

Programming with Numbers and Strings

Reading Assignment

- Chapter 2 Sections 1, 2, 4 and 5.

Chapter Learning Outcomes

At the end of this chapter, you will be able to

- define and use variables and constants
- write arithmetic expressions and assignment statements
- understand the properties and limitations of integers and floating-point numbers
- appreciate the importance of comments and good code layout
- write arithmetic expressions and assignment statements
- create programs that read and process inputs, and display the results
- learn how to use Python strings

Variables

Why do we need variables?

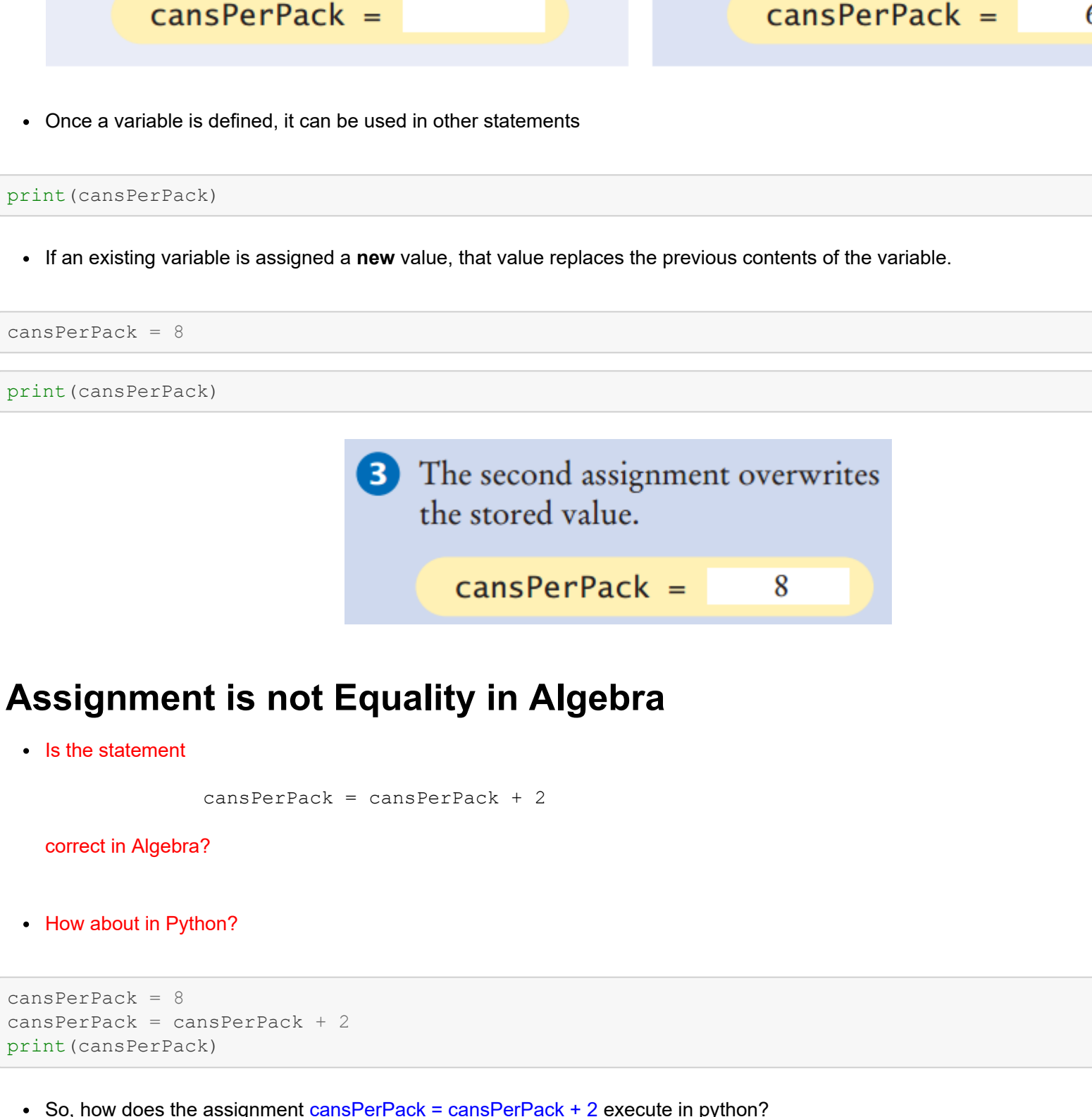
- To carry out computation, we need to store values in order to use them later on.
- These values are stored in variables.
- Let us try to comprehend the use of variables by solving the following problem:

Soft Drinks: Which is more Economic?

- Soft drinks are sold in cans and bottles.
- A store offers a six-pack of 12-ounce cans for the same price as a two-liter bottle.
- Find the volume (in liters) of a six-pack of soda cans and the total volume of a six-pack and a two-liter bottle.
 - Note that 12 fluid ounces equal approximately 0.355 liters.

Defining Variables

- A variable is a storage location in a computer program.
- Each variable has a name and holds a value.



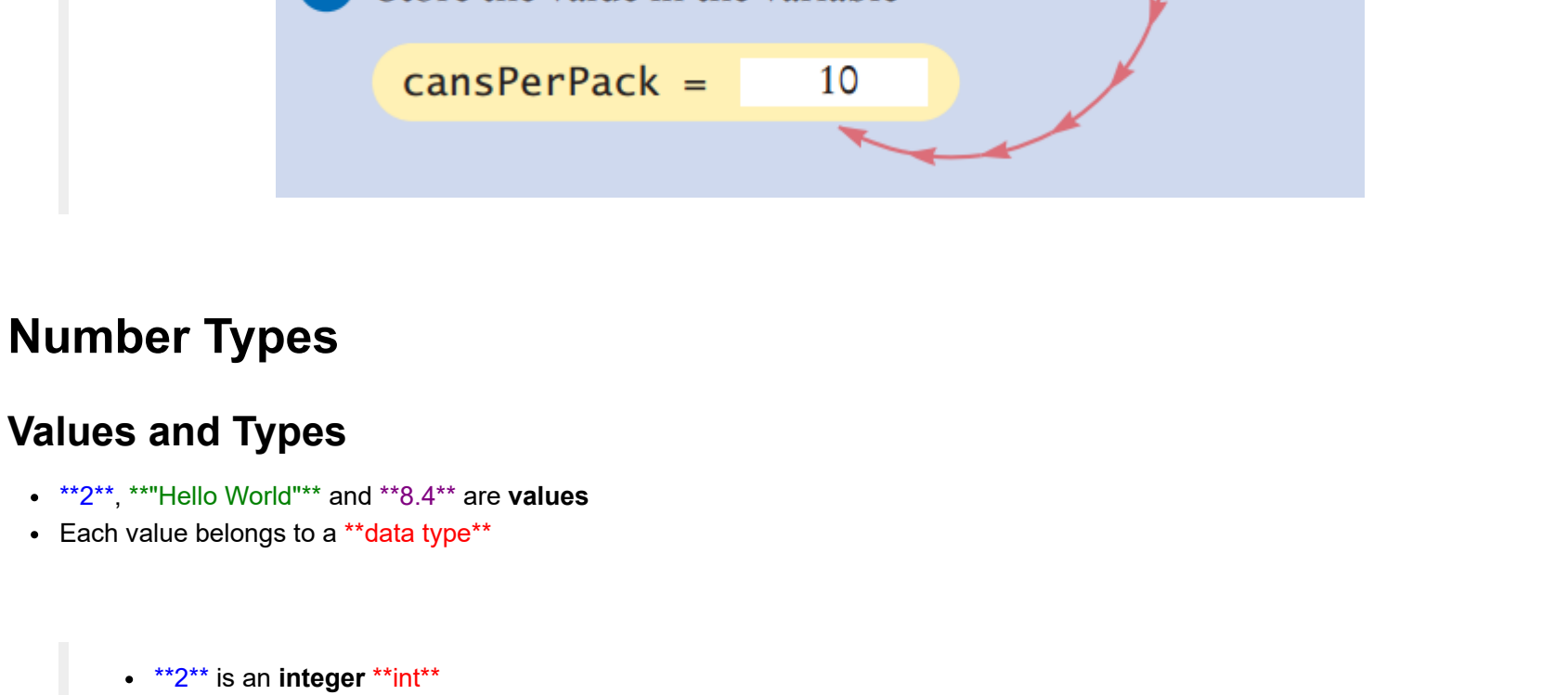
- Just as a parking space has an identifier **J053** and contents **car**

Assignment Statements

- An **assignment** statement is used to place a value into a variable

```
In [ ]: cansPerPack = 6
```

- How does the assignment statement work?
 - The right hand side of the = sign is first evaluated (to the value 6).
 - The value is assigned to the variable on the left hand side of the = sign (to the variable **cansPerPack**).



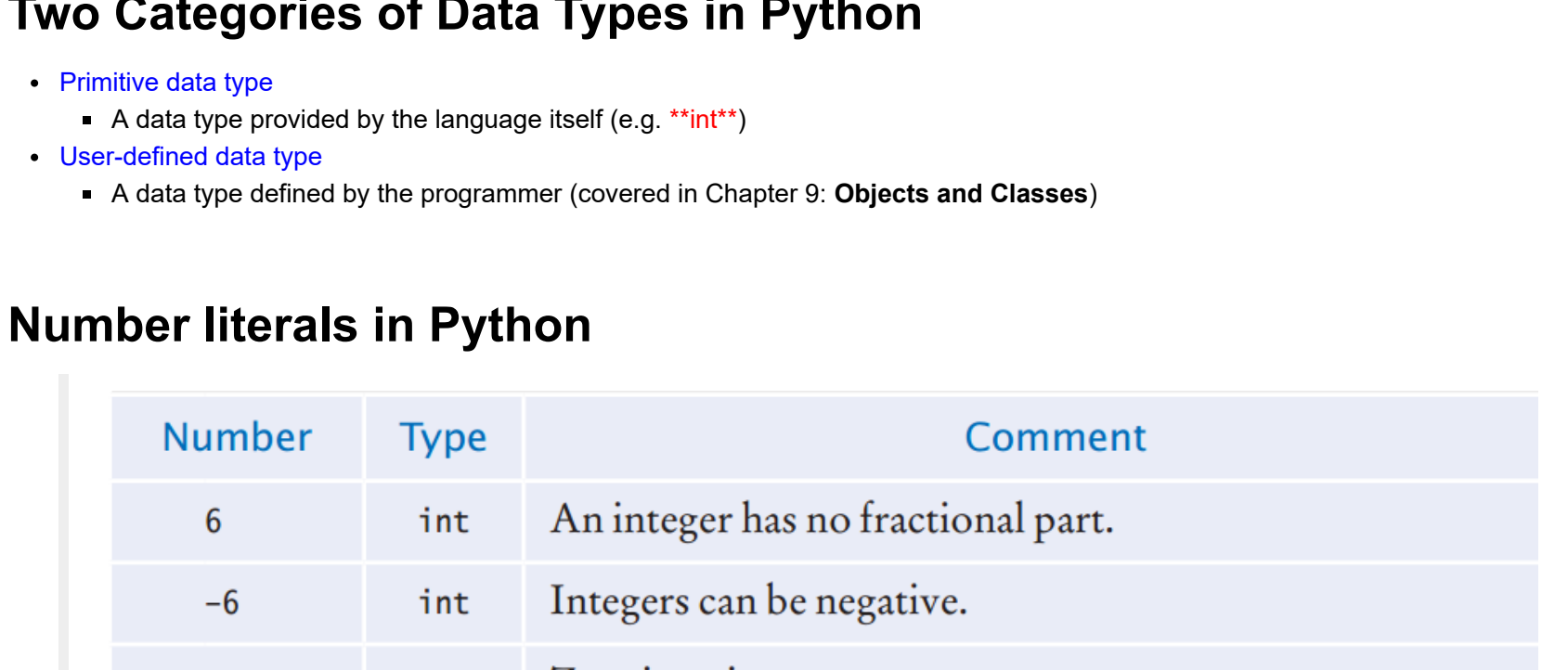
- Once a variable is defined, it can be used in other statements

```
In [ ]: print(cansPerPack)
```

- If an existing variable is assigned a **new** value, that value replaces the previous contents of the variable.

```
In [ ]: cansPerPack = 8
```

```
In [ ]: print(cansPerPack)
```



Assignment is not Equality in Algebra

- Is the statement

```
cansPerPack = cansPerPack + 2
```

correct in Algebra?

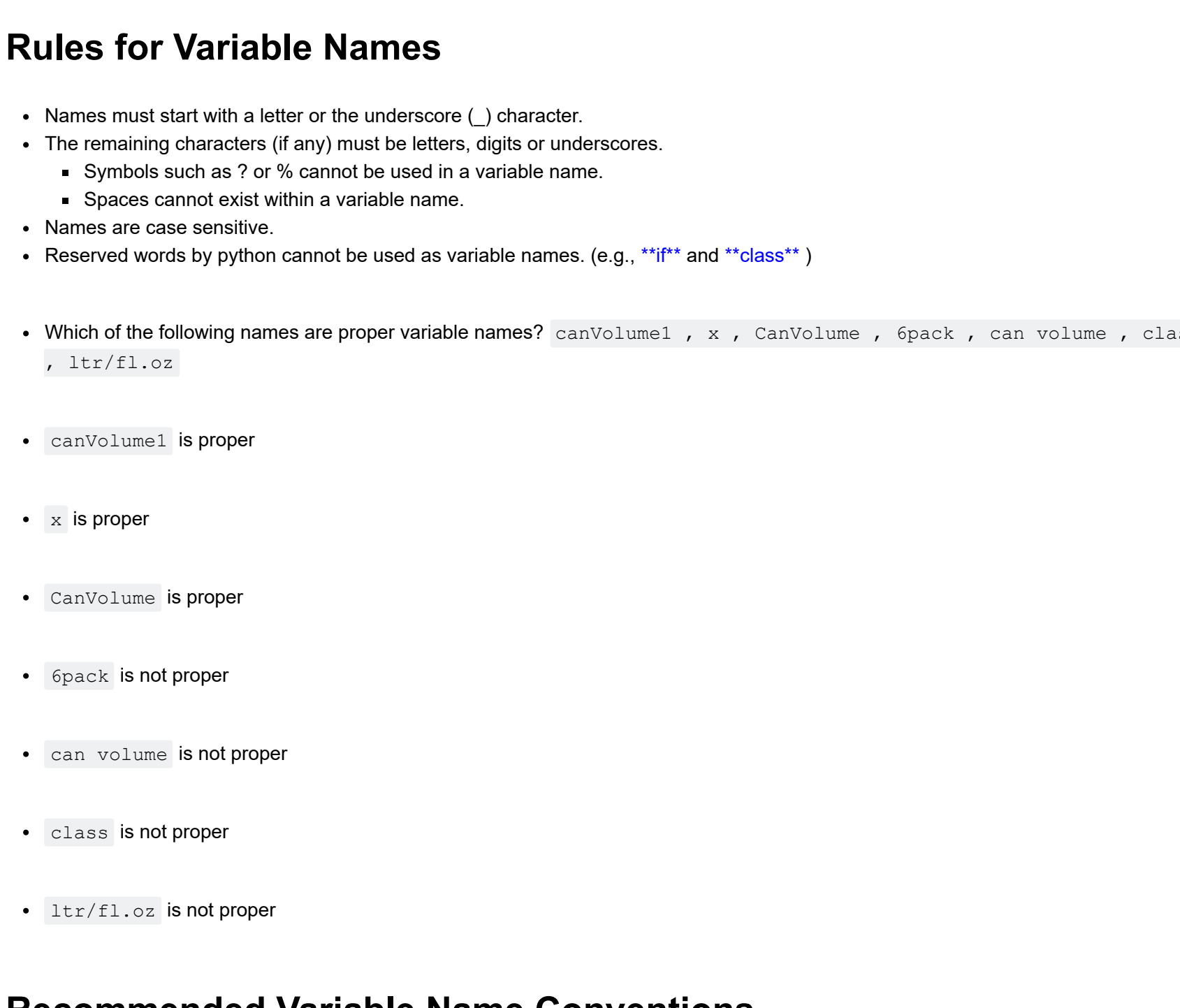
- How about in Python?

```
In [ ]: cansPerPack = 8
cansPerPack = cansPerPack + 2
print(cansPerPack)
```

- So, how does the assignment **cansPerPack = cansPerPack + 2** execute in python?

- First, the right hand side is executed
 - This is done by fetching the current value of the variable **cansPerPack**
 - Then, carrying out the addition

- Second, the value of the addition is stored in the variable **cansPerPack**



Number Types

Values and Types

- "2*", "Hello World" and "8.4" are **values**
- Each value belongs to a **"data type"**

- "2*" is an **integer** **"int"**
- "Hello World" is a **string** **"str"**
- "8.4" is a **float** **"float"**
- "2" and "8.4" are called **number literals**.

Why Data Types?

- A **data type** of a value determines

- how the data type is represented in the computer, and
- what operations can be performed on that data.

Two Categories of Data Types in Python

- Primitive data type**
 - A data type provided by the language itself (e.g. **"int"**)
- User-defined data type**
 - A data type defined by the programmer (covered in Chapter 9: **Objects and Classes**)

Number literals in Python

Number	Type	Comment
6	int	An integer has no fractional part.
-6	int	Integers can be negative.
0	int	Zero is an integer.
0.5	float	A number with a fractional part has type float.
1.0	float	An integer with a fractional part .0 has type float.
1E6	float	A number in exponential notation: 1×10^6 or 1000000. Numbers in exponential notation always have type float.
2.96E-2	float	Negative exponent: $2.96 \times 10^{-2} = 2.96 / 100 = 0.0296$
100,000		Error: Do not use a comma as a decimal separator.
3 1/2		Error: Do not use fractions; use decimal notation: 3.5.

- The value determines the type of the variable.
- For example, the following piece of code is correct, but not recommended

```
In [ ]: taxRate = 5
print(taxRate)
taxRate = 5.5
print(taxRate)
taxRate = "five point five"
print(taxRate)
```

- This is not a good idea, as it may lead to an error if you use the wrong operation on the variable

```
In [ ]: taxRate = taxRate + 10
```

- Once a variable is initialized with a value of a type, keep storing values of the same type.

Rules for Variable Names

- Names must start with a letter or the underscore (**_**) character.
- The remaining characters (if any) must be letters, digits or underscores.
- Symbols such as % or % cannot be used in a variable name.
- Spaces cannot exist within a variable name.
- Names are case sensitive.
- Reserved words by python cannot be used as variable names. (e.g., **"if"** and **"class"**)

- Which of the following names are proper variable names? `canVolume1` , `x` , `CanVolume` , `6pack` , `can volume` , `class` , `ltr/fl.oz`

- `canVolume1` is proper

- `x` is proper

- `CanVolume` is proper

- `6pack` is not proper

- `can volume` is not proper

- `class` is not proper

- `ltr/fl.oz` is not proper

Recommended Variable Name Conventions

- These are not strict rules for variable names, but are **rules of good taste** that you should respect when writing code.
 - Use a descriptive name, such as **cansPerPack**, than a terse name, such as **cpp**
 - If the variable name consists of more than one word, start the word with a capital letter, as shown above.
 - A variable starts with a small letter
 - A constant consists of all capital letters, where words are separated by the underscore **_** character, such as **CAN_VOLUME**
 - A user defined data type starts with a capital letter (as we will see later), such as **GraphicsWindow**.

Therefore,

Variable Name	Comment
<code>canVolume1</code>	Variable names consist of letters, numbers, and the underscore character.
<code>x</code>	In mathematics, you use short variable names such as <code>x</code> or <code>y</code> . This is legal in Python, but not very common, because it can make programs harder to understand (see Programming Tip 2.1 on page 34).
<code>CanVolume</code>	Caution: Variable names are case sensitive. This variable name is different from <code>canVolume</code> , and it violates the convention that variable names should start with a lowercase letter.
<code>6pack</code>	Error: Variable names cannot start with a number.
<code>can volume</code>	Error: Variable names cannot contain spaces.
<code>class</code>	Error: You cannot use a reserved word as a variable name.
<code>ltr/fl.oz</code>	Error: You cannot use symbols such as <code>.</code> or <code>/</code> .

Constants

- A constant variable, or simply a **constant**, is a variable whose value should not be changed after it has been assigned an initial value.
- Some languages provide an explicit mechanism of declaring constants.
 - Hence, any attempt to change it after it has been assigned generates a syntax error.
- Python leaves it to the programmer to make sure that constants are not changed.
 - Hence, the use of all capital letters for naming constants tells you and other programmers that you should not change the value of this **variable** once it is assigned.

- Constants can make your code much more understandable.

- For example, compare the following two statements:
 - `totalVolume = bottles * 2`
 - `totalVolume = bottles * BOTTLE_VOLUME`
- Note that in the case where the bottle volume is changed from 2 to 2.5, then
 - in the first case, you need to change every line of code that has volume 2 to 2.5.
 - in the second case, all you need to do is change the value of the constant **BOTTLE_VOLUME** to 2.5 in one line ONLY. Every other occurrence of **BOTTLE_VOLUME** in the code will automatically have the new volume value.

Comments

- As your programs get more complex, you should add **comments**, *explanations for human readers of your code*.

```
In [ ]: CAN_VOLUME = 0.355 # liters in a 12-ounce can
```

- This comment explains the significance of the value 0.355 to a human reader.

- Python's interpreter does not execute comments at all.
 - It ignores everything from a **#** delimiter to the end of the line.

Why Write Comments?

- Helps programmers who read your code understand your intent.

- Helps you when you review your code (after some time).

How to Write Comments?

- Provide a comment at the top of your source file that explains the purpose of the program.

- The textbook follows the following style:

```
In [ ]: ##
# This program computes the volume (in liters) of a six-pack of soda cans.
#
```

Time to Solve the Problem at the Beginning of this Chapter

Soft Drinks: Which is more Economic?

- Soft drinks are sold in cans and bottles.
- A store offers a six-pack of 12-ounce cans for the same price as a two-liter bottle.
- Which one should you buy?

Solution Steps

- Compute the **totalVolume** you get when you buy a six-pack
 - Define **CAN_VOLUME** and the number of **cansPerPack**
 - `totalVolume = cansPerPack * CAN_VOLUME`
 - print the **totalVolume**

- Now you can compare the **totalVolume** to the value **2.0** and determine which one to buy

```
In [ ]: ##
# This program computes the volume (in liters) of a six-pack of soda
# cans and the total volume of a six-pack and a two-liter bottle.
#
# liters in a 12-ounce can and a two-liter bottle.
CAN_VOLUME = 0.355
BOTTLE_VOLUME = 2
#
# Number of cans per pack.
cansPerPack = 6
#
# Calculate total volume in the cans.
totalVolume = cansPerPack * CAN_VOLUME
print("A six-pack of 12-ounce cans contains", totalVolume, "liters.")
#
# Calculate total volume in the cans and a two-liter bottle.
totalVolume = totalVolume + BOTTLE_VOLUME
print("A six-pack and a two-liter bottle contain", totalVolume, "liters.")
```

Final Tips on Variables

- Do not use undefined variables
 - `canVolume = 12 * literPerOunce # Error`
 - `literPerOunce = 0.0296`
- Choose descriptive variable names
 - canVolume** is better than **cv**

- Do not use **magic numbers**
 - `totalVolume = cansPerPack * 0.355`

2.2 Arithmetic

Basic Arithmetic Operations

- Python supports addition **+**, subtraction **-**, multiplication ***** and division **/**
- +**, **-**, ***** **/** are called **operators**
- The combination of variables, literals, operators, and parentheses is called an arithmetic **expression**
 - For example, the mathematical formula $\frac{a+b}{2}$ is written in python as `(a + b) / 2`
 - Note that the parentheses are used to determine in which order the parts of the expression are computed.
 - For example, which mathematical formula is `a + b / 2`?
- Python uses the exponential operator ****** to denote the power operation.
 - For example, a^2 is `a ** 2`

Precedence of Arithmetic Operators

- Python uses the precedence rules for algebraic notation

Precedence	Operator(s)	Description
1	()	Parentheses
2	*, *	Power
3	*, /	Multiplication and Division
4	+, -	Addition and Subtraction

Order of Evaluation of Arithmetic Operators

- Addition, subtraction, multiplication and division are left associative, i.e. they are evaluated from left to right.
 - For example, `10 + 2 + 3` is evaluated as `(10 + 2) + 3 = 15`
 - Note that when two operators of the same precedence follow each other, they are also evaluated from left to right.
- The power operation is right associative, i.e. it is evaluated from right to left.
 - For example, `10 ** 2 ** 3` is evaluated as `10** (2**3)` which is the same as `10** 8 = 100000000`

Example

- Consider the mathematical expression

```
b * (1 + r / 100) ** n
```

- It is evaluated as follows

- The expression between the parentheses is first considered, viz., `(1 + r / 100)`.

- Since division is higher than addition, division is evaluated: $\frac{r}{100}$.

- Now, addition is evaluated and hence we get the expression: `1 + $\frac{r}{100}$`

- Since we have multiplication and exponentiation, we carry out the exponentiation and the result becomes `(1 + $\frac{r}{100}$)n`

- Finally, we carry out the multiplication to get the Mathematical Expression: `b * (1 + $\frac{r}{100}$)n`

Floor Division and Remainder

- Division of two integers results in a floating-point value
 - `7 // 4` yields `1.75`
- The floor division operator `//` when applied on positive integers computes the quotient and discards the fractional part.
 - `7 // 4` yields `1`
- The **modulus** operator `%` can be used to get the remainder of the floor division.
 - `7 % 4` yields `3`, the remainder of the floor division of 7 by 4.
 - Some also call it **modulo** or **mod**

Floor Division and Remainder

Expression (where n = 1729)	Value	Comment
<code>n % 10</code>	9	For any positive integer n, <code>n % 10</code> is the last digit of n.
<code>n // 10</code>	172	This is n without the last digit.
<code>n % 100</code>	29	The last two digits of n.
<code>n % 2</code>	1	<code>n % 2</code> is 0 if n is even, 1 if n is odd (provided n is not negative)
<code>-n // 10</code>	-173	-173 is the largest integer ≤ -172.9 . We will not use floor division for negative numbers in this book.

Calling Functions

- We have been using the `print` function to display information, but there are many other functions available in Python.
- Most functions **return** a value.
 - i.e., when the function completes its task, it passes a value back to the point where the function was called.
 - For example, the call `abs(-123)` returns the value 123.
- The value returned by a function can be stored in a variable.
 - `distance = abs(x)`
 - Note that `x` is called the **argument** of the `abs` function.
- It can also be used anywhere that a value of the same type can be used
 - `print("The distance from the origin is ", abs(x))`

Arguments of a Function

- When calling a function, you must provide the correct number of arguments.
 - `abs(-10, 2)` or `abs()` will generate an error.
 - Hence, the `abs` function requires exactly one argument.

```
In [ ]: abs(-10)
```

- Some functions have optional arguments that you only provide in certain situations
- Consider the `round` function:
 - With one argument `r`, it returns the nearest integer to `r`.
 - For example, `round(7.624)` returns ???
 - With two arguments `r` and `d`, it returns the nearest floating-point number to `r` with `d` decimal digits.
 - For example, `round(7.624,2)` returns ???

- Note regarding the `round` function:
 - In many other languages and calculators, `round(2.5)` returns 3. Not in Python.
 - Python uses a *different* way of computing the `round` function when it comes to 5, which is called **round half to even**.
 - This means that if we are to round `x.5`, we round to the closest even integer (whether it is `x` or `x + 1`).
 - For example, `round(24.5)` will round down to 24 [even], whereas `round(25.5)` will round up to 26.

```
In [ ]: print(round(7.624))
print(round(2.5))
print(round(2.501))
print(round(3.5))
print(round(7.624,2))
print(round(7.625,2))
print(round(7.645,2))
print(round(7.655,2))
```

- Some functions take an arbitrary number of arguments
 - For example, the `max` and `min` functions.
 - `min(7.25, 10.95, 5.95, 6.05, 8)` returns the minimum of the function's arguments; in this case the number 5.95

```
In [ ]: min(7.25, 10.95, 5.95, 6.05, 8)
```

Calling Functions

Libraries

- A **library** is a collection of code that has been written and translated by someone else, ready for you to use in your program.
 - A **standard library** is a library that is considered part of the language and must be included with any Python system.
- Python's standard library is organized into modules.
 - Related functions and data types are grouped into the same module.

Mathematical Functions

- Python's **math** module includes a number of mathematical functions.
- You must **import** it before you can use any of its functions
 - Note that `sin` is called the **argument** of the `abs` function.
- It can also be used anywhere that a value of the same type can be used
 - `print("The distance from the origin is ", abs(x))`

```
In [ ]: from math import sqrt
x = sqrt(25)
print("y = ", y)
```

Function	Returns
<code>sqrt(x)</code>	The square root of <code>x</code> . ($x \geq 0$)
<code>trunc(x)</code>	Truncates floating-point value <code>x</code> to an integer.
<code>cos(x)</code>	The cosine of <code>x</code> in radians.
<code>sin(x)</code>	The sine of <code>x</code> in radians.
<code>tan(x)</code>	The tangent of <code>x</code> in radians.
<code>exp(x)</code>	e^x
<code>degrees(x)</code>	Convert <code>x</code> radians to degrees (i.e., returns <code>x * 180/π</code>)
<code>radians(x)</code>	Convert <code>x</code> degrees to radians (i.e., returns <code>x * π/180</code>)
<code>log(x)</code> <code>log(x, base)</code>	The natural logarithm of <code>x</code> (to base e) or the logarithm of <code>x</code> to the given <code>base</code> .

- To import more than one function from **math**, use `from math import *`

Arithmetic Expressions Examples

Mathematical Expression	Python Expression	Comments
$\frac{x+y}{2}$	<code>(x + y) / 2</code>	The parentheses are required; <code>x + y / 2</code> computes <code>x + $\frac{y}{2}$</code> .
$\frac{xy}{2}$	<code>x * y / 2</code>	Parentheses are not required; operators with the same precedence are evaluated left to right.
$\left(1 + \frac{r}{100}\right)^n$	<code>(1 + r / 100) ** n</code>	The parentheses are required.
$\sqrt{a^2 + b^2}$	<code>sqrt(a ** 2 + b ** 2)</code>	You must import the <code>sqrt</code> function from the <code>math</code> module.
π	<code>pi</code>	<code>pi</code> is a constant declared in the <code>math</code> module.

Student Activity

- The volume of a sphere is given by

$$V = \frac{4}{3}\pi r^3$$

- If the radius is given by a variable **radius** that contains a floating-point value, write a Python expression for the volume.

```
In [ ]: # Volume Expression
radius = 2.4
```

2.4 Strings

- A **string** is a sequence of characters
 - Characters** include letters, numbers/digits, punctuation, spaces, special symbols and so on.
- A **string literal** denotes a particular string (e.g. "Hello")
 - Just as a number literal (e.g. 34) denotes a particular number.
 - String literals are specified by enclosing a sequence of characters within a matching pair of either single or double quotes.

```
In [ ]: print("This is a string. ", 'So is this.')
```

- How can I form the strings **I'm a student** or **He said: "You did it!"**?

```
In [ ]: print("I'm a student", "He said: \"You did it!\"")
```

- The number of characters in a string is called the **length** of the string.
 - For example, "Harry" is of length 7 and "World" is of length 5
 - An **empty** string is a string with no characters. It is of length zero and is written as `""` or `''`
- Python's `len` function returns the length of the argument string.

```
In [ ]: length = len("World!")
print(length)
```