

Map (or dictionary or associative array)

● Behaviour

- ▶ Associates some meaningful data (the "key") with a value
- ▶ Stores and accesses values using the key
- ▶ No specific ordering of the data

● Operations:

- ▶ Put (key, value)
- ▶ Get (key) -> value
- ▶ Size () -> integer
- ▶ ContainsKey (key) -> Boolean
- ▶ ContainsValue (value) -> Boolean (optional)
- ▶ Remove (key) -> Boolean (optional)

Map examples

- **Trivial map**

- ▶ Key is the sequence of integers 1, 2, 3, 4, ...
- ▶ Implementation: a standard array

- **More complex map**

- ▶ Key is your Banner ID
- ▶ Value is your netid
- ▶ Implementation: hash table

Recognizing a spot for a standard ADT

● Stack

- ▶ Doing a set of operations that might need undoing in the reverse order
- ▶ Exploring options that involve backtracking (changing or removing the most recent choice)
- ▶ Recursion (implicit or explicit stack)
- ▶ Situations where proper nesting is involved
- ▶ Exploring connected problems that handle depth of coverage before breadth of coverage

● Queue

- ▶ Simulations of scheduling with items arriving at different times
- ▶ Processing a growing list of items in a way that ensures that each item is handled in a “fair” timeframe
- ▶ Exploring connected problems that handle breadth of coverage before depth of coverage

Recognizing a spot for a standard ADT

● Priority Queue

- ▶ I need to store items and retrieve them in an order that I define (order can change)
- ▶ Often used in scheduling

● Set

- ▶ I have a collection of items to store
 - I just care about having one copy
- ▶ I want to access the items randomly
- ▶ I want to iterate over the set
- ▶ I don't have any particular order needed for the data

● List

- ▶ I have a collection of items to store
 - I might have several copies of the same thing
- ▶ I want to access items randomly
- ▶ I want to be able to impose an order to the set by sorting
- ▶ I want to iterate over the set in the sorted order

● Map

- ▶ Random access to key, value pairs when *exact matches to keys* is all that is needed

What is stored in an ADT?

- **Basic data types, like “int” (for integers)**
 - ▶ Behave exactly as we expect them to
- **Objects**
 - ▶ Important to understand exactly what is being stored

Is there a difference?

```
int a;  
int b;
```

```
a = 10;  
b = a;  
a = 20;
```

```
System.out.println( b );
```

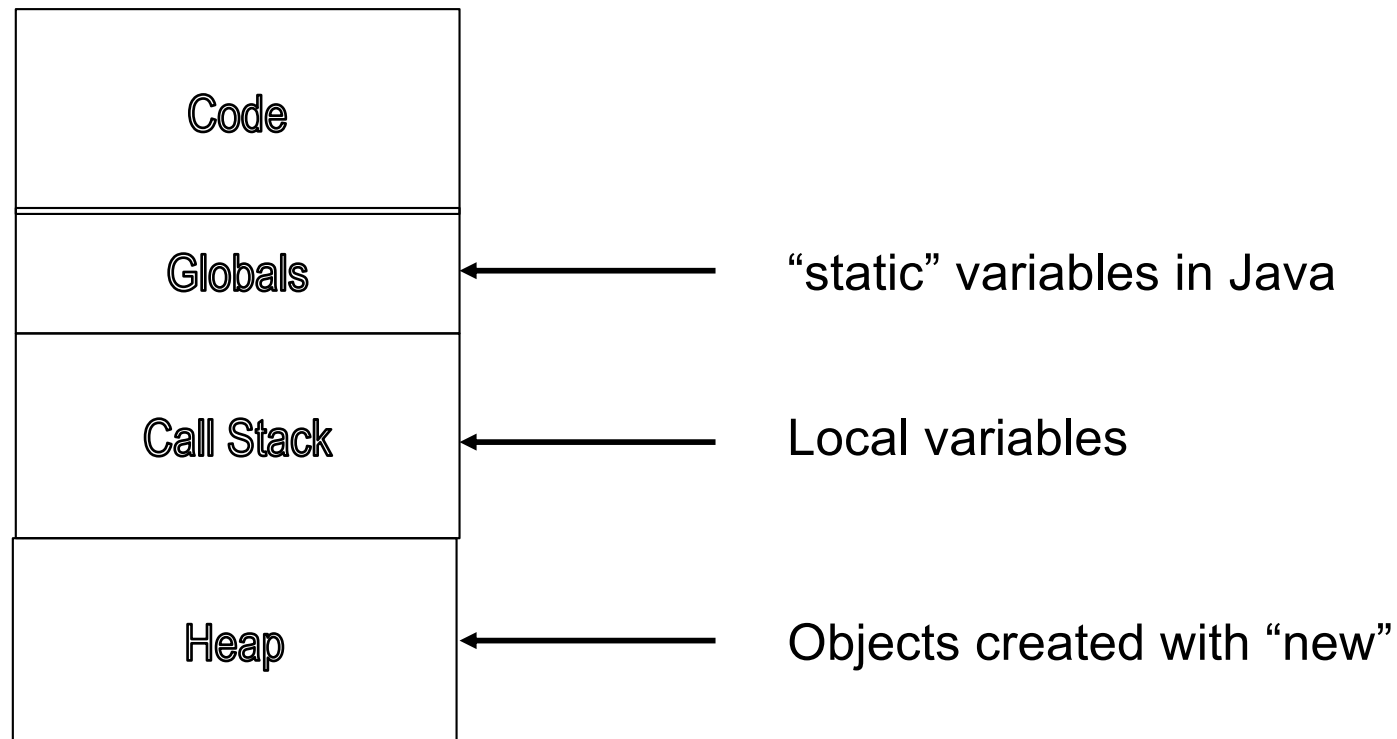
```
myIntClass a;  
myIntClass b;
```

```
a = new myIntClass( 10 );  
b = a;  
a.setValue( 20 );
```

```
System.out.println( b.getValue() );
```

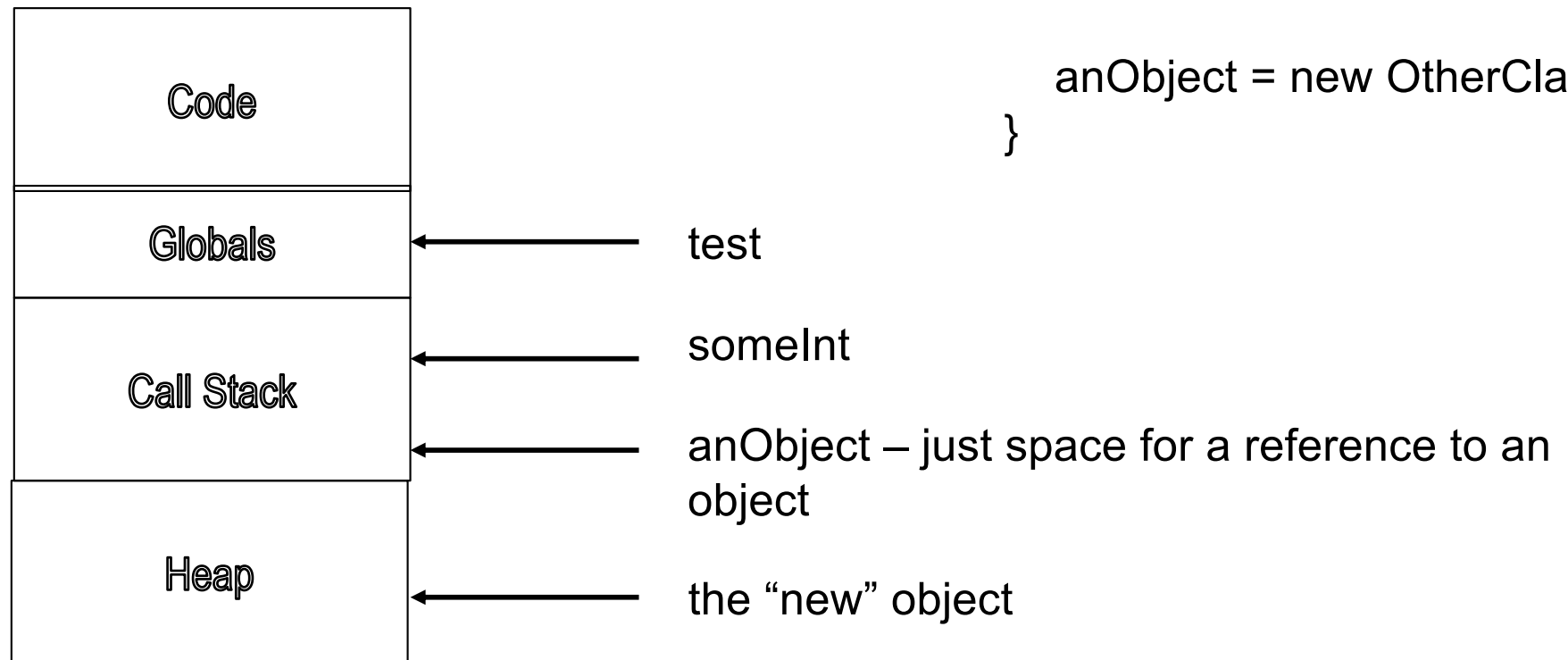
```
Public class myIntClass {  
    int value;  
    public void setValue( int val ) {  
        value = val;  
    }  
    public int getValue( ) {  
        return value;  
    }  
}
```

Elements of a Process



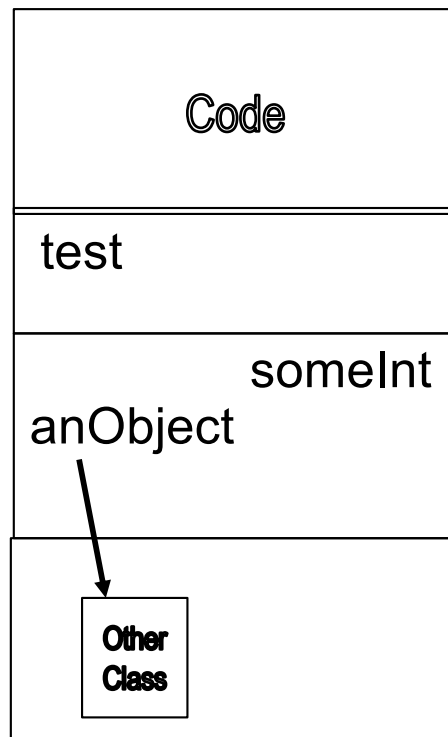
Storing Objects

```
public int myMethod() {  
    int someInt;  
    static boolean test;  
    OtherClass anObject;  
  
    anObject = new OtherClass();  
}
```

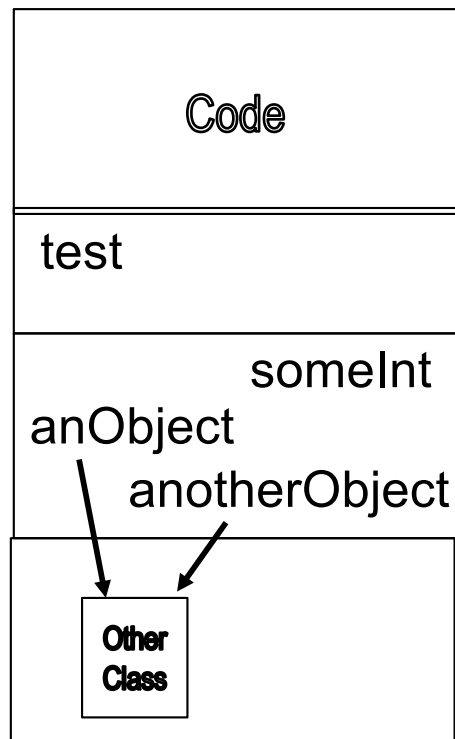


Storing Objects

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public int myMethod() {  
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Storing Objects



```
public int myMethod() {  
    int someInt;  
    static boolean test;  
    OtherClass anObject;
```

```
    anObject = new OtherClass();
```

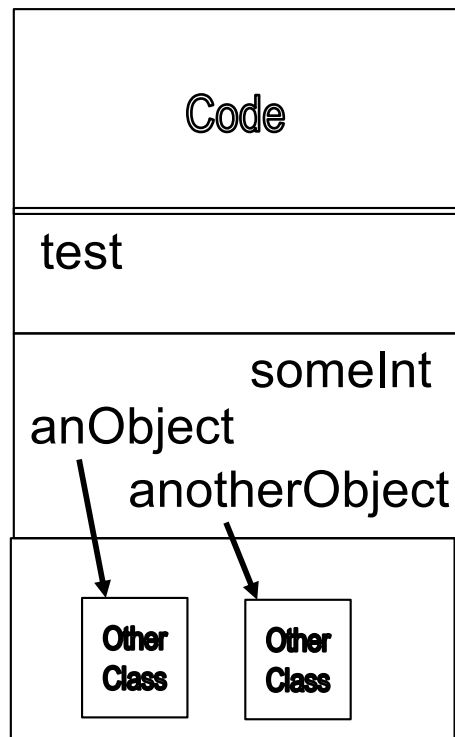
```
    OtherClass anotherObject;
```

```
    anotherObject = anObject;
```

```
}
```

When we assign object values, we are copying the reference to the object. We are not copying the content.

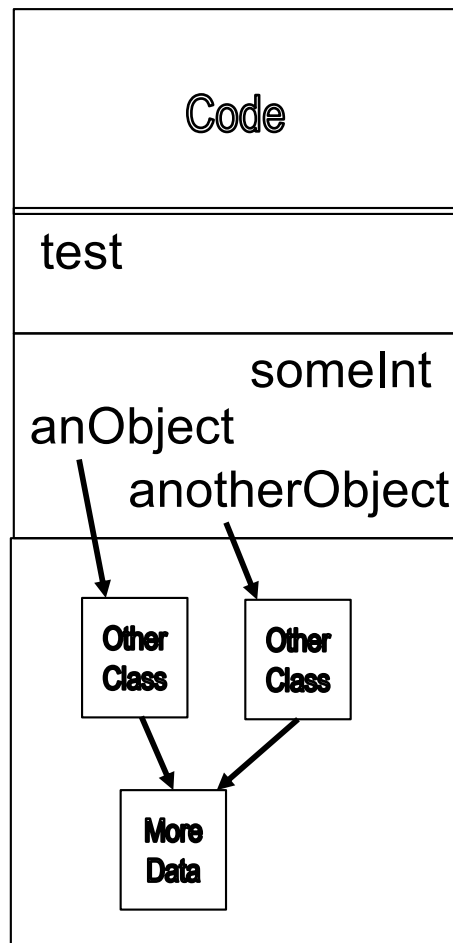
Storing Objects



```
public int myMethod() {  
    int someInt;  
    static boolean test;  
    OtherClass anObject;  
  
    anObject = new OtherClass();  
  
    OtherClass anotherObject;  
  
    anotherObject.copy(anObject);  
}
```

Classes often have a “copy” method to make an actual copy of the class instead.

Storing Objects

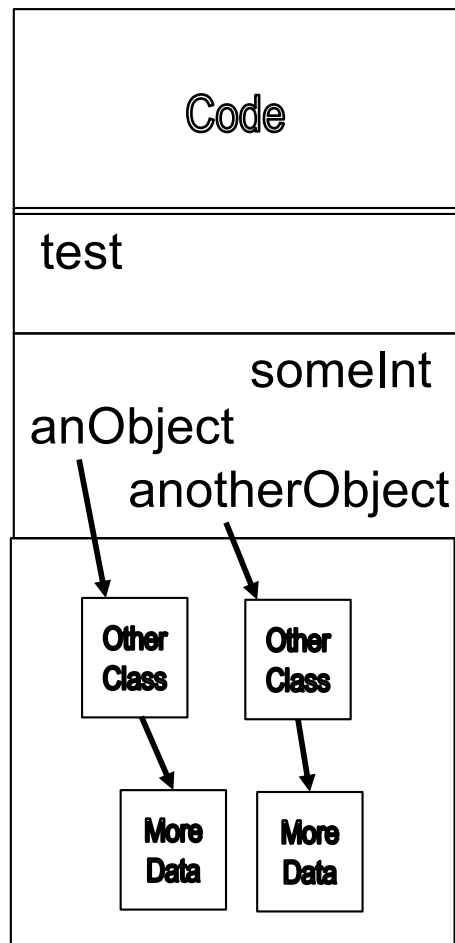


```
public int myMethod() {  
    int someInt;  
    static boolean test;  
    OtherClass anObject;  
  
    anObject = new OtherClass();  
  
    OtherClass anotherObject;  
  
    anotherObject.copy(anObject);  
}
```

An object of a class like OtherClass may reference other objects.

A “copy” method may not always copy the content of those references. That kind of copy is called a “shallow copy”.

Storing Objects



```
public int myMethod() {  
    int someInt;  
    static boolean test;  
    OtherClass anObject;
```

```
    anObject = new OtherClass();
```

```
    OtherClass anotherObject;
```

```
    anotherObject.deepCopy(  
        anObject);
```

```
}
```

A copy method that copies all of the underlying objects is often called a “deep copy” of the object.

What is stored in an ADT?

● Take-away:

- ▶ When you put an object into two ADTs, know whether you expect to have each copy be shared or independent
 - If shared, then put the reference into each ADT
 - If independent then put a copy into each ADT
 - Understand if you need a shallow or a deep copy

Combine ADTs

- You can combine ADTs to meet the need.
- Example
 - ▶ You want to store all items in your house to be retrieved by their colour.
 - Store all items of the same colour in one set.
 - Store these sets in a map where the key is the colour name and the value is the set

Data structures with a fixed size

Array

- **A fixed-size linear sequence of items**
- **Uses integers to identify the order of items in the sequence**
 - ▶ **Start at index number 0 in many programming languages**
 - **Historical context based on implementation efficiency**

Declaring an array in Java

`String[] anArray;` ← Creates a reference to an array, but there is no actual array to store data yet.

`String[] anArray = new String[10];` ← Creates the space for 10 entries in an array. We see that an array is treated like an object of its own.

How would you create a 2d array?

- `Integer[][] arrayName = new Integer[20][15];`

Hash table

- **An organization of data in an array to let us search for an entry quickly.**
- **Key concept:**
 - ▶ **Use a formula to convert the key to store into an array index**
 - Called the “hash function”
 - ▶ **Store the value in the array at the computed index value**
 - ▶ **Have rules to handle the case where two values are converted to the same array index**
 - Called a “collision” in the hash table
- **In a moderately-filled array, you expect to find a search value in constant time.**

Hash table example

- **Array size: 13**
- **Data stored: alphabetic lower-case strings**
- **Hash function: the position in the alphabet of the first letter of the string (starting at position 0)**
- **Array index: take the hash value modulo 13**
- **Expected collisions:**
 - ▶ All the strings that start with the same letter end up at the same index
 - ▶ Two letters of the alphabet converge on the same index

Hash table example

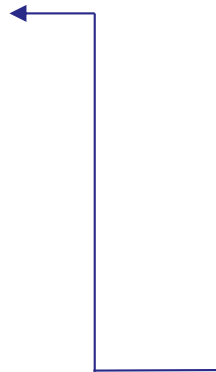
| |
|----------|
| apple |
| |
| pancake |
| density |
| |
| |
| gorilla |
| umbrella |
| |
| |
| |
| yoyo |
| |

Add “quiet”

Hash value is 16 ('q' - 'a')

Index is $16 \bmod 13 = 3$

Store “quiet” here



How to deal with hash table collisions

- Have a data structure at each array index to catch all values that belong at the index (called “open hashing”)
 - ▶ Linked list, binary tree, ...
- In-place: look for another “predictable” place in the array to store the entry (called “closed hashing”)
 - ▶ Move forward k entries in the array until you find an entry spot
 - Linear probing: $k=1$
 - Quadratic probing: k follows a sequence $1^2, 2^2, 3^2, 4^2, \dots$
 - Double hashing: k is the result of applying a second hash function to the value to be stored
 - ▶ More complex resolution schemes
 - Eg. Cuckoo hashing

Hash table example with linear probing

| |
|----------|
| apple |
| mandrake |
| pancake |
| density |
| maple |
| allow |
| gorilla |
| umbrella |
| |
| ape |
| |
| yoyo |
| |

Add “mandrake”

Hash value is 13 (‘m’ – ‘a’)

Index is $13 \bmod 13 = 0$

Try to store “mandrake” here, but the entry is full

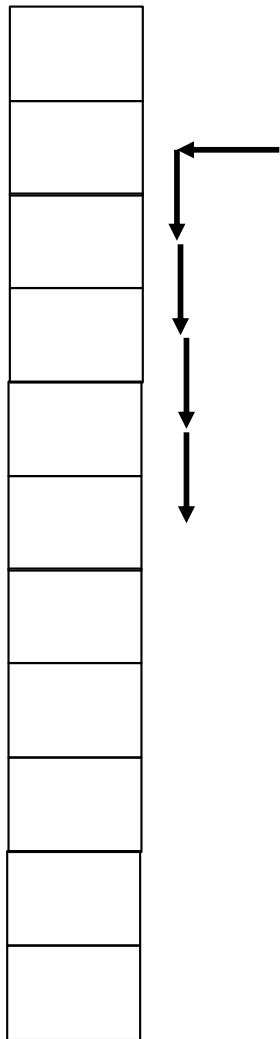
Linear probing: advance by 1 until we find an empty entry

Store “mandrake” in this empty entry

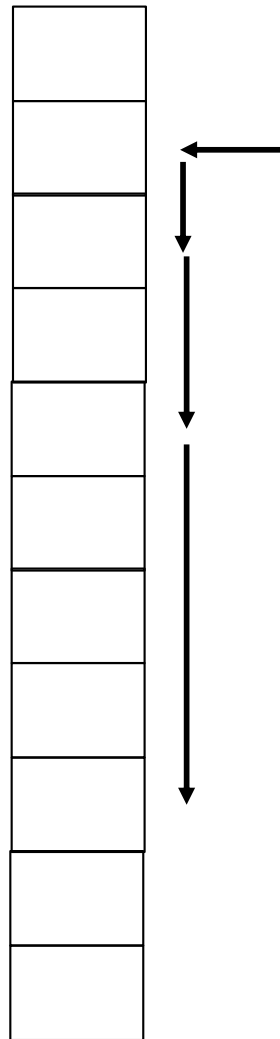
Hash table collisions

- **Other ways to handle hash table collisions**
 - ▶ **Linear probing (already seen)**
 - ▶ **Quadratic probing**
 - ▶ **Double hashing**
 - Use another hash function to tell you how much to jump ahead
 - ▶ **Store a secondary data structure at each entry in the hash table and put all items that map to entry into the secondary structure**
 - Often use a linked list at each entry and call it “chaining”
- **Other specialized approaches, like cuckoo hashing and Robin Hood hashing, also exist.**

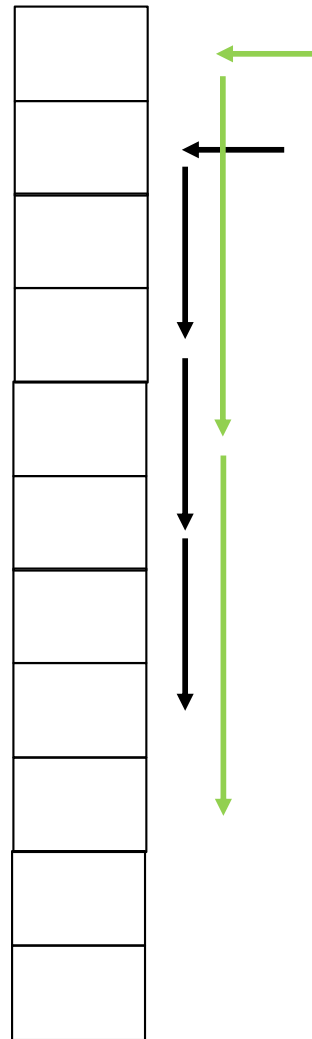
Collision management



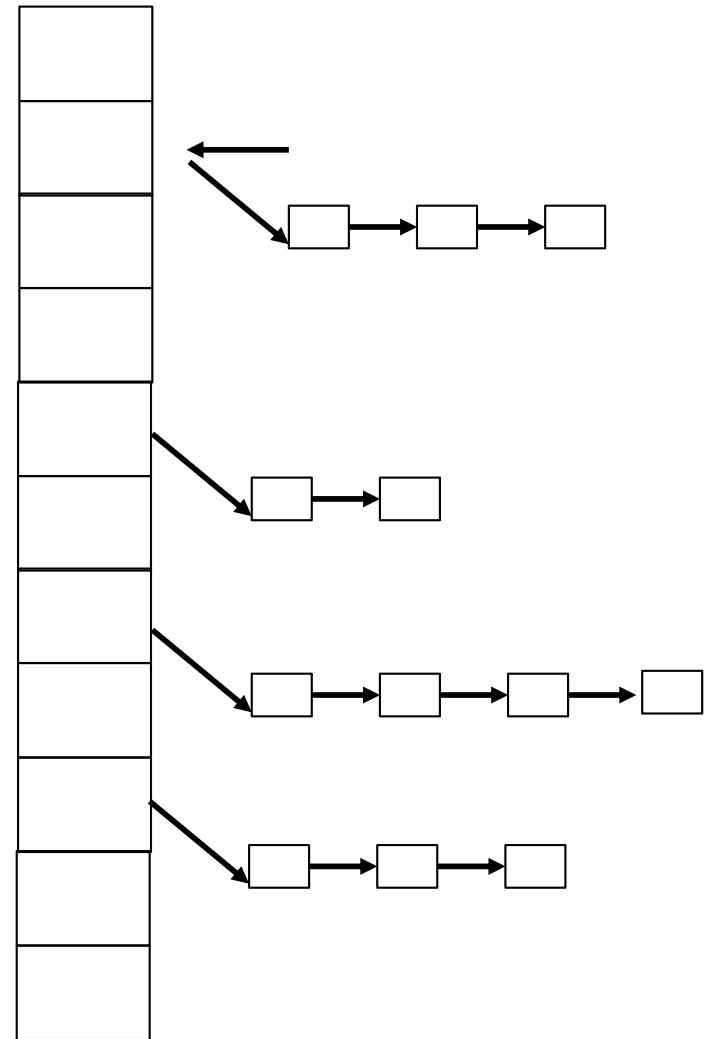
93 Linear probing



Quadratic probing



Double hashing



Chaining