Potenzen und Wurzeln

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1 Übung Potenzen

1.
$$(-1)^{2n-1} = -1$$

2.
$$-10^2 = -100$$

3.
$$(-10)^{-3} = \frac{1}{(-10)^3} = -\frac{1}{1000}$$

4.
$$((-2)^3)^2 = 64$$

5.
$$(-1)^{-2n} = \frac{1}{(-1)^{2n}} = 1$$

6.
$$-\left(\frac{3}{2}\right)^{-4} = -\left(\frac{2}{3}\right)^{-4} = -\frac{16}{81}$$

7.
$$x^7 \cdot x^{-3} \cdot x^{-2} = x^{7-3-2} = x^2$$

8.
$$\frac{y^3 \cdot x^{-2}}{(x \cdot y)^2} = \frac{y^3}{x^2 \cdot y^2 \cdot x^2} = \frac{y}{x^4}$$

9.
$$\left(\frac{z^{-5}}{z^{-2}}\right)^{-2} = \left(\frac{z^2}{z^5}\right)^{-2} = \left(\frac{z^5}{z^2}\right)^2 = (z^3)^2 = z^6$$

10.
$$\left(\frac{3}{5}\right)^4 \div \left(\frac{6}{25}\right)^4 = \left(\frac{3}{5} \cdot \frac{25}{6}\right)^4 = \left(\frac{5}{2}\right)^4 = \frac{625}{16}$$

11.
$$a^{n-2} \cdot a^{1-n} = a^{n-2+1-n} = \frac{1}{a}$$

12.
$$(a-b)^3 \cdot (b-a)^{-3} = \frac{(a-b)^3}{(-1 \cdot (a-b))^3} = -1$$

13.
$$b^{2x-1} \cdot b^{2x+1} \div b^{3x-1} = b^{2x-1+2x+1-3x+1} = b^{x+1} = b \cdot b^x$$

$$14. \left(\frac{a^2}{b^3}\right)^{-2} \cdot \frac{5a^3}{2b^2} \cdot 2ab^{-4} = \left(\frac{b^3}{a^2}\right)^2 \cdot \frac{5a^3}{2b^2} \cdot \frac{2a}{b^4} = 5$$

15.
$$\frac{4n^{-2}m^4}{5c^2x^{-3}} \div \frac{8m^3c^{-1}x}{15n^{-2}c} = \frac{4m^4x^3}{5c^2 \cdot n^2} \cdot \frac{15c \cdot c}{n^2 \cdot 8m^3x} = \frac{3mx^2}{2n^4}$$

16.
$$\frac{u^2 - t^2}{2u^2 + 4ut + 2t^2} = \frac{(u - t) \cdot (u + t)}{2 \cdot (u + t) \cdot (u + t)} = \frac{u - t}{2 \cdot (u + t)}$$

17.
$$(r+r^{-1})^2 - (r-r^{-1})^2 = r^2 + 2 + \frac{1}{r^2} - (r^2 - 2 + \frac{1}{r^2}) = 4$$

18.
$$(2-p)^3 = 8 - 12p + 6p^2 - p^3$$

19.
$$\frac{a^{15} - a^{10}}{a^5} = \frac{a^5 \cdot (a^{10} - a^5)}{a^5} = a^{10} - a^5$$

20.
$$\frac{\frac{a^2 - b^2}{ab + b^2}}{\frac{(a - b)^2}{ab^2}} = \frac{(a + b) \cdot (a - b)}{b \cdot (a + b)} \cdot \frac{ab \cdot b}{(a - b) \cdot (a - b)} = \frac{ab}{a - b}$$

2 Übung Wurzeln

1.
$$\frac{\sqrt{27}}{\sqrt{3}} = 3$$

$$2. \ \sqrt{\frac{4}{49}} = \frac{2}{7}$$

$$3. \sqrt{\frac{b^8}{25c^2}} = \frac{b^4}{5c}$$

$$4. \ \frac{\sqrt{a^3b}}{\sqrt{ab^5}} = \frac{a}{b^2}$$

$$5. \ \sqrt{2ac} \cdot \sqrt{\frac{8a}{c}} = 4a$$

6.
$$\sqrt{\frac{9m^3}{5n}} \div \sqrt{\frac{81m}{20n^5}} = \frac{2}{3}m \cdot n^2$$

7.
$$\sqrt[3]{8r^6t^4} = 2r^2 \cdot t^3 \sqrt[3]{t}$$

$$8. \sqrt{a} \cdot \sqrt[3]{a^2} = \mathbf{a} \cdot \sqrt[6]{a}$$

$$9. \ \frac{\sqrt{a} \cdot \sqrt[3]{a}}{\sqrt[6]{a}} = \sqrt[3]{a^2}$$

10.
$$\frac{\sqrt{x}}{x^{\frac{1}{3}}} = \sqrt[6]{x}$$

11.
$$\frac{y^{\frac{3}{4}} \cdot \sqrt[6]{y}}{y^{\frac{7}{12}}} = \sqrt[3]{y}$$

12.
$$(75x)^{\frac{1}{2}} \div (3x)^{\frac{1}{2}} = 5$$

Nenner ohne Wurzel:

13.
$$\frac{5}{\sqrt{3}+1} = \frac{5 \cdot \sqrt{3}-5}{2}$$

$$14. \ \frac{a-b}{\sqrt{a-b}} = \sqrt{a-b}$$

15.
$$\frac{\sqrt{5} + \sqrt{2}}{\sqrt{5} - \sqrt{2}} = \frac{7 + 2 \cdot \sqrt{10}}{3}$$

16.
$$1000^{-\frac{1}{3}} = \frac{1}{10}$$

17.
$$c^{-\frac{2}{3}} \cdot \sqrt[6]{c} \cdot c^{\frac{1}{2}} = 1$$

$$18. \sqrt[3]{z \cdot \sqrt[4]{\frac{1}{z}}} = \sqrt[4]{z}$$

19.
$$(8x^{-9})^{\frac{1}{3}} = \frac{2}{x^3}$$

$$20. \sqrt[3]{x\sqrt{x}} \cdot \frac{x^{\frac{1}{6}}}{\sqrt[3]{x}} = \sqrt[3]{x}$$

$$21. \ \sqrt[5]{\sqrt[4]{z^{10}}} = \sqrt{z}$$