



Academic Year	Module	Assessment Number	Assessment Type
S20	Introductory Data Structures and Algorithms (DipIT02)	A1	Not so easy question

[Not So Easy Question]

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1-→ Abstract data type are those type or class whose behaviour is defined by a set of value and a set of operations. It is usually implemented by ^{an} array.

The array and array type is also known as an abstract data type which hold a collection of elements that are accessible by an index. The elements which are stored in an array can be anything through primitive type for example: instances of classes which can be integer to more complex types.

Following are the areas in which data-structure are applied extensively:

In Linear

- > Array
- > Link-list
- > stacks
- > Queue

In non-Linear

- > Trees
- > Graphs
- > Tables
- > sets

2 → Asymptotic analysis of an algorithm refers to defining the mathematical boundation / framing of its runtime performance. Therefore 1 sec is equal to 1×10^6 micro second.

	1 sec	1 min	1 Hour	1 Day	7 Day	15 Day	1 month
$\log \log n^2$	5×10^5	2×10^7	1.8×10^9	2.32×10^{10}	2.02×10^{11}	6.048×10^{11}	1.314×10^{12}
\sqrt{n}	1×10^{12}	3.6×10^{15}	1.29×10^{21}	7.46×10^{21}	3.6×10^{23}	1.6×10^{24}	6.7×10^{24}
$2n^3$	79	310	1216	3508	6712	8654	10903
2^n	19	25	31	36	39	40	41
$n!$	9	11	12	13	14	14	15

Hence, from the table the $\log n^2$ is distinguished to be the best time complexity algorithm in compared to others. When we analyze the algorithm, ordered by slowest to fastest growing: ~~then~~ the best on good time complexity is:

$$\log \log n^2 > \sqrt{n} > 2n^3 > 2^n > n!$$

3) Solution

Pseudocode

largestInteger(n)

$$i = 2^{n-1} - 1;$$

Print i ;

for 1 bit

$$2^1 = 2 = 0, 1$$

for 2 bit

$$2^2 = 4 = 0, 1, 10, 11$$

for 3 bit

$$2^3 = 8 = 0, 1, 10, 11, 100, 101, 110, 111$$

for n bit

$$2^n$$

for 32 bit

$$2^{32} = 4294967296$$

for the largest integer

$$2^{n-1} - 1$$

$$= 2^{32-1} - 1$$

$$= 2147483647$$

4 → Solu

Given: $(n + 3y) \cdot (3z - p + 2^t)$

Converting infix to postfix using stack:

S.N	Scanned	Stack	Post fix	Description
1	(((Start
2	n	(n	
3	+	(+	n +	
4	3y	(+	n 3y	
5)		n 3y +	
6	/	/	n 3y +	
7	(/ (n 3y +	
8	3z	/ (n 3y + 3z	
9	-	/ (-	n 3y + 3z	
10	p	/ (-	n 3y + 3z p	
11	+	/ (- +	n 3y + 3z p	
12	2 ^t	/ (- + ^	n 3y + 3z p 2 ^t	
13)		n 3y + 3z p 2 ^t /	End

∴ the postfix value is $n 3y + 3z - p + 2^t /$

5-). Stack - is used to perform Recursion because of the Last In First Out (LIFO) property, which ~~is used to store~~ ^{works by} storing return addresses of the function calls.

For example: Pile of group of weights used in gym machines.

In 'C' code

```
#include <stdio.h>
int sum(int n);
int sum(int n)
{
    if (n != 0)
        return n + sum(n - 1);
    else
        return n;
}

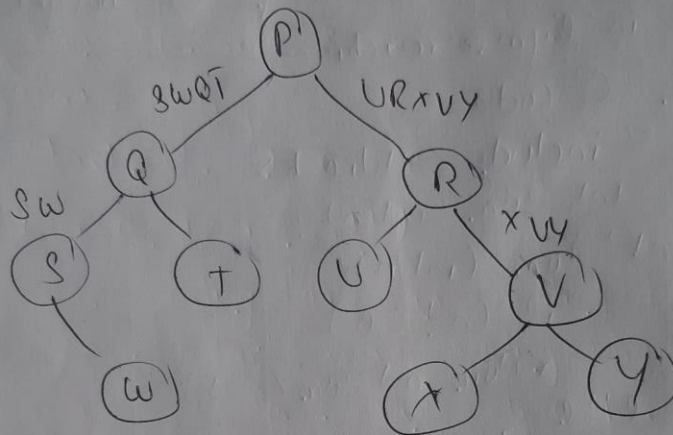
int main()
{
    int number, result;
    printf("Enter a positive integer");
    scanf("%d", &number);
    result = sum(number);
    printf("sum = %d", result);
    return 0;
}
```

6 → Solution.

Given:

In order traversal: SWQT P URXY

Pre order traversal: P Q S W T R U V X Y



7 → Soln

Given:

$T(n) = \begin{cases} 2 & \text{if } n = 2 \\ 2T(n/2) + n & \text{if } n = 2^k, \text{ for } k > 1 \end{cases}$

is $T(n) = n \log n$

Base step

If $n = 2$, then $T(n) = T(2) = 2$ $2 \log 2 = 2$
Thus, $T(2) = 2 \log 2$

Hypothesis step

Assuming $T(n) = n \log n$ is true if $n = 2^k$
for some integer $k > 1$.

Inductive step

If $n = 2^{k+1}$, then

$$\begin{aligned} T(n) &= 2 \cdot T(2^k/2) + 2^{k+1} \\ &= 2 \cdot T(2^k) + 2^{k+1} \\ &= 2 \cdot (2^k \log 2^k) + 2^{k+1} \quad [\because T(n) = n \log n] \\ &= 2^{k+1} ((\log 2^k) + 1) \\ &= 2^{k+1} \log 2^{k+1} \\ &= n \log n \text{ proved} \end{aligned}$$

8-> Header Sentinel refers to header node which has valid next reference by a null previous reference.

Trailer Sentinel refers to trailer node which has valid previous reference by a null next reference.

```
int length()
{
    int count = 0;
    struct node * temp;
    temp = root;
    while (temp != null)
        count++;
    temp = temp->link;
    return count;
}
```

Here, to find the total length of link list temp have to ~~move~~ move till the last that's why the worst-case scenario is $O(n)$

9-1 solution

Given: $[-2, -3, 4, -1, 2, 1, -5, 4]$

Using Kadane's Algorithm
Maximum Sum Subarray

$max_so_far = a[0]$

$max_ending_here = 0$

$start = 0, end = 0, s = 0$

for ($i = 0; i < size; i++$)

$\{ max_ending_far \leq max_ending_here + a[i] \}$

if ($max_so_far < max_ending_here$)

$\{ max_so_far = max_ending_here;$

$start = s, end = i; \}$

if ($max_ending_here < 0$)

$\{ max_ending_here = 0;$

$s = i + 1; \}$

$\}$

for algorithm with example:

~~1-2~~ $[-2, 1, -3, 4, -1, 2, 1, -5, 4]$

$max_so_far = max_ending_here = 0$

for $i = 0, a[0] = -2$

$max_ending_here = max_ending_here + (-2)$

set $max_ending_here = 0$ because $max_ending_here < 0$

for $i = 1, a[1] = 1$

$max_ending_here = max_ending_here + 1$

$max_ending_here = 1$ [$\because max_so_far$ updated]

for $i = 2$, $a[2] = -3$

max-ending-here: max-ending-here + (-3)

max-ending-here: 0

for $i = 3$, $a[3] = 4$

max-ending-here: max-ending-here + (4)

max-ending-here: 4

max-so-far: 4

for $i = 4$, $a[4] = -1$

max-ending-here: max-ending-here + (-1)

max-ending-here: 3

for $i = 5$, $a[5] = 2$

max-ending-here: max-ending-here + (2)

max-ending-here: 5

for $i = 6$, $a[6] = 1$

max-ending-here: max-ending-here + (1)

max-ending-here: 6

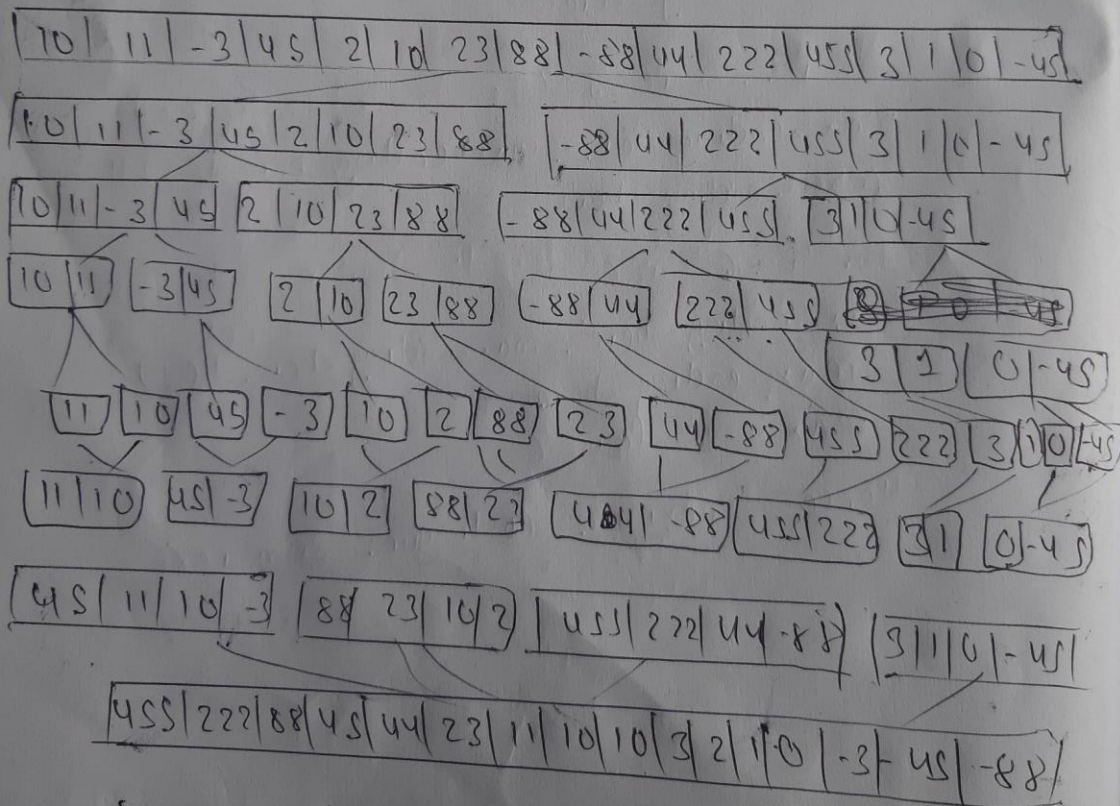
max-so-far: 6

Hence, maximum contiguous sum is 6.

10 → No, Quicksort is not a stable algorithm because its swapping is done according to the pivot's position. It can be stable if two objects with equal keys appear in the same order in sorted output as they appear in the input array to be sorted.

Merge Sort

~~10 11 3 45 2 10~~



The merge sort:

45, 222, 88, 45, 44, 23, 11, 10, 10, 3, 2, 1, 0, -3, -45, -88

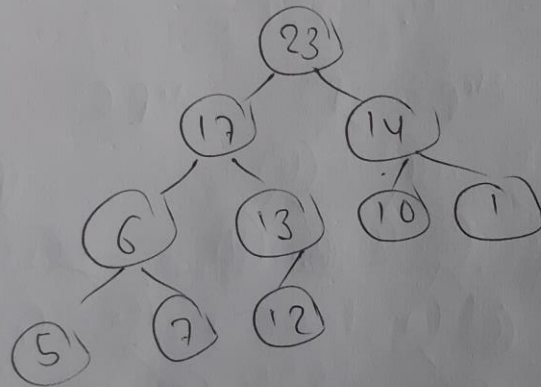
11 → The maximum and minimum numbers of elements in a heap of height h are:

When the leaf node is at height h

$$\text{maximum} = 2^h - 1$$

$$\text{minimum} = 2^{h-1}$$

→ No. the array with value $\langle 23, 17, 14, 6, 13, 10, -1, 5, 7, 12 \rangle$ is not a max-heap because the parent '7' is 6 in the array which violates the max-heap property.

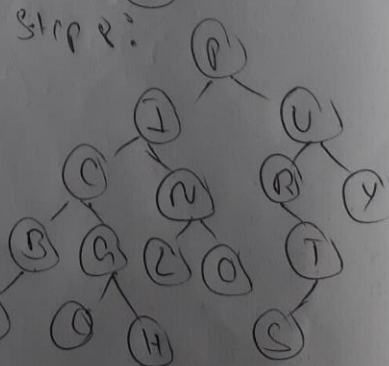
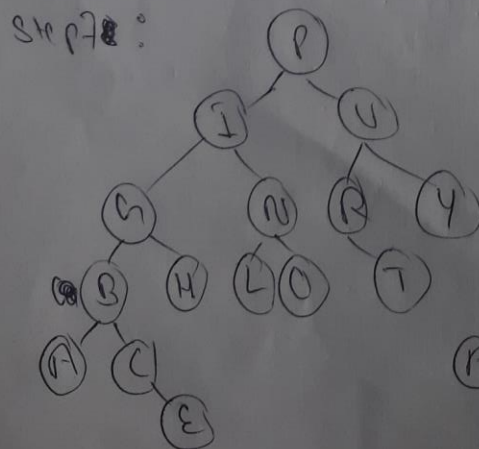
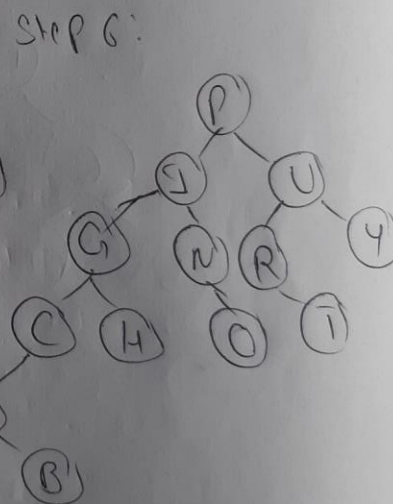
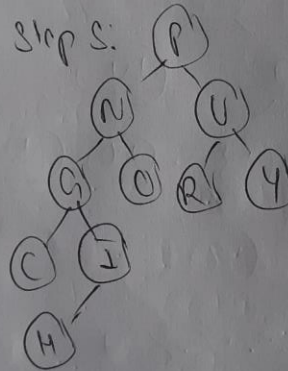
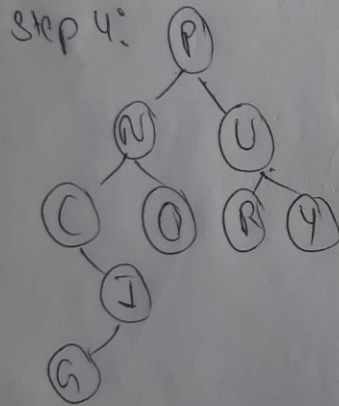
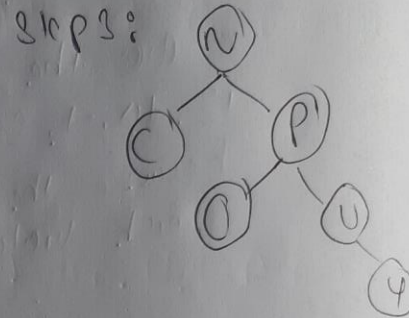
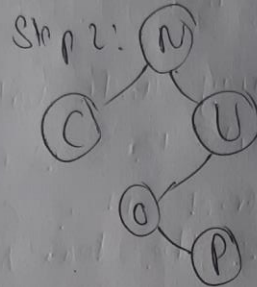
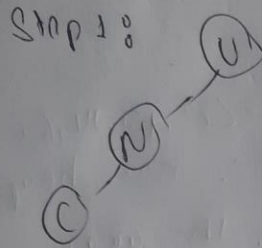


$$\therefore 6 < 7$$

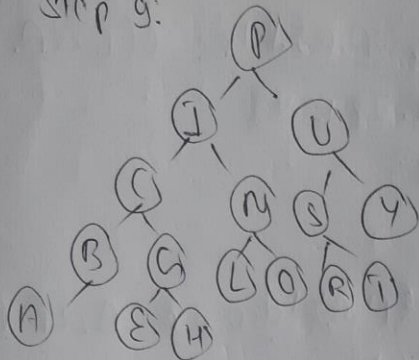
13 → solve

Given: UNCOPYRIGHTABLES

now: constructing AVL tree



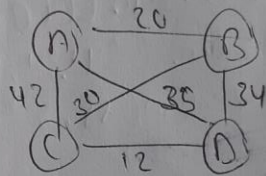
Step 9:



14 → 3010

Given figure

15MP



$S = \{A, Y\}$ which is last only.

The 3 possible ways to get A are:

$$c(B, \{A, Y\}) = \min[c(A, Y) | d_{BA}] = 0 + 20 = 20$$

$$c(C, \{A, Y\}) = \min[c(A, Y) | d_{CA}] = 0 + 42 = 42$$

$$c(D, \{A, Y\}) = \min[c(A, Y) | d_{DA}] = 0 + 35 = 35$$

$$S = \{A, B, Y, \{A, C\}, \{A, D\}\}$$

$$c(C, \{A, B, Y\}) = \min[c(B, \{A, Y\}) | d_{CB}] = 20 + 30 = 50$$

$$c(D, \{A, B, Y\}) = \min[c(B, \{A, Y\}) | d_{DB}] = 20 + 34 = 54$$

$$c(B, \{A, C\}) = \min[c(C, \{A, Y\}) | d_{BC}] = 42 + 30 = 72$$

$$c(D, \{A, C\}) = \min[c(C, \{A, Y\}) | d_{DC}] = 42 + 12 = 54$$

$$c(B, \{A, D\}) = \min[c(D, \{A, Y\}) | d_{BD}] = 35 + 34 = 69$$

$$c(C, \{A, D\}) = \min[c(D, \{A, Y\}) | d_{CD}] = 35 + 12 = 47$$

$$S = \{C, B, A\}, \{D, B, A\}, \{D, C, A\}$$

$$\begin{aligned} c(D, \langle C, B, A \rangle) &= \min [c(C, \langle A, B \rangle) + d_{DC}, c(B, \langle A, C \rangle) + d_{DB}] \\ &= \min [50 + 12, 72 + 34] \\ &= \min [62, 106] \\ &= 62 \end{aligned}$$

$$\begin{aligned} c(C, \langle D, B, A \rangle) &= \min [c(D, \langle A, B \rangle) + d_{CD}, c(B, \langle A, D \rangle) + d_{CB}] \\ &= \min [54 + 12, 69 + 30] \\ &= \min [66, 99] \\ &= 66 \end{aligned}$$

$$\begin{aligned} c(B, \langle D, C, A \rangle) &= \min [c(D, \langle A, C \rangle) + d_{BD}, c(C, \langle A, D \rangle) + d_{BC}] \\ &= \min [54 + 34, 42 + 30] \\ &= \min [88, 72] \\ &= 72 \end{aligned}$$

$$S = \langle D, C, B, A \rangle$$

$$\begin{aligned} c(A, S) &= \min [c(D, \langle C, B, A \rangle) + d_{AD}, c(C, \langle D, B, A \rangle) + d_{AC}, c(B, \langle D, C, A \rangle) + d_{AB}] \\ &= \min [62 + 35, 66 + 42, 72 + 20] \\ &= \min [97, 108, 92] \\ &= 92 \end{aligned}$$

∴ required path $ADCB$
 $ACDBA$

15 -> Electricity(data)

if (Q.is Empty)

Q.enqueue(data)

Q.front = data

else

if (Q.length != array.length - 1)

if (data == Q.front)

dequeue(Q)

if (Q.length == array.length - 1)

dequeue(Q)

else enqueue(data)

else

dequeue(data)

return

enqueue(Q, n)

Q[Q.back] = n

if (Q.back == Q.length)

Q.back = 0

else Q.back = Q.back + 1

dequeue(Q)

n = Q[Q.front]

if (Q.front == Q.length)

Q.front = 0

else Q.front = Q.front + 1

return n

Over Flow()

if array.length == queue.length

return true

else false

∴ time complexity is $O(1)$

16 → Solution.

Given hash function $h(n) = n$
the order of array is

9	18	12	3	14	4	21		
0	1	2	3	4	5	6	7	8

for linear probedion

$$h(n) = n \% 9$$

for A - 9, 14, 4, 18, 12, 3, 21

key (n) Position ($h(n) = n \% 9$)

9 $9 \% 9 = 0$

14 $14 \% 9 = 5$

4 $4 \% 9 = 4$

18 $18 \% 9 = 0$

12 $12 \% 9 = 3$

3 $3 \% 9 = 3$

21 $21 \% 9 = 3$

9	18	12	4	14	3	21		
0	1	2	3	4	5	6	7	8

here, in index we have 4, but in array we have 3. So, it is not suitable

B - 12, 3, 14, 18, 4, 9, 21

key (n) Position ($h(n) = n \% 9$)

12 $12 \% 9 = 3$

3 $3 \% 9 = 3$

14 $14 \% 9 = 5$

18 $18 \% 9 = 0$

4 $4 \% 9 = 4$

9 $9 \% 9 = 0$

21 $21 \% 9 = 3$

0	1	2	3	4	5	6	7	8
18	9		12	3	14	4	21	

Here, In 0 index we have 18, but in array we have 9. so it also can't be the possible one.

C - 12, 14, 3, 9, 4, 18, 21

key(n)

Position (h(n)) : $n \% 9$

12

$$12 \% 9 = 3$$

14

$$14 \% 9 = 5$$

3

$$3 \% 9 = 3$$

9

$$9 \% 9 = 0$$

4

$$4 \% 9 = 4$$

18

$$18 \% 9 = 0$$

21

$$21 \% 9 = 3$$

0	1	2	3	4	5	6	7	8
9	18		12	3	14	4	21	

It is one of the possible answer

D - 9, 12, 14, 3, 4, 21, 18

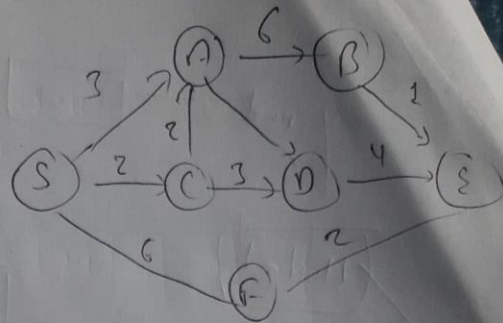
Same as above 'c' in the index 6 there is 21 and the original array is also 21 it is possible answer

E - ~~Same as~~ - 12, 9, 18, 3, 14, 21, 4

Same as above, in the index 6 there is 21. but in our original array it is 4 so, it is not possible answer.

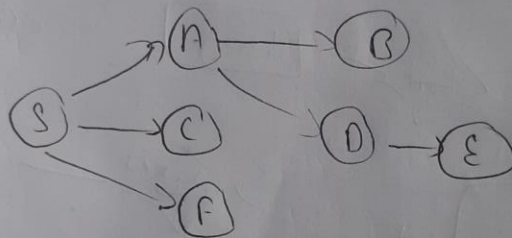
∴ the possible answer is C and D.

17 → Sol'n
Given,



In Dijkstra's algorithm, it will visit following vertices in order
S, C, A, D, F, E, B.

So, the parent of each node should be like this:



Dijkstra's algorithm removes only removes from the priority queue at times. Removal takes $O(\log V)$ time for a total of $O(V \log V)$ time for all vertex removals. For the shortest path to vertices.

Vertices	S	A	B	C	D	E	F
S	0s	3s	∞ s	2s	∞ s	∞ s	6s
A	0s	3s	∞ s	2s	9s	∞ s	6s
B	0s	3s	9s	2s	4s	∞ s	6s
C	0s	3s	9s	2s	4s	8s	6s
D	0s	3s	9s	2s	4s	8s	6s
E	0s	3s	9s	2s	4s	8s	6s
F	0s	3s	9s	2s	4s	8s	6s

∴ Path: S, A, D, E

18 → solution

a procedure to compute $L_1 \cap L_2$

list Intersect (List L_1 , List L_2)

\leftarrow Position L_1 -Pos, L_2 -Pos, Result-Pos;

 List Result;

L_1 -Pos = $L_1 \rightarrow \text{Next}$;

L_2 -Pos = $L_2 \rightarrow \text{Next}$;

 Result-Pos = Result-Make Empty();

 while (L_1 -Pos! = NULL & & L_2 -Pos! = NULL)

 if (L_1 -Pos → Element < L_2 -Pos → Element)

L_1 -Pos = L_1 -Pos → Next;

 else if (L_1 -Pos → Element > L_2 -Pos → Element)

L_2 -Pos = L_2 -Pos → Next;

 else

 Insert (L_1 -Pos → Element, Result, Result-Pos);

L_1 -Pos = L_1 -Pos → Next;

L_2 -Pos = L_2 -Pos → Next;

 Result-Pos = Result-Pos → Next;

 }

 return Result;

 }

∴ the running time is $O(n_1 + n_2)$.

For L1, L2

List Union (List L1, List L2)

2 Position L1 - pos, L2 - pos, Result - pos;

Element Type Insert Element;

List Result;

L1 - pos = L1 → Next;

L2 - pos = L2 → Next;

Result - pos = Result = make Empty();

while (L1 - pos != NULL & L2 - pos != NULL)

{ if (L1 - pos → Element < L2 - pos → Element) {

Insert Element = L1 - pos → Element;

L1 - pos = L1 - pos → Next;

}

else if (L1 - pos → Element > L2 - pos → Element) {

Insert Element = L2 - pos → Element;

L2 - pos = L2 - pos → Next;

}

else {

Insert Element = L1 - pos → Element;

L1 - pos = L1 - pos → Next;

L2 - pos = L2 - pos → Next;

}

Insert (Insert Element, Result, Result - pos);

Result - pos = Result - pos → Next;

while (L1 - pos != NULL) {

Insert (L1 - pos → Element, Result, Result - pos);

L1 - pos = L1 - pos → Next;

Result - pos = Result - pos → Next;

}

while (L2 - pos != NULL) {

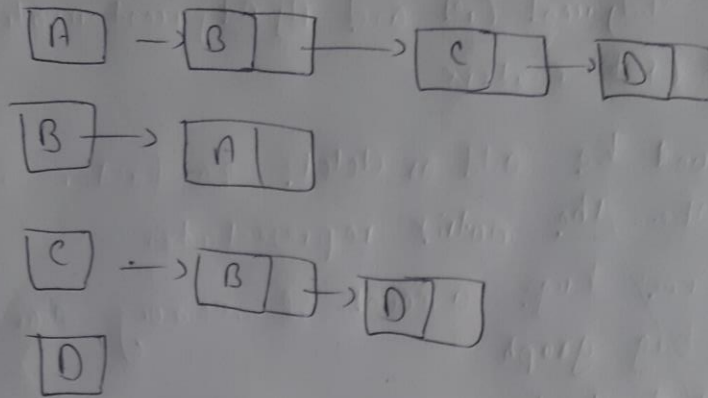
Insert (L2 - pos → Element, Result, Result - pos);

L2 - pos = L2 - pos → Next;

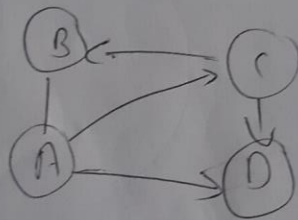
Result - pos = Result - pos → Next;

return Result;

19 → solution
Given:



a → Directed graph



b) Adjacency matrix

	A	B	C	D
A	0	1	1	1
B	1	0	0	0
C	0	1	0	1
D	0	0	0	0

Edges: $\{(A, B), (A, C), (A, D), (B, A), (C, B), (C, D)\}$

c) - Adjacency matrix

Pros - An Adjacency matrix is fast to check ~~and test~~ whether edge between two nodes are exists or not.

- ~~It is~~ Add or delete an edge can be done in $O(1)$ time.

Cons -

- Adjacency matrix consumes a lot of memory for storing big graph.
- The effort for adding or delete ^{nodes} requires huge efforts
- It redundant the information for undirected graph

Adjacency List

Pros -

- Adjacency list ~~allows~~ allows efficient space to store graph.
- The new edges can be added in $O(1)$ time.

Cons

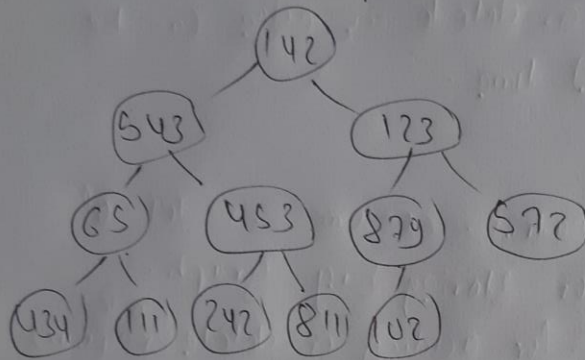
- It does not allow to make an efficient implementation if dynamically change of vertices number is required.
- Adding or deleting edge to it is ~~not~~ hard for adjacency matrix

20-3 The running time of heapsort for presorted input is $O(n \log n)$.

Given data:

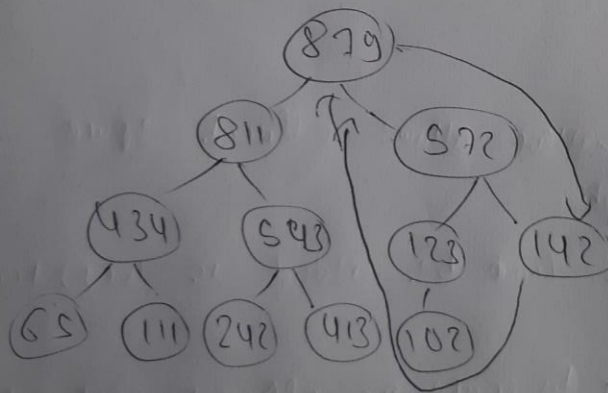
142, 543, 123, 65, 453, 879, 572, 434, 111, 242, 811, 102

Step 1: Build the heap

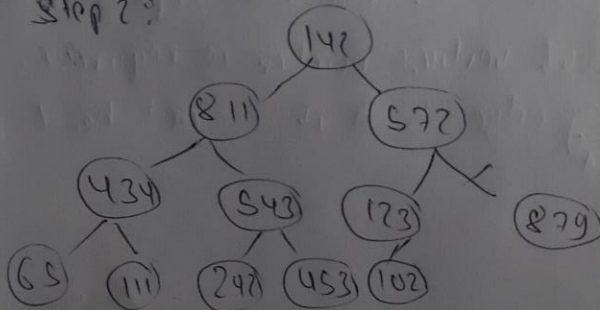


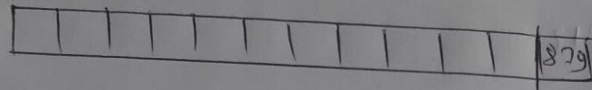
Now,

building into maximum heap.

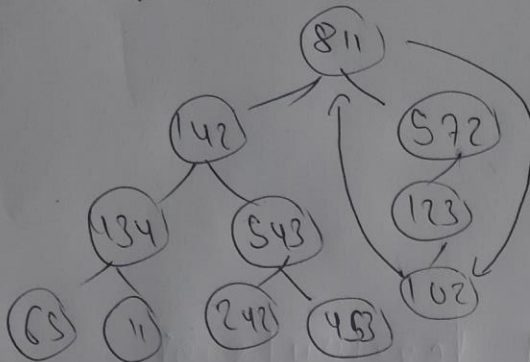


Step 2:

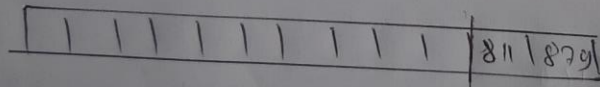
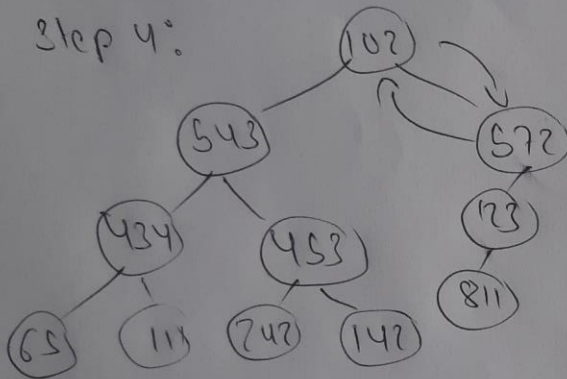




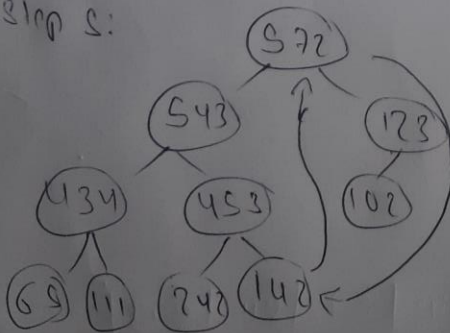
step 3:



step 4:



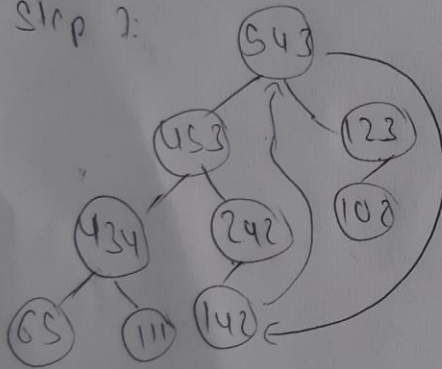
step 5:



310p 6:

```
graph TD; 142((142)) --> 543((543)); 142 --> 123((123)); 543 --> 434((434)); 543 --> 152((152)); 123 --> 102((102)); 434 --> 65((65)); 434 --> 111((111)); 152 --> 242((242)); 152 --> 542((542));
```

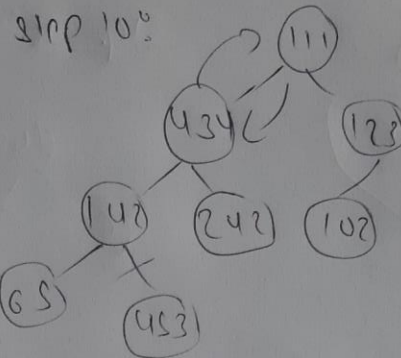
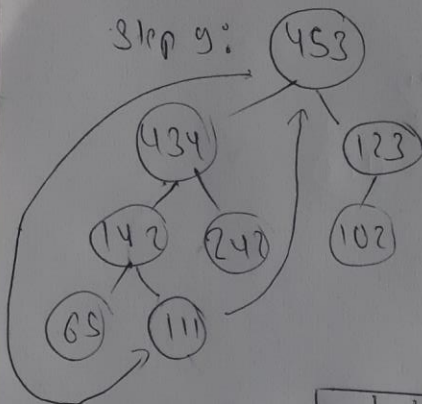
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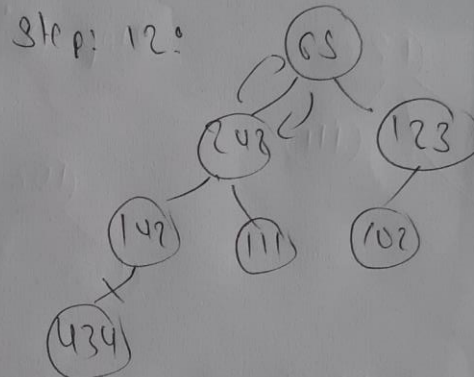
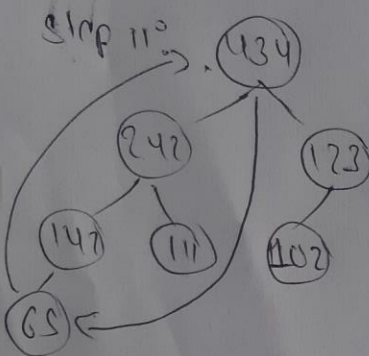
Step 8:

```
graph TD; 142((142)) --- 453((453)); 142 --- 123((123)); 453 --- 434((434)); 453 --- 242((242)); 434 --- 65((65)); 434 --- 114((114)); 242 --- 543((543)); 242 --- 102_1((102)); 123 --- 102_2((102));
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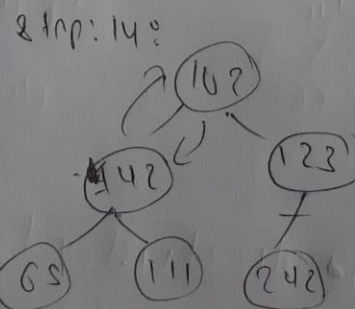
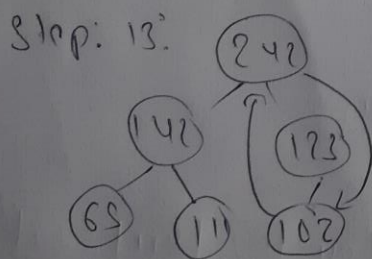
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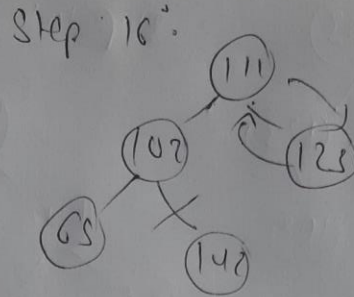
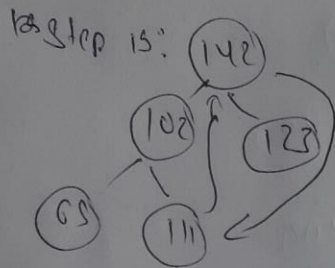
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--	--	--	--	--	--	--	-----	-----	-----	-----	-----



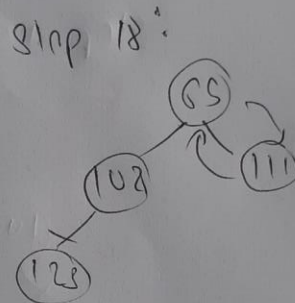
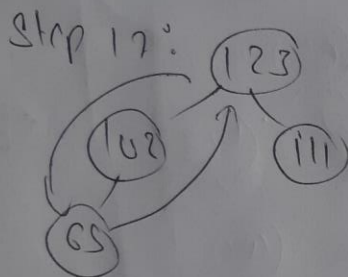
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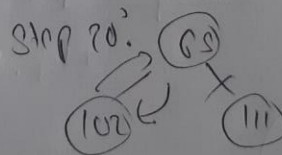
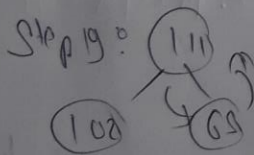
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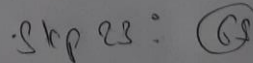
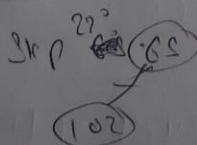
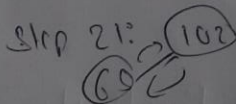
1	1	1	1	42	242	434	453	572	811	879
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				123	142	242	434	453	543	572	811	879
--	--	--	--	-----	-----	-----	-----	-----	-----	-----	-----	-----



				111	123	142	242	434	453	543	572	811	879
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65	102	111	123	42	242	434	453	543	572	811	879
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