

## Problem A. pr0hum and the Weekend

Input file: standard input  
Output file: standard output  
Time limit: 1 second  
Memory limit: 512 megabytes

The Weekend is around the corner, and pr0hum and his friends are throwing a party because, Happy Weekend, for which they have invited  $n$  guests to the party numbered from 1 to  $n$

For an unknown experiment made up just for the sake of this question, pr0hum wants to collect some data and has gathered a list of  $m$  entries of who follows whom on Instagram. For example, if one entry in the list is  $a\ b$ , it implies  $a$  follows  $b$ .

Before the party starts, pr0hum wants you to arrange the data so that he can later work in peace. He wants you to print  $n$  lines where the  $i^{th}$  line would contain all the people person  $i$  follows.

### Input

The first line contains two integers  $n, m$ . The number of guests invited to the party and the number of entries in the list which pr0hum has.

The next  $m$  lines have two integers  $u, v$ . Implying Guest  $u$  follows Guest  $v$ .

$$2 \leq n \leq 10^5$$

$$1 \leq m \leq 2 * 10^5$$

$$1 \leq u, v \leq n$$

### Output

Print  $n$  lines, where the  $i^{th}$  line has all the people person  $i$  follows.

Print the People person  $i$  follows in the order given in the list of entries, i.e. if  $a\ b$  comes before  $a\ c$  then in the  $a^{th}$  line of the output,  $b$  will come before  $c$ .

If someone follows no one print  $-1$  for them.

## Examples

standard input	standard output
10 10 2 5 5 6 1 4 6 8 2 6 3 6 1 10 8 9 2 3 5 8	4 10 5 6 3 6 -1 6 8 8 -1 9 -1 -1
14 8 1 2 2 7 3 4 6 3 5 7 3 8 6 8 11 12	2 7 4 8 -1 7 3 8 -1 -1 -1 -1 12 -1 -1 -1

10 7 6 1 1 4 4 2 2 8 2 5 4 7 5 3	4 8 5 -1 2 7 3 1 -1 -1 -1 -1
5 5 1 2 3 2 5 3 5 4 2 3	2 3 2 -1 3 4

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## Problem B. The Poisoned Knife Problem

Input file: standard input  
Output file: standard output  
Time limit: 1 second  
Memory limit: 256 megabytes

You and your friend have been doing the DSA Assignment this entire week, therefore, in order to take a break, you decide to play a game on the Happy Weekend.

The game is called The Poisoned Knife. In the game, your friend's character (Let's suppose X) has health of  $h$  units, your sole purpose in the game is to kill his character.

You can only attack X with a poisoned knife.

You are given an array,  $A$  where  $A_i$  denotes the time at which you are going to make a poisoned attack with the knife. For e.g., if  $A = [3, 4, 8]$ , then you are going to make the knife attack at time = 3, 4 and 8.

Note : Time array can be given in random order(not necessarily sorted).

When X is stabbed by the poisoned knife, a poison effect occurs on X, dealing 1 damage over the next  $k$  seconds (starting with the second after X was stabbed). However, if X is already poisoned, the knife will cancel the previous poison effect and apply a new one.

For example:

If  $k = 2$ , and  $A = [3, 4, 8]$ , then,

At  $t = 1$ , damage = 0

At  $t = 2$ , damage = 0

At  $t = 3$ , damage = 1

At  $t = 4$ , damage = 1

At  $t = 5$ , damage = 1

At  $t = 6$ , damage = 0

At  $t = 7$ , damage = 0

At  $t = 8$ , damage = 1

At  $t = 9$ , damage = 1

At  $t \geq 10$ , damage = 0

Therefore, total damage dealt to  $X = 5$

Now, you have to find the minimum value of  $k$  such that the total damage dealt to  $X$  is greater than or equal to  $h$ .

## Input

The first line contains a single integer  $q$  ( $1 \leq q \leq 1000$ ) — the number of test cases. The first line of the test case contains two integers  $n$  and  $h$  ( $1 \leq n \leq 100$ ;  $1 \leq h \leq 10^{18}$ ) — the number of attacks and the amount of damage that needs to be dealt. The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$  ( $1 \leq a_i \leq 10^9$ ), where  $a_i$  is the second when the  $i$ -th attack is performed.

## Output

For each test case, print a single integer — the minimum value of  $k$  such that the total damage dealt to  $X$  is greater than or equal to  $h$ .

## Examples

standard input	standard output
3 1 294 77 3 10 2 4 10 5 3 1 11 21 31 41	294 4 1
1 4 99 21 19 2 5	80
1 2 100 7 3	96
2 2 20 22 21 2 40 4 21	19 23

5 3 100 22 31 26 3 100 45 68 17 3 100 79 19 48 3 100 57 89 41 3 100 1 49 50	91 49 40 52 51
1 5 45 14 11 10 17 12	38

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## Problem C. Smooth, Smoother, Smoothest

Input file: standard input

Output file: standard output

Time limit: 1 second

Memory limit: 256 megabytes

*It is a universally accepted fact that the smoother the better.*

You are given an array  $A$  of size  $N$ . You can perform the following operations on the array:

Choose an  $i$  ( $1 \leq i \leq N$ ) and set  $A_i = x$  ( $1 \leq x \leq 10^9$ ).

Find the minimum number of operations needed to make the array  $A$   $k$ -smooth.

Let's first define a  $k$ -beautiful array. An array  $A$  is  $k$ -beautiful if all its elements are equal to  $k$ . For example,  $[3, 3, 3, 3]$  is  $3$ -beautiful.

Let  $|A|$  denote the size of the array  $A$ . An array  $A$  is called  $k$ -smooth if at least one of the following condition holds:

- $|A| > 1$ , first half of  $A$  is  $k$ -beautiful and the second half of  $A$  is  $(k+1)$ -smooth •
- $|A| > 1$ , second half of  $A$  is  $k$ -beautiful and the first half of  $A$  is  $(k+1)$ -smooth •
- $|A| = 1$ , and  $A$  is  $k$ -beautiful

The first half of an array  $A$  is the subarray  $A_1, A_2, \dots, A_{(n+1)/2}$ . The second half of an array  $A$  is the subarray  $A_{((n+1)/2)+1}, A_{((n+1)/2)+2}, \dots, A_n$ . (Here  $n$  is the size of the array.)

For example, for the array  $[3, 6, 3, 4, 3]$ ,  $[3, 6, 3]$  is the first half, and  $[4, 3]$  is the second half. **Input**

The first line contains two integers,  $N$  and  $k$ . The next line contains  $A_1, A_2, \dots, A_N$

$1 \leq N \leq 10^5$

$1 \leq k \leq 10^5$

$1 \leq A_i \leq 10^9$  for all  $(1 \leq i \leq N)$

## Output

Print the minimum number of operations needed to make the array  $A$

$k$ -smooth. Examples

standard input	standard output
5 4 5 5 6 4 4	0
8 1 3 5 1 1 1 1 2 2	4

## Note

In the first test case, the array  $A$  is already  $4$ -smooth.

In the second test case, we convert the array to  $[1, 1, 1, 1, 3, 4, 2, 2]$ . This takes 4 operations and the array is now  $1$ -smooth. The first half  $[1, 1, 1, 1]$  is  $1$ -beautiful and the second half  $[3, 4, 2, 2]$  is  $2$ -smooth. Then the second half of this  $[2, 2]$  is  $2$ -beautiful and  $[3, 4]$  is  $3$ -smooth. Finally,  $[3]$  is  $3$ -beautiful and  $[4]$  is  $4$ -smooth.