```
clc; close all; clear;
h = 10; % height of the cylinder
r_base = 1; % base radius of the cylinder
a = 0.1; % quadratic coefficient
num_points = 100; % number of points for each circle
wind_direction = [1, 0, 0]; % wind direction vector (assumed to be in x-
direction)
wind_intensity = 0.1; % wind intensity (scaling factor for bending)
% Create height values
z = linspace(0, h, 20);
% Create radii as a function of height with quadratic modulation
r = r_base + a*z.^2;
% Apply wind bending to the cylinder
X = zeros(numel(z), num_points);
Y = zeros(numel(z), num_points);
Z = zeros(numel(z), num_points);
boundary_points = cell(numel(z), 1); % Store boundary points for each height
for i = 1:numel(z)
    theta = linspace(0, 2*pi, num_points);
    bend_factors = wind_intensity * z(i) * (cos(theta)*wind_direction(1) +
sin(theta)*wind_direction(2)); % Calculate bending factor for each point
    X(i, :) = (r(i) + bend_factors) .* cos(theta); % Apply bending factor to
x-coordinate
    Y(i, :) = (r(i) + bend_factors) .* sin(theta); % Apply bending factor to
y-coordinate
    Z(i, :) = z(i) * ones(1, num_points);
    % Store boundary points for each height
    boundary_points\{i\} = [X(i, :); Y(i, :); Z(i, :)]';
end
% Plot the bent cylinder
figure;
surf(X, Y, Z, 'FaceColor', 'blue', 'EdgeColor', 'none');
hold on;
% Plot the boundary lines
for i = 1:numel(boundary_points)
    plot3(boundary_points{i}(:, 1), boundary_points{i}(:, 2),
boundary_points\{i\}(:, 3), 'r'\};
end
xlabel('X');
ylabel('Y');
zlabel('Z');
title('Bent Cylinder with Wind Deformation and Boundary Tracking');
view(3); % set view to 3D
hold off;
```

```
figure();
for p=1:2:11
    X0=[X(p,1) Y(p,1) Z(p,1) 0 0 0 0 0 0 0];
    Xe=[X(p+2,1) Y(p+2,1) Z(p+2,1) 0 0 0 0 0 0 0];
    syms phi(t) theta(t) psi(t)
    % Transformation matrix for angular velocities from inertial frame
    % to body frame
    W = [1, 0,
                        -sin(theta);
        0, cos(phi), cos(theta)*sin(phi);
        0, -sin(phi), cos(theta)*cos(phi) ];
    % Rotation matrix R_ZYX from body frame to inertial frame
    R = rotationMatrixEulerZYX(phi,theta,psi);
    % Create symbolic variables for diagonal elements of inertia matrix
    syms Ixx Iyy Izz
    % Jacobian that relates body frame to inertial frame velocities
    I = [Ixx, 0, 0; 0, Iyy, 0; 0, 0, Izz];
    J = W.'*I*W;
    % Coriolis matrix
    dJ_dt = diff(J);
   h_dot_J = [diff(phi,t), diff(theta,t), diff(psi,t)]*J;
    grad_temp_h = transpose(jacobian(h_dot_J,[phi theta psi]));
    C = dJ_dt - 1/2*grad_temp_h;
    C = subsStateVars(C,t);
    % Define fixed parameters and control inputs
    % k: lift constant
    % 1: distance between rotor and center of mass
    % m: quadrotor mass
    % b: drag constant
    % g: gravity
    % ui: squared angular velocity of rotor i as control input
    syms k l m b g u1 u2 u3 u4
    % Torques in the direction of phi, theta, psi
    tau_beta = [1*k*(-u2+u4); 1*k*(-u1+u3); b*(-u1+u2-u3+u4)];
    % Total thrust
    T = k*(u1+u2+u3+u4);
    % Create symbolic functions for time-dependent positions
    syms x(t) y(t) z(t)
    % Create state variables consisting of positions, angles,
    % and their derivatives
    state = [x; y; z; phi; theta; psi; diff(x,t); diff(y,t); ...
       diff(z,t); diff(phi,t); diff(theta,t); diff(psi,t)];
    state = subsStateVars(state,t);
```

```
f = [ % Set time-derivative of the positions and angles
    state(7:12);
    % Equations for linear accelerations of the center of mass
    -g*[0;0;1] + R*[0;0;T]/m;
    % Euler-Lagrange equations for angular dynamics
    inv(J)*(tau_beta - C*state(10:12))
    ];
f = subsStateVars(f,t);
% Replace fixed parameters with given values here
IxxVal = 1.2;
IvyVal = 1.2;
IzzVal = 2.3;
kVal = 1;
1Val = 0.25;
mVal = 2;
bVal = 0.2;
gVal = 9.81;
f = subs(f, [Ixx Iyy Izz k l m b g], ...
    [IxxVal IyyVal IzzVal kVal lVal mVal bVal gVal]);
f = simplify(f);
% Calculate Jacobians for nonlinear prediction model
A = jacobian(f,state);
control = [u1; u2; u3; u4];
B = jacobian(f,control);
% Create QuadrotorStateFcn.m with current state and control
% vectors as inputs and the state time-derivative as outputs
matlabFunction(f,"File","QuadrotorStateFcn", ...
    "Vars", {state, control});
% Create OuadrotorStateJacobianFcn.m with current state and control
% vectors as inputs and the Jacobians of the state time-derivative
% as outputs
matlabFunction(A,B,"File","QuadrotorStateJacobianFcn", ...
    "Vars", {state, control});
% Confirm the functions are generated successfully
while isempty(which('QuadrotorStateJacobianFcn'))
    pause(0.1);
end
%no of state, inputs and outputs for non linear mpc controller
nx=12; %no of prediction model states
ny=12; %no of prediction model outputs
nu=4; %no of prediction model inputs
%create a non linear object whose prediction model has nx states, ny
```

```
outputs, and nu inputs, where all inputs are manipulated variables.
    nlobj=nlmpc(nx,ny,nu);
    %prediction model Sample time
    Ts=0.3;
    nlobj.Ts = Ts;
    %prediction horizon steps
    p = 15;
    nlobj.PredictionHorizon = p;
    %control horizon steps
    c = 15;
    nlobj.ControlHorizon = c;
    X_{end}=Xe;
    nlobj.Model.StateFcn = "QuadrotorStateFcn";
    nlobj.Jacobian.StateFcn = @QuadrotorStateJacobianFcn;
    % %Optimisation function based on minimisation of thrust inputs thereby
fuel
    nlobj.Optimization.CustomCostFcn = @(X,U,e,data) Ts*sum(sum(U(1:p,:)));
    nlobj.Optimization.ReplaceStandardCost = true;
    nlobj.Optimization.CustomEqConFcn = @(X,U,data) X(end,:)'-X_end';
    % min_thrust = 0; % Minimum thrust constraint
    % max_thrust = 1;
    for ct = 1:nu
        nlobj.MV(ct).Min =0;% min_thrust * ones(p,1);
        nlobj.MV(ct).Max =1; %max_thrust * ones(p,1);
    end
    x0 = X0';
    u0 = zeros(nu,1);
    validateFcns(nlobj,x0,u0);
    [\sim, \sim, info] = nlmpcmove(nlobj, x0, u0);
    plot3(info.Xopt(:,1),info.Xopt(:,2),info.Xopt(:,3),'-')
    hold on;
end
function [Rz,Ry,Rx] = rotationMatrixEulerZYX(phi,theta,psi)
% Euler ZYX angles convention
Rx = [1,
                                 0;
                    0,
                           -sin(phi);
    0,
                 cos(phi),
                 sin(phi),
                             cos(phi) ];
Ry = [\cos(theta), 0,
                                 sin(theta);
                             0;
                 1,
    -sin(theta), 0,
                              cos(theta) ];
```

```
Rz = [\cos(psi),
                  -sin(psi), 0;
    sin(psi),
                  cos(psi),
                              0;
    0,
                  0,
                              1 ];
if nargout == 3
    % Return rotation matrix per axes
    return;
end
% Return rotation matrix from body frame to inertial frame
Rz = Rz*Ry*Rx;
end
function stateExpr = subsStateVars(timeExpr,var)
if nargin == 1
    var = sym("t");
end
repDiff = @(ex) subsStateVarsDiff(ex,var);
stateExpr = mapSymType(timeExpr, "diff", repDiff);
repFun = @(ex) subsStateVarsFun(ex,var);
stateExpr = mapSymType(stateExpr, "symfunOf", var, repFun);
stateExpr = formula(stateExpr);
end
function newVar = subsStateVarsFun(funExpr,var)
name = symFunType(funExpr);
name = replace(name, "_Var", "");
stateVar = "_" + char(var);
newVar = sym(name + stateVar);
end
function newVar = subsStateVarsDiff(diffExpr,var)
if nargin == 1
    var = sym("t");
end
c = children(diffExpr);
if ~isSymType(c{1}, "symfunOf", var)
    % not f(t)
    newVar = diffExpr;
    return;
end
if \sim any([c{2:end}] == var)
    % not derivative wrt t only
    newVar = diffExpr;
    return;
end
name = symFunType(c{1});
name = replace(name, "_Var", "");
extension = "_" + join(repelem("d", numel(c)-1), "") + "ot";
stateVar = "_" + char(var);
newVar = sym(name + extension + stateVar);
Zero weights are applied to one or more OVs because there are fewer MVs than
OVs.
Model.StateFcn is OK.
```

Jacobian.StateFcn is OK.

No output function specified. Assuming "y = x" in the prediction model.

Optimization.CustomCostFcn is OK.

Optimization.CustomEqConFcn is OK.

Analysis of user-provided model, cost, and constraint functions complete.

Slack variable unused or zero-weighted in your custom cost function.

All constraints will be hard.

Zero weights are applied to one or more OVs because there are fewer MVs than OVs.

Model.StateFcn is OK.

Jacobian.StateFcn is OK.

No output function specified. Assuming "y = x" in the prediction model.

Optimization.CustomCostFcn is OK.

Optimization.CustomEqConFcn is OK.

Analysis of user-provided model, cost, and constraint functions complete.

Slack variable unused or zero-weighted in your custom cost function.

All constraints will be hard.

Zero weights are applied to one or more OVs because there are fewer MVs than ${\it OVs}$.

Model.StateFcn is OK.

Jacobian.StateFcn is OK.

No output function specified. Assuming "y = x" in the prediction model.

Optimization.CustomCostFcn is OK.

Optimization.CustomEqConFcn is OK.

Analysis of user-provided model, cost, and constraint functions complete.

Slack variable unused or zero-weighted in your custom cost function.

All constraints will be hard.

Zero weights are applied to one or more OVs because there are fewer MVs than ${\it OVs}$.

Model.StateFcn is OK.

Jacobian.StateFcn is OK.

No output function specified. Assuming "y = x" in the prediction model.

Optimization.CustomCostFcn is OK.

Optimization.CustomEqConFcn is OK.

Analysis of user-provided model, cost, and constraint functions complete.

Slack variable unused or zero-weighted in your custom cost function.

All constraints will be hard.

Zero weights are applied to one or more OVs because there are fewer MVs than OVs.

Model.StateFcn is OK.

Jacobian.StateFcn is OK.

No output function specified. Assuming "y = x" in the prediction model.

Optimization.CustomCostFcn is OK.

Optimization.CustomEqConFcn is OK.

Analysis of user-provided model, cost, and constraint functions complete.

Slack variable unused or zero-weighted in your custom cost function.

All constraints will be hard.

Zero weights are applied to one or more OVs because there are fewer MVs than OVs.

Model.StateFcn is OK.

Jacobian.StateFcn is OK.

No output function specified. Assuming "y = x" in the prediction model.

Optimization.CustomCostFcn is OK.

Optimization.CustomEqConFcn is OK.

Analysis of user-provided model, cost, and constraint functions complete. Slack variable unused or zero-weighted in your custom cost function. All constraints will be hard.

Bent Cylinder with Wind Deformation and Boundary Tracking





