Unit-7 Polyphase circuits

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Introduction

- The generator producing a single-phase supply has only one armature winding.
- But if the generator is arranged to have three separate but identical winding displaced 120 degree apart and rotate in a common magnetic field, it produces three voltages of same magnitude and frequency but displaced by 120 degree electrical from one another. This is called a three-phase system.

Advantages of 3-phase system over ³ single-phase system

- 1. **Constant Power:-** In a single phase system, output power varies sinusoidally at a frequency twice the supply frequency.
- This pulsating nature of current is harmful to some applications whereas the balanced 3-phase system supplies constant current at all instants of time.
- 2. **Self start:-** The 3-phase systems are self starting as they do not require any starting device.
- ▶ However, single phase systems require starting device.

Advantages of 3-phase system over single-phase system

- 3. **Greater output:-** The power generated by a 3-phase system is greater than that of a single phase system for a given volume and weight of the generator.
- ▶ This is the distinct advantages over the single phase generator
- 4. **More economical:-** The 3-phase system is much smaller and less expensive than single phase system because less material is required for a given output power at a given voltage.

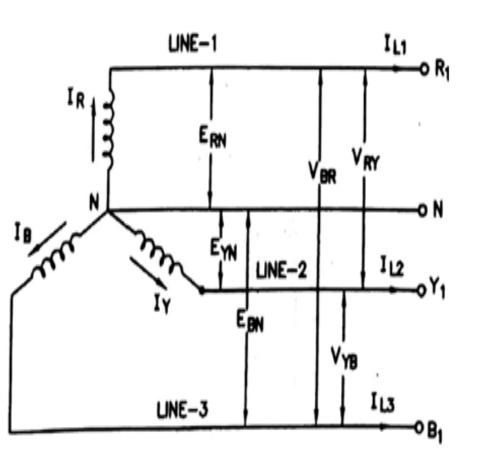
Advantages of 3-phase system over single-phase system

- 5. Less voltage drop:- The voltage drop from the generator to the load is less in a 3-phase system in comparison to the single-phase system
- 6. **Power transmission economics:-** The conductor material required to transmit a given power at a given voltage of material required in single phase system.
- ▶ This means a saving in material and strength of transmitting towers.
- 7. **High Efficiency:-** The 3-phase motors are efficient and have a higher power factor than single phase motors of the same capacity.

Phase sequence

- In three phase system, there are three voltages having same magnitude and frequency displaced by an electrical angle of 120 degree.
- They are attaining their positive maximum value in a particular order.
- The order in which voltages in the three-phase attain their maximum positive value is known as phase sequence.

Voltage and current relation in star connected system



- The emf across each winding is called phase voltage.
- They are denoted by E_{RN} , E_{YN} and E_{BN} .
- ▶ The voltage between any two lines is called line voltage.
- They are represented by V_{RY} , V_{YB} and V_{BR} respectively.
- Similarly currents flowing in the each winding is known as the phase current and current flowing in each line is called the line current.

Since the system is balanced, $I_R = I_Y = I_B = I_{Ph}$ $I_{L1} = I_{L2} = I_{L3} = I_L$ $E_{RN} = E_{YN} = E_{BN} = E_{Ph}$ $V_{RY} = V_{YB} = V_{BR} = V_L$

▶ Relation between line current and phase current:

From Fig. 1, it is clear that

$$I_{R} = I_{L1} \rightarrow I_{Ph} = I_{L}$$

$$I_{Y} = I_{L2} \rightarrow I_{Ph} = I_{L}$$

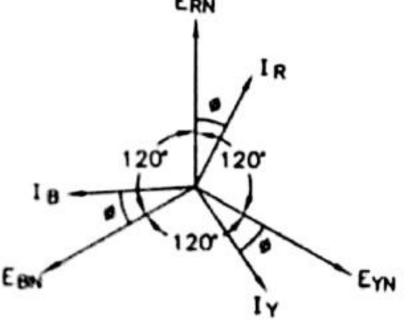
$$I_{B} = I_{L3} \rightarrow I_{Ph} = I_{L}$$

Thus in star connection,

Line current, I_L = Phase current, I_{Ph}

- **Relation between line voltage and phase voltage:**
- It is seen from figure that in star connection, there are two phase windings between each pair of line terminals.
- Since similar ends of these two winding are connected together, the emfs across them oppose each other and their instantaneous values will have opposite polarities.
- Therefore the rms value of line voltage between any two lines will be obtained by the vector difference of the two phase voltages.

The phasor diagram of the phase emfs and currents in a star connected system is shown below:

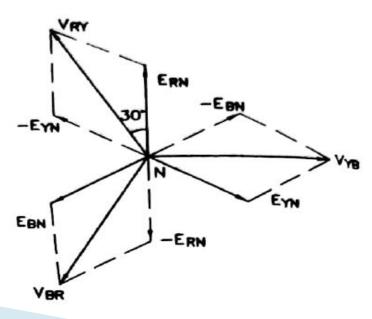


Line voltage between terminals R and Y, $V_{RY} = E_{RN} + E_{NY}$ $= E_{RN} + (-E_{YN})$ $= E_{RN} - E_{YN}$ = phasor difference

Similarly

$$E_{YB} = E_{YN} - E_{BN}$$
 and $E_{BR} = E_{BN} - E_{RN}$

- ▶ Hence it is clear that in a star connected system, the line voltage is obtained as the vector difference of the two corresponding phase voltages.
- This is shown in fig below, for examples V_{RY} is found by adding V_{RN} and V_{YN} reversed and its magnitude is given by the diagonal of the parallelogram.



- Since side of the parallelogram are of equal length and angle between two phase voltages is 60 degree.
- The line voltage is given by,

$$V_{RY} = V_{RN} - V_{YN}$$

$$= 2 V_{Ph} \cos \frac{60^{\circ}}{2}$$

$$= 2 V_{Ph} \cos 30^{\circ}$$

$$= 2 E_{Ph} \times \frac{\sqrt{3}}{2}$$

$$= \sqrt{3} E_{Ph}$$
Similarly $V_{YB} = V_{BR} = \sqrt{3} E_{Ph} = V_{L}$

Thus in balanced star connected system,

$$V_L = \sqrt{3} E_{Ph}$$

 $V_L = \sqrt{3} \ E_{Ph}$ i.e. Line voltage = $\sqrt{3} \times$ phase voltage

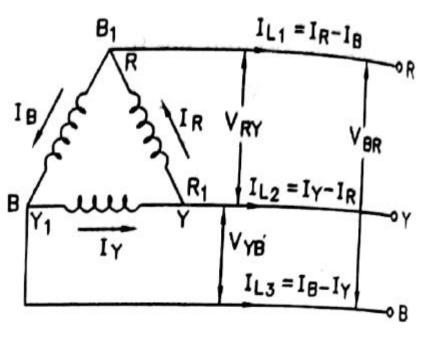
The total power dissipated in the 3-phase star connected system is the arithmetic sum of the powers dissipated in the three phases.

Total power =
$$3 \times \text{power per phase}$$

= $3 \times V_{\text{ph}} \times I_{\text{ph}} \times \cos \phi$
= $3 \times \frac{V_L}{\sqrt{3}} \times I_L \times \cos \phi$
= $\sqrt{3} V_L I_L \cos \phi$

It should be noted that ϕ is the angle between phase voltage and phase current and not between the line voltage and line current.

Voltage and current relation in delta connected system



- The emf across each winding is called phase voltage.
- ▶ They are denoted by E_R , E_Y and E_B .
- The voltage between any two lines is called line voltage.
- They are represented by V_{RY} , V_{YB} and V_{BR} respectively.
- Similarly currents flowing in the each winding is known as the phase current and current flowing in each line is called the line current.

• Since the system is balanced, $I_R = I_Y = I_B = I_{PL}$

$$I_{R} = I_{Y} = I_{B} = I_{Ph}$$

$$I_{L1} = I_{L2} = I_{L3} = I_{L}$$

$$E_{R} = E_{Y} = E_{B} = E_{Ph}$$

$$V_{RY} = V_{YB} = V_{BR} = V_{L}$$

▶ Relation between line voltage and phase voltage:

It is clear that

$$E_R = V_{RY} \rightarrow E_{Ph} = V_L$$

$$E_Y = V_{YB} \rightarrow E_{Ph} = V_L$$

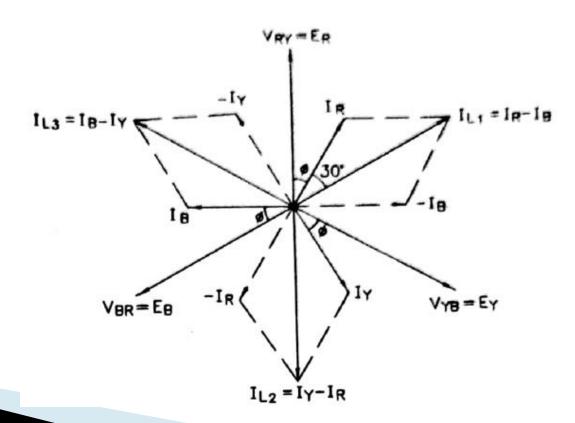
$$E_B = V_{BR} \rightarrow E_{Ph} = V_L$$

Thus in delta connection,

Line voltage, V_L = Phase voltage, E_{Ph}

Relation between line current and phase current:

- It is seen from figure that current flowing in each line is the vector difference of the two phase currents.
- Current in line 1, $I_{L1} = I_R I_B$
- Current in line 2, $I_{L2} = I_y I_R$
- Current in line 3, $I_{L3} = I_B I_Y$
- Current in line 1 can be found as the vector difference of the two corresponding phase currents. This is shown in fir below:



- I_{L1} can be obtained by adding I_R and I_B reversed and its value is given by the diagonal of the parallelogram as shown in vector diagram.
- ▶ Since the sides of parallelogram are equal in magnitude and the angle between them is 60 degree, the line current is given as:

$$I_{L1} = I_R - I_B \text{ (vector difference)}$$

 $= 2 \times I_{Ph} \times \cos \frac{60^{\circ}}{2}$
 $= 2 \times I_{Ph} \times \cos 30^{\circ}$
 $= 2 \times I_{Ph} \times \frac{\sqrt{3}}{2}$
 $= \sqrt{3} I_{Ph}$
Similarly $I_{L2} = I_{L3} = \sqrt{3} I_{Ph} = I_L$

Thus, in delta connection,

Line current, $I_L = \sqrt{3} \times \text{Phase current}$

- The total power in the 3-phase circuit is equal to the arithmetic sum of three phase power.
- ▶ Hence,

Total power =
$$3 \times \text{power per phase}$$

$$= 3 \times V_{ph} I_{ph} \cos \phi$$

1. A 415 V, 3-phase voltage is applied to a balanced star-connected 3-phase load of phase impedance (3+j4) ohms each. Calculate (i) line current and (ii) total power supplied in kW.

 $V_{i} = 415 \text{ V}$

$$V_P = \frac{V_L}{\sqrt{3}}$$
 $Z_{ph} = 3 + j + 4$
 $= \frac{415}{\sqrt{3}}$
 $= 239.6 \text{ Volt}$
 $Z_{ph} = 3 + j + 4$
 $= \sqrt{3^2 + 4^2}$
 $= 5 \Omega$

$$Z_{ph} = 3 + j + 4$$

$$I_{Ph} = \frac{V_{Ph}}{Z_{Ph}}$$

$$= \frac{239.6}{5}$$

$$= 47.92 \text{ A}$$

$$l_L = l_{ph} = 47.92 \text{ A}$$

$$\cos \phi = \frac{R_{Ph}}{Z_{Ph}} = \frac{3}{5} = 0.6$$

Power =
$$\sqrt{3} V_L I_L \cos \phi$$

= $\sqrt{3} \times 415 \times 47.92 \times 0.6$
= 20.666 kW

2. A balanced mesh-connected load of 6+j8 ohms per phase is connected to a 3-phase, 230 V supply. Find the line current, p.f and power.

Solution: - Connection Delta

$$Z_{ph} = 6 + j 8$$
 $V_L = V_{ph} = 230 \text{ V}$
= 10 \Omega (magnitude)

$$\therefore I_{ph} = \frac{V_{ph}}{Z_{ph}} = \frac{230}{10} = 23 \text{ A}$$

$$\therefore I_L = \sqrt{3} I_{ph} = \sqrt{3} \times 23 = \boxed{39.83 \text{ A}}$$

Power factor =
$$\cos \phi = \frac{R_{ph}}{Z_{ph}}$$

= $\frac{6}{10}$
= 0.6 (lag)

Power = $\sqrt{3}$ V_L I_L $\cos \phi$
= $\sqrt{3} \times 230 \times 39.83 \times 0.6$
= 9.520 kW

3. Three similar coils each of resistance 15 ohms and inductance of 0.25 H are connected (i) in star and (ii) in delta to a 3-phase, 400 V, 50 Hz supply. Calculate line and phase values of current and voltage in both the cases. Also calculate the power absorbed.

Solution:-
$$R_{Ph} = 15 \Omega$$
, $L_{Ph} = 0.25 \text{ H}$ $X_{Ph} = \omega L_{Ph} = 2 \times \pi \times 50 \times 0.25 = 78.54$
 $Z_{Ph} = \sqrt{R_{Ph}^2 + X_{Ph}^2} = \sqrt{15^2 + 78.54^2} = 79.96 \Omega$

Star connection:

$$V_L = \boxed{400 \text{ V}}$$

$$V_{Ph} = \frac{V_L}{\sqrt{3}} = \frac{400}{\sqrt{3}} = 230.94 \text{ V}$$

$$I_{Ph} = \frac{V_{Ph}}{Z_{Ph}} = \frac{230.94}{79.96} = \boxed{2.888 \text{ A}}$$

$$l_L = 2.888 \text{ A}$$

Power factor
$$\cos \phi = \frac{R_{Ph}}{Z_{Ph}} = \frac{15}{79.96} = 0.1875 \text{ (lagging)}$$

Total power =
$$\sqrt{3} V_L I_L \cos \phi$$
 (or = 3 × $V_{Ph} \times I_{Ph} \cos \phi$)
= $\sqrt{3} \times 400 \times 2.888 \times 0.1875$
= 375.17 W

Delta connection:

$$V_L = \boxed{400 \text{ V}}$$

$$V_{Ph} = V_L = 400 \text{ V}$$

$$I_{Ph} = \frac{V_{Ph}}{Z_{Ph}} = \frac{400}{79.96} = 5.0025 \text{ A}$$

$$l_L = \sqrt{3} \ l_{Ph} = \sqrt{3} \times 5.0025 =$$
8.664 A

$$\cos \phi = \frac{R_{Ph}}{Z_{Ph}} = \frac{15}{79.96} = 0.1875 \text{ (lag)}$$

Total power =
$$\sqrt{3} V_L I_L \cos \phi = \sqrt{3} \times 400 \times 8.664 \times 0.1875$$

= 1125.56 watt

Thank you