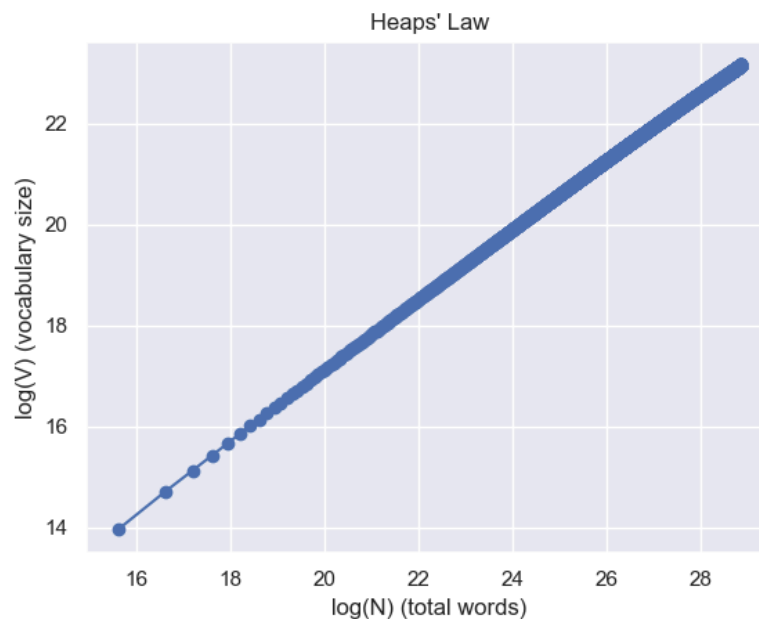
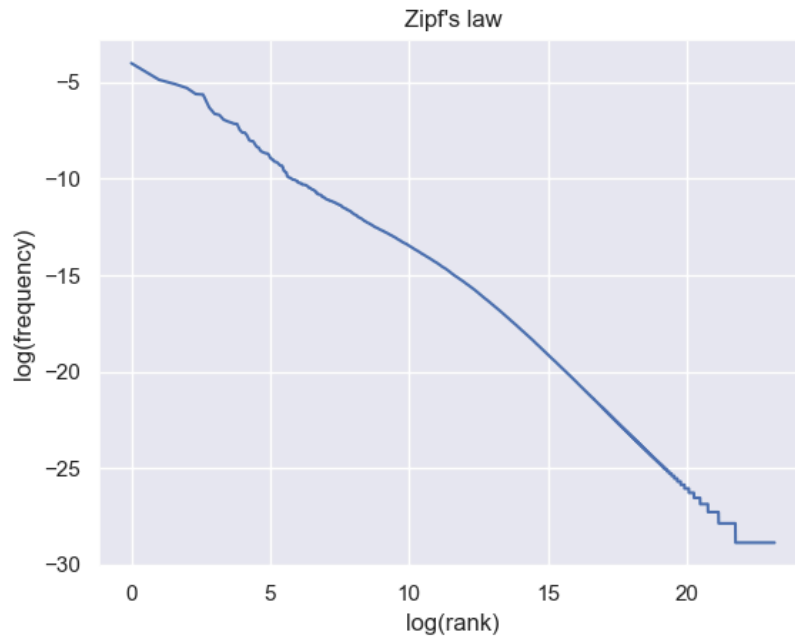


Assignment #1

Task #1: testing the Heaps' law in natural language



We checked whether our plot matches Heaps' law. According to the lecture, Heaps' law says $V = k \cdot (N^B)$ with typical values $0.67 < B < 0.75$ and $10 < k < 100$ for natural language.

:If we take logarithms on both sides we get

$$\log V = \log K + B \log N$$

.which is a straight line in log-log space, with slope B and intercept logK

In our plot of $\log V$ vs. $\log N$ we see an approximately straight, increasing line, which is exactly the pattern expected from this linear form. We did not estimate precise numeric values for K and B , but the overall shape and behavior of the curve are consistent with the ranges given in class, so we conclude that our results are in line with Heaps' law

Task #2: statistical language models – solving a cloze

Chance Accuracy:

I estimated that when sampling a large amount of solutions, the mean accuracy will be around $1/n$ (where n is the number of candidates per blank). And that was the reality, as the mean accuracy from 1000 random solutions was 8.2% and then the number of candidates in our example was 12 (and $1/12$ is around 8.3%). Thus, With multiple candidates per blank, random selection performs poorly.

```
solving this cloze randomly over 1000 solutions would give an accuracy of: 8.20%
```

Comparison with My Solution:

My n-gram-based solution achieved 100% accuracy, a large improvement over chance. This shows that:

- The n-gram model captures meaningful linguistic patterns
- The scoring mechanism effectively distinguishes correct candidates
- The approach is far better than random selection

```
cloze solved with accuracy: 100.00%  
elapsed time: 181.91 seconds  
cloze solution: ['notation', 'system', 'remote', 'open', 'technologies', 'faster', 'commonly', 'browsers', 'displayed', 'people', 'half', 'methods']
```

Technical Details of My Solution:

- N-gram models up to 5-grams (bigrams through 5-grams)
- Laplace smoothing (add-k) to handle unseen n-grams
- Log probabilities for numerical stability
- Weighted combination favoring higher-order n-grams
- The difference (100% vs 8.2%) indicates the model uses contextual information rather than guessing. The low chance accuracy (8.2%) confirms the task is non-trivial and that the model's performance is meaningful.