

# **Deep Learning (CNN) in 3D Point Cloud Processing**

Yongcheng Liu

2019.04

# **Introduction**

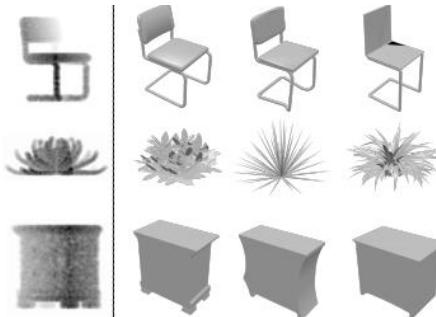
# Introduction tasks

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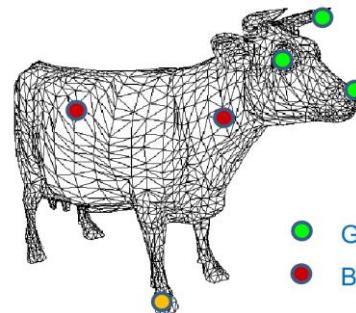


→ lamp

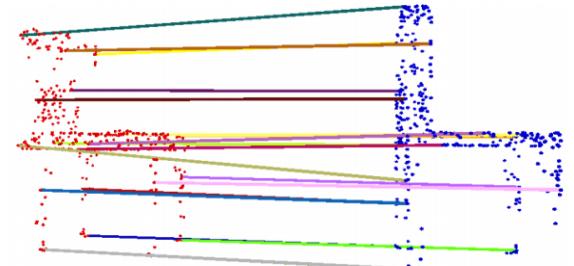
shape classification



shape retrieval



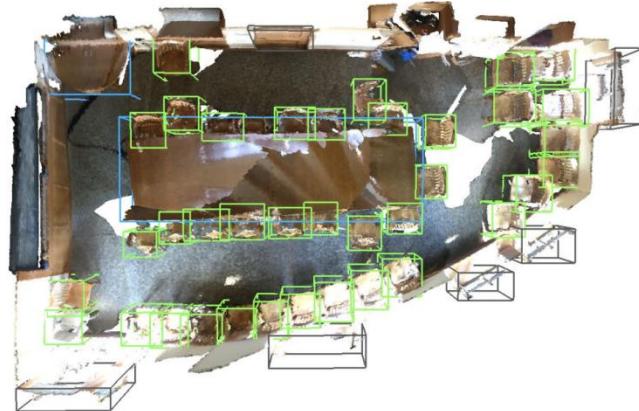
keypoint detection



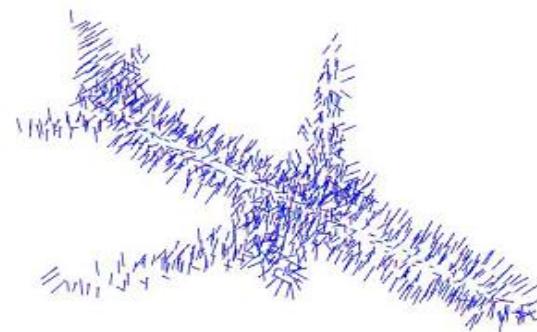
shape correspondence



semantic segmentation



object detection

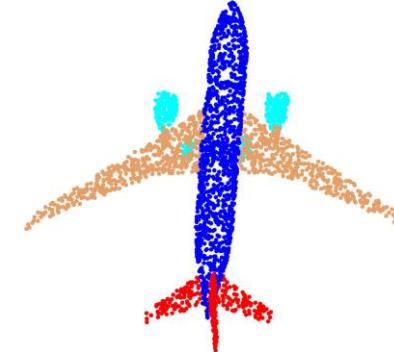
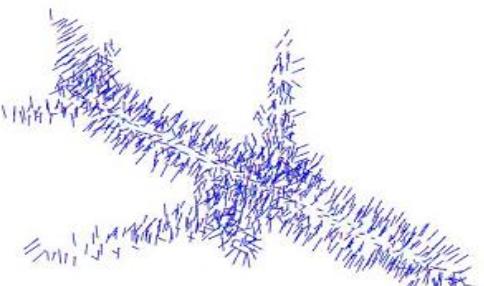


normal estimation

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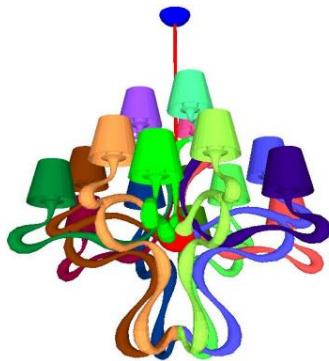
# Introduction databases

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Princeton ModelNet: 1k

ShapeNet Part: 2k



Coarse → Fine-grained



.....

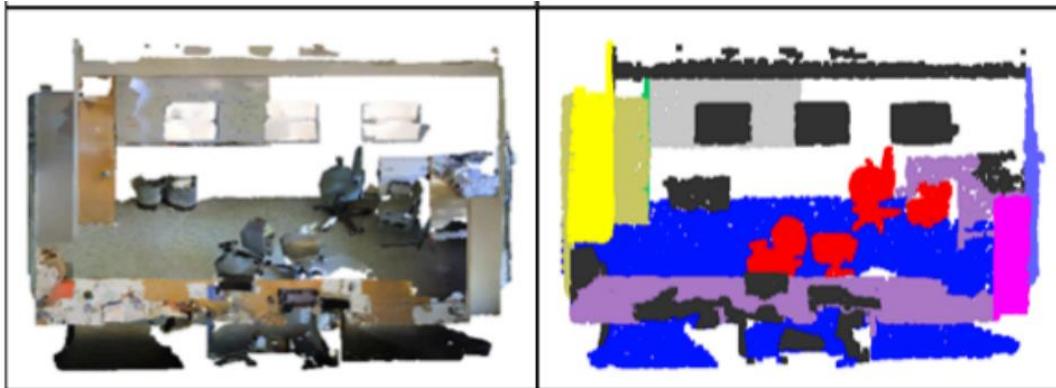
PartNet models

Hierarchical Semantic Segmentation

Mo et al. PartNet: A Large-scale Benchmark for Fine-grained and Hierarchical Part-level 3D Object Understanding. CVPR 2019.  
Yi et al. A scalable active framework for region annotation in 3D shape collections. TOG 2016.  
Wu et al. 3D ShapeNets: A Deep Representation for Volumetric Shapes. CVPR 2015.

# Introduction datasets

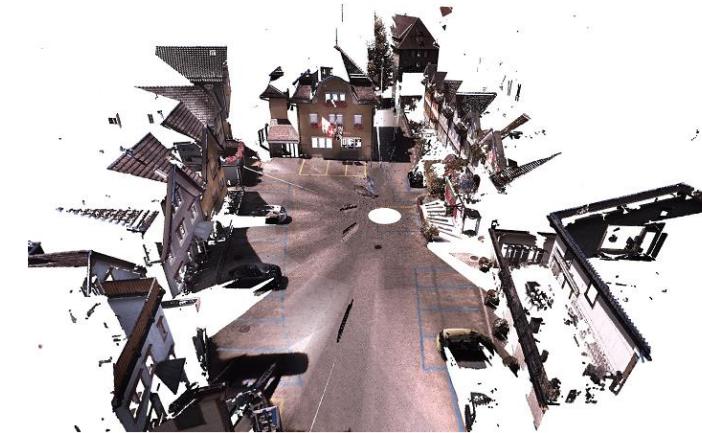
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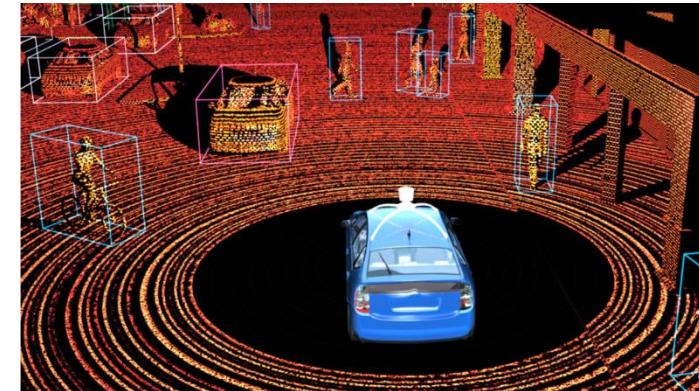
Stanford 3D indoor scene: 8k



ScanNet: seg + det



Semantic 3D: 4 billion in total



KITTI: det

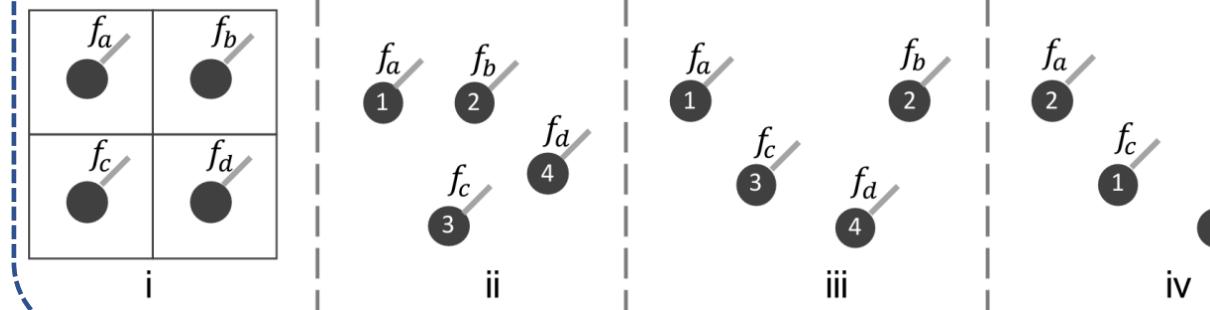
Dai et al. ScanNet: Richly-annotated 3D Reconstructions of Indoor Scenes. CVPR 2017.

Armeni et al. 3d semantic parsing of large-scale indoor spaces. CVPR 2016.

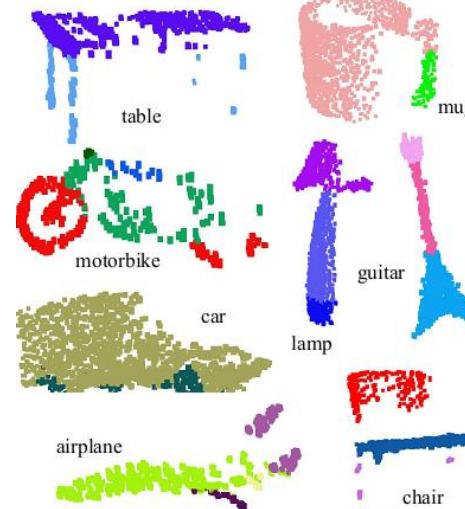
Hackel et al. Semantic3d.net: A new large-scale point cloud classification benchmark. ISPRS 2017.

# Introduction some challenges

Irregular (unordered): permutation invariance

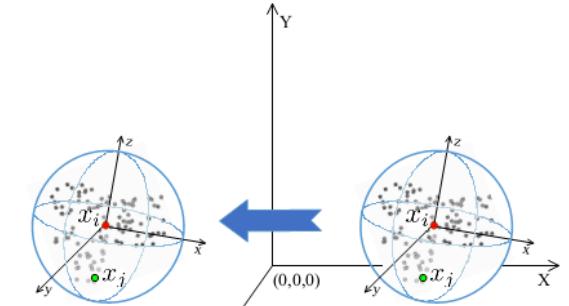


Robustness to corruption, outlier, noise; partial data

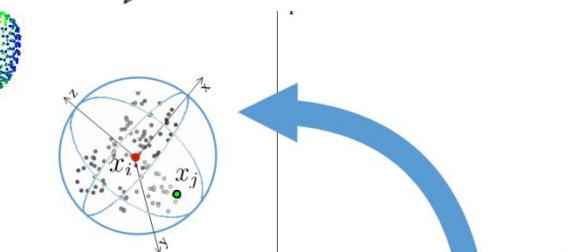


Robustness to rigid transformations

scale



translation



rotation

# Introduction 3D representations

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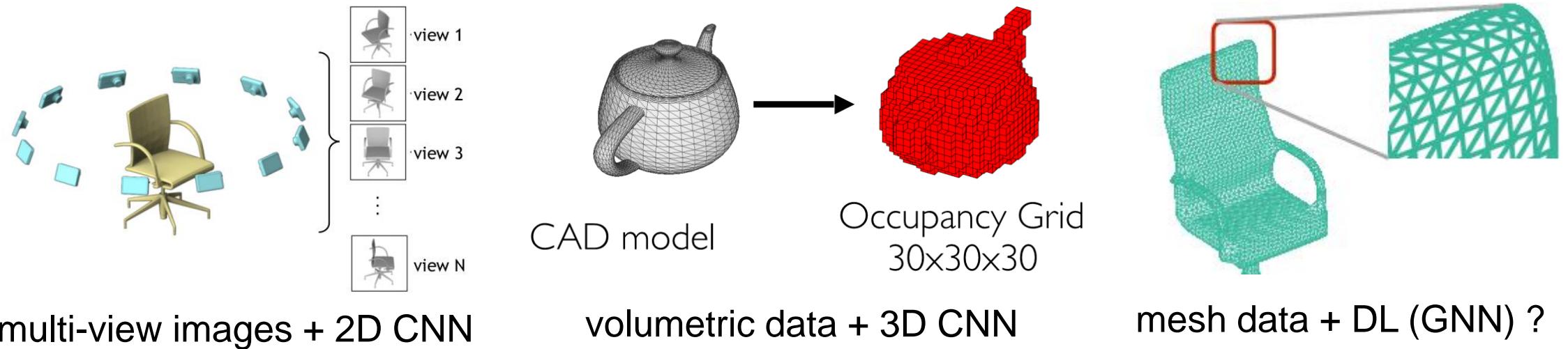
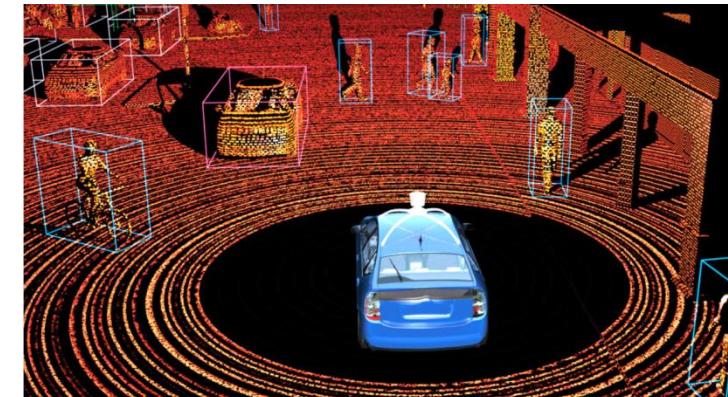


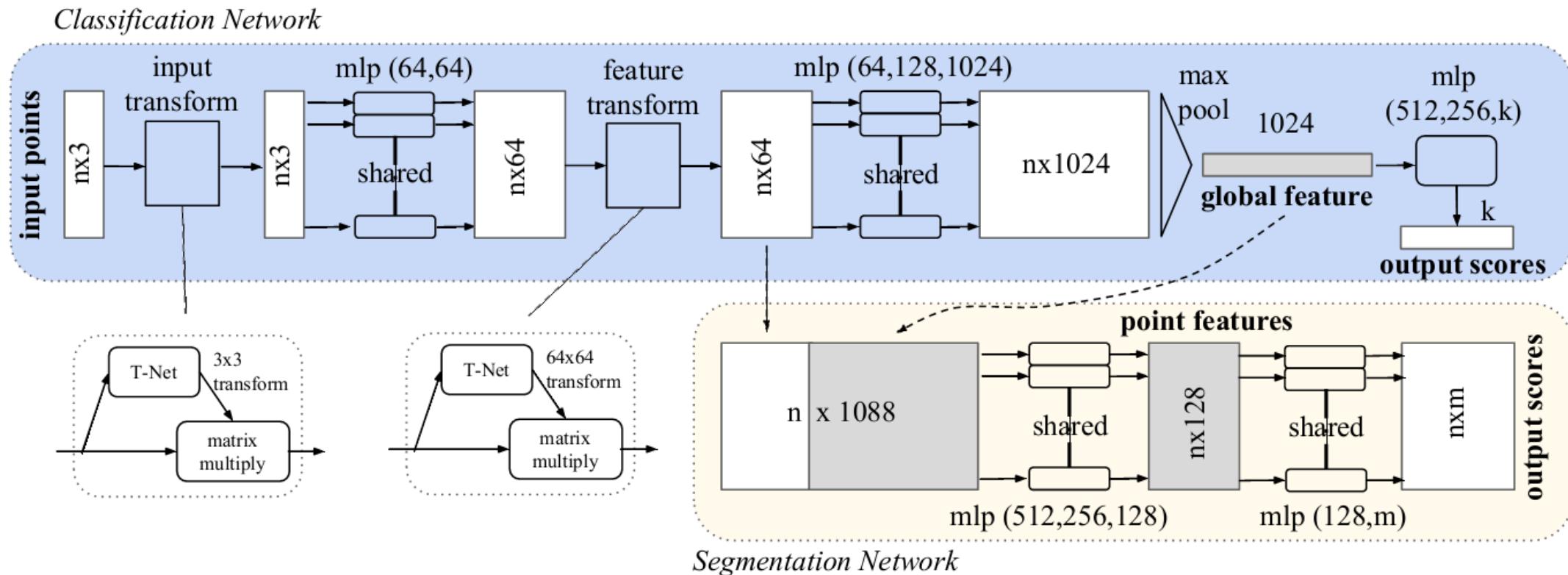
image depth + CNN



point cloud + DL (CNN) ?

## **Related work – PointNet family**

# Related Work *PointNet: permutation invariance*

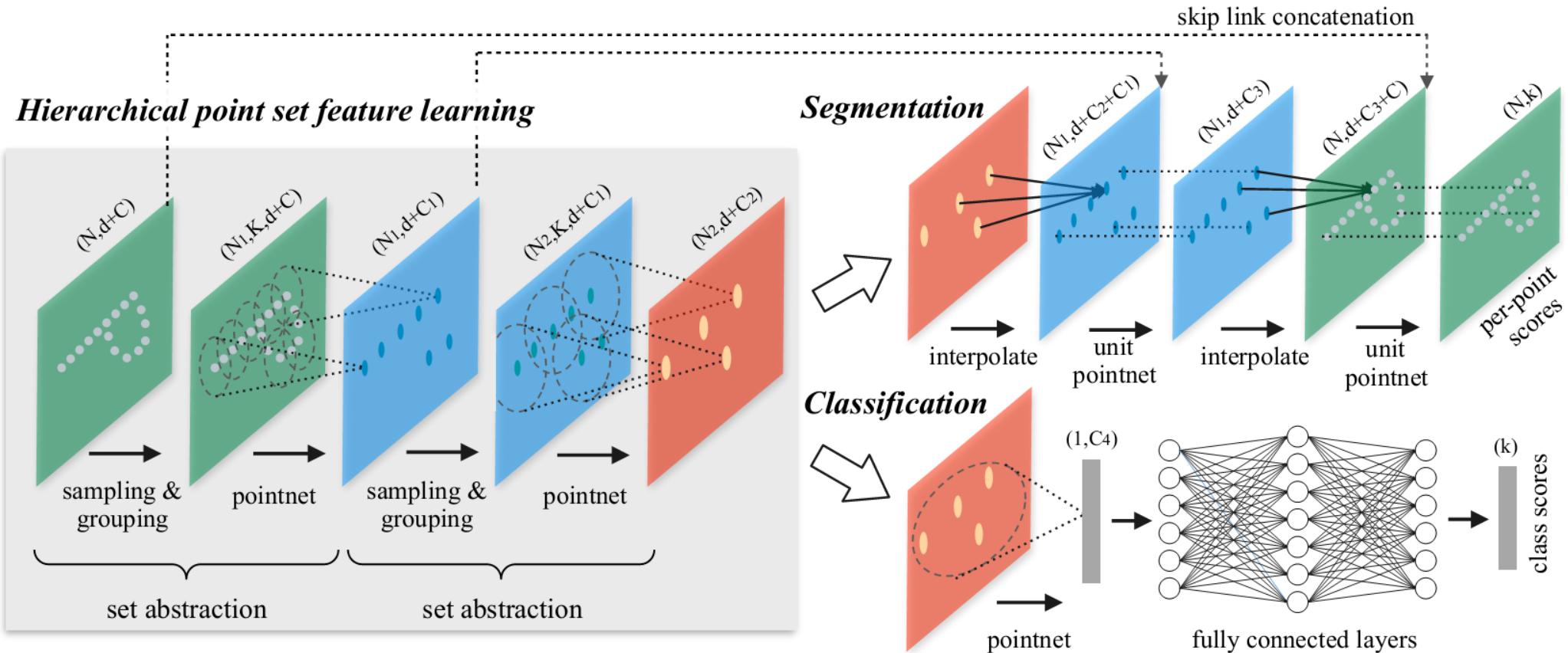


Shared MLP + max pool (symmetric function)

No local patterns capturing

# Related Work

## PointNet++: local to global

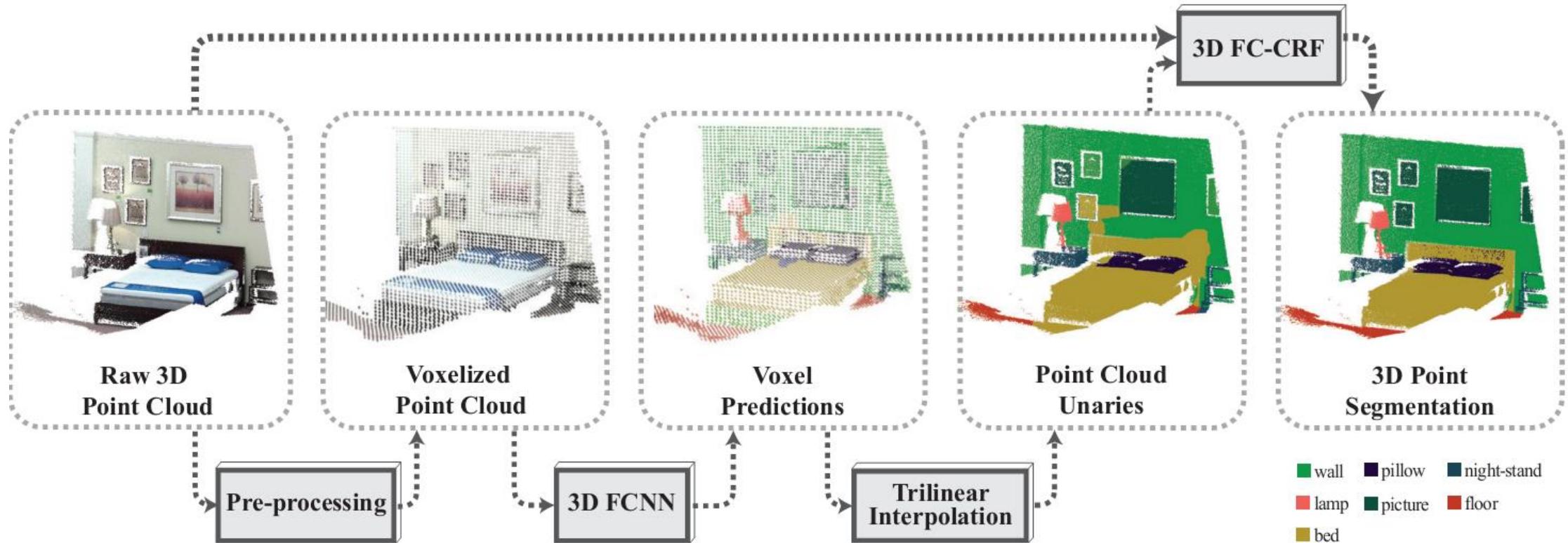


Sampling + Grouping + PointNet

## **Related work – regularization**

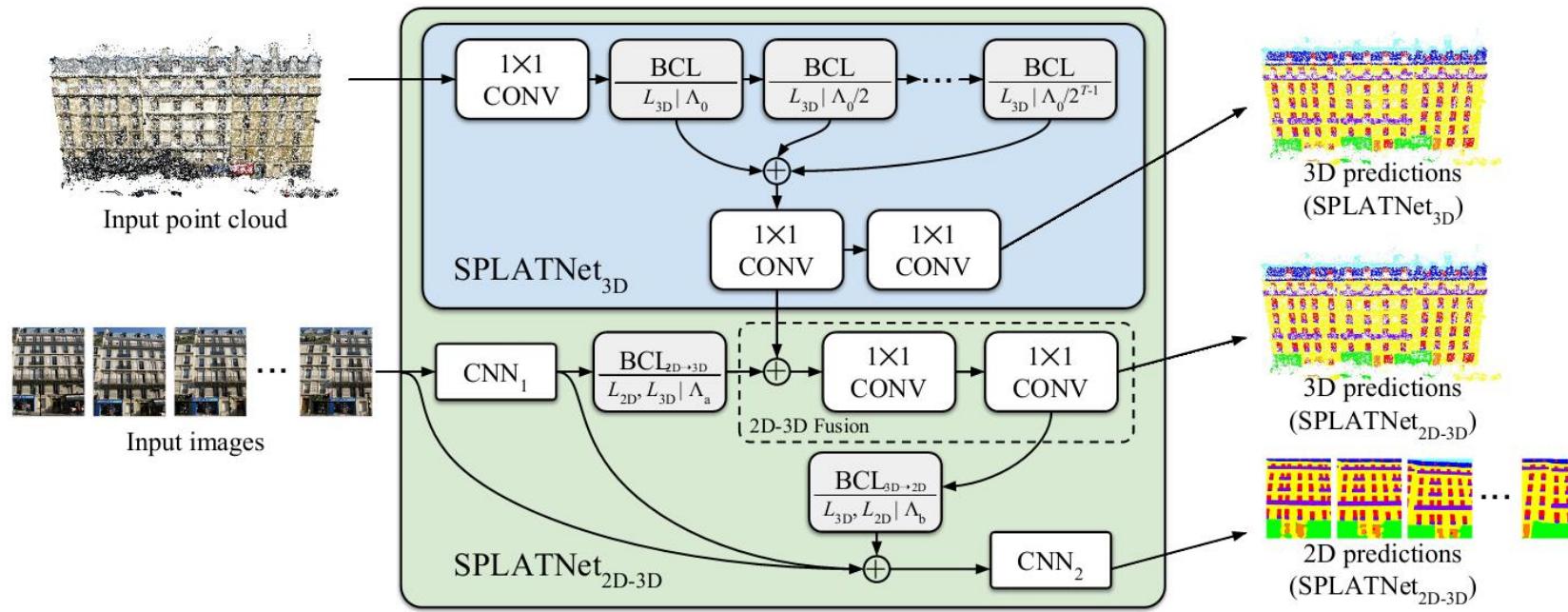
# Related Work

## SEGCloud: voxelization

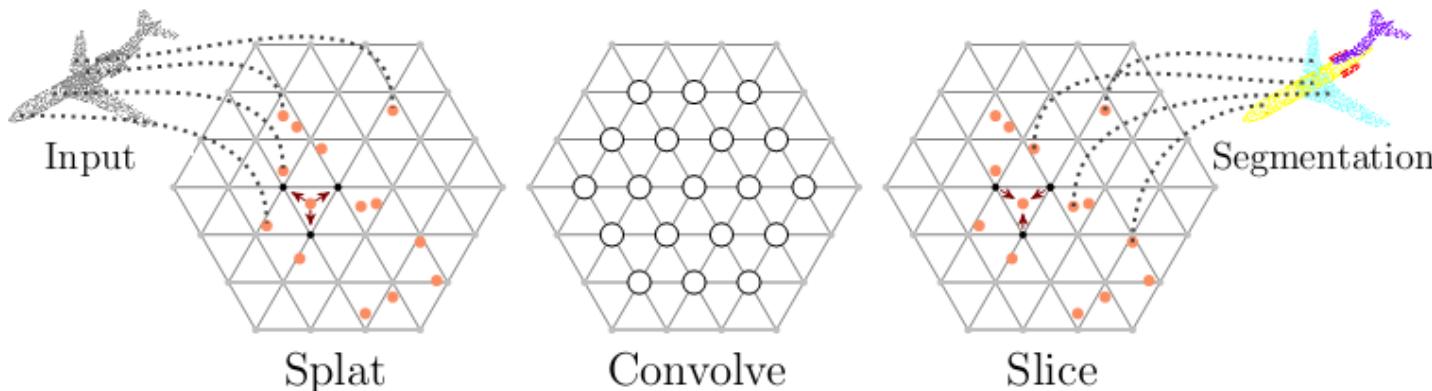


# Related Work

## SPLATNet: high-dimensional lattice

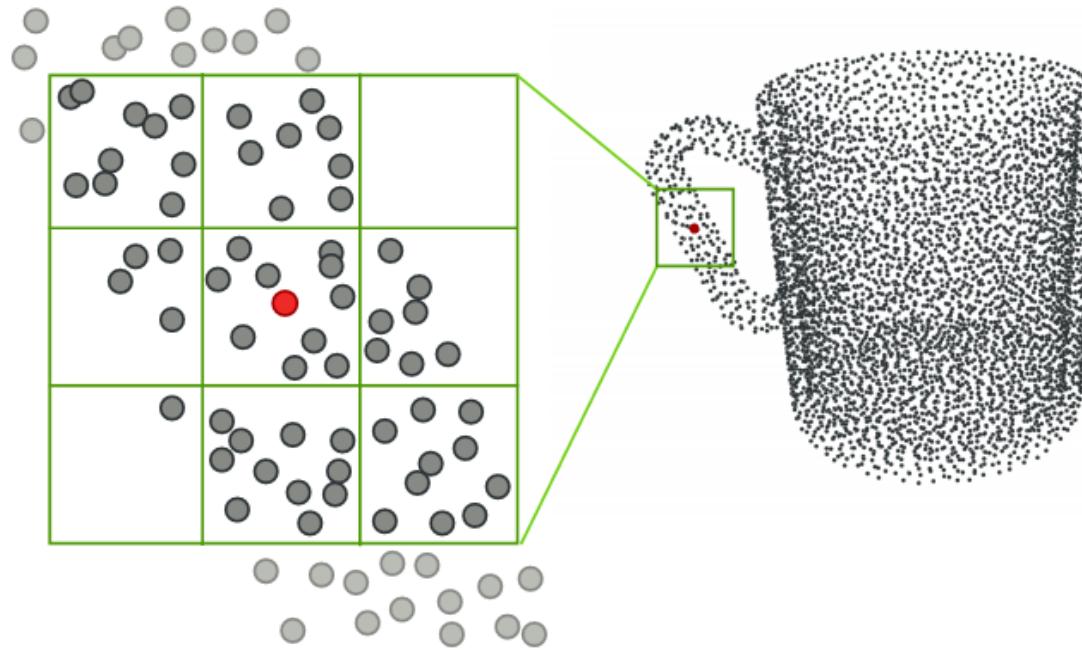


BCL: Bilateral convolution  
layer



# Related Work

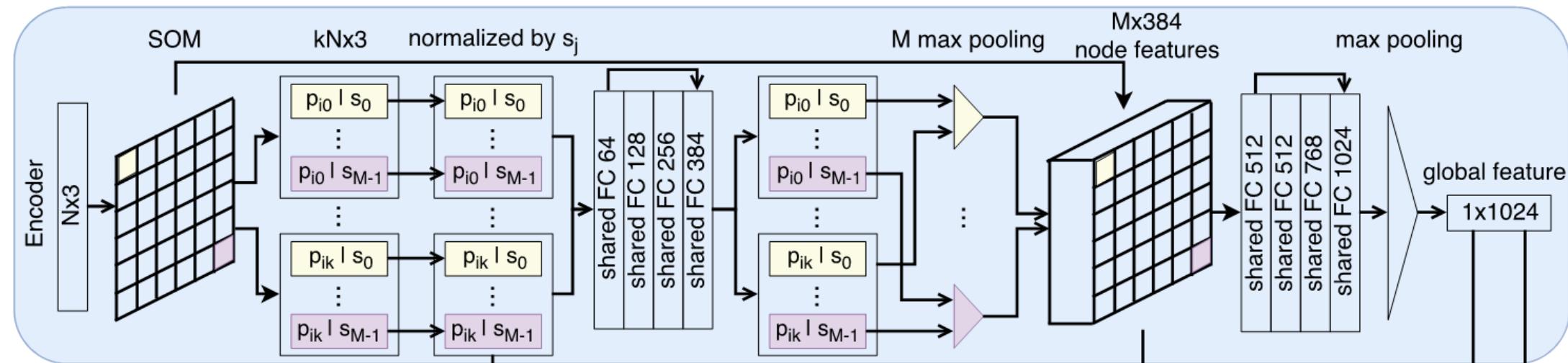
## Pointwise CNN: k-NN binned kernel



$$x_i^\ell = \sum_k w_k \frac{1}{|\Omega_i(k)|} \sum_{p_j \in \Omega_i(k)} x_j^{\ell-1}$$

# Related Work

## SO-Net: Self-Organizing Map (SOM)

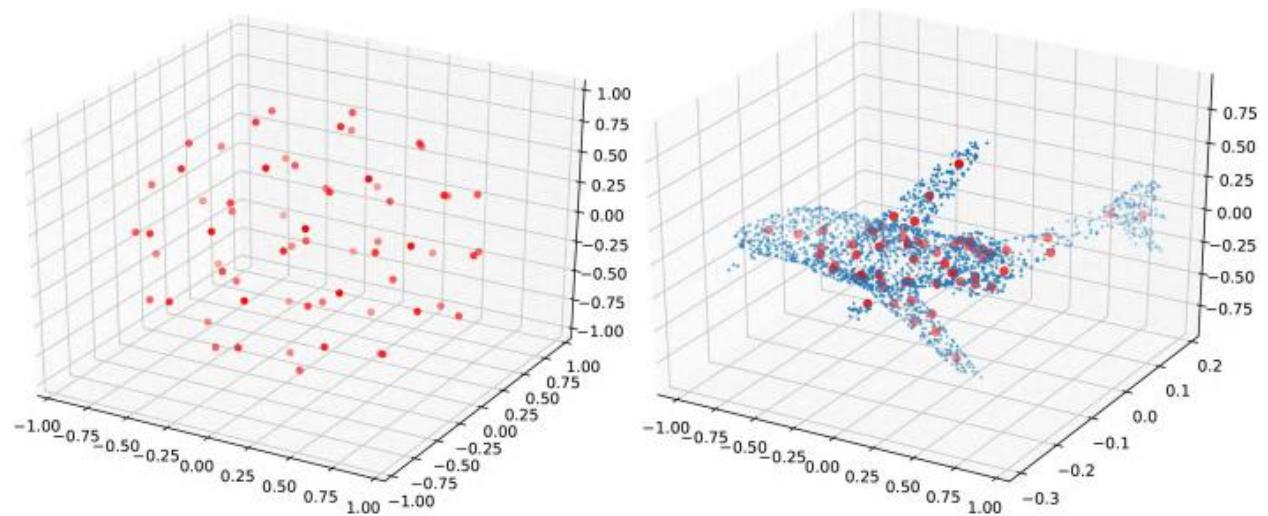


$$s_{ik} = \text{kNN}(p_i | s_j, j = 0, \dots, M - 1).$$

$$p_{ik} = p_i - s_{ik}.$$

$$p_{ik}^{l+1} = \phi(W^l p_{ik}^l + b^l).$$

$$s_j^0 = \max(\{p_{ik}^l, \forall s_{ik} = s_j\}).$$



# Related Work

## PointCNN: X-transformation

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In this paper, we propose to learn a  $K \times K \mathcal{X}$ -transformation for the coordinates of  $K$  input points  $(p_1, p_2, \dots, p_K)$ , with a multilayer perceptron [39], i.e.,  $\mathcal{X} = MLP(p_1, p_2, \dots, p_K)$ . Our aim is to use it to simultaneously weight and permute the input features, and subsequently apply a typical convolution on the transformed features. We refer to this process as  $\mathcal{X}$ -Conv, and it is the basic

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### ALGORITHM 1: $\mathcal{X}$ -Conv Operator

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**Input** :  $\mathbf{K}, p, \mathbf{P}, \mathbf{F}$

**Output**:  $\mathbf{F}_p$

- 1:  $\mathbf{P}' \leftarrow \mathbf{P} - p$
- 2:  $\mathbf{F}_\delta \leftarrow MLP_\delta(\mathbf{P}')$
- 3:  $\mathbf{F}_* \leftarrow [\mathbf{F}_\delta, \mathbf{F}]$
- 4:  $\mathcal{X} \leftarrow MLP(\mathbf{P}')$
- 5:  $\mathbf{F}_{\mathcal{X}} \leftarrow \mathcal{X} \times \mathbf{F}_*$
- 6:  $\mathbf{F}_p \leftarrow \text{Conv}(\mathbf{K}, \mathbf{F}_{\mathcal{X}})$

- ▷ Features “projected”, or “aggregated”, into representative point  $p$ 
  - ▷ Move  $\mathbf{P}$  to local coordinate system of  $p$
- ▷ **Individually** lift each point into  $C_\delta$  dimensional space
- ▷ Concatenate  $\mathbf{F}_\delta$  and  $\mathbf{F}$ ,  $\mathbf{F}_*$  is a  $K \times (C_\delta + C_1)$  matrix
  - ▷ Learn the  $K \times K \mathcal{X}$ -transformation matrix
  - ▷ Weight and permute  $\mathbf{F}_*$  with the learnt  $\mathcal{X}$
- ▷ Finally, typical convolution between  $\mathbf{K}$  and  $\mathbf{F}_{\mathcal{X}}$

# Related Work

## PointSIFT: SIFT-like network

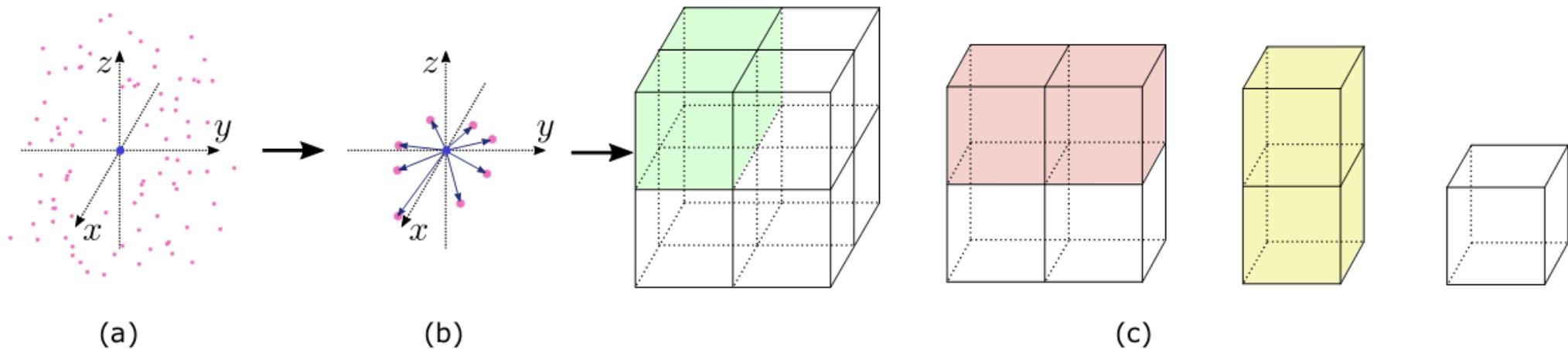
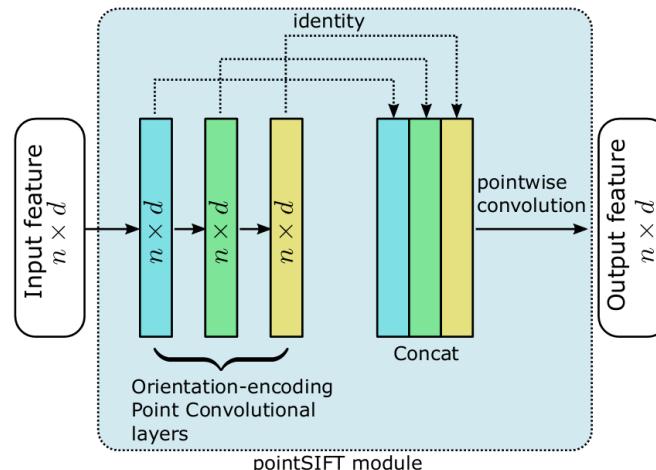


Figure 4: Illustration of the details in Orientation-encoding Point Convolutional layer. (a): point clouds in 3D space. (b) neighbors in eight directions. (c) three stages convolution combines all the features.

SIFT :

- orientation-encoding
- scale-awareness (shortcut connections)



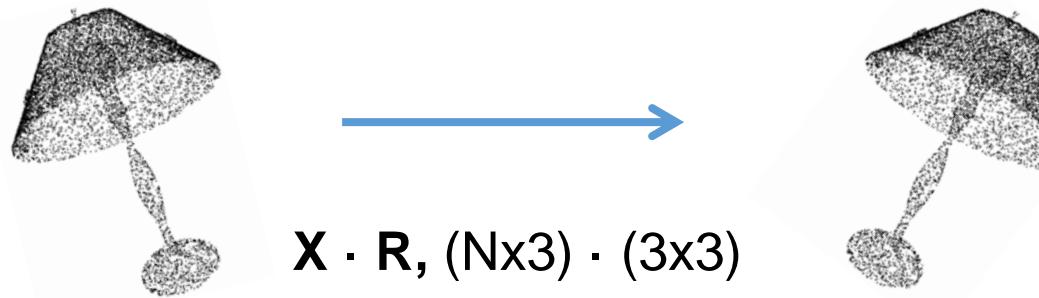
## **Related work – robustness to rigid transformation**

# Related Work

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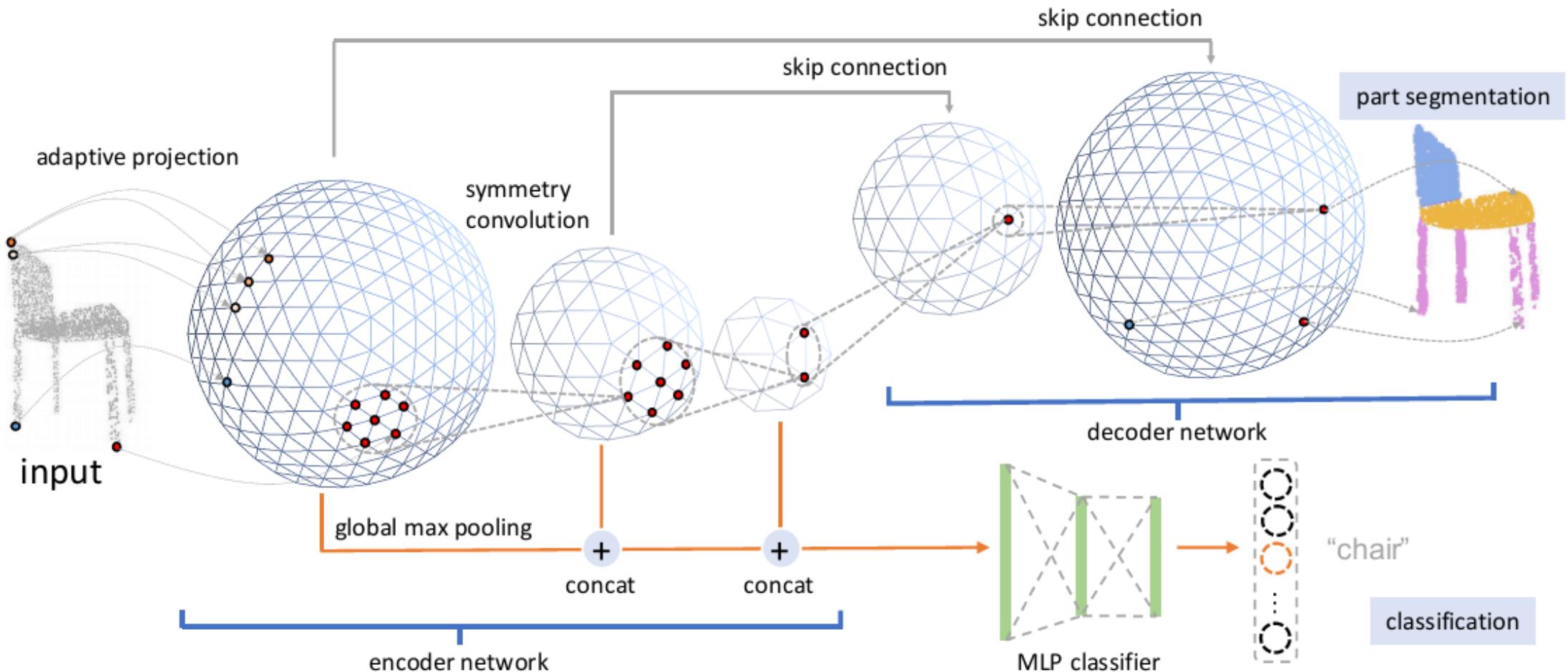
Normalization:

- ✓ Translation
- ✓ Scale
- ✗ *Rotation*



# Related Work

## SFCNN: Spherical Fractal CNN



Cohen et al. Spherical CNNs. ICLR 2018.

Rao et al. Spherical Fractal Convolution Neural Networks for Point Cloud Recognition. CVPR 2019.

## **Related work – relation modeling**

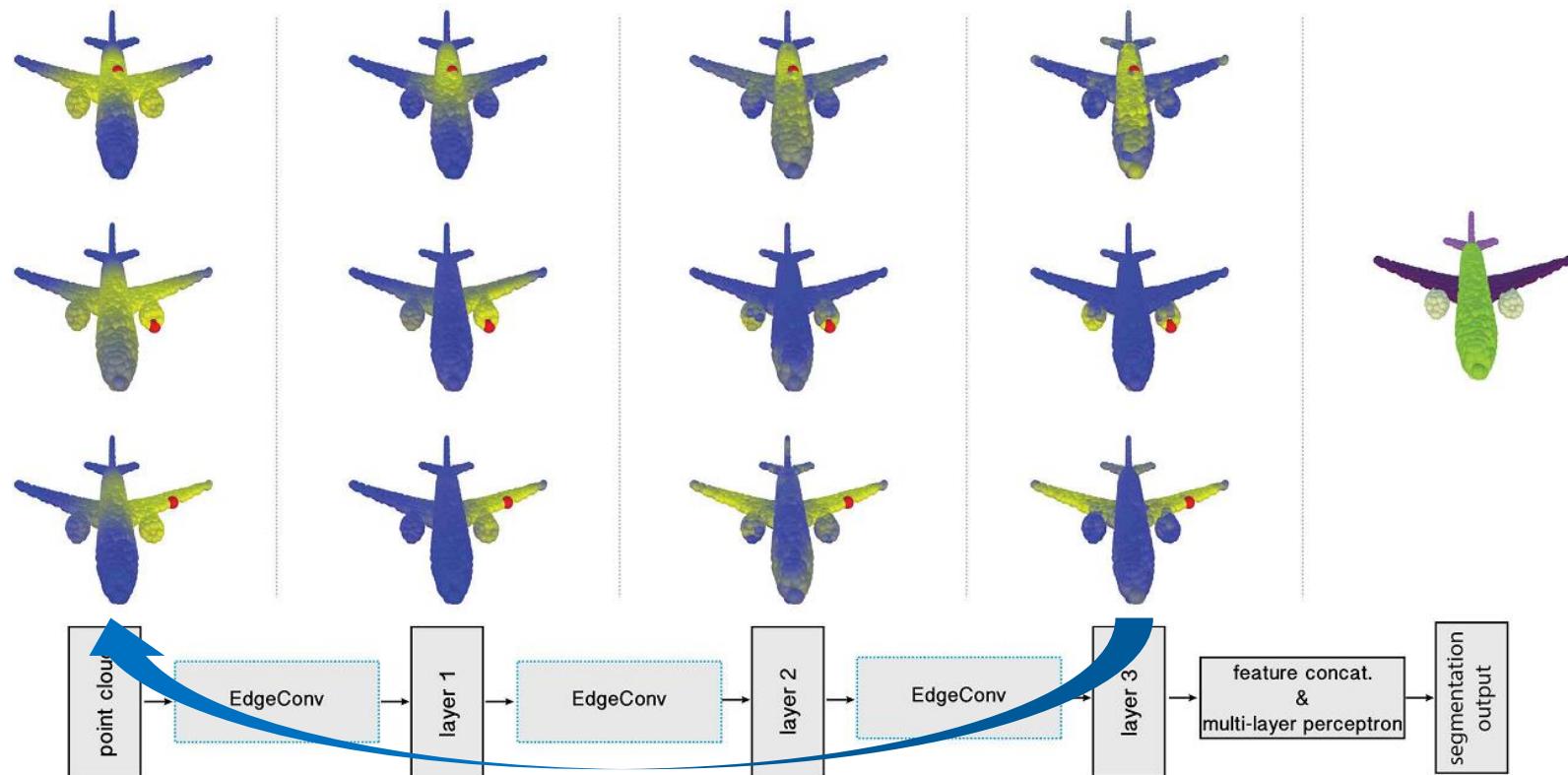
# Related Work DGCNN

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Points in high-level feature space captures semantically similar structures.

Despite a large distance between them in the original 3D space.

Dynamic Graph CNN (DGCNN)

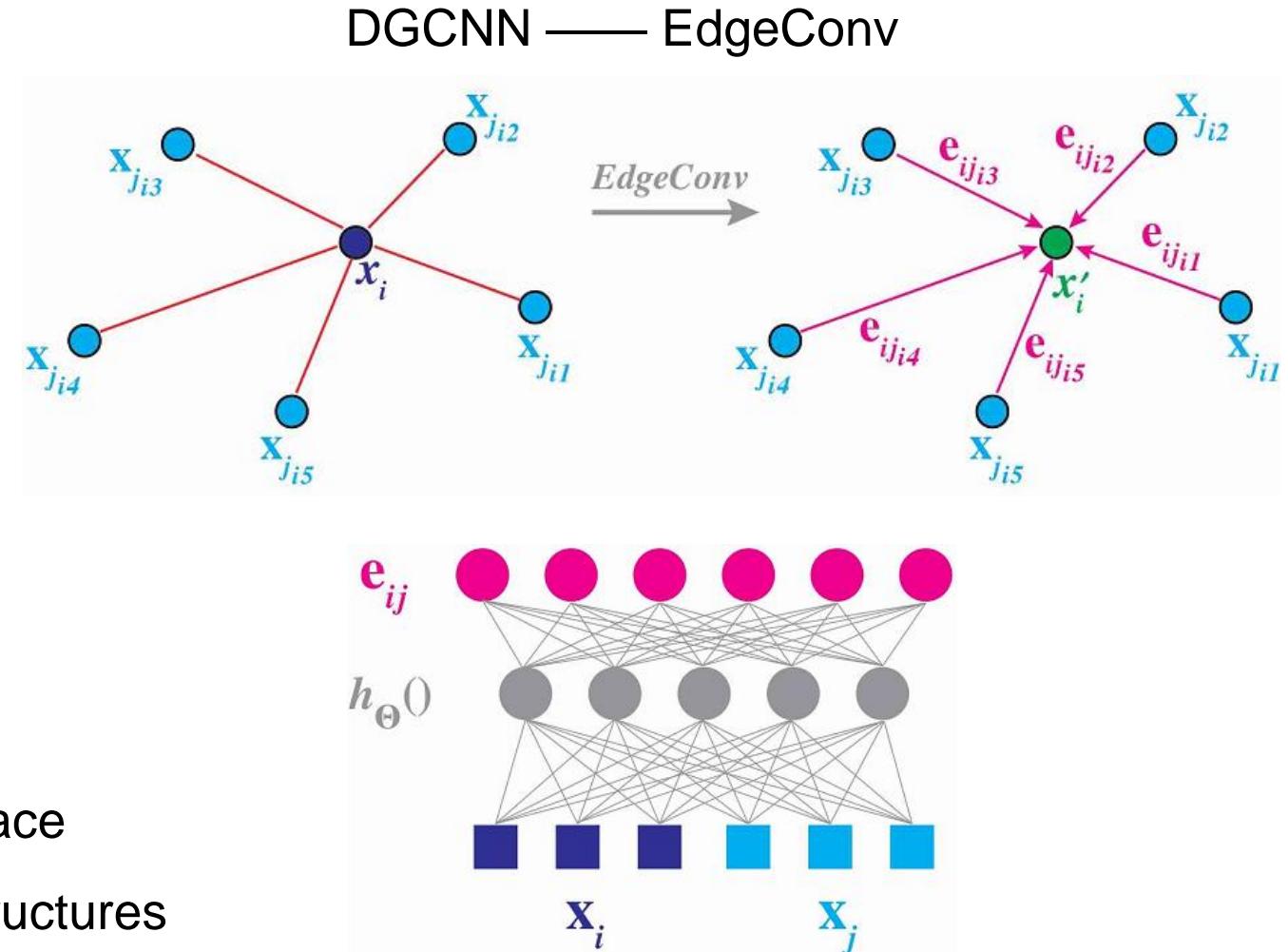


# Related Work DGCNN

global info.      local info.

$$h_{\Theta}(x_i, \boxed{x_j - x_i})$$

$$x'_i = \max_{j:(i,j) \in \mathcal{E}} h_{\Theta}(x_i, x_j).$$

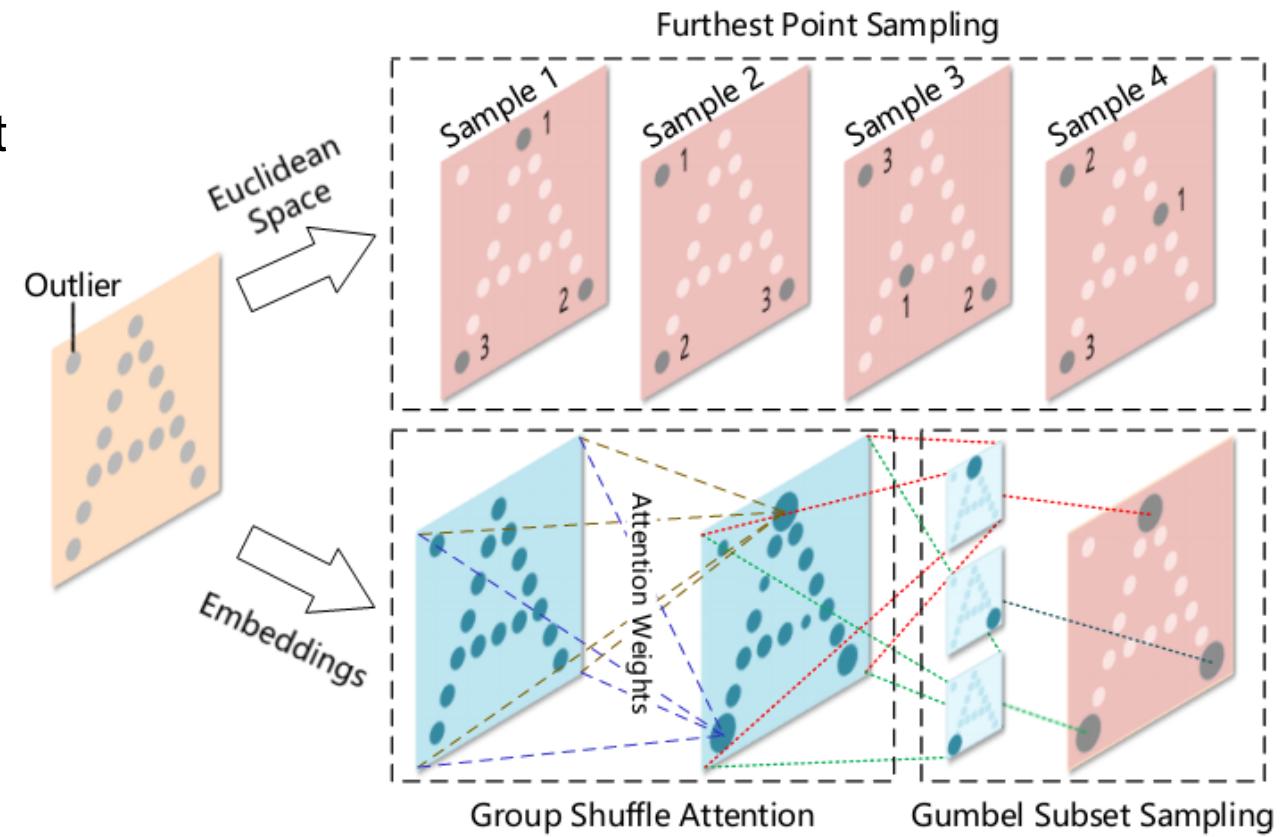


- Neighbors are found in feature space
- Learn from semantically similar structures

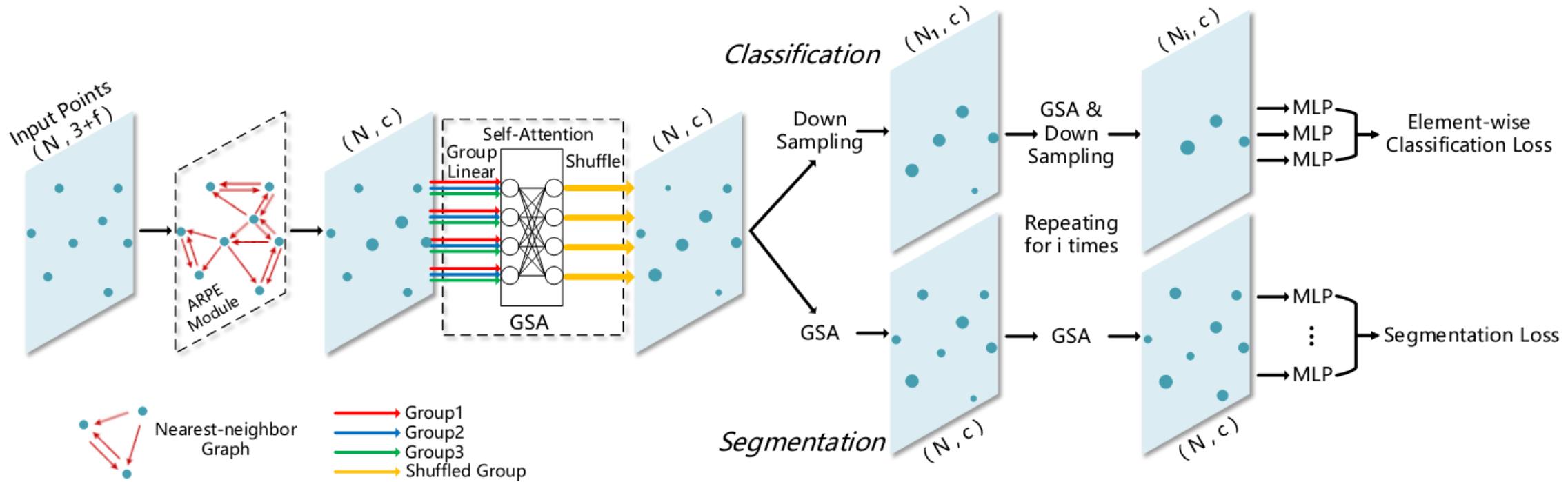
# Related Work self-attention

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- Relation modeling: self-attention
- Gumbel Subset Sampling VS. Farthest Point Sampling
  - permutation-invariant
  - high-dimension embedding space
  - differentiable



# Related Work self-attention



Embedding: PointNet

$$X'_p = \{(x_p, x_i - x_p) \mid i \neq p\}.$$

Self-attention:

group convolution + channel shuffle + pre-activation

# Related Work self-attention

$$X_i \in \mathbb{R}^{N_i \times c}$$

$$X_{i+1} \in \mathbb{R}^{N_{i+1} \times c} \subseteq X_i$$

Gumbel Subset Sampling:

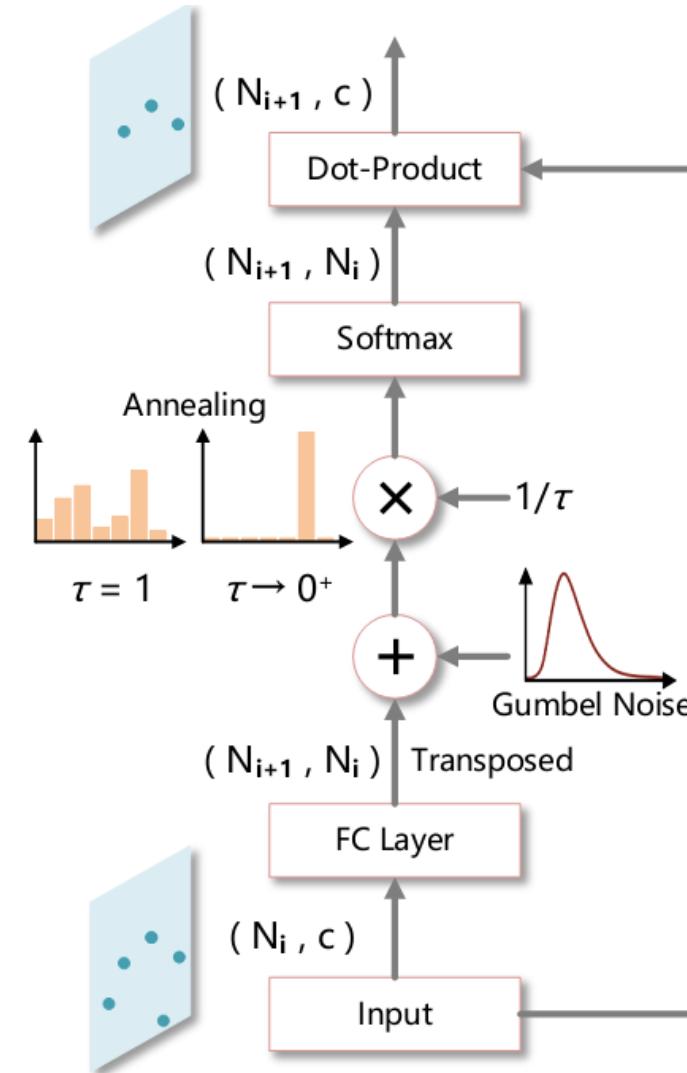
$$y = \text{softmax}(w X_i^T) \cdot X_i, \quad w \in \mathbb{R}^c.$$

↓ discrete reparameterization trick

$$y_{\text{gumbel}} = \text{gumbel\_softmax}(w X_i^T) \cdot X_i, \quad w \in \mathbb{R}^c.$$

↓ multiple point version

$$GSS(X_i) = \text{gumbel\_softmax}(W X_i^T) \cdot X_i, \quad W \in \mathbb{R}^{N_{i+1} \times c}.$$



## **Related work – convolution on point cloud**

# Related Work Kernel Point Convolution

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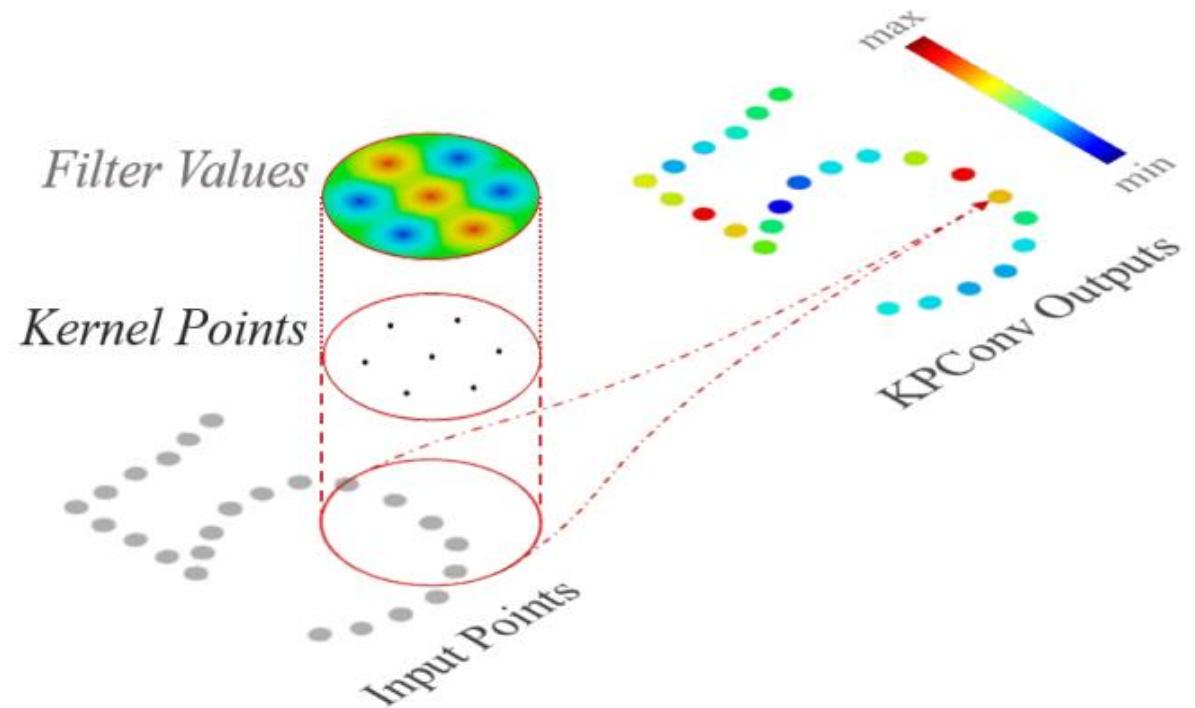
$$(\mathcal{F} * g)(x) = \sum_{x_i \in \mathcal{N}_x} g(x_i - x) f_i$$

$$\begin{aligned} y_i &= x_i - x \\ \mathcal{B}_r^3 &= \{y \in \mathbb{R}^3 \mid \|y\| \leq r\} \end{aligned}$$

$$g(y_i) = \sum_{k < K} h(y_i, \tilde{x}_k) W_k$$

kernel points:  $\{\tilde{x}_k \mid k < K\} \subset \mathcal{B}_r^3$   
 $\{W_k \mid k < K\} \subset \mathbb{R}^{D_{in} \times D_{out}}$

$$h(y_i, \tilde{x}_k) = \max \left( 0, 1 - \frac{\|y_i - \tilde{x}_k\|}{\sigma} \right)$$



# Related Work Kernel Point Convolution

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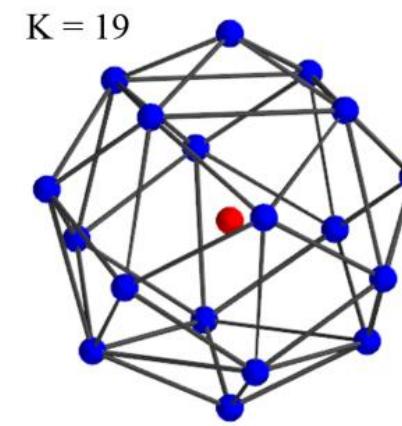
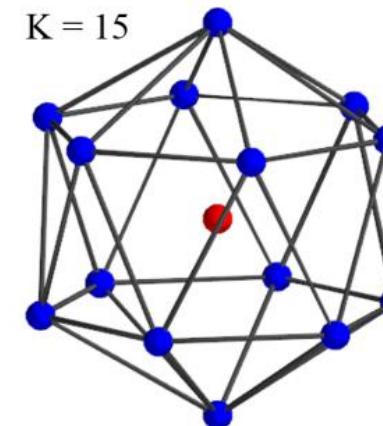
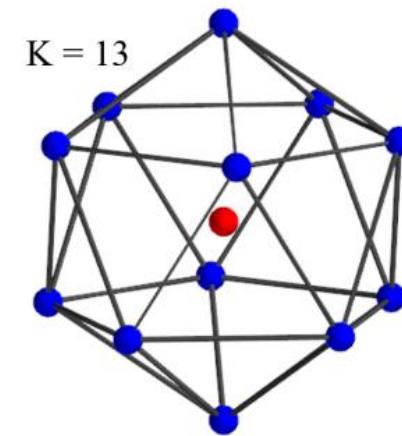
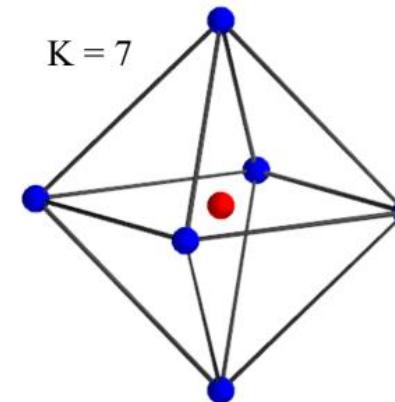
repulsive potential:

$$\forall x \in \mathbb{R}^3, \quad E_k^{rep}(x) = \frac{1}{\|x - \tilde{x}_k\|}$$

attractive potential:

$$\forall x \in \mathbb{R}^3, \quad E^{att}(x) = \|x\|^2$$

$$E^{tot} = \sum_{k < K} \left( E^{att}(\tilde{x}_k) + \sum_{l \neq k} E_k^{rep}(\tilde{x}_l) \right)$$



# Related Work Kernel Point Convolution

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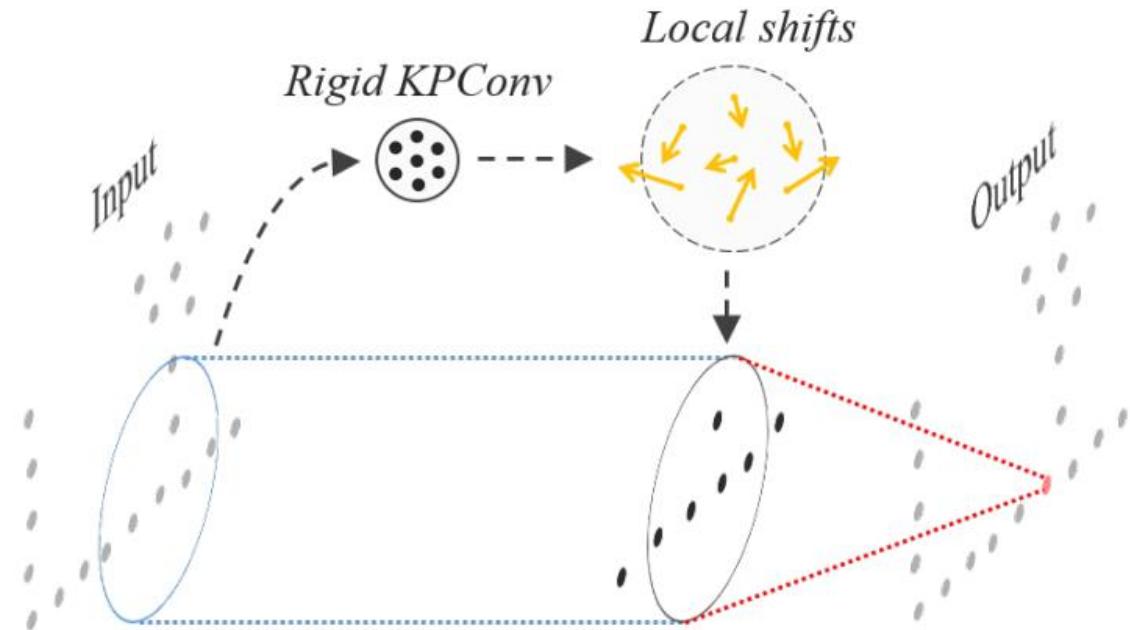
Rigid:  $(\mathcal{F} * g)(x) = \sum_{x_i \in \mathcal{N}_x} g(x_i - x) f_i$

$$g(y_i) = \sum_{k < K} h(y_i, \tilde{x}_k) W_k$$

Deformable: fit the local geometry

$$(\mathcal{F} * g)(x) = \sum_{x_i \in \mathcal{N}_x} g_{deform}(x - x_i, \Delta(x)) f_i$$

$$g_{deform}(y_i, \Delta(x)) = \sum_{k < K} h(y_i, \tilde{x}_k + \Delta_k(x)) W_k$$



# Github: [awesome-point-cloud-analysis](#)



## - Recent papers (from 2017)

### Keywords

`dat.` : dataset | `cls.` : classification | `rel.` : retrieval | `seg.` : segmentation  
`det.` : detection | `tra.` : tracking | `pos.` : pose | `dep.` : depth  
`reg.` : registration | `rec.` : reconstruction | `aut.` : autonomous driving  
`oth.` : other, including normal-related, correspondence, mapping, matching, alignment, compression...

### 2017

- [CVPR] PointNet: Deep Learning on Point Sets for 3D Classification and Segmentation. [[tensorflow](#)][[pytorch](#)] [ `cls.` `seg.` `det.` ]
- [CVPR] Dynamic Edge-Conditioned Filters in Convolutional Neural Networks on Graphs. [ `cls.` ]
- [CVPR] SyncSpecCNN: Synchronized Spectral CNN for 3D Shape Segmentation. [[torch](#)] [ `seg.` `oth.` ]
- [CVPR] ScanNet: Richly-annotated 3D Reconstructions of Indoor Scenes. [[project](#)][[git](#)] [ `dat.` `cls.` `rel.` `seg.` `oth.` ]
- [CVPR] Scalable Surface Reconstruction from Point Clouds with Extreme Scale and Density Diversity. [ `oth.` ]
- [CVPR] Efficient Global Point Cloud Alignment using Bayesian Nonparametric Mixtures. [[code](#)] [ `oth.` ]
- [CVPR] Discriminative Optimization: Theory and Applications to Point Cloud Registration. [ `reg.` ]
- [CVPR] 3D Point Cloud Registration for Localization using a Deep Neural Network Auto-Encoder. [[git](#)] [ `reg.` ]

# **Relation-Shape Convolutional Neural Network for Point Cloud Analysis (RS-CNN)**

**Yongcheng Liu, Bin Fan, Shiming Xiang, Chunhong Pan**

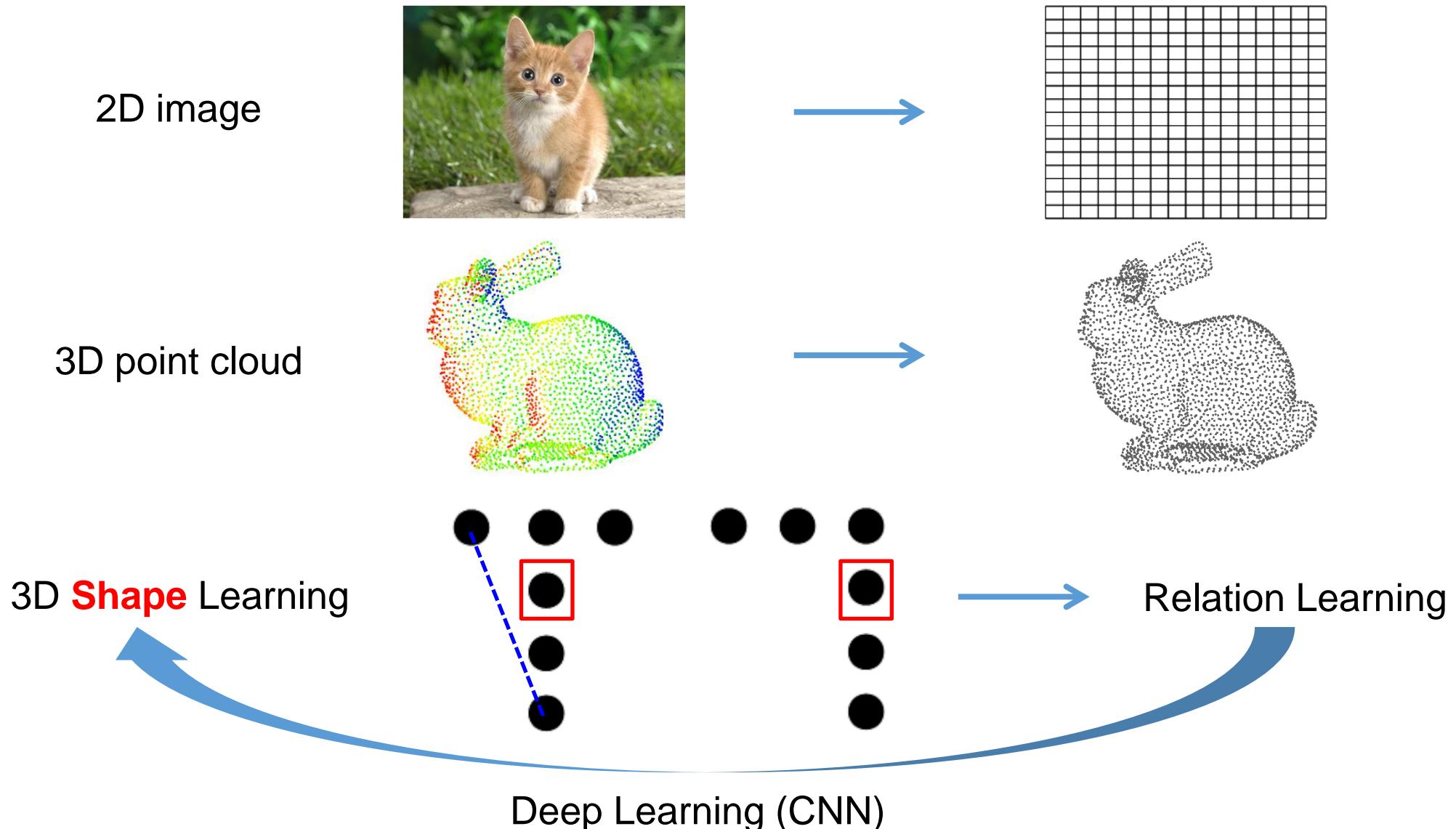
**CVPR 2019 Oral Presentation**

**Project Page:** <https://yochengliu.github.io/Relation-Shape-CNN/>



# RS-CNN

## Motivation



### Relation-Shape Convolution (RS-Conv)

local point subset  $P_{\text{sub}} \subset \mathbb{R}^3 \longrightarrow$  spherical neighborhood:  $x_i + x_j \in \mathcal{N}(x_i)$

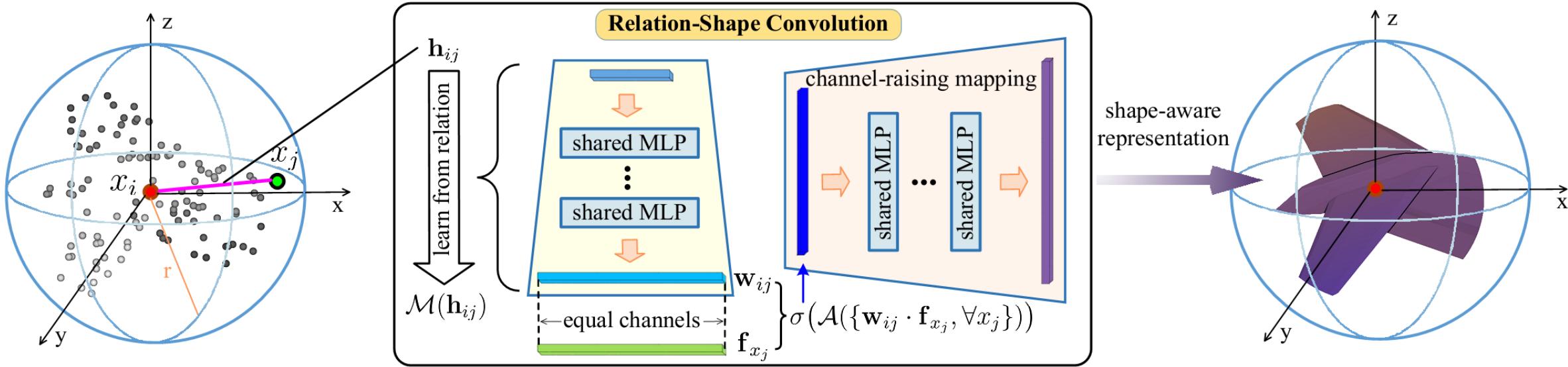
$$\mathbf{f}_{P_{\text{sub}}} = \sigma(\mathcal{A}(\{\mathcal{T}(\mathbf{f}_{x_j}), \forall x_j\}))^1, d_{ij} < r \quad \forall x_j \in \mathcal{N}(x_i) \quad y = \sigma(\sum \mathbf{W} * \mathbf{X})$$

$\mathcal{T}$ : feature transformation     $\mathcal{A}$ : feature aggregation

- Permutation invariance: only when  $A$  is symmetric and  $T$  is shared over each point
  - Limitations of CNN: weight is not shared  
gradient only w.r.t single point - implicit
  - Conversion: learn from relation
- $\mathcal{T}(\mathbf{f}_{x_j}) = \mathbf{w}_j \cdot \mathbf{f}_{x_j}$
- $\mathbf{h}_{ij}$ : predefined geometric priors  $\rightarrow$  low-level relation
- $\mathbf{f}_{P_{\text{sub}}} = \sigma(\mathcal{A}(\{\mathcal{M}(\mathbf{h}_{ij}) \cdot \mathbf{f}_{x_j}, \forall x_j\}))$
- $\mathcal{M}$ : mapping function(shared MLP)  $\rightarrow$  high-level relation

# RS-CNN

## Method



high-level relation encoding + channel raising mapping

low-level relation  $\mathbf{h}_{ij}$  : (3D Euclidean distance,  $x_i - x_j$ ,  $x_i$ ,  $x_j$ ) 10 channels

$$\mathbf{f}_{P_{\text{sub}}} = \sigma(\mathcal{A}(\{\mathcal{M}(\mathbf{h}_{ij}) \cdot \mathbf{f}_{x_j}, \forall x_j\}))$$

- ✓ Permutation invariance
- ✓ Robustness to rigid transformation in Relation Learning, e.g., 3D Euclidean distance
- ✓ Points' interaction
- ✓ Weight sharing

Revisiting 2D Conv:

$$\text{output} = \sum_{j=1}^9 w_j x_j$$

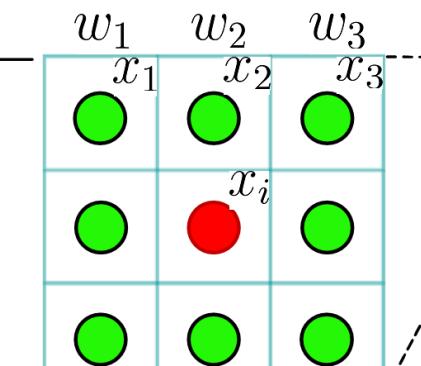
$w_1 \rightarrow w_{i1}$ : top left

$w_2 \rightarrow w_{i2}$ : right above

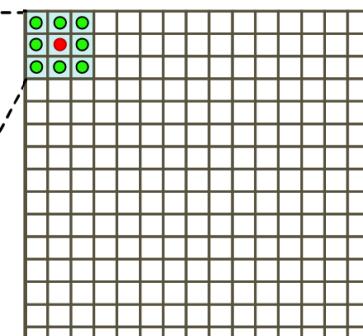
$w_3 \rightarrow w_{i3}$ : top right

⋮

grid relation



convolution kernel

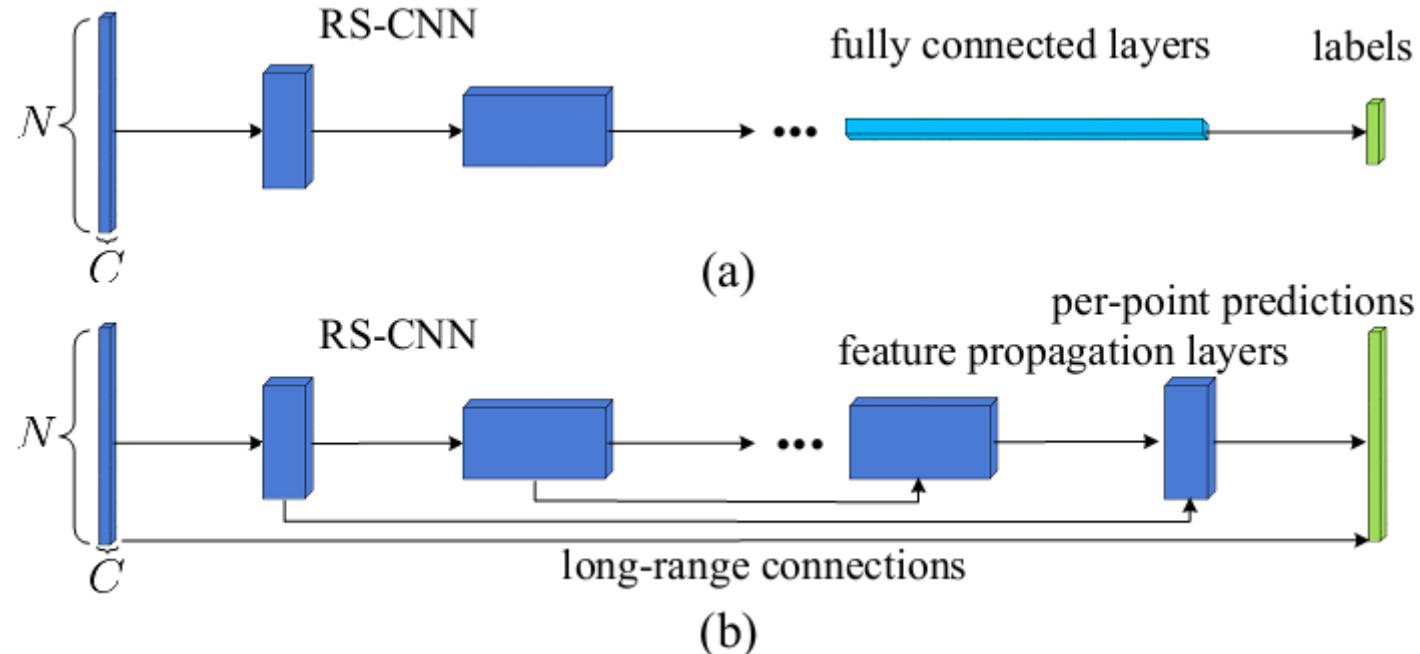


feature map

RS-Conv with relation learning is more general and can be applied to model 2D grid spatial relationship.

# RS-CNN

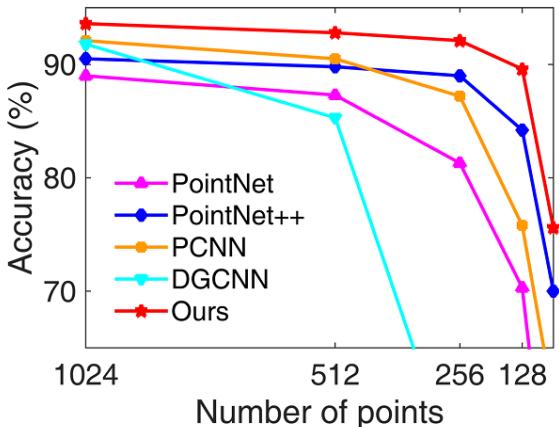
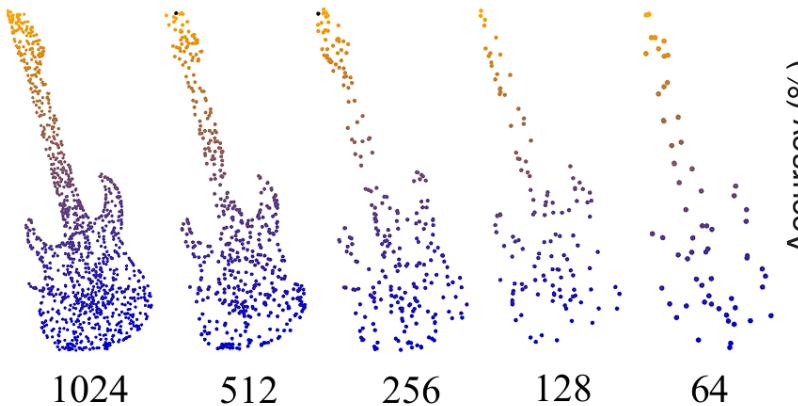
## RS-CNN



Farthest Point Sampling + Sphere Neighborhood + RS-Conv

## ModelNet40 benchmark

## Robustness to sampling density

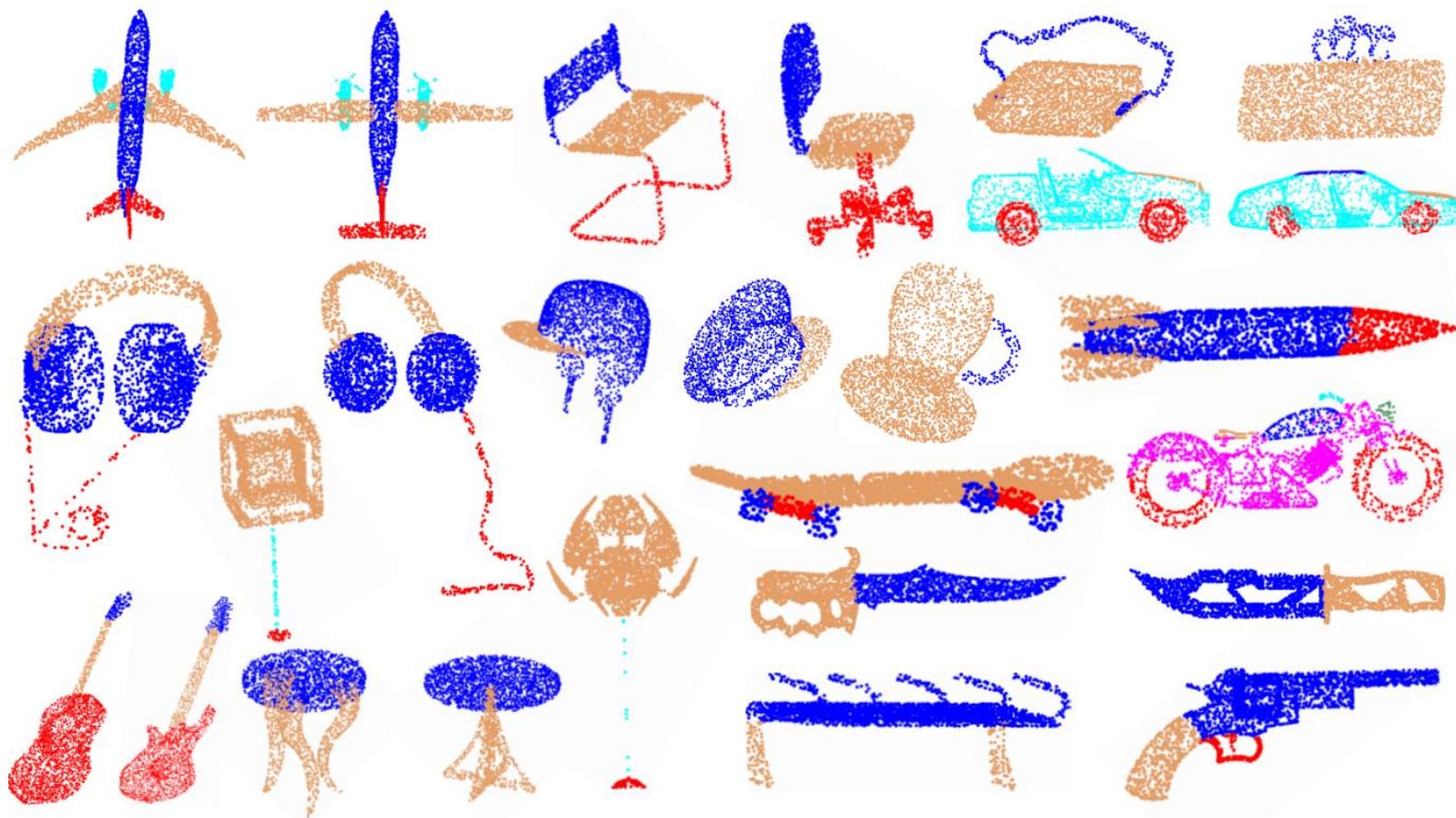


method	input	#points	acc.
Pointwise-CNN [10]	xyz	1k	86.1
Deep Sets [48]	xyz	1k	87.1
ECC [31]	xyz	1k	87.4
PointNet [24]	xyz	1k	89.2
SCN [44]	xyz	1k	90.0
Kd-Net(depth=10) [16]	xyz	1k	90.6
PointNet++ [26]	xyz	1k	90.7
KCNet [30]	xyz	1k	91.0
MRTNet [3]	xyz	1k	91.2
Spec-GCN [38]	xyz	1k	91.5
PointCNN [21]	xyz	1k	91.7
DGCNN [41]	xyz	1k	92.2
PCNN [1]	xyz	1k	92.3
<b>Ours</b>	<b>xyz</b>	<b>1k</b>	<b>93.6</b>
SO-Net [19]	xyz	2k	90.9
Kd-Net(depth=15) [16]	xyz	32k	91.8
O-CNN [39]	xyz, nor	-	90.6
Spec-GCN [38]	xyz, nor	1k	91.8
PointNet++ [26]	xyz, nor	5k	91.9
SpiderCNN [45]	xyz, nor	5k	92.4
SO-Net [19]	xyz, nor	5k	93.4

method	input	class	instance	air	bag	cap	car	chair	ear	guitar	knife	lamp	laptop	motor	mug	pistol	rocket	skate	table
		mIoU	mIoU	plane					phone					bike				board	
Kd-Net [16]	4k	77.4	82.3	80.1	74.6	74.3	70.3	88.6	73.5	90.2	87.2	81.0	94.9	57.4	86.7	78.1	51.8	69.9	80.3
PointNet [24]	2k	80.4	83.7	83.4	78.7	82.5	74.9	89.6	73.0	91.5	85.9	80.8	95.3	65.2	93.0	81.2	57.9	72.8	80.6
RS-Net [11]	-	81.4	84.9	82.7	<b>86.4</b>	84.1	78.2	90.4	69.3	91.4	87.0	83.5	95.4	66.0	92.6	81.8	56.1	75.8	82.2
SCN [44]	1k	81.8	84.6	83.8	80.8	83.5	79.3	90.5	69.8	<b>91.7</b>	86.5	82.9	96.0	69.2	93.8	82.5	<b>62.9</b>	74.4	80.8
PCNN [1]	2k	81.8	85.1	82.4	80.1	85.5	79.5	90.8	73.2	91.3	86.0	85.0	95.7	73.2	94.8	83.3	51.0	75.0	81.8
SPLATNet [34]	-	82.0	84.6	81.9	83.9	88.6	79.5	90.1	73.5	91.3	84.7	84.5	<b>96.3</b>	69.7	<b>95.0</b>	81.7	59.2	70.4	81.3
KCNet [30]	2k	82.2	84.7	82.8	81.5	86.4	77.6	90.3	76.8	91.0	87.2	84.5	95.5	69.2	94.4	81.6	60.1	75.2	81.3
DGCNN [41]	2k	82.3	85.1	<b>84.2</b>	83.7	84.4	77.1	90.9	78.5	91.5	87.3	82.9	96.0	67.8	93.3	82.6	59.7	75.5	82.0
<b>Ours</b>	<b>2k</b>	<b>84.0</b>	<b>86.2</b>	83.5	84.8	<b>88.8</b>	<b>79.6</b>	<b>91.2</b>	<b>81.1</b>	91.6	<b>88.4</b>	<b>86.0</b>	96.0	<b>73.7</b>	94.1	<b>83.4</b>	60.5	<b>77.7</b>	<b>83.6</b>
PointNet++ [26]	2k,nor	81.9	85.1	82.4	79.0	87.7	77.3	90.8	71.8	91.0	85.9	83.7	95.3	71.6	94.1	81.3	58.7	76.4	82.6
SyncCNN [47]	mesh	82.0	84.7	81.6	81.7	81.9	75.2	90.2	74.9	93.0	86.1	84.7	95.6	66.7	92.7	81.6	60.6	82.9	82.1
SO-Net [19]	1k,nor	80.8	84.6	81.9	83.5	84.8	78.1	90.8	72.2	90.1	83.6	82.3	95.2	69.3	94.2	80.0	51.6	72.1	82.6
SpiderCNN [45]	2k,nor	82.4	85.3	83.5	81.0	87.2	77.5	90.7	76.8	91.1	87.3	83.3	95.8	70.2	93.5	82.7	59.7	75.8	82.8

class mIoU 1.7↑      instance mIoU 1.1↑

Best results over 10 categories

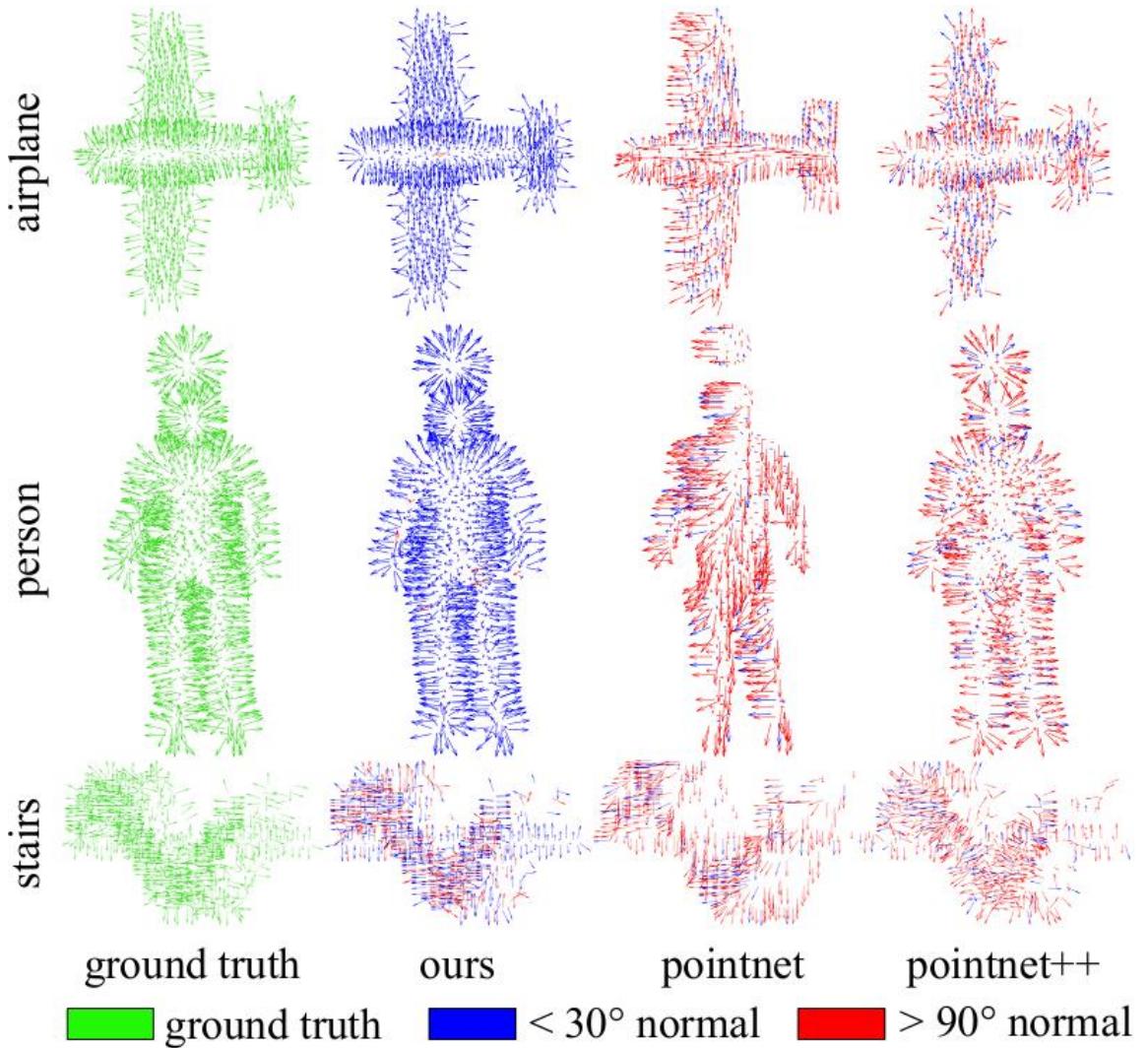


Diverse, confusing shapes

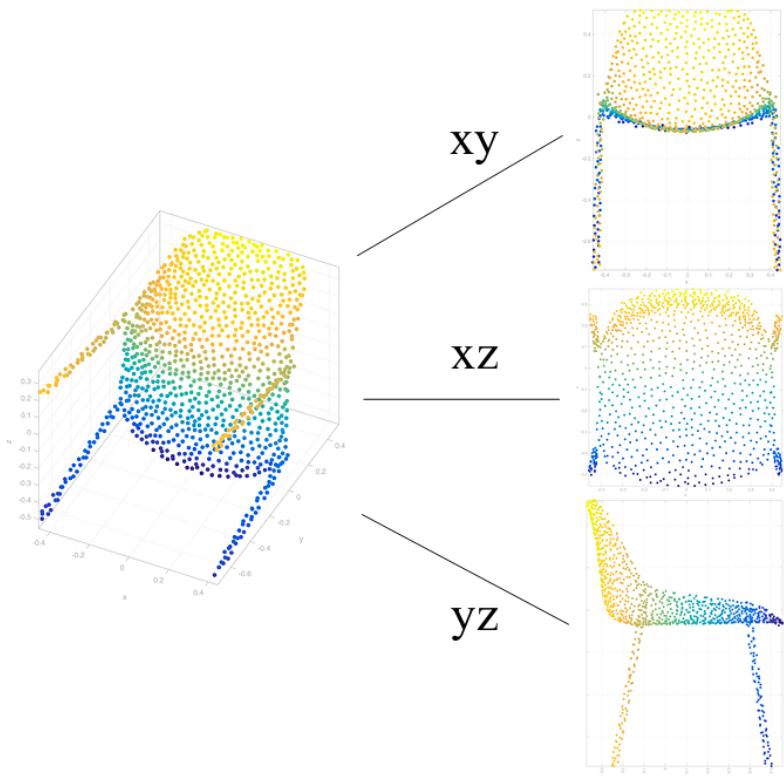
Table 3. Normal estimation error on ModelNet40 dataset.

dataset	method	#points	error
ModelNet40	PointNet [1]	1k	0.47
	PointNet++ [1]	1k	0.29
	PCNN [1]	1k	0.19
	<b>Ours</b>	<b>1k</b>	<b>0.15</b>

less effective for some intractable shapes,  
such as spiral stairs and intricate plants



$$\mathbf{f}_{P_{\text{sub}}} = \sigma(\mathcal{A}(\{\mathcal{M}(\mathbf{h}_{ij}) \cdot \mathbf{f}_{x_j}, \forall x_j\}))$$



model	low-level relation $\mathbf{h}$	channels	acc.
A	(3D-Ed)	1	92.5
B	(3D-Ed, $x_i - x_j$ )	4	93.0
C	(3D-Ed, $x_i - x_j, x_i, x_j$ )	10	<b>93.6</b>
D	(3D-cosd, $x_i^{\text{nor}}, x_j^{\text{nor}}$ )	7	92.8
E	(2D-Ed, $x'_i - x'_j, x'_i, x'_j$ )	10	$\approx 92.2$

low-level relation $\mathbf{h}$	channels	acc.
(XY-Ed, $x_i^{\text{xy}} - x_j^{\text{xy}}, x_i^{\text{xy}}, x_j^{\text{xy}}$ )	10	92.1
(XY-Ed, $x_i^{\text{xz}} - x_j^{\text{xz}}, x_i^{\text{xz}}, x_j^{\text{xz}}$ )	10	92.1
(XY-Ed, $x_i^{\text{yz}} - x_j^{\text{yz}}, x_i^{\text{yz}}, x_j^{\text{yz}}$ )	10	92.2
fusion of above three views		92.5

## Robustness to point permutation and rigid transformation

relation: 3D

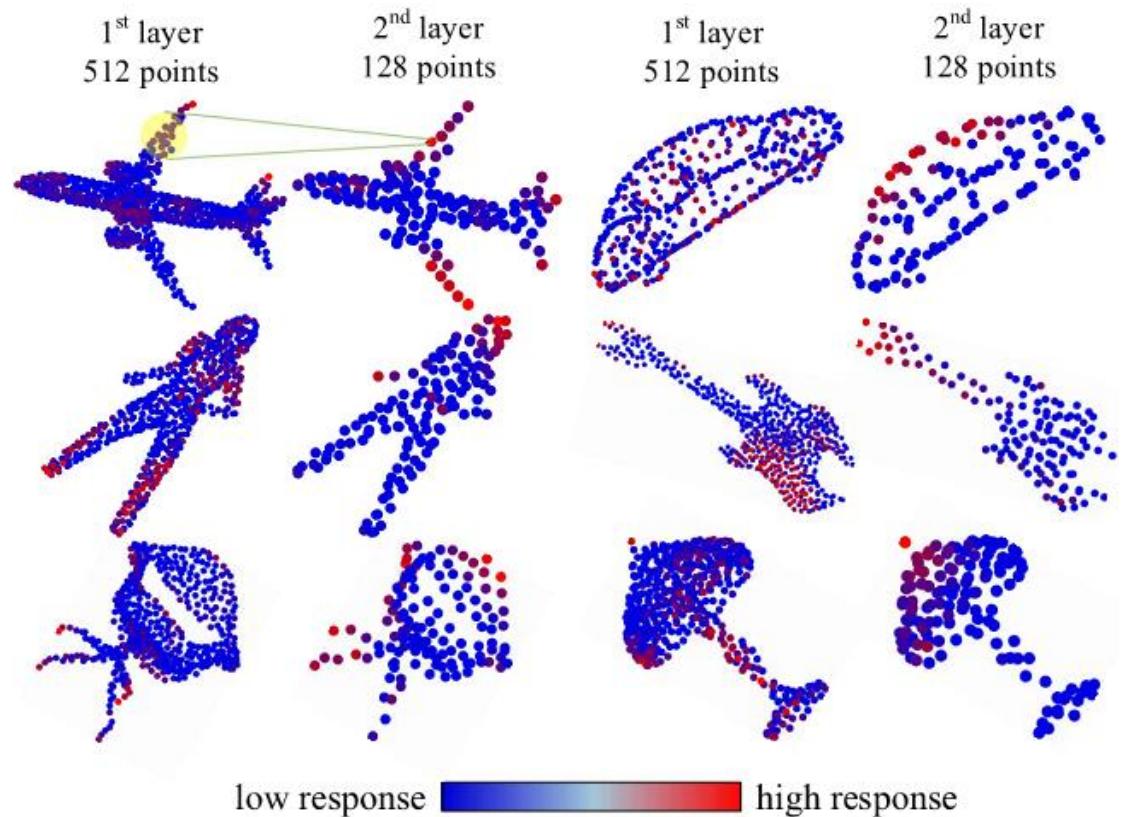
Euclidean distance

	method	acc.	perm.	+0.2	-0.2	90°	180°
PointNet [24]	88.7	88.7	70.8	70.6	42.5	38.6	
PointNet++ [26]	88.2 <sup>†</sup>	88.2	88.2	88.2	47.9	39.7	
<b>Ours</b>	<b>90.3<sup>†</sup></b>	<b>90.3</b>	<b>90.3</b>	<b>90.3</b>	<b>90.3</b>	<b>90.3</b>	

$$\mathbf{f}_{P_{\text{sub}}} = \sigma(\mathcal{A}(\{\mathcal{M}(\mathbf{h}_{ij}) \cdot \mathbf{f}_{x_j}, \forall x_j\}))$$

## Model complexity

method	#params	#FLOPs/sample
PointNet [24]	3.50M	440M
PointNet++ [21]	1.48M	1684M
PCNN [21]	8.20M	<b>294M</b>
<b>Ours</b>	<b>1.41M</b>	295M



# **Relation-Shape Convolutional Neural Network for Point Cloud Analysis**

We propose a learn-from-relation convolution operator, which extends 2D CNN to irregular configuration for point cloud analysis.

**Thanks for your attention !**