

## Report Section: UT Network

### a) Minimum Cost to Connect to UT (Dijkstra)

1. **Function findMinimumStudentCost (start, dest):**
  - a. **For each student  $s$  in students:**
    - i.  $S.minCost = \text{infinity}$
  - b.  $Start.minCost = 0$
  - c.  $H = \text{buildHeap}(\text{students})$
  - d. **While  $H$  is not empty:**
    - i. **If  $current == dest$ :**
      1. **Return  $current.minCost$**
    - ii. **For each neighbor  $v$  of  $current$  with edge cost  $c$ :**
      1. **If  $current.minCost + c < v.minCost$ :**
        - a.  $V.minCost = current.minCost + c$
        - b.  $\text{changeKey}(H, v, v.minCost)$
  - e. **return -1 since destination is unreachable**

**RunTime:  $V = \text{students}$   $E = \text{wires}$   $O((V+E) \log V)$**

### b) Minimum Cost to Connect Entire Class to UT (Prim's)

2. **Function findMinimumClassCost():**
  - a. **For each student  $s$  in students:**
    - i.  $S.minCost = \text{infinity}$
  - b.  $start = UT$  looking for the last student in the list
  - c.  $start.minCost = 0$
  - d.  $visited = \text{array}[v]$  initialized to false
  - e.  $totalcost = 0$
  - f.  $heap = \text{buildHeap}(\text{students})$
  - g.  $visitedCount = 0$
  - h. **while  $heap$  is not empty:**
    - i.  $current = \text{extractMin}(heap)$
    - ii. **if  $visited[current.name]$ : continue**
    - iii.  $visited[current.name] = \text{true}$
    - iv.  $visitedCount += 1$
    - v.  $total\ Cost += current.minCost$
    - vi. **for each neighbor  $v$  of  $current$  with edge cost  $c$ :**
      1. **if not  $visited[v.name]$  and  $c < v.minCost$ :**
        - a.  $v.minCost = c$
        - b.  $\text{changeKey}(heap, v, c)$
  - i. **if  $visitedCount < v$ :**
    - i. **return -1 disconnected graph**
  - j. **return total cost**

**RunTime:  $V = \text{students}$   $E = \text{wires}$   $O((V+E) \log V)$**

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## Programming Assignment #2

### c) Notes on Heap Usage

1. **buildHeap =  $O(V)$**
  2. **extractMin =  $O(\log V)$**
  3. **changeKey =  $O(\log V)$**
- **Dijkstra finds the minCost to connect to UT**
  - **Prim's MST finds the min total cost to connect the entire class**
  - **Both algorithms rely on a minheap to effectively select the next cheapest student. Tie breakers are done using the student ID in minCost is equal**
  - **Both run in  $O((V+E) \log V)$**