

PBE-Based Selective Abstraction and Refinement for Efficient Property Falsification of Embedded Software

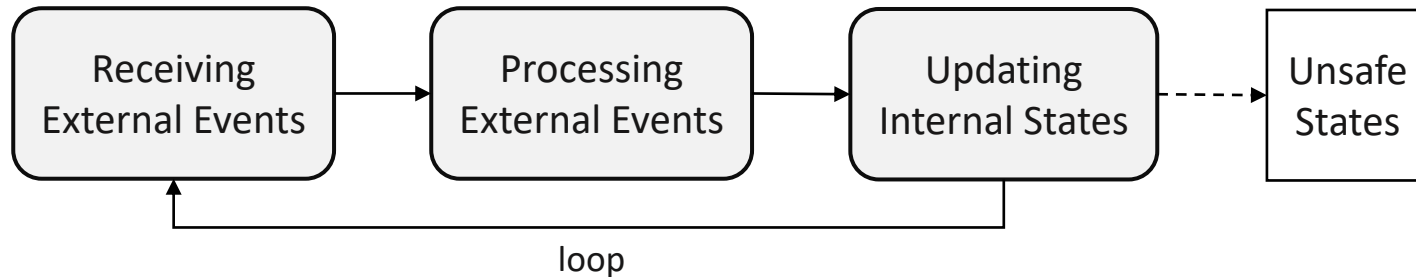
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Motivation

- Major characteristics of **embedded software**:
 - It constantly interacts with external events within an **infinite loop**
 - It maintains **internal states** whose updates must be traced
 - **Safety properties** may be violated only after many loop iterations



Motivation

- **Verification/Falsification** of embedded software:
 - e.g., (dis)proving “A car reduces its speed within a specified time”
- We have seen decades of effort for this:
 - Most of them were **model-based** approaches applied to cyber-physical systems, automobiles, or medical devices, etc.
 - **Code-based** property verification/falsification is very **expensive**

Table 1: Code-based property falsification of an elevator controller (about 900 LoC)

Tools	# of refinements	Time usage	Memory usage
CBMC	N/A	8.3 hours	> 80 GB (OOM)
CPAchecker	418	> 72 hours (T/O)	7.1 GB

Motivating Example

Embedded Control Program

```
int process(int *data) {
    int max_area = -1;
    int max_index = -1;
    for(int i = 0; i < data[0]; i++) {
        if(data[5 * i + 1] != 0) {
            int xul = data[i * 5 + 2];
            int xlr = data[i * 5 + 3];
            int yul = data[i * 5 + 4];
            int ylr = data[i * 5 + 5];
            int width = abs(xul - xlr);
            int height = abs(yul - ylr);
            int area = width * height;
            if(area >= max_area) {
                max_area = area;
                max_index = i;
            }
        }
    }
    return max_index; }
}
```

```
int timer = 0;
int speed = 0;
#define MAX_SPEED 100

int main() {
    int data[41];
    int i;
    while(1) {
        data = receive();
        i = process(data);
        if(i >= 0) {
            update(i, data);
        }
        assert(is_safe());
    }
}
```

```
void update(int i, int *data) {
    speed = speed + data[i * 5 + 1];
    if(speed > MAX_SPEED) {
        speed = MAX_SPEED; }
}
```

```
int is_safe() {
    if(speed >= MAX_SPEED){
        timer = timer + 1;
    }
    else timer = 0;
    return timer < 1000;}
```

- Checking this **concrete** program suffers from state space explosion (OOM)
- Abstracting this program too **coarsely** produces many false alarms

Motivating Example

Embedded Control Program

```
int process(int *data) {  
    int max_area = -1;  
    int max_index = -1;  
    for(int i = 0; i < data[0]; i++) {  
        if(data[5 * i + 1] != 0) {  
            int val = data[i * 5 + 2];  
            int  
            int  
            int  
            int  
            int  
            int  
            int  
            if(area >= max_area) {  
                max_area = area;  
                max_index = i;  
            }  
        }  
    }  
    return max_index; }  
}
```

```
int timer = 0;  
int speed = 0;  
#define MAX_SPEED 100  
int main() {  
    if(i >= 0) {  
        update(i, data);  
    }  
    assert(is_safe());  
}
```

**We need to find a better abstraction approach
for embedded software domain**

```
if(i >= 0) {  
    update(i, data);  
}  
assert(is_safe());  
}
```

```
int is_safe() {  
    if(speed >= MAX_SPEED){  
        timer = timer + 1;  
    }  
    else timer = 0;  
    return timer < 1000;}
```

- Checking this **concrete** program suffers from state space explosion (OOM)
- Abstracting this program too **coarsely** produces many false alarms

Main Idea 1: Selective Abstraction

Auxiliary Function

```
int process(int *data) {
    int max_area = -1;
    int max_index = -1;
    for(int i = 0; i < data[0]; i++) {
        if(data[5 * i + 1] != 0) {
            int xul = data[i * 5 + 2];
            int xlr = data[i * 5 + 3];
            int yul = data[i * 5 + 4];
            int ylr = data[i * 5 + 5];
            int width = abs(xul - xlr);
            int height = abs(yul - ylr);
            int area = width * height;
            if(area >= max_area) {
                max_area = area;
                max_index = i;
            }
        }
    }
    return max_index; }
```

Main Control Logic

```
int timer = 0;
int speed = 0;
#define MAX_SPEED 100

int main() {
    int data[41];
    int i;
    while(1) {
        data = receive();
        i = process(data);
        if(i >= 0) {
            update(i, data);
        }
        assert(is_safe());
    }
}
```

```
void update(int i, int *data) {
    speed = speed + data[i * 5 + 1];
    if(speed > MAX_SPEED) {
        speed = MAX_SPEED; }
}
```

```
int is_safe() {
    if(speed >= MAX_SPEED){
        timer = timer + 1;
    }
    else timer = 0;
    return timer < 1000;}
```

- **Auxiliary functions:** functions that do *not* update any internal states (e.g., global variables)

Main Idea 1: Selective Abstraction

Auxiliary Function

```
int process(int *data) {
    int max_area = -1;
    int max_index = -1;
    for(int i = 0; i < data[0]; i++) {
        if(data[5 * i + 1] != 0) {
            int xul = data[i * 5 + 2];
            // ... (omitted) ...
            int height = abs(yul - ylr);
            int area = width * height;
            if(area >= max_area) {
                max_area = area;
                max_index = i;
            }
        }
    }
    return max_index; }
```

Abstraction!

Main Control Logic

```
int timer = 0;
int speed = 0;
#define MAX_SPEED 100

int main() {
    int data[41];
    int i;
    while(1) {
        data = receive();
        i = process(data);
        if(i >= 0) {
            update(i, data);
        }
        assert(is_safe());
    }
}
```

**No
Abstraction**

```
i, int *data) {
    + data[i * 5 + 1];
    X_SPEED) {
        SPEED; }}
```

```
int is_safe() {
    if(speed >= MAX_SPEED){
        timer = timer + 1;
    }
    else timer = 0;
    return timer < 1000;}
```

- **Main control logic** has a significant impact on the program & property
- Abstracting the **main control logic** is likely to produce many false alarms

Main Idea 2: PBE-Based Abstraction

(1) Initial Abstraction

```
int process(int *data) {  
    return nondet();  
}
```

240 seconds, but **false alarm**

(2) Refined Abstraction

```
int process(int *data) {  
    if(0 != data[36])  
        if(data[0] >= data[15]) return 6;  
        else return 7;  
    else if(0 != data[1])  
        if(data[12] < data[40]) return 5;  
        else if(data[18] >= data[20]) return 1;  
        else return 0;  
    else if(0 != data[21]) return 4;  
    else return -1; }
```

260 seconds, and **true alarm!**

(3) No Abstraction

```
int process(int *data) {  
    int max_area = -1;  
    int max_index = -1;  
    for(int i = 0; i < data[0]; i++) {  
        if(data[5 * i + 1] != 0) {  
            int xul = data[i * 5 + 2];  
            int xlr = data[i * 5 + 3];  
            int yul = data[i * 5 + 4];  
            int ylr = data[i * 5 + 5];  
            int width = abs(xul - xlr);  
            int height = abs(yul - ylr);  
            int area = width * height;  
            if(area >= max_area) {  
                max_area = area;  
                max_index = i;  
            }  
        }  
    }  
    return max_index; }
```

Out-Of-Memory

Scalable & Imprecise

Precise & Scalable

Precise & Expensive

Coarsest

refinements...

Concrete

Main Idea 2: PBE-Based Abstraction

(1) Initial Abstraction

```
int process(int *data) {  
    return nondet();  
}
```

240 seconds, but **false alarm**

(2) Programming-By-Example (PBE) Based Abstraction

```
int process(int *data) {  
    if(0 != data[36])  
        if(data[0] >= data[15]) return 6;  
        else return 7;  
    else if(0 != data[1])  
        if(data[12] < data[40]) return 5;  
        else if(data[18] >= data[20]) return 1;  
        else return 0;  
    else if(0 != data[21]) return 4;  
    else return -1; }
```

260 seconds, and **true alarm!**

(3) No Abstraction

```
int process(int *data) {  
    int max_area = -1;  
    int max_index = -1;  
    for(int i = 0; i < data[0]; i++) {  
        if(data[5 * i + 1] != 0) {  
            int xul = data[i * 5 + 2];  
            int xlr = data[i * 5 + 3];  
            int yul = data[i * 5 + 4];  
            int ylr = data[i * 5 + 5];  
            int width = abs(xul - xlr);  
            int height = abs(yul - ylr);  
            int area = width * height;  
            if(area >= max_area) {  
                max_area = area;  
                max_index = i;  
            }  
        }  
    }  
    return max_index; }
```

Out-Of-Memory

**We could synthesize this abstraction
using only 33 input-output examples!**

Scalable & Imprecise

Precise & Scalable

Precise & Expensive

Coarsest

Concrete

PBEAR: PBE-Based Selective Abstraction and Refinement

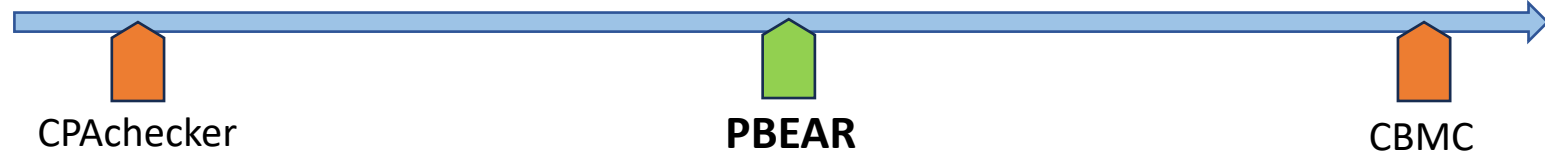
- ✓ **PBEAR** suggests **selective abstraction** for efficient property falsification of embedded software
- ✓ **PBEAR** is **the first approach** utilizing **PBE** for more precise & scalable abstraction
- ✓ Out of 15 safety properties from three embedded software, **PBEAR** finds **5 to 12 more true alarms** than CBMC and CPAchecker

Imprecise: 13 T/Os with 2,556 refinements

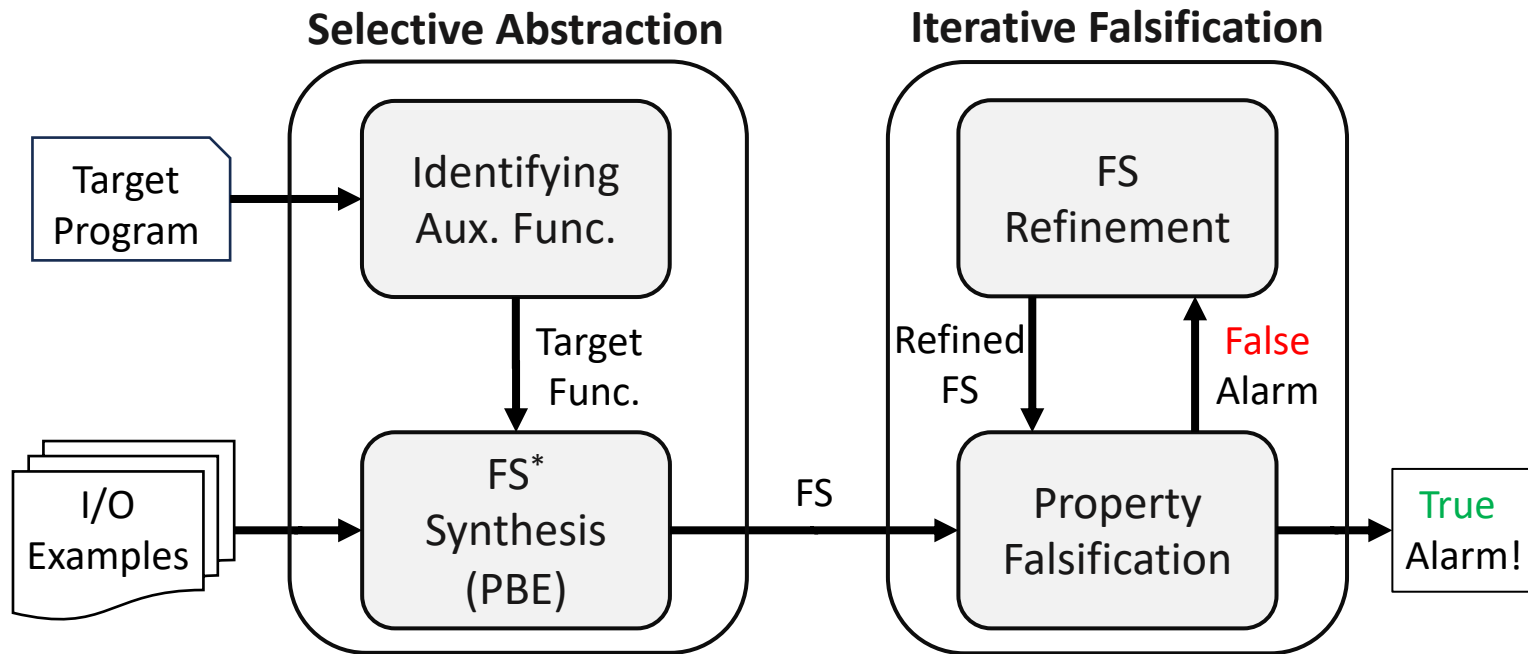
Scalable: 30% less memory than PBEAR

Precise: no need for refinement

Expensive: Out-Of-Memory in 6 cases



Overall Process of PBEAR



*FS: Function Summary

Problems & Solutions for Utilizing PBE

- **PBE** takes input/output (I/O) examples and produces a program that satisfies the given examples

Auxiliary Function

```
int gcd(int a, int b){  
    if (a < 0) a = -a;  
    if (b < 0) b = -b;  
    while (b != 0) {  
        int t = b;  
        b = a % b;  
        a = t;  
    }  
    return a;  
}
```

I/O Examples

```
gcd(1, -1) == 1  
gcd(4, 2) == 2  
gcd(9, -3) == 3
```

PBE

Function Summary (FS)

```
int fs_gcd(int a, int b){  
    if (b < 0) return -b;  
    else return b;  
}
```

1. Overfitting problems in PBE:

- ✓ Iterative function summary synthesis

2. PBE-based refinement may reproduce infeasible paths:

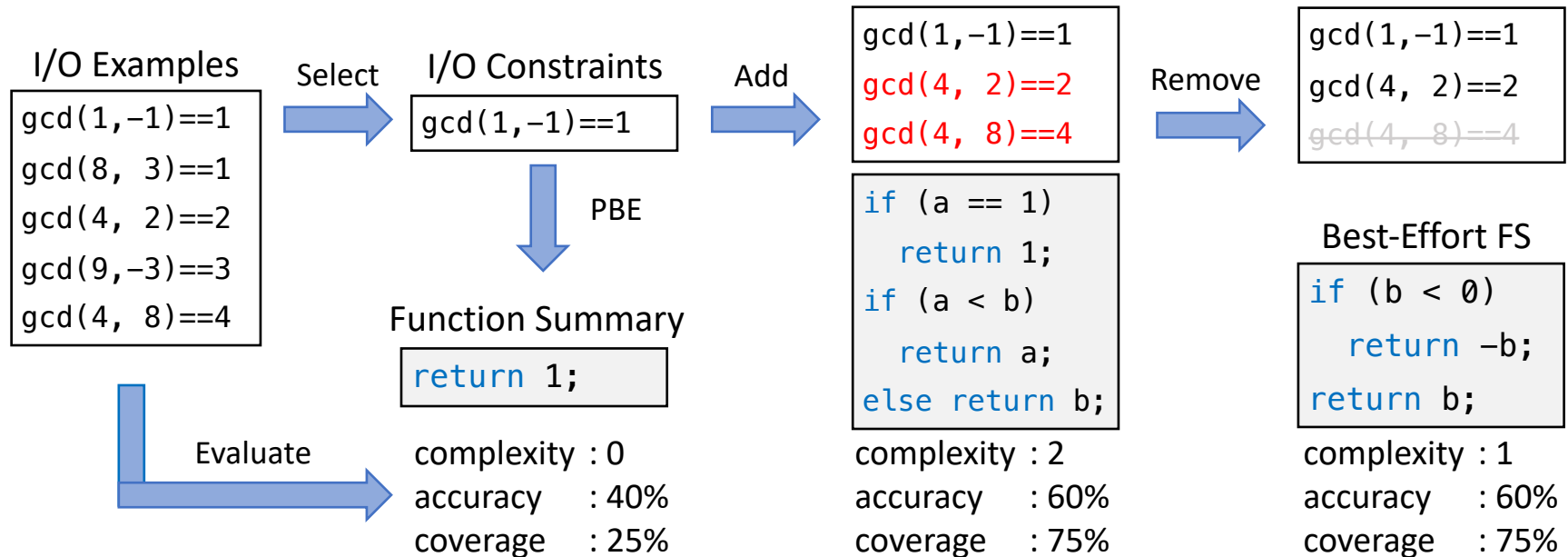
- ✓ A novel PBE-based refinement with symbolic alarm filtering

1. Overfitting → Iterative FS Synthesis

Measurement:

- **Complexity:** # of branch statements
- **Similarity:** accuracy and output coverage

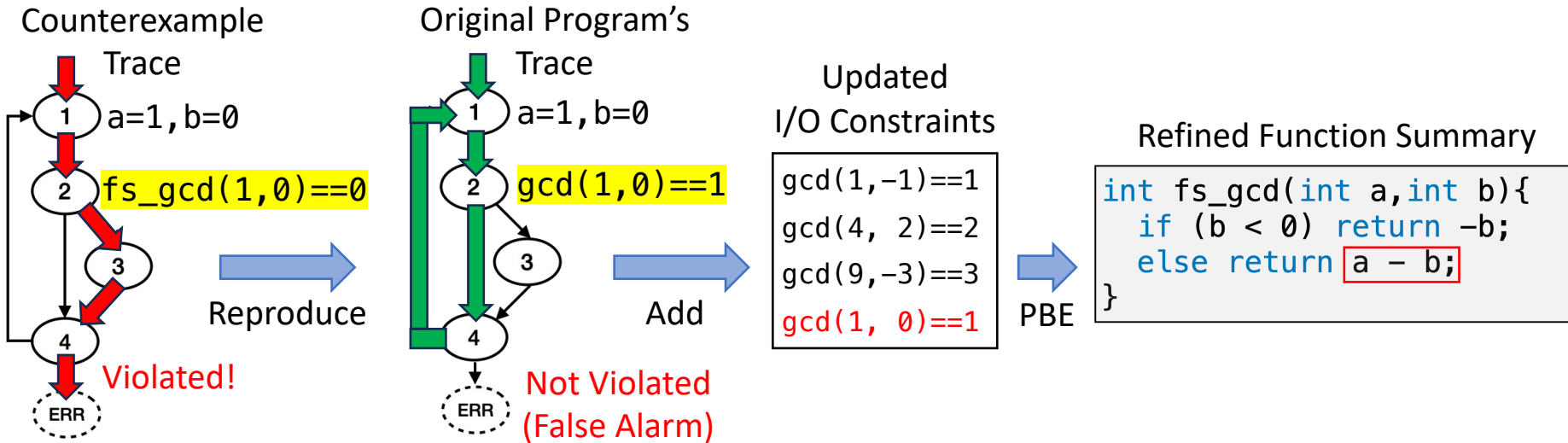
Synthesize until a given
time budget (1 hour)



2. PBE Produces Infeasible Paths

Baseline of refinement approach:

1. Add new I/O constraints from the **false alarm**
2. Re-synthesize FS using the updated I/O constraints



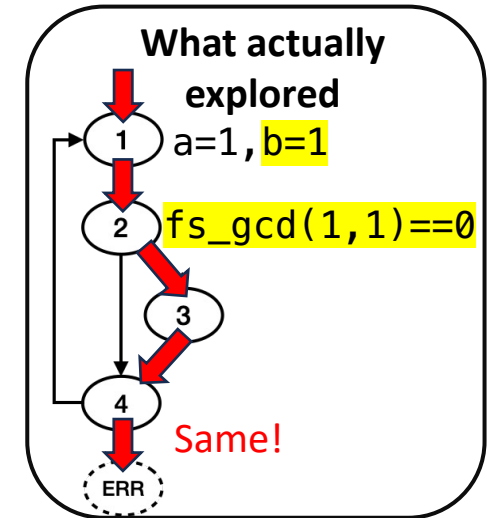
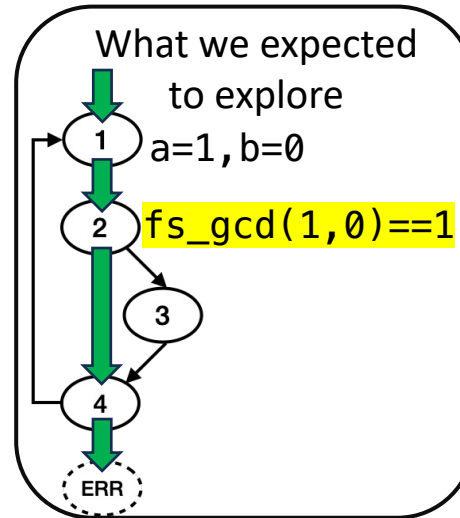
2. PBE Reproduces Infeasible Paths

Problem: No guarantee for avoiding re-exploration of **previously identified infeasible paths**

Refined Function Summary

```
int fs_gcd(int a, int b){  
  if (b < 0) return -b;  
  else return a - b;  
}
```

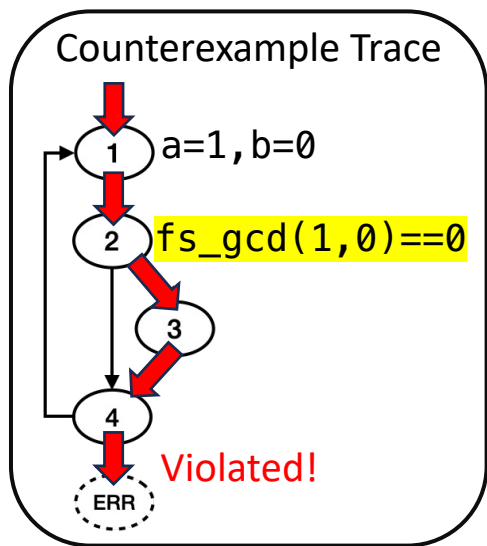
Falsify



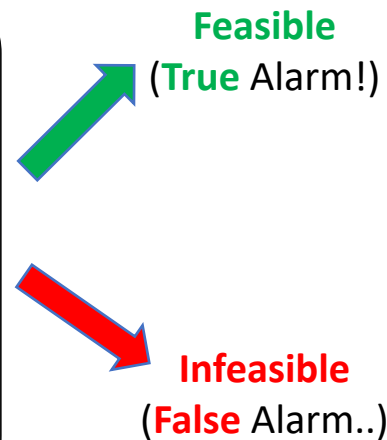
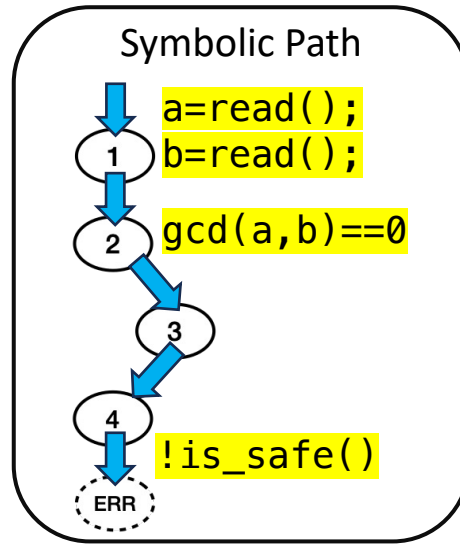
There is **another I/O example** leading to the same infeasible path

2. Solution: PBE-Based Refinement with Symbolic Alarm Filtering

1. Convert the counterexample trace into a **symbolic path**
2. Check the feasibility of the symbolic path using SAT solving

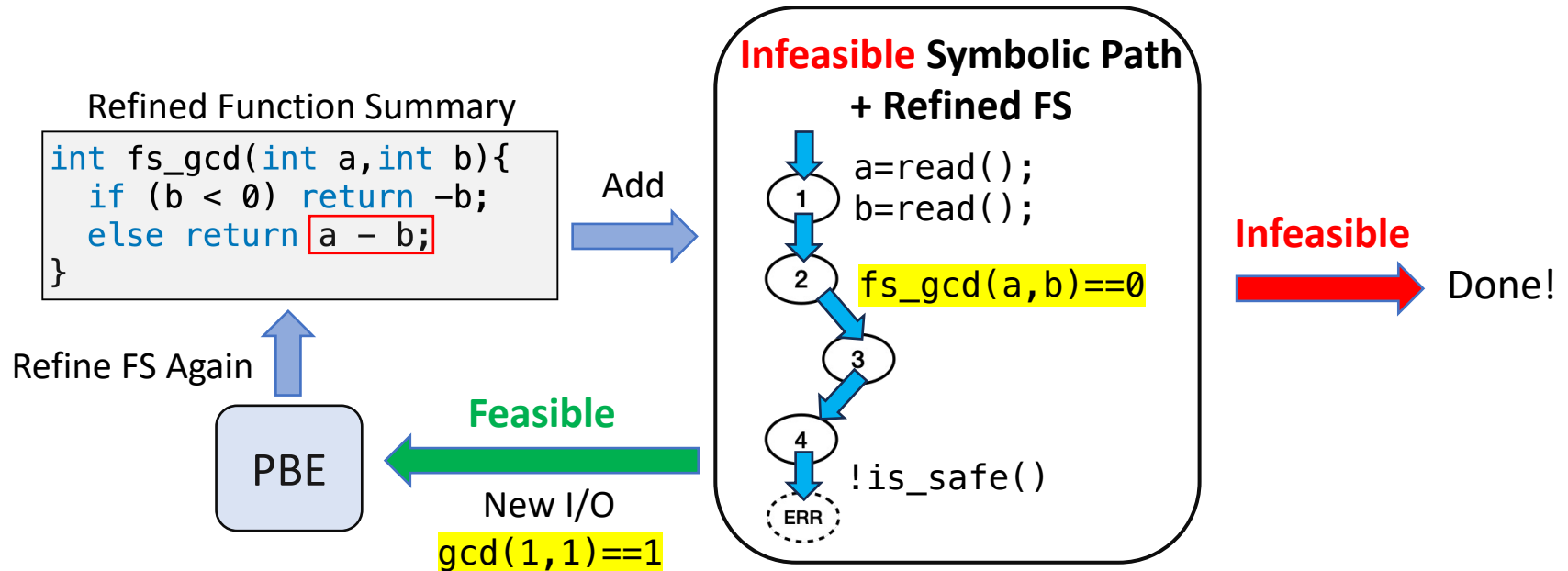


Symbolize

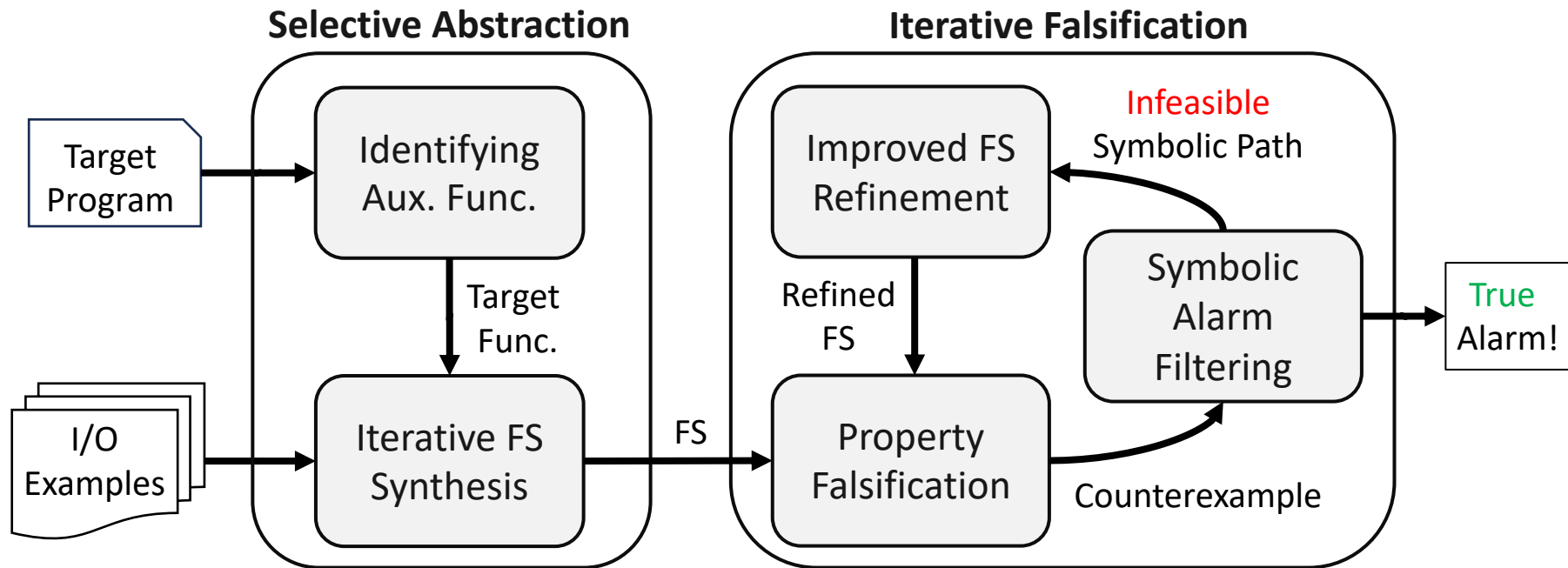


2. Solution: PBE-Based Refinement with Symbolic Alarm Filtering

3. Iteratively refine FS using PBE until it does not make **infeasible** symbolic path **feasible**



(Refined) Overall Process of PBEAR



Experiments

- Target
 - Checking assertion violations for 16 benchmark programs from SV-COMP
 - 15 safety properties from 3 embedded software (about 800~1,000 LoC)
 - Object following car, elevator controller, and clean-up robot
- RQ1: Performance of PBEAR vs. two state-of-the-art model checkers,
 - CBMC: bounded model checker
 - CPAchecker: predicate abstraction
- RQ2: Effectiveness of our improved FS refinement vs. PBEAR^{base}
 - PBEAR^{base}: baseline of refinement approach; no symbolic alarm filtering

* PBEAR uses DUET for function summary synthesis and CBMC for property falsification

RQ1: Performance of PBEAR (on SV-COMP)

Tools	# of refinements	Total time	Total memory	# of detected true alarms
PBEAR	9	485 s	3.1 GB	15/16
CBMC	N/A	177 s	3.9 GB	16/16
CPAchecker	57	4,334 s	10.3 GB	13/16

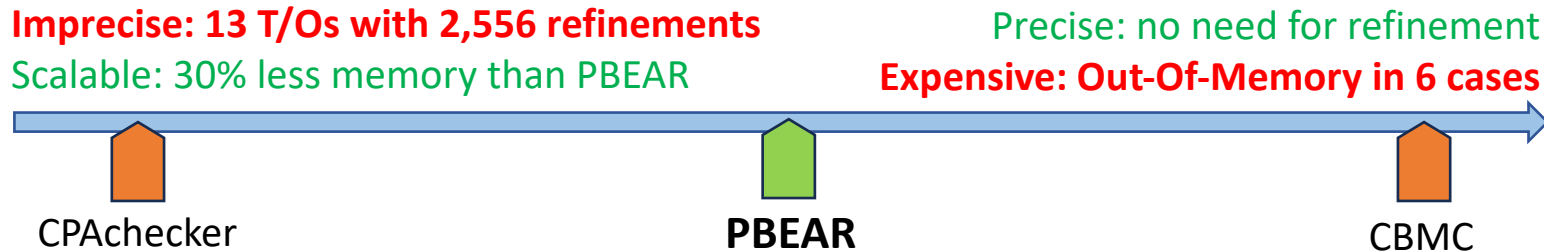
* T/O: 900 s

- CBMC was the best: the overhead of refinement did not pay off on these programs
- **PBEAR** showed competitive performance on **general-purpose programs**

RQ1: Performance of PBEAR (on Embedded Software)

Tools	# of refinements	Total time	Total memory	# of detected true alarms
PBEAR	77	135.4 h	423.5 GB	14/15
CBMC	N/A	96.9 h	748.9 GB	9/15
CPAchecker	2,556	936.3 h	336.8 GB	2/15

* T/O: 72 hours; Out-Of-Memory: 80 GB



RQ2: Effectiveness of Our Improved FS Refinement

Tools	# of refinements	Total time	# of detected true alarms
PBEAR	86	133.6 h	13/15
PBEAR ^{base} (without symbolic alarm filtering)	210	217.4 h	12/15

* We omitted benchmarks where any refinements were not conducted by PBEAR^{base}

PBEAR^{base} took additional 124 refinements and 83.6 more hours

Conclusion

- Contributions
 - **PBEAR is the first work** utilizing **PBE** for **selective abstraction**
 - We suggested **a novel refinement approach** with **symbolic alarm filtering**
 - PBEAR showed **promising results** on three **embedded software** and competitive performance on general-purpose programs
- Future Work
 - PBEAR is highly dependent on the performance & limitation of PBE
 - We may need to combine PBEAR with other abstraction techniques
 - We plan to further investigate the applicability of PBEAR to:
 - Programs in other domains with control-oriented structures