



Academic Year	Module	Assessment Number	Assessment Type
S20	Introductory Data Structures and Algorithms (DipIT02)	A1	Assignment Submission

[Assignment Submission]

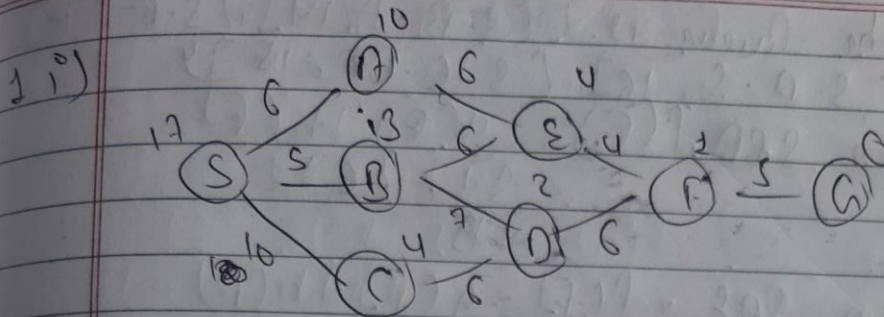
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Sol:

For initial stage:

$$f(S) = g(S) + h(S) \\ = 0 + 17 \\ = 17$$

∴ The Queue = $\{ [S, 17] \}$.

$$\text{From } S, f(A) = g(A) + h(A) \\ = 6 + 10 = 16$$

$$f(B) = g(B) + h(B) \\ = 5 + 13 = 18$$

$$f(C) = g(C) + h(C) \\ = 10 + 4 = 14$$

∴ The Queue is = $\{ [S-C, 14], [S-A, 16], [S-B, 18] \}$

$$\text{From } S-C, f(D) = g(D) + h(D) \\ = 10 + 4 = 14$$

$$\text{From } S-B, f(D) = g(D) + h(D) \\ = 5 + 7 = 12$$

$$f(E) = g(E) + h(E) \\ = 6 + 4 = 10$$

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∴ The Queue is $\{ [S-B-D, 14], [S-B-E, 15], [S-A-E, 16], [S-C-D, 18] \}$

$$\begin{aligned} \text{From SBD, } f(F) &= g(F) + h(F) \\ &= 5 + 7 + 6 + 1 \\ &= 19 \end{aligned}$$

$$\begin{aligned} \text{From SAE, } f(F) &= g(F) + h(F) \\ &= 6 + 4 + 6 + 1 \\ &= 17 \end{aligned}$$

$$\begin{aligned} \text{From SBE, } f(F) &= g(F) + h(F) \\ &= 5 + 1 + 6 + 1 = 13 \end{aligned}$$

$$\begin{aligned} \text{From SCD, } f(F) &= g(F) + h(F) \\ &= 10 + 6 + 1 = 17 \end{aligned}$$

$$\begin{aligned} \text{From SBD, } f(F) &= g(F) + h(F) \\ &= 10 + 6 + 6 + 1 = 23 \end{aligned}$$

∴ The Queue is $\{ [S-B-E-F, 16], [S-A-E-F, 17], [S-B-D-F, 19], [S-C-D-F, 23] \}$

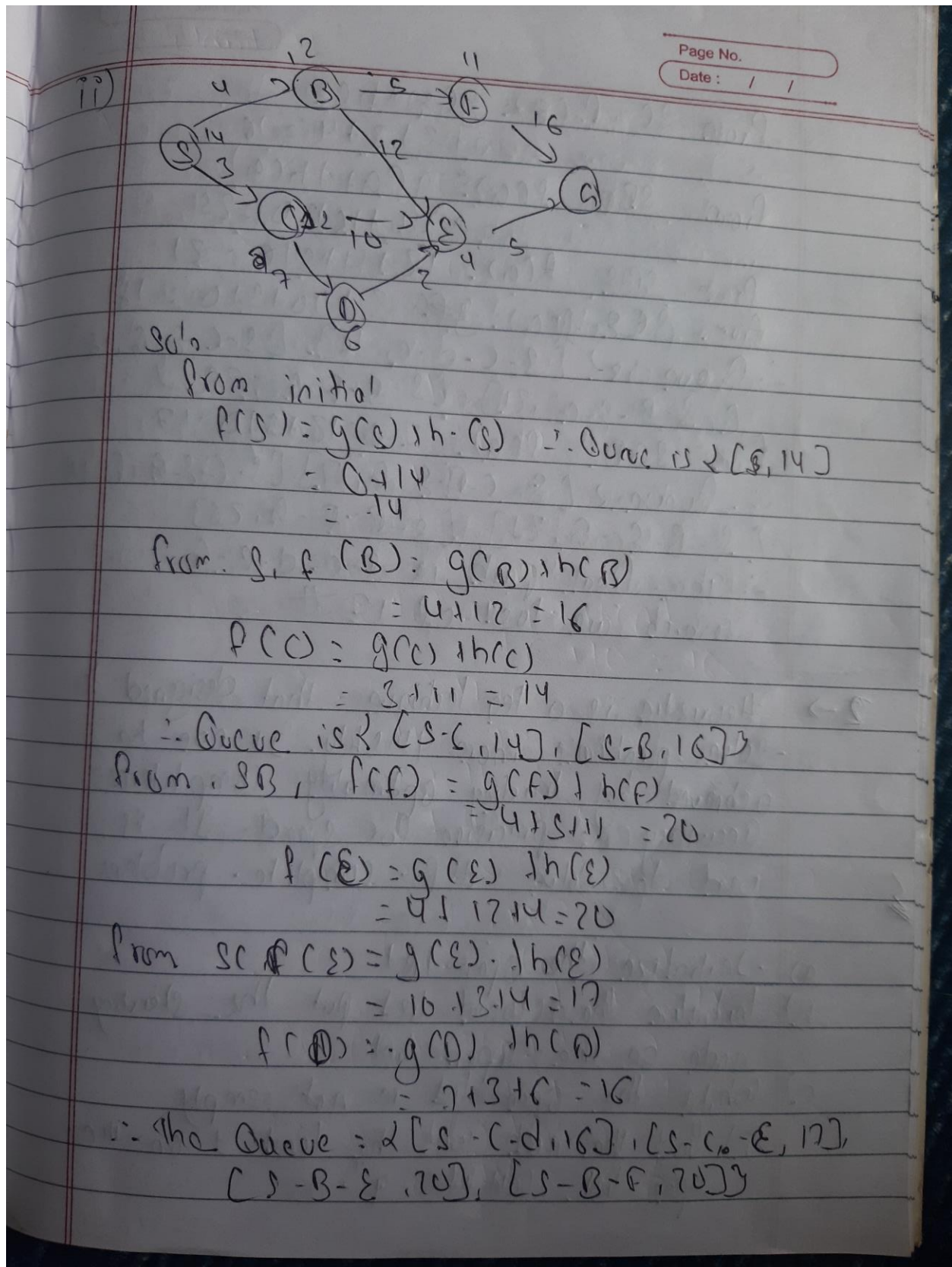
$$\begin{aligned} \text{From SAEF, } f(G) &= g(G) + h(G) \\ &= 6 + 6 + 4 + 3 + 0 = 19 \end{aligned}$$

$$\begin{aligned} \text{From SBDEF, } f(G) &= g(G) + h(G) \\ &= 6 + 5 + 4 + 3 + 0 = 18 \end{aligned}$$

$$\begin{aligned} \text{From SCDF, } f(G) &= 10 + 6 + 6 + 3 + 0 = 25 \end{aligned}$$

∴ Queue is $\{ [S-B-E-F-G, 18], [S-A-E-F-G, 19], [S-B-D-F-G, 21], [S-C-D-F-G, 25] \}$

Final path is S-B-E-F-G with cost of 18



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$$\text{From SC, } f(c) = g(c) + h(c) \\ = 2 + 3 + 2 + 4 = 11$$

$$\text{From SB, } f(a) = g(a) + h(a) \\ = 5 + 4 + 1 + 0 = 10$$

$$\text{From SD, } f(a) = 12 + 4 + 5 + 0 = 21$$

$$\text{From SE, } f(a) = 3 + 1 + 0 + 5 + 0 = 9$$

\therefore Queue is $\{ [S-C-D-E, 11], [S-C-E-G, 10], [S-B-E-G, 21], [S-B-F-G, 25] \}$

$$\text{From SCDE, } f(a) = 7 + 3 + 2 + 5 + 0 = 17$$

\therefore Queue $\{ [S-C-D-E-G, 17], [S-C-E-G, 10], [S-B-E-G, 21], [S-B-F-G, 25] \}$

\therefore The final path is S-C-D-E-G which we lost at 17 \neq

2 \rightarrow Heuristic is a technique that designed to solve problem's more quickly. It can be achieved by trading optimality (completeness, accuracy or precision for speed. It is used to solve NP-complete problems.

- Initialize the open list
- Initialize the closed list put the starting node on the open list.
- While the open list is not empty
 - Find the node with the least f on the open list, call it "q".

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ii.) ~~Pop~~ Pop q off the Open list.
iii.) generate q 's 8 successors and set their parents to q

iv.) for each successor

a) if Successor is the goal, stop search
Successor.g = $q.g + \text{distance between Successor and } q$.

Successor.h = distance from goal to Successor

Successor.f = Successor.g + Successor.h

b) if a node with the same position as Successor is in the Open list which has a lower f than Successor. Skip this Successor.

c) if a node with the same position as Successor is in the closed list which has a lower f than Successor. Skip this Successor.

d) push q on the closed list.
end (while loop)

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3 → - An admissible heuristic is the function which never overestimates the cost of reaching the goal, from a node or the minimum cost path from a node to the goal node. So, a heuristic is a specific to a particular state space and also to a particular goal state in that state space. It will lead to search paths that are not to be more costly than the optimal path. If $h(n)$ and $h^*(n)$ be estimated and actual heuristics respectively then for admissible heuristic $h(n) \leq h^*(n)$

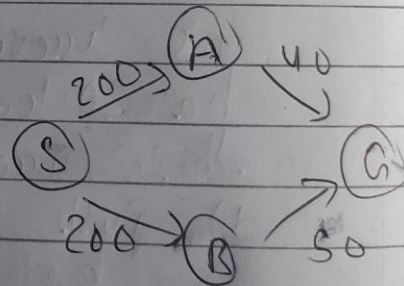
Overestimation:

$$\text{if } h(n) \geq h^*(n)$$

We have,

$$h^*(A) = 40$$

$$h^*(B) = 50$$

Now, let's take $h(A) = 80$ and

$$h(B) = 70$$

From n^* Algorithm

$$f(A) = g(A) + h(A)$$

$$= 200 + 80 = 280$$

$$f(B) = g(B) + h(B)$$

$$= 200 + 70 = 270$$

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From SB, $f(A) = g(A) + h(A)$

$$\text{which} = 200 + 50 + 0 = 250$$

\therefore ~~SA~~ is not the optimal solution.

Underestimation

$$\forall h(n) \leq h^*(n)$$

We have

$$n \neq (A) = 40$$

$$n \neq (B) = 50$$

$$\text{Again, } h(A) = 20$$

$$h(B) = 20$$

From the A* algorithm

$$f(A) = g(A) + h(A)$$

$$= 200 + 30 + 0 = 230$$

$$f(B) = g(B) + h(B)$$

$$= 200 + 20 + 0 = 220$$

Now, from SB, $f(A) = g(A) + h(A)$

$$\text{From SA, } f(A) =$$

$$200 + 50 + 0 = 250$$

$$\text{From SA, } f(A) = g(A) + h(A)$$

$$= 200 + 40 + 0 = 240$$

which is the optimal solution.

\therefore To make the graph admissible we need

to choose heuristic function $n(n) \leq n^*(n)$

$$\& n(B) \leq n^*(B)$$

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4 → A consistent heuristic is a function which never over estimates the cost of reaching the goal line. Converse however, is not always true. This is proved by induction on n . By assumption, $h(n) \leq h^*(n)$ where $h^*(n)$ denotes the cost of the shortest path from n .

The benefits of consistent heuristic are:

- i) It never overestimates the cost of reaching the goal.
- ii) It helps to denote the cost of the shortest path from n to the goal.
- iii) The length of the best from node to the goal.

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5. → The advantages of A* algorithm.
- i) It is complete and optimal.
 - ii) It is the best one from other techniques.
 - iii) It is used to solve very complex problems.
 - iv) It is optimally efficient i.e. there is no other optimal algorithm guaranteed to expand fewer nodes than A*.

The disadvantages of A* algorithm.

- i) ~~This~~ It is algorithm is contains with complexity problems.
- ii) The speed execution of A* search is highly dependent on the accuracy of the heuristic algorithm that is used to compute $h(n)$.
- iii) The algorithm is complete if the branching factor is finite and every action has fixed cost.