$

State17:

$A \rightarrow kmA \bullet d, d$

State18:

$A \rightarrow kmAd \bullet, d$

State19:

$A \rightarrow HkH \bullet m, d$

State20:

$A \rightarrow HkHm \bullet, d$

A list of transitions:

From **State0**:

Simbol	State
A	State1
d	State2
H	State3
k	State4

From **State3**:

Simbol	State
k	State5

From **State4**:

Simbol	State
m	State6

From **State5**:

Simbol	State
H	State9
k	State7
d	State8

From **State6**:

Simbol	State
k	State11
d	State2
H	State12
A	State13

From **State9**:

Simbol	State
--------	-------

m	State10
---	---------

From **State11**:

Simbol	State
m	State16

From **State12**:

Simbol	State
k	State15

From **State13**:

Simbol	State
d	State14

From **State15**:

Simbol	State
k	State7
d	State8
H	State19

From **State16**:

Simbol	State
k	State11
A	State17

From **State17**:

Simbol	State
d	State18

From **State19**:

Simbol	State
m	State20

