

Homework Assignment 7

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12/01/2023

Question 1 (Exercise 6.19 on Page 225):

a)

False. Because confidence interval only contains positive values.

b)

True.

c)

True.

d)

True.

e)

False. The confidence interval is already calculated and provided in the context.

Question 2 (Exercise 6.20 on Page 226):

a)

False. The significance level of 0.05 is not met with the p-value of 1, so there is no convincing evidence to reject the null hypothesis.

b)

False. The confidence interval is between -0.16 and 0.02, so this does not mean it is 16% more to 2% fewer.

c)

False. Because the 90% confidence interval is narrower than 95% confidence interval.

d)

True.

Question 3 (Exercise 6.22 on Page 226):

$n1 = 11545$ $n2 = 4691$ $\text{phat1} = 0.08$ $\text{phat2} = 0.088$ significance level = $1 - 0.95 = 0.05$ $Z = 1.96$ $CI = (0.08 - 0.088) \pm 1.96 * \sqrt{(0.08 * (1 - 0.08) / 11545 + 0.088 * (1 - 0.088) / 4691)} = (-0.0175, 0.0015)$

A 95% confidence interval for the difference between the proportions of Californians and Oregonians who are sleep deprived is $(-0.0175, 0.0015)$. We are 95% confident that the difference between the proportions of Californians and Oregonians who are sleep deprived is between 0.0015 and 0.0175.

Question 4 (Exercise 6.24 on Page 226):

a)

$n1 = 11545$ $n2 = 4691$ $\text{phat1} = 0.08$ $\text{phat2} = 0.088$ $H_0: \text{phat1} - \text{phat2} = 0$ $H_A: \text{phat1} - \text{phat2}$ is not equal to 0

check conditions:

$n1 * \text{phat1} = 11545 * 0.08 = 923.6$ $n1 (1 - \text{phat1}) = 11545 * (1 - 0.08) = 10621.4$ $n2 * \text{phat2} = 4691 * 0.088 = 412.808$ $n2 (1 - \text{phat2}) = 4691 * (1 - 0.088) = 4278.19$

Since above are all greater than 10, $\text{phat1} - \text{phat2}$ is approximately normal and we can use large sample hypothesis test.

$p = (n1 * \text{phat1} + n2 * \text{phat2}) / (n1 + n2) = (923.6 + 412.808) / (11545 + 4691) = 0.0823$ $z = (0.08 - 0.088) / \sqrt{0.0823 * (1 - 0.0823) * (1/11545 + 1/4691)} = -1.68$ $p_value = 2 * P(Z \leq -1.96) = 2 * 0.0465 = 0.093$ $p_value > 0.05$, fail to reject null hypothesis

There is no sufficient evidence to conclude that the rate of sleep deprivation is different for the two states.

b)

Type II error.

Question 5 (Exercise 6.27 Page 227):

$x1 = 35$ $n1 = 292$ $\text{phat1} = x1 / n1 = 35 / 292 = 0.1199$ $x2 = 35$ $n2 = 203$ $\text{phat2} = x2 / n2 = 35 / 203 = 0.1724$ $H_0: \text{phat1} - \text{phat2} = 0$ $H_A: \text{phat1} - \text{phat2}$ is not equal to 0 $p = (x1 + x2) / (n1 + n2) = (35 + 35) / (292 + 203) = 0.1414$ $z = (0.1199 - 0.1724) / \sqrt{0.1414 * (1 - 0.1414) * (1/292 + 1/203)} = -1.65$ $p_value = 0.992$ $p_value > 0.05$, fail to reject null hypothesis

There is no sufficient evidence to conclude that there is a difference between the proportions of truck drivers and non-transportation workers.

Question 6 (Exercise 6.28 on Page 228):

a)

HO: pvitamin = pnovitamin HA: pvitamin is not equal to pnovitamin

b)

$x_1 = 143$ $n_1 = 254$ $p_{\text{vitamin}} = 143/254 = 0.563$ $x_2 = 159$ $n_2 = 229$ $p_{\text{novitamin}} = 159/229 = 0.694$ $z = (0.563 - 0.694) / \sqrt{0.563 * (1 - 0.563) / 254 + 0.694 * (1 - 0.694) / 229} = -2.9774$ $p_value = 0.0029$ $p_value < 0.05$, reject the null hypothesis

There is sufficient evidence to conclude that there is a difference in the proportion of the use of prenatal vitamins during the three months before pregnancy and autism.

c)

It is a appropriate title since vitamins might help to prevent autism statistically.

Alternative title: Prenatal vitamins could help to prevent autism.

Question 7 (Exercise 6.29 on Page 228):

a)

```
results <- matrix(c(26,94,120,10,110,120,36,204,240),ncol=3,byrow=TRUE)
colnames(results) <- c("Yes","No","Total")
rownames(results) <- c("Nevaripine","Lopinavir","Total")
results <- as.table(results)
results
```

```
##           Yes  No Total
## Nevaripine  26  94   120
## Lopinavir   10 110   120
## Total       36 204   240
```

b)

HO: $p_1 = p_2$ HA: p_1 is not equal to p_2

c)

```
# Data
failures <- c(26, 10)
total <- c(120, 120)

# Proportions
prop_failures <- failures / total
```

```

# Two-sample z-test for proportions
test_result <- prop.test(failures, total, alternative = "two.sided")

# Print the test result
print(test_result)

##
## 2-sample test for equality of proportions with continuity correction
##
## data:  failures out of total
## X-squared = 7.3529, df = 1, p-value = 0.006695
## alternative hypothesis: two.sided
## 95 percent confidence interval:
##  0.03623882 0.23042785
## sample estimates:
##      prop 1      prop 2
## 0.21666667 0.08333333

```

p_value < 0.05, reject null hypothesis

There is sufficient evidence to conclude that there is difference in virologic failure rates between treatment groups.