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ANALYSIS AND DESIGN OF ALGORITHMS (23CS4PCADA)

Submitted by

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in partial fulfillment for the award of the degree of BACHELOR OF ENGINEERING in COMPUTER SCIENCE AND ENGINEERING



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This is to certify that the Lab work entitled "ANALYSIS AND DESIGN OF ALGORITHMS" carried out by Dama Yohitesh Naveen Sai (1BM23CS085), who is bonafide student of B. M. S. College of Engineering. It is in partial fulfillment for the award of Bachelor of Engineering in Computer Science and Engineering of the Visvesvaraya Technological University, Belgaum during the year 2024-25. The Lab report has been approved as it satisfies the academic requirements in respect of Analysis and Design of Algorithms Lab - (23CS4PCADA) work prescribed for the said degree.

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Course outcomes:

CO1	Analyze time complexity of Recursive and Non-recursive algorithms using	
	asymptotic notations.	
CO2	Apply various design techniques for the given problem.	
CO3	Apply the knowledge of complexity classes P, NP, and NP-Complete and prove certain problems are NP-Complete	
CO4	Design efficient algorithms and conduct practical experiments to solve problems.	

a. Write a program to obtain the Topological ordering of vertices in a given digraph.

```
#include<stdio.h>
#include<stdlib.h>
#define SIZE 100
void topological_sort(int graph[SIZE][SIZE],int n){
  int indegree[n];
  for(int i = 0; i < n; i++) indegree[i]=0;
  for(int i = 0; i < n; i++){
     for(int j = 0; j < n; j++){
       if(graph[i][j]==1){
          indegree[j]++;
        }
     }
  }
  int source[n];
  int front = 0;
  int last = 0;
  for(int i = 0; i < n; i++){
     if(indegree[i]==0) source[last++]=i;
  }
  int sorted[n];
  int ind = 0;
```

```
while(front<last){</pre>
     int temp = source[front++];
     sorted[ind++]= temp;
     for(int i = 0; i < n; i++){
       if(graph[temp][i]==1){
          indegree[i]--;
          if(indegree[i]==0)source[last++]=i;
        }
     }
  }
  if(ind == n){
     printf("Topological Sorted Order is:");
     for(int i = 0; i < n; i++){
      printf(" %d ",sorted[i]);
     printf("\n");
  }
  else{
     printf("Topological Sorting not possible.\n");
  }
int main(){
  int graph[SIZE][SIZE];
  int n;
  printf("Enter Number of Vertices: ");
```

}

```
scanf("%d",&n);

printf("Enter adjacency matric:\n");

for(int i = 0;i<n;i++){
    for(int j = 0; j<n;j++){
        scanf("%d",&graph[i][j]);
    }

    topological_sort(graph,n);
    return 0;
}</pre>
```

```
Enter Number of Vertices: 4
Enter adjacency matric:
0 1 0 0
1 0 0 0
0 0 1 0
0 0 0 1
Topological Sorting not possible.
```

b. LeetCode Program related to Topological sorting

LeetCode 851. Loud and Rich

There is a group of n people labeled from 0 to n - 1 where each person has a different amount of money and a different level of quietness.

You are given an array richer where richer[i] = [ai, bi] indicates that ai has more money than bi and an integer array quiet where quiet[i] is the quietness of the ith person. All the given data in richer are logically correct (i.e., the data will not lead you to a situation where x is richer than y and y is richer than x at the same time).

Return an integer array answer where answer[x] = y if y is the least quiet person (that is, the person y with the smallest value of quiet[y]) among all people who definitely have equal to or more money than the person x.

Submission Code:

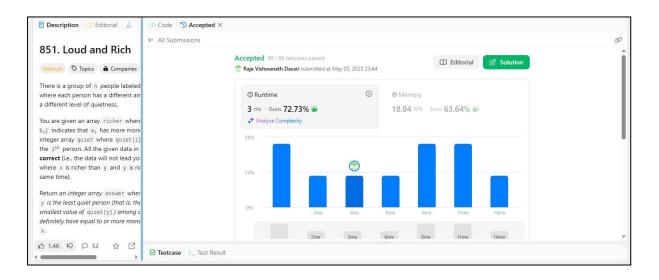
```
#define MAXN 510
```

```
int* loudAndRich(int** richer, int richerSize, int* richerColSize, int* quiet, int quietSize,
int* returnSize) {
  int n = quietSize;
  int graph[MAXN][MAXN] = \{0\};
  int indegree[MAXN] = \{0\};
  int answer[MAXN];
  int queue[MAXN], front = 0, rear = 0;
  for (int i = 0; i < richerSize; i++) {
     int a = richer[i][0], b = richer[i][1];
    if (!graph[a][b]) {
       graph[a][b] = 1;
       indegree[b]++;
     }
  }
  for (int i = 0; i < n; i++) {
     answer[i] = i;
    if (indegree[i] == 0) {
       queue[rear++] = i;
     }
  }
  while (front < rear) {
     int u = queue[front++];
```

```
for (int v = 0; v < n; v++) {
     if (graph[u][v]) {
        if (quiet[answer[u]] < quiet[answer[v]]) {</pre>
           answer[v] = answer[u];
        }
        indegree[v]--;
       if (indegree[v] == 0) {
          queue[rear++] = v;
        }
   }
}
int* result = (int*)malloc(n * sizeof(int));
for (int i = 0; i < n; i++) {
  result[i] = answer[i];
*returnSize = n;
return result;
```

Result:

}



Implement Johnson Trotter algorithm to generate permutations.

```
#include<stdio.h>
#include<stdlib.h>
void swap(int *a, int *b){
  int temp = *a;
  *a = *b;
  *b = temp;
void print_perm(int p[],int n){
  printf("Permutation: ");
  for(int i = 0; i < n; i++){
     printf("%d ",p[i]);
  printf("\n");
void johnson_trotter(int n){
  int p[n];
  int d[n];
  for(int i = 0; i < n; i++){
     p[i] = i+1;
     d[i] = -1;
  print_perm(p,n);
  while(1){
     int largest_mob = -1;
     int largest_ind = -1;
     for(int i=0; i< n; i++){
       if(d[i] == -1 \&\& i>0 \&\& p[i]>p[i-1]){
          if(p[i]>largest_mob){
             largest_mob = p[i];
             largest_ind = i;
          }
        else if(d[i] == 1 &\& i < n-1 &\& p[i] > p[i+1]){
          if(p[i]>largest_mob){
             largest\_mob = p[i];
```

```
largest_ind = i;
          }
       }
     }
     if(largest_mob == -1) break;
     int ind = largest_ind;
     if(d[ind]==-1){
       swap(&p[ind],&p[ind-1]);
       swap(\&d[ind],\&d[ind-1]);
     }
     else if(d[ind]==1){
       swap(&p[ind],&p[ind+1]);
       swap(&d[ind],&d[ind+1]);
     for(int j = 0; j < n; j++){
       if(p[j]>largest_mob){
          d[j] = d[j] * -1;
       }
     }
   print_perm(p,n);
  }
}
int main(){
  int n;
  printf("Enter number of elements to be permuted: ");
  scanf("%d",&n);
  johnson_trotter(n);
}
```

```
Enter number of elements to be permuted: 3
Permutation: 1 2 3
Permutation: 3 1 2
Permutation: 3 2 1
Permutation: 2 3 1
Permutation: 2 1 3

Process returned 0 (0x0) execution time: 1.497 s
Press any key to continue.
```

```
ols 🕨 🗆
    C:\Users\student\Desktop\Jol X
   Enter number of elements to be permuted: 4
  Permutation: 1 2 3 4
   Permutation: 1 2 4 3
  Permutation: 1 4 2 3
   Permutation: 4 1 2 3
  Permutation: 4 1 3 2
   Permutation: 1 4 3 2
  Permutation: 1 3 4 2
  Permutation: 1 3 2 4
  Permutation: 3 1 2 4
  Permutation: 3 1 4 2
  Permutation: 3 4 1 2
  Permutation: 4 3 1 2
   Permutation: 4 3 2 1
  Permutation: 3 4 2 1
   Permutation: 3 2 4 1
  Permutation: 3 2 1 4
   Permutation: 2 3 1 4
  Permutation: 2 3 4 1
  Permutation: 2 4 3 1
  Permutation: 4 2 3 1
  Permutation: 4 2 1 3
  Permutation: 2 4 1 3
  Permutation: 2 1 4 3
  Permutation: 2 1 3 4
  Process returned 0 (0x0)
                              execution time : 5.506 s
  Press any key to continue.
```

a. Sort a given set of N integer elements using Merge Sort technique and compute its time taken. Run the program for different values of N and record the time taken to sort.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
// Merge function
void merge(int arr[], int left, int mid, int right) {
  int n1 = mid - left + 1;
  int n2 = right - mid;
  int *L = (int *)malloc(n1 * sizeof(int));
  int *R = (int *)malloc(n2 * sizeof(int));
  for (int i = 0; i < n1; i++) L[i] = arr[left + i];
  for (int i = 0; i < n2; i++) R[i] = arr[mid + 1 + i];
  int i = 0, j = 0, k = left;
  while (i < n1 \&\& j < n2) {
     if (L[i] \le R[j]) arr[k++] = L[i++];
     else arr[k++] = R[j++];
  }
  while (i < n1) arr[k++] = L[i++];
  while (j < n2) arr[k++] = R[j++];
  free(L);
  free(R);
}
// Merge Sort function
void merge_sort(int arr[], int left, int right) {
  if (left < right) {
     int mid = left + (right - left) / 2;
     merge_sort(arr, left, mid);
     merge\_sort(arr, mid + 1, right);
     merge(arr, left, mid, right);
```

```
}
}
int main() {
  int n_values[] =
{100000,200000,300000,400000,500000,600000,700000,800000,900000,1000000};
  int num_tests = sizeof(n_values) / sizeof(n_values[0]);
  for (int i = 0; i < num\_tests; i++) {
    int n = n_values[i];
    int *array = (int *)malloc(n * sizeof(int));
    // Average Case: Randomized Input
    for (int j = 0; j < n; j++) array[j] = rand() % 1000000;
    clock_t start = clock();
     merge\_sort(array, 0, n - 1);
     clock_t end = clock();
     printf("n = %d \mid Avg: \%.6f\n", n, (double)(end - start) / CLOCKS_PER_SEC);
    free(array);
  }
  return 0;
}
```

```
Merge Sort Time Complexity Analysis:

n = 100000 | Avg: 0.037664

n = 200000 | Avg: 0.079346

n = 300000 | Avg: 0.120634

n = 400000 | Avg: 0.164329

n = 500000 | Avg: 0.209077

n = 600000 | Avg: 0.251556

n = 700000 | Avg: 0.294781

n = 800000 | Avg: 0.339544

n = 900000 | Avg: 0.386991

n = 1000000 | Avg: 0.429733
```

b. LeetCode Program related to Binary Search Tree.

LeetCode 230. Kth Smallest Element in a BST

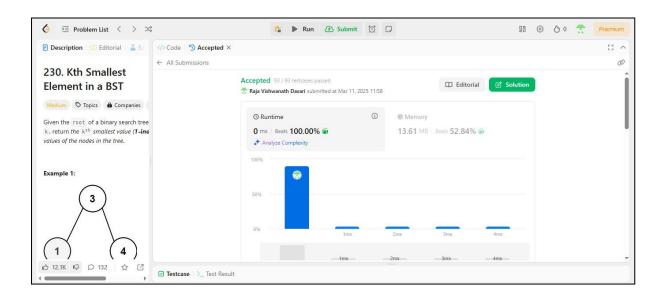
Given the root of a binary search tree, and an integer k, return the kth smallest value (1-indexed) of all the values of the nodes in the tree.

Submission Code:

```
* Definition for a binary tree node.
* struct TreeNode {
    int val:
    struct TreeNode *left;
    struct TreeNode *right;
* };
*/
#include <stdio.h>
#include <stdlib.h>
int kthSmallest(struct TreeNode* root, int k) {
  int findMin(struct TreeNode* root){
     while(root->left!=NULL){
       root = root->left;
     }
    return root->val;
  struct TreeNode* delete_min(struct TreeNode* root){
     struct TreeNode* parent = root;
     struct TreeNode* child = root;
    if(root==NULL){
       return root;
     }
     while(child->left!=NULL){
       parent = child;
       child = child->left;
     parent->left = child->right;
     return root;
  for(int i = 0; i < k-1; i++){
     root = delete_min(root);
  }
```

```
int r = findMin(root);
return r;
}
```

Result:



a. Sort a given set of N integer elements using Quick Sort technique and compute its time taken.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
// Swap function
void swap(int *a, int *b) {
  int temp = *a;
  *a = *b;
  *b = temp;
}
// Median-of-three pivot selection for best case
int median_of_three(int arr[], int low, int high) {
  int mid = low + (high - low) / 2;
  if (arr[low] > arr[mid]) swap(&arr[low], &arr[mid]);
  if (arr[low] > arr[high]) swap(&arr[low], &arr[high]);
  if (arr[mid] > arr[high]) swap(&arr[mid], &arr[high]);
  return mid; // Return index of the median element
}
// Partition function using last element as pivot
int partition(int arr[], int low, int high) {
  int pivot = arr[high]; // Worst and average case use last element as pivot
```

```
int i = low - 1;
  for (int j = low; j < high; j++) {
     if (arr[j] <= pivot) {
       i++;
       swap(&arr[i], &arr[j]);
     }
  }
  swap(\&arr[i+1], \&arr[high]);
  return i + 1;
}
// Partition function using median-of-three pivot for best case
int partition_median(int arr[], int low, int high) {
  int median = median_of_three(arr, low, high);
  swap(&arr[median], &arr[high]); // Move median pivot to the end
  return partition(arr, low, high);
}
// Quick sort with normal partitioning
void quick_sort(int arr[], int low, int high) {
  if (low < high) {
     int pi = partition(arr, low, high);
     quick_sort(arr, low, pi - 1);
     quick_sort(arr, pi + 1, high);
  }
}
```

```
// Quick sort with median pivot for best case
void quick_sort_best(int arr[], int low, int high) {
  if (low < high) {
     int pi = partition_median(arr, low, high);
     quick_sort_best(arr, low, pi - 1);
     quick_sort_best(arr, pi + 1, high);
  }
}
int main() {
  int n_{\text{values}}[] = \{10000, 20000, 30000, 40000, 50000, 60000, 70000, 80000, 90000, 100000\};
  int num_tests = sizeof(n_values) / sizeof(n_values[0]);
  for (int i = 0; i < num\_tests; i++) {
     int n = n_values[i];
     int *array = (int *)malloc(n * sizeof(int));
     // Best Case: Median Pivot (Balanced Partitioning)
     for (int j = 0; j < n; j++) array[j] = j;
     clock_t start = clock();
     quick_sort_best(array, 0, n - 1);
     clock_t end = clock();
     printf("n = %d | Best: %.6f | ", n, (double)(end - start) / CLOCKS_PER_SEC);
     // Average Case: Randomized Input
     for (int j = 0; j < n; j++) array[j] = rand() % 100000;
     start = clock();
     quick_sort(array, 0, n - 1);
     end = clock();
```

```
printf("Avg: %.6f | ", (double)(end - start) / CLOCKS_PER_SEC);

// Worst Case: Already Sorted in Ascending Order (Last Element Pivot)
for (int j = 0; j < n; j++) array[j] = j;
start = clock();
quick_sort(array, 0, n - 1);
end = clock();
printf("Worst: %.6f\n", (double)(end - start) / CLOCKS_PER_SEC);

free(array);
}
return 0;
}</pre>
```

```
n = 10000
           Best: 0.000733 | Avg: 0.001543 |
                                            Worst: 0.349421
n = 20000
           Best: 0.001842 | Avg: 0.003396
                                            Worst: 1.364989
 = 30000
           Best: 0.002432 | Avg: 0.005338
                                             Worst: 3.761610
                                             Worst: 5.478223
 = 40000
           Best: 0.003336 | Avg: 0.007314
 = 50000
           Best: 0.004516 | Avg: 0.009029
                                            Worst: 9.220020
  = 60000
           Best: 0.005158 | Avg: 0.011119
                                             Worst: 13.013741
                                             Worst: 17.445868
 = 70000
           Best: 0.005970 | Avg: 0.013162
 = 80000
           Best: 0.007140 | Avg: 0.015433
                                             Worst: 23.256661
          | Best: 0.008138 | Avg: 0.018496
 = 90000
                                           | Worst: 29.237170
n = 100000 | Best: 0.012229 | Avg: 0.024076 | Worst: 35.982174
```

b. LeetCode Program related to Binary Trees.

LeetCode 124. Binary Tree Maximum Path Sum

A path in a binary tree is a sequence of nodes where each pair of adjacent nodes in the sequence has an edge connecting them. A node can only appear in the sequence at most once. Note that the path does not need to pass through the root.

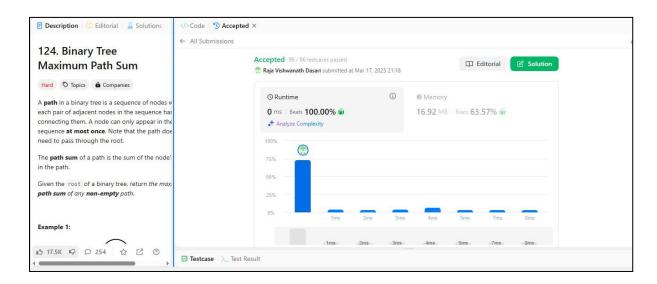
The path sum of a path is the sum of the node's values in the path.

Given the root of a binary tree, return the maximum path sum of any non-empty path.

Submission Code:

```
struct TreeNode {
  int val;
  struct TreeNode *left;
  struct TreeNode *right;
};
int dfs(struct TreeNode* root, int* res) {
  if (root == NULL) {
     return 0;
  }
  int left = dfs(root->left, res);
  int right = dfs(root->right, res);
  left = (left > 0)? left : 0;
  right = (right > 0)? right : 0;
  *res = (*res > left + right + root->val) ? *res : (left + right + root->val);
  return root->val + ((left > right) ? left : right);
}
int maxPathSum(struct TreeNode* root) {
  dfs(root, &res);
  return res;
}
```

Result:



Sort a given set of N integer elements using Heap Sort technique and compute its time taken.

```
#include <stdio.h>
#include <stdlib.h>
#include <time.h>
void heapify(int arr[], int n, int i) {
  int l = 2 * i + 1, r = 2 * i + 2, m = i;
  if (1 < n \&\& arr[1] > arr[m]) m = 1;
  if (r < n \&\& arr[r] > arr[m]) m = r;
  if (m != i) {
     int t = arr[i];
     arr[i] = arr[m];
     arr[m] = t;
     heapify(arr, n, m);
  }
}
void heapsort(int arr[], int n) {
  for (int i = n / 2 - 1; i >= 0; i--) heapify(arr, n, i);
  for (int i = n - 1; i > 0; i - -) {
     int t = arr[0];
     arr[0] = arr[i];
     arr[i] = t;
     heapify(arr, i, 0);
  }
}
int main() {
  int n_values[] =
{100000,200000,300000,400000,500000,600000,700000,800000,900000,1000000};
  int num_tests = sizeof(n_values) / sizeof(n_values[0]);
  printf("Heap Sort Time Complexity Analysis: \n");
  for (int i = 0; i < num\_tests; i++) {
     int n = n_values[i];
     int *array = (int *)malloc(n * sizeof(int));
     for (int j = 0; j < n; j++) array[j] = rand() % 1000000;
```

```
clock_t start = clock();
heapsort(array, n);
clock_t end = clock();

printf("n = %d | Avg: %.6f sec\n", n, (double)(end - start) / CLOCKS_PER_SEC);
free(array);
}
return 0;
}
```

```
Heap Sort Time Complexity Analysis:

n = 100000 | Avg: 0.032810 sec

n = 200000 | Avg: 0.076087 sec

n = 300000 | Avg: 0.109885 sec

n = 400000 | Avg: 0.151516 sec

n = 500000 | Avg: 0.198166 sec

n = 600000 | Avg: 0.235795 sec

n = 700000 | Avg: 0.294872 sec

n = 800000 | Avg: 0.331766 sec

n = 900000 | Avg: 0.369062 sec

n = 1000000 | Avg: 0.435496 sec
```

a. Implement 0/1 Knapsack problem using dynamic programming

```
#include<stdio.h>
#include<stdlib.h>
int max(int a,int b){
  int m = a > b?a:b;
  return m;
}
void knapsack(int v[], int w[], int n, int W){
  int dp[n+1][W+1];
  for(int i = 0; i <= n; i++){
     for(int j = 0; j <= W; j++){
       dp[i][j] = 0;
     }
  }
  for(int i = 1; i <= n; i++){
     for(int j = 1; j <= W; j++){
       if(w[i-1] <= j){
          dp[i][j] = max(dp[i-1][j], v[i-1]+dp[i-1][j-w[i-1]]);
        }
       else{
          dp[i][j]=dp[i-1][j];
        }
     }
  printf("Maximum value: %d\n", dp[n][W]);
  printf("Selected item: ");
  int res = dp[n][W];
  int j = W;
  for (int i = n; i > 0 && res > 0; i--) {
     if (res != dp[i-1][j]) {
       printf("%d", i);
       res -= v[i-1];
       j = w[i-1];
```

```
}
  printf("\n");
}
int main() {
  int n, W;
  int values[100], weights[100];
  printf("Enter the number of items: ");
  scanf("%d", &n);
  printf("Enter the capacity of the knapsack: ");
  scanf("%d", &W);
  printf("Enter the values of the items:\n");
  for (int i = 0; i < n; i++) {
     scanf("%d", &values[i]);
  printf("Enter the weights of the items:\n");
  for (int i = 0; i < n; i++) {
     scanf("%d", &weights[i]);
  }
  knapsack(values, weights, n, W);
  return 0;
}
```

```
Enter the number of items: 5
Enter the capacity of the knapsack: 7
Enter the values of the items:
100 120 90 70 50
Enter the weights of the items:
2 3 6 1 4
Maximum value: 290
Selected item: 4 2 1

Process returned 0 (0x0) execution time: 32.291 s
Press any key to continue.
```

b. LeetCode Program related to Knapsack problem or Dynamic Programming.

LeetCode 474. Ones and Zeroes

You are given an array of binary strings strs and two integers m and n.

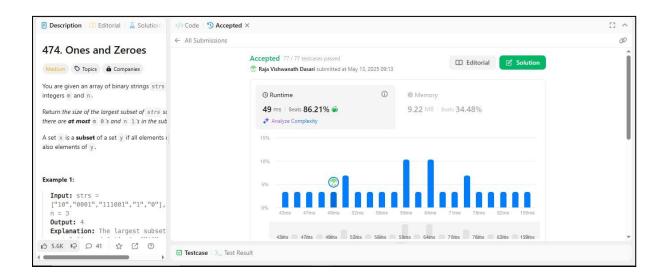
Return the size of the largest subset of strs such that there are at most m 0's and n 1's in the subset.

A set x is a subset of a set y if all elements of x are also elements of y.

Submission Code:

```
#include <string.h>
int findMaxForm(char** strs, int strsSize, int m, int n) {
  int dp[101][101] = \{0\};
  for (int k = 0; k < strsSize; ++k) {
     int zeros = 0, ones = 0;
     for (int i = 0; strs[k][i]; ++i) {
        if (strs[k][i] == '0') zeros++;
        else ones++;
     for (int i = m; i \ge zeros; --i) {
        for (int j = n; j >= ones; --j) {
          if (dp[i][j] < dp[i - zeros][j - ones] + 1) {
             dp[i][j] = dp[i - zeros][j - ones] + 1;
          }
        }
     }
  }
  return dp[m][n];
}
```

Result:



a. Implement All Pair Shortest paths problem using Floyd's algorithm.

```
#include<stdio.h>
#include<stdlib.h>
#includeimits.h>
#define SIZE 100
int min(int a, int b){
  int m = a > b?b:a;
  return m;
}
void floyd_warshall(int graph[SIZE][SIZE],int n){
  int D[n][n];
  for(int i = 0; i < n; i++){
     for(int j = 0; j < n; j++){
       D[i][j] = graph[i][j];
     }
  }
  for(int k = 0; k < n; k++){
     for(int i = 0; i < n; i++){
       for(int j = 0; j < n; j++){
          if(D[i][k]!=INT\_MAX \&\& D[k][j]!=INT\_MAX){
             D[i][j] = min(D[i][j], D[i][k] + D[k][j]);
          }
        }
     }
  printf("The final matrix D is:\n");
  for(int i = 0; i < n; i++){
     for(int j = 0; j < n; j++){
       if(D[i][j]!=INT_MAX)printf("%d",D[i][j]);
       else printf("INF ");
     printf("\n");
  for(int i = 0; i < n; i++){
     for(int j = 0; j < n; j++){
```

```
if(D[i][j]!=0 && D[i][j]!=INT_MAX){
          printf("Shortest Path from %d to %d : %d\n", i,j,D[i][j]);
       }
     }
}
int main(){
  int n;
  int graph[SIZE][SIZE];
  printf("Enter number of vertices :");
  scanf("%d",&n);
  printf("For no direct edge enter -1\n");
  for(int i = 0; i < n; i++){
     for(int j =0; j<n;j++) scanf("%d",&graph[i][j]);
  }
  for(int i = 0; i < n; i++){
     for(int j = 0; j < n; j++){
       if(graph[i][j]==-1) graph[i][j]=INT_MAX;
     }
  floyd_warshall(graph,n);
  return 0;
}
```

```
Enter number of vertices :4
For no direct edge enter -1
0 -1 3 -1
2 0 -1 -1
-1701
6 -1 -1 0
The final matrix D is:
0 10 3 4
2 0 5 6
7701
6 16 9 0
Shortest Path from 0 to 1 : 10
Shortest Path from 0 to 2 : 3
Shortest Path from 0 to 3 : 4
Shortest Path from 1 to 0 : 2
Shortest Path from 1 to 2 : 5
Shortest Path from 1 to 3 : 6
Shortest Path from 2 to 0 : 7
Shortest Path from 2 to 1 : 7
Shortest Path from 2 to 3 : 1
Shortest Path from 3 to 0 : 6
Shortest Path from 3 to 1 : 16
Shortest Path from 3 to 2 : 9
```

```
Enter number of vertices :5
For no direct edge enter -1
0 6 2 4 -1
-1 0 -1 -1 -1
-1 3 0 -1 1
-1 1 -1 0 -1
-1 1 -1 -1 0
The final matrix D is:
0 4 2 4 3
INF 0 INF INF INF
INF 2 0 INF 1
INF 1 INF 0 INF
INF 1 INF INF 0
Shortest Path from 0 to 1 : 4
Shortest Path from 0 to 2 : 2
Shortest Path from 0 to 3 : 4
Shortest Path from 0 to 4 : 3
Shortest Path from 2 to 1 : 2
Shortest Path from 2 to 4 : 1
Shortest Path from 3 to 1 : 1
Shortest Path from 4 to 1 : 1
```

b. LeetCode Program related to shortest distance calculation.

LeetCode 1334. Find the City With the Smallest Number of Neighbors at a Threshold Distance

There are n cities numbered from 0 to n-1. Given the array edges where edges[i] = [fromi, toi, weighti] represents a bidirectional and weighted edge between cities fromi and toi, and given the integer distanceThreshold.

Return the city with the smallest number of cities that are reachable through some path and whose distance is at most distanceThreshold, If there are multiple such cities, return the city with the greatest number.

Notice that the distance of a path connecting cities i and j is equal to the sum of the edges' weights along that path.

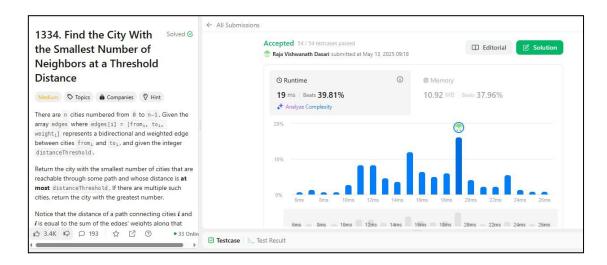
Submission Code:

```
#include inits.h>
#include <stdlib.h>
#define INF 1000000000 // A large number representing infinity
int findTheCity(int n, int** edges, int edgesSize, int* edgesColSize, int distanceThreshold) {
  int dist[100][100]; // n \le 100
  // Initialize distances
  for (int i = 0; i < n; i++) {
     for (int j = 0; j < n; j++) {
       dist[i][j] = (i == j) ? 0 : INF;
     }
  }
  // Set initial edge weights
  for (int i = 0; i < edgesSize; i++) {
     int u = edges[i][0];
     int v = edges[i][1];
     int w = edges[i][2];
     dist[u][v] = w;
     dist[v][u] = w; // because it's bidirectional
  }
   // Floyd-Warshall algorithm
   for (int k = 0; k < n; k++) {
     for (int i = 0; i < n; i++) {
```

```
for (int j = 0; j < n; j++) {
        if (dist[i][k] + dist[k][j] < dist[i][j]) {
           dist[i][j] = dist[i][k] + dist[k][j];
        }
   }
int result = -1;
int minReachable = n + 1; // Start with max possible
for (int i = 0; i < n; i++) {
  int count = 0;
  for (int j = 0; j < n; j++) {
     if (i != j && dist[i][j] <= distanceThreshold) {
        count++;
     }
   }
  // Choose the city with the smallest number of reachable cities.
  // If tied, choose the larger index.
  if (count <= minReachable) {
     minReachable = count;
     result = i;
  }
}
return result;
```

Result:

}



a. Find Minimum Cost Spanning Tree of a given undirected graph using Prim's algorithm.

```
#include <stdio.h>
#include inits.h>
#define MAX 100
int minKey(int key[], int mstSet[], int V) {
  int min = INT_MAX, min_index = -1;
  for (int v = 0; v < V; v++) {
    if (mstSet[v] == 0 \&\& key[v] < min) {
       min = key[v];
       min_index = v;
     }
  return min_index;
}
void printMST(int parent[], int graph[MAX][MAX], int V) {
  printf("Edge \tWeight\n");
  for (int i = 1; i < V; i++) {
    printf("\%d - \%d \t\%d\n", parent[i], i, graph[i][parent[i]]);
  }
}
void primMST(int graph[MAX][MAX], int V) {
  int parent[MAX];
  int key[MAX];
  int mstSet[MAX];
  for (int i = 0; i < V; i++) {
    key[i] = INT\_MAX;
    mstSet[i] = 0;
  }
  key[0] = 0;
  parent[0] = -1;
```

```
for (int count = 0; count < V - 1; count++) {
    int u = minKey(key, mstSet, V);
    mstSet[u] = 1;
    for (int v = 0; v < V; v++) {
       if (graph[u][v] \&\& mstSet[v] == 0 \&\& graph[u][v] < key[v]) {
          parent[v] = u;
          key[v] = graph[u][v];
       }
    }
  }
  printMST(parent, graph, V);
}
int main() {
  int V, graph[MAX][MAX];
  printf("Enter the number of vertices: ");
  scanf("%d", &V);
  printf("Enter the adjacency matrix (0 if no edge):\n");
  for (int i = 0; i < V; i++) {
    for (int j = 0; j < V; j++) {
       scanf("%d", &graph[i][j]);
     }
  }
  primMST(graph, V);
  return 0;
}
```

```
Enter the number of vertices: 5
Enter the adjacency matrix (0 if no edge):
0 10 0 0 5
10 0 12 13 0
 12 0 20 0
 13 20 0 6
 0 0 6 0
       Weight
Edge
        12
        6
 - 4
        5
                           execution time : 142.404 s
Process returned 0 (0x0)
Press any key to continue.
```

b. Find Minimum Cost Spanning Tree of a given undirected graph using Kruskal's algorithm

```
#include <stdio.h>
#define MAX 100
int parent[MAX];
int find(int i) {
    while (parent[i] != i)
        i = parent[i];
    return i;
}

void unionSet(int i, int j) {
    int a = find(i);
    int b = find(j);
    parent[b] = a;
}

int main() {
    int V;
    int graph[MAX][MAX];
```

```
printf("Enter number of vertices: ");
scanf("%d", &V);
printf("Enter the adjacency matrix (0 if no edge):\n");
for (int i = 0; i < V; i++) {
  for (int j = 0; j < V; j++) {
     scanf("%d", &graph[i][j]);
  }
}
for (int i = 0; i < V; i++)
  parent[i] = i;
int edgeCount = 0, minCost = 0;
printf("Edge \tWeight\n");
while (edgeCount < V - 1) {
  int min = 99999, a = -1, b = -1;
  for (int i = 0; i < V; i++) {
     for (int j = 0; j < V; j++) {
       if (graph[i][j] != 0 && graph[i][j] < min && find(i) != find(j)) {
          min = graph[i][j];
          a = i;
          b = j;
        }
     }
  }
  if (a != -1 \&\& b != -1) {
     unionSet(a, b);
     printf("%d - %d \t%d\n", a, b, min);
     minCost += min;
     edgeCount++;
  } else {
     break;
  }
}
printf("Total weight of MST: %d\n", minCost);
return 0;
```

}

```
Enter number of vertices: 5
Enter the adjacency matrix (0 if no edge):
0 10 0 0 5
10 0 12 13 0
0 12 0 20 0
0 13 20 0 6
5 0 0 6 0
Edge Weight
0 - 4 5
3 - 4 6
0 - 1 10
1 - 2 12
Total weight of MST: 33

Process returned 0 (0x0) execution time : 114.168 s
Press any key to continue.
```

Lab Program 9

a. Fractional Knapsack using Greedy technique.

Code:

```
#include<stdio.h>
#include<stdlib.h>
int partition(double arr[][3], int low, int high) {
  double pivot = arr[high][2];
  int i = (low - 1);
  for (int j = low; j < high; j++) {
     if (arr[j][2] > pivot) {
       i++;
        double temp0 = arr[i][0], temp1 = arr[i][1], temp2 = arr[i][2];
        arr[i][0] = arr[j][0];
        arr[i][1] = arr[j][1];
        arr[i][2] = arr[j][2];
        arr[j][0] = temp0;
        arr[j][1] = temp1;
        arr[j][2] = temp2;
     }
  double temp0 = arr[i + 1][0], temp1 = arr[i + 1][1], temp2 = arr[i + 1][2];
  arr[i + 1][0] = arr[high][0];
  arr[i + 1][1] = arr[high][1];
  arr[i + 1][2] = arr[high][2];
  arr[high][0] = temp0;
  arr[high][1] = temp1;
  arr[high][2] = temp2;
  return i + 1;
}
void quick_sort(double arr[][3], int low, int high) {
  if (low < high) {
     int pi = partition(arr, low, high);
     quick_sort(arr, low, pi - 1);
     quick_sort(arr, pi + 1, high);
  }
}
```

```
void fractional_knapsack(int v[], int w[], int n, int W) {
  double items[n][3];
  for (int i = 0; i < n; i++) {
     items[i][0] = v[i];
     items[i][1] = w[i];
     items[i][2] = (double)v[i] / (double)w[i];
  }
  quick_sort(items, 0, n - 1);
  double K = W;
  double total_val = 0.0;
  double x[n];
  for (int i = 0; i < n; i++) {
     x[i] = 0.0;
  for (int i = 0; i < n & K > 0; i++) {
     if (items[i][1] \le K) {
       total_val += items[i][0];
       K = items[i][1];
       x[i] = 1.0;
     } else {
       total_val += K * items[i][2];
       x[i] = K / items[i][1];
       K = 0;
     }
  }
  printf("Total Value: %f\n", total_val);
  printf("Item fractions: ");
  for (int i = 0; i < n; i++) {
     printf("%f ", x[i]);
  printf("\n");
}
int main(){
  int n, W;
  printf("Enter capacity of knapsack: ");
  scanf("%d", &W);
  printf("Enter number of items: ");
```

```
scanf("%d", &n);
  if (n \le 0) {
    printf("Invalid number of items.\n");
    return 0;
  }
  int v[n];
  int w[n];
  printf("Enter weights of items: ");
  for (int i = 0; i < n; i++) {
    scanf("%d", &w[i]);
  }
  printf("Enter values of items: ");
  for (int i = 0; i < n; i++) {
    scanf("%d", &v[i]);
  }
  fractional_knapsack(v, w, n, W);
  return 0;
}
```

```
Enter capacity of knapsack: 50
Enter number of items: 3
Enter weights of items: 10 20 30
Enter values of items: 60 100 120
Total Value: 240.000000
Item fractions: 1.000000 1.000000 0.666667

Process returned 0 (0x0) execution time : 18.795 s
Press any key to continue.
```

b. LeetCode Program related to Greedy Technique algorithms.

LeetCode 1584. Min Cost to Connect All Points

You are given an array points representing integer coordinates of some points on a 2D-plane, where points[i] = [xi, yi].

The cost of connecting two points [xi, yi] and [xj, yj] is the manhattan distance between them: |xi - xj| + |yi - yj|, where |val| denotes the absolute value of val.

Return the minimum cost to make all points connected. All points are connected if there is exactly one simple path between any two points.

Submission Code:

```
#include <stdio.h>
#include <stdlib.h>
#include inits.h>
#define MAX_POINTS 1000
int visited[MAX_POINTS];
int minDist[MAX_POINTS];
int absVal(int x) {
  return x < 0? -x: x;
}
int manhattan_distance(int* a, int* b) {
  return absVal(a[0] - b[0]) + absVal(a[1] - b[1]);
}
int minCostConnectPoints(int** points, int pointsSize, int* pointsColSize) {
  for (int i = 0; i < pointsSize; i++) {
     visited[i] = 0;
     minDist[i] = INT\_MAX;
  }
  int totalCost = 0;
  minDist[0] = 0;
  for (int i = 0; i < pointsSize; i++) {
    int u = -1;
     for (int j = 0; j < pointsSize; j++) {
       if (!visited[j] && (u == -1 \parallel minDist[j] < minDist[u])) {
          u = j;
```

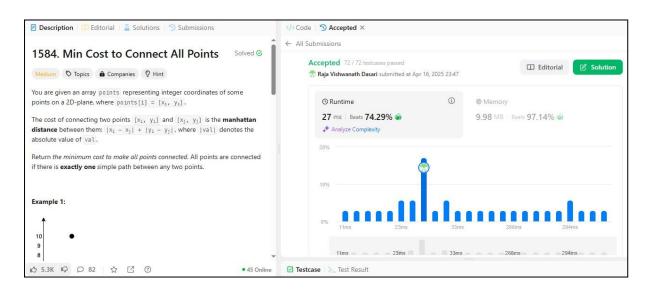
```
}

visited[u] = 1;
totalCost += minDist[u];

for (int v = 0; v < pointsSize; v++) {
    if (!visited[v]) {
        int dist = manhattan_distance(points[u], points[v]);
        if (dist < minDist[v]) {
            minDist[v] = dist;
        }
    }
}

return totalCost;
</pre>
```

Result:



Lab Program 10

From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm.

Code:

```
#include<stdio.h>
#include<stdlib.h>
#includeimits.h>
#define MAX 100
int findMin(int dist[], int visited[], int V){
  int min = INT_MAX;
  int min_ind;
  for(int i=0; i< V; i++){
     if(visited[i]==0 \&\& dist[i]<min){}
       min = dist[i];
       min_ind = i;
     }
  }
  return min_ind;
}
void printPath(int prev[], int j) {
  if (prev[j] == -1) {
     printf("%d", j);
     return;
  printPath(prev, prev[j]);
  printf("-> %d ", j);
}
void djikstra(int graph[MAX][MAX],int src,int V){
  int dist[V];
  int visited[V];
  int prev[V];
  for(int i = 0; i < V; i++){
     dist[i]=INT_MAX;
     visited[i]=0;
```

```
prev[i] = -1;
  dist[src] = 0;
  for(int j = 0; j < V-1; j++){
     int u = findMin(dist, visited, V);
     visited[u] = 1;
     for(int v = 0; v < V; v + +){
       if(visited[v] == 0 \&\& graph[u][v]!=0 \&\& dist[u]!=INT\_MAX){
          if(dist[u]+graph[u][v] < dist[v]){
             dist[v] = dist[u] + graph[u][v];
             prev[v] = u;
          }
        }
     }
  }
  printf("Vertex \t Shortest Distance\n");
  for(int i = 0; i < V; i++){
     printf("%d\t %d\t\t",i,dist[i]);
     printf("Shortest Path: ");
     printPath(prev, i);
     printf("\n");
  }
}
int main(){
  int V;
  int graph[MAX][MAX];
  printf("Number of vertices: ");
  scanf("%d",&V);
  printf("Enter Weighted Adjacency Matrix ( 0 if no edge ):\n");
  for(int i = 0; i < V; i++){
     for(int j = 0; j < V; j++){
       scanf("%d",&graph[i][j]);
     }
  }
```

```
printf("\nSource Vertex: ");
scanf("%d",&src);

djikstra(graph,src,V);
return 0;
}
```

```
Number of vertices: 9
Enter Weighted Adjacency Matrix ( 0 if no edge ):
040000080
4 0 8 0 0 0 0 11 0
080704002
0 0 7 0 0 14 0 0 0
0 0 0 9 0 10 0 0 0
0 0 4 14 10 0 2 0 0
000002016
8 11 0 0 0 0 1 0 7
002000670
Source Vertex: 0
Vertex
        Shortest Distance
0
                       Shortest Path: 0
1
        4
                       Shortest Path: 0 -> 1
2
                       Shortest Path: 0 -> 1 -> 2
        12
3
        19
                       Shortest Path: 0 -> 1 -> 2 -> 3
4
                       Shortest Path: 0 -> 7 -> 6 -> 5 -> 4
        21
5
        11
                       Shortest Path: 0 -> 7 -> 6 -> 5
6
        9
                       Shortest Path: 0 -> 7 -> 6
7
        8
                       Shortest Path: 0 -> 7
8
        14
                       Shortest Path: 0 -> 1 -> 2 -> 8
Process returned 0 (0x0) execution time : 5.754 s
Press any key to continue.
```

Lab Program 11

Implement "N-Queens Problem" using Backtracking.

Code:

```
#include <stdio.h>
#include <stdbool.h>
#define MAX_N 10
void printBoard(int board[MAX_N][MAX_N], int n) {
  for (int i = 0; i < n; i++) {
     for (int j = 0; j < n; j++) {
       printf("%d", board[i][j]);
     printf("\n");
  printf("\n");
bool isSafe(int board[MAX_N][MAX_N], int row, int col, int n) {
  for (int i = 0; i < row; i++) {
     if (board[i][col] == 1) {
       return false;
     if (col - (row - i) >= 0 && board[i][col - (row - i)] == 1) {
       return false;
     }
     if (col + (row - i) < n \&\& board[i][col + (row - i)] == 1) {
       return false;
     }
  return true;
void solveNQueens(int board[MAX_N][MAX_N], int row, int n, int* solutionCount) {
  if (row == n) {
     (*solutionCount)++;
     printBoard(board, n);
     return;
  }
  for (int col = 0; col < n; col ++) {
     if (isSafe(board, row, col, n)) {
       board[row][col] = 1;
```

```
solveNQueens(board, row + 1, n, solutionCount);
       board[row][col] = 0;
     }
  }
}
int main() {
  int n;
  printf("Enter the size of the board (n): ");
  scanf("%d", &n);
  if (n < 1 || n > MAX_N) {
    printf("Please enter a number between 1 and %d.\n", MAX_N);
    return 1;
  }
  int board[MAX_N][MAX_N] = \{0\};
  int solutionCount = 0;
  solveNQueens(board, 0, n, &solutionCount);
  if (solutionCount == 0) {
    printf("No solution exists.\n");
  } else {
    printf("Total solutions found: %d\n", solutionCount);
  }
  return 0;
}
```

```
Enter the size of the board (n): 4
0 1 0 0
0 0 0 1
1 0 0 0
0 0 1 0
0 0 1 0
1 0 0 0
0 0 0 1
0 1 0 0
Total solutions found: 2
```