



Academic Year	Module	Assessment Number	Assessment Type
S20	Introductory Data Structures and Algorithms (DipIT02)	A1	Assignment Submission

[Assignment Submission]

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Tutorial - 8 - 1

- 1- \rightarrow We can divide a number by 2 until it reaches 1.
- 1- \rightarrow We can divide $\log_2(n)$ number by 2 until it reaches 1.
- 2- \rightarrow The worst case time for sequential search for finding an element in an array is linear time.
- 3- \rightarrow Array must be sorted for binary search.
- 4- \rightarrow Two entries with different keys have the same hash value.

S-1

key	hash value = $k \% 9$
5	$5 \% 9 = 5$
29	$29 \% 9 = 2$
20	$20 \% 9 = 2$
0	$0 \% 9 = 0$
27	$27 \% 9 = 0$
18	$18 \% 9 = 0$

By linear probing the hash table will be

Hash table:

0	0
1	27
2	29
3	20
4	18
5	5
6	
7	

Order by elements:
0, 27, 29, 20, 18, 5

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6 → load factor = $\frac{\text{no. of elements}}{\text{capacity of table}}$

$$= \frac{81}{812}$$

$$= 0.0998$$

7 → Direct hashing → Distinct position for every ~~pass~~ passing key.

9 →

keys	Hash value (h(k)) = key % 9	
5	$5 \% 9 = 5$	
28	$28 \% 9 = 1$	
19	$19 \% 9 = 1$	
19	$15 \% 9 = 6$	
20	$20 \% 9 = 2$	
23	$23 \% 9 = 5$	
33	$33 \% 9 = 6$	
12	$17 \% 9 = 8$	
17	$17 \% 9 = 8$	
10	$10 \% 9 = 1$	

Hash table for chaining.

0		
1	28	19
2	20	
3	12	
4		
5	5	
6	15	33
7		
8	17	

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8 → Hashing is a search technique that rely on the concept of hash table we provide key to a hash function to generate hash value.

Let's, Assume that we have the following hash function.

$$H(x) = x \bmod 10$$

$$\text{key}(x) = 21, 56, 72, 39, 48, 986, 13$$

Keys	Hash value
21	$21 \% 10 = 1$
56	$56 \% 10 = 6$
72	$72 \% 10 = 2$
39	$39 \% 10 = 9$
48	$48 \% 10 = 8$
986	$986 \% 10 = 6$ (collision occurs)
13	$13 \% 10 = 3$

Now, storing the hash value in hash table

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Hash Table

0		
1	21	
2	22	
3	13	
4		
5		
6	56	
7		
8	48	
9	39	

→ 986

10 ⇒ Soln. i low = L Bound

i High = U Bound

Do while i low <= i High

i middle = (i low + i High) / 2

if Target = Data Array (i middle) then
b found = true

Exit DO

else if Target < Data Array (i middle) then
i High = (i middle - 1)

else

i Low = (i middle + 1)

End if loop.

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Tutorial-8-2

1a).

Solution

Linear Probing

Keys	$h(k) = k \% 7$
19	$19 \% 7 = 5$
26	$26 \% 7 = 5$
13	$13 \% 7 = 6$
48	$48 \% 7 = 6$
17	$17 \% 7 = 3$

Hash table	
0	13
1	48
2	
3	17
4	
5	19
6	26

Order by elements: 13, 48, —, 17, —, 19, 26

b)

Keys	$h(k) = k \% 7$
19	$19 \% 7 = 5$
26	$26 \% 7 = 5$
13	$13 \% 7 = 6$
48	$48 \% 7 = 6$
17	$17 \% 7 = 3$

Separate chaining
Hash table

0		
1		
2		
3	17	
4		
5	19	→ 26
6	13	→ 48

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c Double Hashing

Keys	$h_1(k) = k \% 7$	$h_2(k) = 5 - (k_1 \% 5)$	Hash table	
19	$19 \% 7 = 5$	(Empty as no collision)	1	19
26	$26 \% 7 = 5$	$5 - (26 \% 5) = 4$	2	26
13	$13 \% 7 = 6$	(Empty)	3	13
48	$48 \% 7 = 6$	$5 - (48 \% 5) = 2$	4	
17	$17 \% 7 = 3$	(Empty)	5	17
			6	13

For hash value of 28 we use,

 $\{h_1(k) + i \cdot h_2(k)\} \% \text{table size}$ where $0 \leq i \leq$

$$\text{table size} = (5 + 4) \% 7$$

= 2 Similarly, for 48 new position is 1.

3. → As the functions have mod 10 so let's exclude them

Keys	$i = 2$	$i = 3$	$i = 4$	$i = 5$
0	0	2	0	0
1	1	1	1	1
2	4	8	4	2
3	9	22	9	3
4	16	64	16	4
5	25	125	25	5
6	36	216	36	6
7	49	343	49	7
8	64	512	64	8
9	81	729	81	9

11 represents the remainder after divided by 10.

As remainder value is repeated in every hash function.

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4-5 Solu

For a.

keys $h(k) = k \% 10$

46 $46 \% 10 = 6$

42 $42 \% 10 = 2$

34 $34 \% 10 = 4$

52 $52 \% 10 = 2$

23 $23 \% 10 = 3$

33 $33 \% 10 = 3$

0

1

2

3

4

5

6

7

8

42

23

34

32

546

33

No. as it doesn't match table format

For b

34 4

42 2

23 3

52 2

33 3

46 6

For c

46 6

34 4

42 2

23 3

33 2

33 3

as
Yes it does not
match table
format

No. as it does not match table format

For d.

42 2

46 6

33 3

23 3

34 4

52 2

No. as it does not match table format.

