HW 7 Report

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Introduction

Social network, and many other types of networks, are dynamic over a period of time, where ERGMs are not suitable to apply. A network can change over time is called the dynamic network. For dynamic network, it can grow (more nodes) or shrink (less nodes), leading to network composition changes and the ties can also change among the network nodes. Social selection and influence are two crucial concepts of dynamic network. Social selection occurs when an actor (vertex) selects or forms a new social tie (edge) with another actor (vertex) who shares some similar or relevant characteristics. Social influence occurs when the behavior of one actor (vertex) is changed to become more similar (or dissimilar) to the behavior of one or more other actors (vertices). SIENA standing for Simulation Investigation for Empirical Network Analysis is special for modeling longitudinal network data which is a type of dynamic network data. Specifically, for longitudinal network data, the dataset has been collected for the same network at several time points and at each time point, there is a network dataset.

In an RSiena model, a network variable is the basic dependent variable with a behavior variable being another type of dependent variable which is a node characteristic that changes over time, a coCovar being a constant node attribute that does not change over time, and a varCovar, on the other hand, being an attribute that does change over time. For effects, "sameX" represents the hypothesis that the likelihood of forming a new tie is higher with a same X status; "egoX" represents the hypothesis that an actor is less/more likely to form a tie based on own X status; "altX" represents the hypothesis that an actor is less/more likely to form a tie based on others' X status; "avSim" represents the hypothesis that likelihood of changing behavior is related to the average similarity of all actors' behavior status; "totSim" represents the hypothesis that likelihood of changing behavior is related to the total similarity of all actors' behavior status; "recip" represents the hypothesis that the tendency for ties is related to the reciprocity and "transTrip" represents the hypothesis that the tendency for ties is related to the transitivity.

I Specify the model in slide #168

1. Create the RSiena variables

We load the four network datasets from Coevole data. Then we use function <code>as.matrix(get.adjacency())</code> to get the adjacency matrix of network. For example, for data 1, we use <code>fr_w1 <- Coevolve\$fr_w1</code> to load the data and use <code>fr_w1</code> to represent the first network data. And use the function <code>matw1 <- as.matrix(get.adjacency(fr_w1))</code> to get and save the adjacency matrix. The similar procedures will be applied to other 3 datasets. Then we use function <code>fr4wav<-sienaDependent(array(c(matw1, matw2, matw3, matw4), dim=c(37,37,4))</code>, <code>sparse=FALSE</code>) to create the time-varying dependent network variable. And use <code>gender <- coCovar(V(fr_w1)\$gender,centered = FALSE)</code> to create the time-stable covariate gender with the same vertex values of network <code>fr_w1</code> since the option center does not make sense here so we use <code>FALSE</code> here. Finally, the behavior variable is created by function <code>smokebeh <- sienaDependent(array(c(V(fr_w1)\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1)\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1)\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1)\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1)\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1)\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1))\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1))\$smoke,V(fr_w2)\$smoke, or sienaDependent(array(c(V(fr_w1))\$smoke,V(fr_w2)</code>

V(fr_w3)\$smoke,V(fr_w4)\$smoke),dim=c(37,4)), type = "behavior"). After all different types of objects are ready, we combine them into a single RSiena object by function friend <- sienaDataCreate(fr4wav, smokebeh, gender)

2. Create the effects of RSiena object

Then we use function frndeff <- getEffects (friend) to get the basic effects of the RSiena object. Then after comparing it with the result on slide #169, we find we need to add 7 more effects in the RSiena object. They are the transitivity effect, the "sameX" effect for gender, the "altX" effect for smoke behavior, the "egoX" for smoke behavior, the "sameX" effect for smoke behavior, "avSim" and "totSim" effects for smoke behavior. Then we use function includeEffects to realize the goal. And the codes are shown below:

```
frndeff <- includeEffects(frndeff, sameX, interaction1="gender", name="fr4wav")

frndeff <- includeEffects(frndeff, egoX, interaction1="smokebeh", name="fr4wav")

frndeff <- includeEffects(frndeff, altX, interaction1="smokebeh", name="fr4wav")

frndeff <- includeEffects(frndeff, sameX, interaction1="smokebeh", name="fr4wav")

frndeff <- includeEffects(frndeff, avSim, interaction1="fr4wav", name="smokebeh")

frndeff <- includeEffects(frndeff, totSim, interaction1="fr4wav", name="smokebe")

frndeff <- includeEffects(frndeff, transTrip, name="fr4wav")</pre>
```

Then we get the same effects with slide #169 as show below: frndeff

##		name	effectName	include	fix test
##	1	fr4wav	constant fr4wav rate (period 1	1) TRUE	FALSE FALSE
##	2	fr4wav	constant fr4wav rate (period 2	2) TRUE	FALSE FALSE
##	3	fr4wav	constant fr4wav rate (period 3	3) TRUE	FALSE FALSE
##	4	fr4wav	outdegree (density)	TRUE	FALSE FALSE
##	5	fr4wav	reciprocity	TRUE	FALSE FALSE
##	6	fr4wav	transitive triplets	TRUE	FALSE FALSE
##	7	fr4wav	same gender	TRUE	FALSE FALSE
##	8	fr4wav	smokebeh alter	TRUE	FALSE FALSE
##	9	fr4wav	smokebeh ego	TRUE	FALSE FALSE
##	10	fr4wav	same smokebeh	TRUE	FALSE FALSE
##	11	smokebeh	rate smokebeh (period 1)	TRUE	FALSE FALSE
##	12	smokebeh	rate smokebeh (period 2)	TRUE	FALSE FALSE
##	13	smokebeh	rate smokebeh (period 3)	TRUE	FALSE FALSE
##	14	smokebeh	smokebeh linear shape	TRUE	FALSE FALSE
##	15	smokebeh	smokebeh average similarity	TRUE	FALSE FALSE
##	16	smokebeh	smokebeh total similarity	TRUE	FALSE FALSE

However, to get the model in slide #168 we still need to add the "altX" and "egoX" effects for gender:

```
frndeff <- includeEffects(frndeff,egoXinteraction1="gender",name="fr4wav")
frndeff <- includeEffects(frndeff,altX,interaction1="gender",name="fr4wa")</pre>
```

Then we get the same effects with slide #168 as show below:

##		name	effectName	include	fix t	est
##	1	fr4wav	constant fr4wav rate (period	1) TRUE	FALSE	FALSE
##	2	fr4wav	constant fr4wav rate (period	2) TRUE	FALSE	FALSE
##	3	fr4wav	constant fr4wav rate (period	3) TRUE	FALSE	FALSE
##	4	fr4wav	outdegree (density)	TRUE	FALSE	FALSE
##	5	fr4wav	reciprocity	TRUE	FALSE	FALSE
##	6	fr4wav	transitive triplets	TRUE	FALSE	FALSE
##	7	fr4wav	gender alter	TRUE	FALSE	FALSE
##	8	fr4wav	gender ego	TRUE	FALSE	FALSE
##	9	fr4wav	same gender	TRUE	FALSE	FALSE
##	10	fr4wav	smokebeh alter	TRUE	FALSE	FALSE
##	11	fr4wav	smokebeh ego	TRUE	FALSE	FALSE
##	12	fr4wav	same smokebeh	TRUE	FALSE	FALSE
##	13	smokebeh	rate smokebeh (period 1)	TRUE	FALSE	FALSE
##	14	smokebeh	rate smokebeh (period 2)	TRUE	FALSE	FALSE
##	15	smokebeh	rate smokebeh (period 3)	TRUE	FALSE	FALSE
##	16	smokebeh	smokebeh linear shape	TRUE	FALSE	FALSE
##	17	smokebeh	smokebeh average similarity	TRUE	FALSE	FALSE
##	18	smokebeh	smokebeh total similarity	TRUE	FALSE	FALSE

II Re-run the model specified in slide #168

Then we use the function <code>sienaAlgorithmCreate(projname='coevol')</code> to create the algorithm and function <code>siena07</code> to estimate the model with RSiena object generated from data Coevolve, option returnDeps=TRUE, batch=TRUE, verbose=FALSE, useCluster=TRUE, initC=TRUE, nbrNodes=3 in siena07() and set.seed(999). The details are shown below:

```
myalgorithm <- sienaAlgorithmCreate(projname='coevol', seed=999)
RSmod1 <- siena07(myalgorithm,data = friend,effects = frndeff,batch=TRUE,
verbose=FALSE,useCluster=TRUE,initC=TRUE,nbrNodes=3,returnDeps=TRUE)</pre>
```

The results are shown below:

Estimates, standard errors and convergence t-ratios

##		Estimate	Standard	Convergence
##			Error	t-ratio
## N	Network Dynamics			
##	1. rate constant fr4wav rate (period	1 1) 1.15	35 (0.6114)	0.0256
##	2. rate constant fr4wav rate (period	1 2) 1.15	10 (0.3725)	-0.0278
##	3. rate constant fr4wav rate (period	1 3) 1.15	06 (0.2138)	0.0874
##	eval outdegree (density)	-3.10	33 (1.8159)	0.0820
##	5. eval reciprocity	0.79	44 (0.4644)	0.0133
##	6. eval transitive trinlets	0.09	35 (0.0756)	0.0664

##	7. eval	gender alter	-0.3260 (1.1787)	0.0794
##	8. eval	gender ego	0.3087 (0.6028)	0.0596
##	9. eval	same gender	1.2623 (1.9439)	0.0872
##	10. eval	smokebeh alter	0.7076 (0.3769)	0.0010
##	11. eval	smokebeh ego	-0.0547 (0.4443)	0.0981
##	12. eval	same smokebeh	1.1636 (1.2834)	0.0223
## I	Behavior D	ynamics		
##	13. rate	rate smokebeh (period 1)	0.2961 (1.0825)	0.1017
##	14. rate	rate smokebeh (period 2)	0.3162 (0.6081)	0.0569
##	15. rate	rate smokebeh (period 3)	0.3147 (0.5767)	0.0985
##	16. eval	smokebeh linear shape	18.4840 (4300.5717)	0.1286
##	17. eval	smokebeh average similarity	138.7131 (18520.1485	5) -0.3288
##	18. eval	smokebeh total similarity	-17.2877 (2056.9832)	-0.1838

III Use the first set of simulated data to construct models

1. Transform the simulated data

We can get the first simulated data from the previous model by RSmod1\$sims[[1]][[1]] [[1]] [[1]] [[1]]. In the simulated data, there is only information of the network after each period. Since the simulated data is not in the network form, we still need to transform the simulated data into network form. Then we use the function el2sim <- RSmod1\$sims[[1]][[1]][[1]] [[1]] [[1]] to get the information of edgelist and sb2sim <- RSmod1\$sims[[1]][[1]][[1]][[1]] to get the information of smoke behavior. Then use the function fr_w2_sim <- graph.data. frame(el2,directed = TRUE) to create the graph and V(fr_w2_sim)\$smoke <- sb2sim as well asV(fr_w2_sim)\$gender <- V(fr_w2)\$gender to set the values of smoke and gender vertex attributes. It is the same procedure for the network information after period 2 and 3 respectively. Then we can get fr_w2_sim, fr_w3_sim and fr_w4_sim three simulated network datasets.

2. Create the RSiena variables from simulated data

We load the one original and three simulated network datasets from Coevole data. Then we use function as.matrix(get.adjacency()) to get the adjacency matrix of network. For example, for data 1, we use fr_w1 <- Coevolve\$fr_w1 to load the data and use fr w1 to represent first network data. And the function the use matw1 as.matrix(get.adjacency(fr_w1)) to get and save the adjacency matrix. The similar procedures will be applied to other 3 datasets. Then we use function fr4wav sim<sienaDependent(array(c(matw1,matw2_sim,matw3_sim,matw4_sim),dim=c(37,37,4), sparse=FALSE) to create the time-varying dependent network variable. And use gender sim <- coCovar(V(fr_w1)\$gender,centered = FALSE) to create the time-stable covariate gender with the same vertex values of network fr w1 since the option center does not make sense here so we use FALSE here, to create the time-stable covariate gender with the same vertex values of network fr w1. Finally, the behavior variable is created by function smokebeh sim <- sienaDependent(array(c(V(fr w1)\$smoke,V(fr w2 sim)\$smoke,</pre> $V(fr_w3_sim)$ \$smoke, $V(fr_w4_sim)$ \$smoke),dim=c(37,4)), type = "behavior"). After all different types of objects are ready, we combine them into a single RSiena object by function friend sim <- sienaDataCreate(fr4wav sim, smokebeh sim, gender sim).</pre>

3. Create the effects of model 1 for RSiena object with simulated data

Then we use function frndeff_sim <- getEffects(friend_sim) to get the basic effects of the RSiena object. Then after comparing it with the result on slide #168, we find we need to add 9 more effects in the RSiena object. They are the transitivity effect, the "sameX" effect for gender_sim, the "altX" effect for simulated smoke behavior and gender_sim, the "egoX" for simulated smoke behavior and gender_sim, the "sameX" effect for simulated smoke behavior, "avSim" and "totSim" effects for simulated smoke behavior. Then we use function includeEffects to realize the goal. And the codes are shown below:

```
frndeff_sim <- includeEffects(frndeff_sim,sameX,interaction1="gender_sim",name="fr4wav_sim")
frndeff_sim <- includeEffects(frndeff_sim,egoX,interaction1="smokebeh_sim",name="fr4wav_sim")
frndeff_sim <- includeEffects(frndeff_sim,altX,interaction1="smokebeh_sim",name="fr4wav_sim")
frndeff_sim <- includeEffects(frndeff_sim,sameX,interaction1="smokebeh_sim",name="fr4wav_sim")
frndeff_sim <- includeEffects(frndeff_sim,avSim,interaction1="fr4wav_sim",name="smokebeh_sim")
frndeff_sim <- includeEffects(frndeff_sim,totSim,interaction1="fr4wav_si",name="smokebeh_sim")
frndeff_sim <- includeEffects(frndeff_sim, transTrip,name="fr4wav_s")
frndeff_sim <- includeEffects(frndeff_sim,egoX,interaction1="gender_sim",name="fr4wav_sim")
frndeff_sim <- includeEffects(frndeff_sim,altX,interaction1="gender_sim",name="fr4wav_sim")</pre>
```

Then we get the effects of model 1 for simulated data as show below:

##		name	effectName	include fi	x test
##	1	fr4wav_sim	<pre>constant fr4wav_sim rate (period</pre>	1) TRUE	FALSE FALSE
##	2	fr4wav_sim	<pre>constant fr4wav_sim rate (period</pre>	2) TRUE	FALSE FALSE
##	3	fr4wav_sim	<pre>constant fr4wav_sim rate (period</pre>	3) TRUE	FALSE FALSE
##	4	fr4wav_sim	outdegree (density)	TRUE	FALSE FALSE
##	5	fr4wav_sim	reciprocity	TRUE	FALSE FALSE
##	6	fr4wav_sim	transitive triplets	TRUE	FALSE FALSE
##	7	fr4wav_sim	<pre>gender_sim alter</pre>	TRUE	FALSE FALSE
##	8	fr4wav_sim	gender_sim ego	TRUE	FALSE FALSE
##	9	fr4wav_sim	same gender_sim	TRUE	FALSE FALSE
##	10	fr4wav_sim	smokebeh_sim alter	TRUE	FALSE FALSE
##	11	fr4wav_sim	smokebeh_sim ego	TRUE	FALSE FALSE
##	12	fr4wav_sim	same smokebeh_sim	TRUE	FALSE FALSE
##	13	smokebeh_sin	n rate smokebeh_sim (period 1)	TRUE	FALSE FALSE
##	14	smokebeh_sin	n rate smokebeh_sim (period 2)	TRUE	FALSE FALSE
##	15	smokebeh_sin	n rate smokebeh_sim (period 3)	TRUE	FALSE FALSE
##	16	smokebeh_sin	n smokebeh_sim linear shape	TRUE	FALSE FALSE
##	17	smokebeh_sin	n smokebeh_sim average similarity	TRUE	FALSE FALSE
##	18	smokebeh sin	n smokebeh sim total similarity	TRUE	FALSE FALSE

4. Create the effects of model 2 for RSiena object with simulated data

There are two paths to create the effects of model 2. One is that we use function frndeff_sim2 <- getEffects(friend_sim) to get the basic effects of the RSiena object. Then after comparing it with the result on slide #172, we find we only need to add 2 more effects in the RSiena object. They are the "sameX" effects for gender_sim and simulated smoke behavior. Then we use function includeEffects to realize the goal. And the codes are shown below:

```
frndeff2_sim <- includeEffects(frndeff2_sim,sameX,interaction1="gender_sim",name="fr4wav_sim")

frndeff2_sim <- includeEffects(frndeff2_sim,sameX,interaction1="smokebeh_sim",name="fr4wav_sim")</pre>
```

The other one is that we use the results of the effects of model 1 and use function **includeEffects** to delete some effects to meet the requirement of model 2. Then after comparing the result on slide #172 with the result on slide #168, we find we need to delete 7 more effects in the RSiena object. They are the transitivity effect, the "altX" effect for simulated smoke behavior and gender_sim, the "egoX" for simulated smoke behavior and gender_sim, "avSim" and "totSim" effects for simulated smoke behavior. Then we use function **includeEffects** to realize the goal. And the codes are shown below:

```
Frndeff2_sim <- includeEffects(frndeff_sim,egoX,interaction1="smokebeh_sim",name="fr4wav_sim", include = FALSE)

Frndeff2_sim <- includeEffects(frndeff2_sim,altX,interaction1="smokebeh_sim",name="fr4wav_sim", include = FALSE)

Frndeff2_sim <- includeEffects(frndeff2_sim,avSim,interaction1="fr4wav_sim",name="smokebeh_sim", include = FALSE)

Frndeff2_sim <- includeEffects(frndeff2_sim,totSim,interaction1="fr4wav_si",name="smokebeh_sim", include = FALSE)

Frndeff2_sim <- includeEffects(frndeff2_sim, transTrip,name="fr4wav_s", include = FALSE)

Frndeff2_sim <- includeEffects(frndeff2_sim,egoX,interaction1="gender_sim",name="fr4wav_sim", include = FALSE)

Frndeff2_sim <- includeEffects(frndeff2_sim,altX,interaction1="gender_sim",name="fr4wav_sim", include = FALSE)</pre>
```

Then we get the effects of model 2 for simulated data as show below:

##	name	effectName	include fi	ix test
## 1	fr4wav_sim	constant fr4wav_sim rate (period	1) TRUE	FALSE FALSE
## 2	fr4wav_sim	constant fr4wav_sim rate (period	2) TRUE	FALSE FALSE
## 3	fr4wav_sim	constant fr4wav_sim rate (period	3) TRUE	FALSE FALSE
## 4	fr4wav_sim	outdegree (density)	TRUE	FALSE FALSE
## 5	fr4wav_sim	reciprocity	TRUE	FALSE FALSE
## 6	fr4wav_sim	same gender_sim	TRUE	FALSE FALSE
## 7	fr4wav_sim	same smokebeh_sim	TRUE	FALSE FALSE
## 8	smokebeh_sim	n rate smokebeh_sim (period 1)	TRUE	FALSE FALSE

5. Estimate the model 1 and model 2

Then we use the function **sienaAlgorithmCreate**(projname='coevol_sim1') to create the algorithm and function **siena07** to estimate the model 1 with RSiena object generated from simulated data, option returnDeps=TRUE, batch=TRUE, verbose=FALSE, useCluster=TRUE, initC=TRUE, nbrNodes=3 in siena07() and set.seed(999). The details for model 1 are shown below:

```
myalgorithm1 <- sienaAlgorithmCreate( projname='coevol_sim1', seed=999)
RSmod1_sim <- siena07(myalgorithm1,data = friend_sim,effects = frndeff_sim,
batch=TRUE,verbose=FALSE,useCluster=TRUE,initC=TRUE,nbrNodes=3,returnDeps=
TRUE)</pre>
```

The results for model 1 are shown below:

```
## Estimates, standard errors and convergence t-ratios
##
                                              Estimate
                                                         Standard
                                                                    Convergence
##
                                                          Error
                                                                     t-ratio
## Network Dynamics
     1. rate constant fr4wav_sim rate (period 1) 1.3155 (0.2255)
##
                                                                      -0.0085
     2. rate constant fr4wav_sim rate (period 2) 3.7087 (0.4918)
                                                                      -0.1015
     3. rate constant fr4wav sim rate (period 3) 3.2133 (0.4326)
                                                                      -0.0261
     4. eval outdegree (density)
##
                                                   -2.8236 (0.3723)
                                                                       0.0255
     5. eval reciprocity
                                                    0.7756 (0.1694)
                                                                       0.0020
     6. eval transitive triplets
                                                   0.1556 (0.0480)
##
                                                                       0.0194
     7. eval gender sim alter
                                                  -0.0029 (0.2083)
                                                                       0.0280
     8. eval gender_sim ego
                                                   0.1967 (0.2100)
##
                                                                       0.0308
     9. eval same gender sim
                                                   1.1430 (0.2176)
                                                                       0.0165
    10. eval smokebeh_sim alter
                                                  0.1068 (0.2789)
##
                                                                      -0.0560
##
    11. eval smokebeh sim ego
                                                  0.2497 (0.2692)
                                                                      0.0261
    12. eval same smokebeh sim
                                                  0.2047 (0.3473)
                                                                      0.0039
## Behavior Dynamics
    13. rate rate smokebeh sim (period 1)
                                                  0.2138 (0.1631)
                                                                     -0.0186
    14. rate rate smokebeh_sim (period 2)
##
                                                  0.7383 (0.3556)
                                                                     -0.0143
    15. rate rate smokebeh sim (period 3)
                                                  2.3657 (1.9074)
                                                                      -0.0682
    16. eval smokebeh_sim linear shape
##
                                                  0.1174 (0.4236)
                                                                      0.0549
    17. eval smokebeh sim average similarity
                                                   4.8444 (9.4918)
                                                                      0.0184
    18. eval smokebeh_sim total similarity
                                                  -0.6137 (1.8038)
                                                                      0.0164
```

Then we use the function **sienaAlgorithmCreate**(projname='coevol_sim2') to create the algorithm and function **siena07** to estimate the model 2 with RSiena object generated from simulated data, option returnDeps=TRUE, batch=TRUE, verbose=FALSE, useCluster=TRUE, initC=TRUE, nbrNodes=3 in siena07() and set.seed(999). The details for model 2 are shown below:

myalgorithm2 <- sienaAlgorithmCreate(projname='coevol_sim2', seed=999)
RSmod2_sim <- siena07(myalgorithm2,data = friend_sim,effects = frndeff2_si
m, batch=TRUE,verbose=FALSE,useCluster=TRUE,initC=TRUE,nbrNodes=3,returnDe
ps=TRUE)</pre>

The results for model 2 are shown below:

##	Estimates,	standard	errors an	d conve	rgence	t-ratio	5	
		2 22.1001 0	c c. 5 dii		601100			Canvanaanaa
##						Estimate	Standard	Convergence
##							Error	t-ratio
##	Network Dy	namics						
##	1. rate	constant	fr4wav_si	n rate	(period	1) 1.2	708 (0.2227)	0.0340
##	2. rate	constant	fr4wav_si	n rate	(period	2) 3.5	522 (0.4450	0.0124
##	3. rate	constant	fr4wav_si	n rate	(period	3) 3.1	825 (0.4129	9) -0.0164
##	4. eval	outdegree	e (density))		-2.3	3531 (0.2482) -0.0584
##	5. eval	reciproci	ty			0.90	065 (0.1572)	-0.0444
##	6. eval	same gend	ler_sim			1.3	749 (0.1933)	-0.0620
##	7. eval	same smok	cebeh_sim			0.0	430 (0.2890) -0.0608
##	Behavior D	ynamics						
##	8. rate	rate smok	cebeh_sim	(period	1)	0.15	646 (0.1040)	0.0007
##	9. rate	rate smok	cebeh_sim	(period	2)	0.59	0.2560)	-0.0079
##	10. rate	rate smok	kebeh_sim	(period	3)	2.21	L81 (2.0580)	0.0580
##	11. eval	smokebeh	sim linea	shape	!	-0.13	376 (0.3937)	0.0392

IV Compare the results

1. Results analysis of two models

Table 1 Results for model 1

		Estimate	Stderror	t-stats	t-ratio
	1. rate constant fr4wav_sim rate (period 1)	1.3155	0.2255	5.8337	-0.0085
	2. rate constant fr4wav_sim rate (period 2)	3.7087	0.4918	7.5410	-0.1015
	3. rate constant fr4wav_sim rate (period 3)	3.2133	0.4326	7.4278	-0.0261
Network	4. eval outdegree (density)	-2.8236	0.3723	-7.5842	0.0255
	5. eval reciprocity	0.7756	0.1694	4.5785	0.0020
	6. eval transitive triplets	0.1556	0.0480	3.2416	0.0194
Dynamics	7. eval gender_sim alter	-0.0029	0.2083	-0.0139	0.0280
	8. eval gender_sim ego	0.1967	0.2100	0.9366	0.0308
	9. eval same gender_sim	1.1430	0.2176	5.2527	0.0165
	10. eval smokebeh_sim alter	0.1068	0.2789	0.3829	-0.0560
	11. eval smokebeh_sim ego	0.2497	0.2692	0.9275	0.0261
	12. eval same smokebeh_sim	0.2047	0.3473	0.5894	0.0039
	13. rate rate smokebeh_sim (period 1)	0.2138	0.1631	1.3108	-0.0186
	14. rate rate smokebeh_sim (period 2)	0.7383	0.3556	2.0762	-0.0143
Behavior	15. rate rate smokebeh_sim (period 3)	2.3657	1.9074	1.2402	-0.0682
	16. eval smokebeh_sim linear shape	0.1174	0.4236	0.2771	0.0549
Dynamics	17. eval smokebeh_sim average similarity	4.8444	9.4918	0.5103	0.0184

For the results, the RSiena manual suggests that absolute values less than 0.10 indicate excellent convergence, and absolute values less than 0.15 are reasonable. Here we see that all of the parameters except rate constant fr4wav_sim rate (period 2), have excellent convergence and the parameter of rate constant fr4wav_sim rate (period 2) shows only reasonable convergence.

The significance of these evaluation function weights can be determined by dividing the estimates by their standard errors. These are distributed as t-statistics, so any absolute values greater than 2 are significant at the 0.05 significance level.

For our results, we can see the t-stats of three rates in network dynamics, outdegree, reciprocity, transitivity, same gender_sim and rate of smokebeh_sim (period 2) are greater than 2 so these corresponding estimates are significant.

Specifically, we can see that our friendship formation is more likely with people who have the same gender. Conversely, it appears that the main effects of ego smoking and gender, same smoking, alter smoking and gender are not significant predictors of tie formation. Outdegree, transitivity and reciprocity are significant structural predictors.

		Estimate	Stderror	t-stats	t-ratio
	1. rate constant fr4wav_sim rate (period 1)	1.2708	0.2227	5.7063	0.0340
	2. rate constant fr4wav_sim rate (period 2)	3.5522	0.4450	7.9824	-0.0124
Network	3. rate constant fr4wav_sim rate (period 3)	3.1825	0.4129	7.7076	-0.0164
	4. eval outdegree (density)	-2.3531	0.2482	-9.480	-0.0584
	5. eval reciprocity	0.9065	0.1572	5.7665	-0.0444
Dynamics	6. eval same gender_sim	1.3749	0.1933	7.1127	-0.0620
	7. eval same smokebeh_sim	0.0430	0.2890	0.1487	-0.0608
	8. rate rate smokebeh_sim (period 1)	0.1546	0.1040	1.4865	0.0007
Behavior	9. rate rate smokebeh_sim (period 2)	0.5907	0.2560	2.3074	-0.0079
Dynamics	10. rate rate smokebeh_sim (period 3)	2.2181	2.0580	1.0777	0.0580
	11. eval smokebeh_sim linear shape	-0.1376	0.3937	-0.349	0.0392

Table 2 Results for model 2

For the results, the RSiena manual suggests that absolute values less than 0.10 indicate excellent convergence, and absolute values less than 0.15 are reasonable. Here we see that all of the parameters have excellent convergence.

The significance of these evaluation function weights can be determined by dividing the estimates by their standard errors. These are distributed as t-statistics, so any absolute values greater than 2 are significant at the 0.05 significance level.

For our results, we can see the t-stats of three rates in network dynamics, outdegree, reciprocity, transitivity, same gender_sim and rate of smokebeh_sim (period 2) are greater than 2 so these corresponding estimates are significant.

Specifically, we can see that our friendship formation is more likely with people who have the same gender. Conversely, it appears that the main effects of ego smoking and gender, same smoking, alter smoking and gender are not significant predictors of tie formation. Outdegree, transitivity and reciprocity are significant structural predictors.

2. Results comparison of two models

From the results, we can see three rates in network dynamics, outdegree, reciprocity, transitivity, same gender_sim and rate of smokebeh_sim (period 2) are all significant no matter for model 1 or model 2. Also, the estimates of these significant parameters are similar for these two models. And the results for two models in convergence accessing are similar. That is, all parameters have reasonable convergence. For model 1, all parameters except rate constant fr4wav_sim rate (period 2), have excellent convergence and the parameter of rate constant fr4wav_sim rate (period 2) shows only reasonable convergence. For model 2, all parameters have excellent convergence.

Appendix

```
library(igraph)
library("UserNetR")
library(RSiena)
data(Coevolve) # Load the data
fr_w1 <- Coevolve$fr_w1 # Get the data 1</pre>
fr w2 <- Coevolve$fr w2 # Get the data 2
fr_w3 <- Coevolve$fr_w3 # Get the data 3</pre>
fr w4 <- Coevolve$fr w4 # Get the data 4
matw1 <- as.matrix(get.adjacency(fr_w1))# Get the adjacency matraix and tra
nsform it into matrix form storing in matw1
matw2 <- as.matrix(get.adjacency(fr w2))</pre>
# Get the adjacency matraix and transform it into matrix form storing in ma
tw2
matw3 <- as.matrix(get.adjacency(fr w3))</pre>
# Get the adjacency matraix and transform it into matrix form storing in ma
tw3
matw4 <- as.matrix(get.adjacency(fr w4))</pre>
# Get the adjacency matraix and transform it into matrix form storing in ma
fr4wav<-sienaDependent(array(c(matw1,matw2,matw3,matw4),dim=c(37,37,4)), s
parse=FALSE)# Create thetime-varying dependent network variable.
fr4wav# Show the fr4wav
gender vect <- V(fr w1)$gender# Get the gender values of graph fr w1
gender <- coCovar(gender_vect, centered = FALSE) #create the time-stable cov</pre>
ariate gender with the same vertex values of network fr_w1 since the option
center does not make sense here so we use FALSE here.
smoke <- array(c(V(fr w1)$smoke, V(fr w2)$smoke, V(fr w3)$smoke, V(fr w4)$s</pre>
moke),
dim=c(37,4))#Preparation for Creating the behavior variable
smokebeh <- sienaDependent(smoke, type = "behavior")# Create the behavior va</pre>
riable
friend <- sienaDataCreate(fr4wav,smokebeh,gender)#After all different types</pre>
of objects are ready, we combine them into a single RSiena object
print01Report(friend, modelname="sample")# Generate the initial report
frndeff <- getEffects(friend)#get the basic effects of the RSiena object.
frndeff# Show the basic effect
```

```
frndeff <- includeEffects(frndeff, sameX,</pre>
interaction1="gender", name="fr4wav")# Add the "sameX" effect for gender
frndeff <- includeEffects(frndeff,egoX,</pre>
interaction1="smokebeh", name="fr4wav")
# add the "egoX" effect for smokebehavior
frndeff <- includeEffects(frndeff,altX,</pre>
interaction1="smokebeh",name="fr4wav")
# add the "altX" effect for smokebehavior
frndeff <- includeEffects(frndeff, sameX,</pre>
interaction1="smokebeh", name="fr4wav")
# add the "sameX" effect for smokebehavior
frndeff <- includeEffects(frndeff,avSim,</pre>
interaction1="fr4wav", name="smokebeh")
# add the "avSim" effect for smokebehavior
frndeff <- includeEffects(frndeff,totSim,interaction1="fr4wav",name="smoke</pre>
beh")
# add the "totSim" effect for smokebehavior
frndeff <- includeEffects(frndeff,recip,transTrip,</pre>
name="fr4wav")
# add the transitivity effect
frndeff # Show the effect
frndeff <- includeEffects(frndeff,egoX,</pre>
interaction1="gender",name="fr4wav")
# add the "egoX" effect for gender
frndeff <- includeEffects(frndeff,altX,</pre>
interaction1="gender",name="fr4wav")
# add the "altX" effect for gender
frndeff#SHow the effects
myalgorithm <- sienaAlgorithmCreate(</pre>
   projname='coevol',seed =999)# Create the akgorithm and set the seed=999
RSmod1 <- siena07(myalgorithm, data = friend,
```

```
effects = frndeff,
batch=TRUE,
verbose=FALSE,useCluster=TRUE,
initC=TRUE,nbrNodes=3,
returnDeps=TRUE)# Estimate the model
summary(RSmod1)# Show the results of fitting
```

Simulation

fr_w2_sim

```
el2 <- RSmod1$sims[[1]][[1]][[1]]# GET the edgelist of simulated netwo rk for first wave

sb2 <- RSmod1$sims[[1]][[1]][[2]][[1]]# GET the smokebehavior of simulated network network for first wave

fr_w2_sim <- graph.data.frame(el2,directed = TRUE)

# Create the first wave network

V(fr_w2_sim)$smoke <- sb2 # Set the smokebehavior values

V(fr_w2_sim)$gender <- V(fr_w2)$gender# Set the gender values

fr_w2_sim# SHow the network fr_w2_sim
```

fr_w3_sim

```
el3 <- RSmod1$sims[[1]][[1]][[2]]

#GET the edgeList of simulated network for second wave

sb3 <- RSmod1$sims[[1]][[1]][[2]][[2]]

#GET the smokebehavior of simulated network network for second wave

fr_w3_sim <- graph.data.frame(el3,directed = TRUE)

# Create the second wave network

V(fr_w3_sim)$smoke <- sb3# Set the smokebehavior values

V(fr_w3_sim)$gender <- V(fr_w3)$gender# Set the gender values

fr_w3_sim# SHow the network fr_w3_sim
```

fr_w4_sim

```
el4 <- RSmod1$sims[[1]][[1]][[1]][[3]]
#GET the edgeList of simulated network for third wave
sb4 <- RSmod1$sims[[1]][[1]][[2]][[3]]
#GET the smokebehavior of simulated network network for third wave
fr_w4_sim <- graph.data.frame(el4,directed = TRUE)
# Create the third wave network
V(fr_w4_sim)$smoke <- sb4# Set the smokebehavior values</pre>
```

```
V(fr_w4_sim)$gender <- V(fr_w4)$gender
# Set the gender values
fr_w4_sim# SHow the network fr_w3_sim</pre>
```

Construct #168 model

```
matw1 <- as.matrix(get.adjacency(fr_w1))</pre>
# Get the adjacency matraix and transform it into matrix form storing in ma
matw2 sim <- as.matrix(get.adjacency (fr w2 sim))</pre>
# Get the adjacency matraix and transform it into matrix form storing in ma
tw2_sim
matw3_sim <- as.matrix(get.adjacency (fr_w3_sim))</pre>
# Get the adjacency matraix and transform it into matrix form storing in ma
tw3 sim
matw4_sim <- as.matrix(get.adjacency (fr_w4_sim))</pre>
# Get the adjacency matraix and transform it into matrix form storing in ma
tw4_sim
fr4wav sim<-sienaDependent(array(c(matw1,matw2 sim,matw3 sim,matw4 sim),di</pre>
m=c(37,37,4)), sparse=FALSE)# Create thetime-varying dependent network vari
able.
fr4wav_sim# Show fr4wav_sim
gender vect <- V(fr w1)$gender# Get the gender values of graph fr w1
gender_sim <- coCovar(gender_vect,centered = FALSE)#create the time-stable</pre>
covariate gender with the same vertex values of network fr w1 since the opt
ion center does not make sense here so we use FALSE here.
smoke_sim <- array(c(V(fr_w1)$smoke, V(fr_w2_sim)$smoke,V(fr_w3_sim)$smok</pre>
e, V(fr w4 sim)$smoke),
dim=c(37,4))
smokebeh sim <- sienaDependent(smoke sim, type = "behavior")#Preparation for</pre>
Creating the behavior variable
smokebeh sim# Create the behavior variable
friend_sim <- sienaDataCreate(fr4wav_sim,smokebeh_sim,gender_sim)#After al</pre>
l different types of objects are ready, we combine them into a single RSien
a object
print01Report(friend sim, modelname="sample")# Show the initial report
frndeff sim <- getEffects(friend sim)#Get the basic effects
frndeff_sim# Show the basic efects
```

```
frndeff sim <- includeEffects(frndeff sim, sameX,</pre>
interaction1="gender_sim",name="fr4wav_sim")# Add the "sameX" effect for ge
nder_sim
frndeff_sim <- includeEffects(frndeff_sim,egoX,</pre>
interaction1="smokebeh_sim",name="fr4wav_sim")# Add the "egoX" effect for s
mokebeh sim
frndeff_sim <- includeEffects(frndeff_sim,altX,</pre>
interaction1="smokebeh_sim",name="fr4wav_sim")# Add the "altX" effect for s
mokebeh sim
frndeff_sim <- includeEffects(frndeff_sim,sameX,</pre>
interaction1="smokebeh sim", name="fr4wav sim")# Add the "sameX" effect for
smokebeh sim
frndeff sim <- includeEffects(frndeff sim,avSim,</pre>
interaction1="fr4wav_sim",name="smokebeh_sim")# Add the "avSim" effect for
smokebeh_sim
frndeff sim <- includeEffects(frndeff sim,totSim,</pre>
interaction1="fr4wav_sim",name="smokebeh_sim")# Add the "totSim" effect for
 smokebeh sim
frndeff_sim <- includeEffects(frndeff_sim,transTrip,name="fr4wav_sim")# Ad</pre>
d the "transitivity" effect
frndeff_sim <- includeEffects(frndeff_sim,egoX,</pre>
interaction1="gender_sim", name="fr4wav_sim")# Add the "egoX" effect for gen
der sim
frndeff sim <- includeEffects(frndeff sim,altX,</pre>
interaction1="gender_sim", name="fr4wav_sim")# Add the "altX" effect for gen
der_sim
frndeff sim# SHow the effects
frndeff2_sim <- getEffects(friend_sim)# Get the basic effets</pre>
frndeff2_sim# Show the basic effets
frndeff2 sim <- includeEffects(frndeff2 sim, sameX,</pre>
interaction1="gender_sim",name="fr4wav_sim")# Add the "sameX" effect for ge
nder_sim
     effectName
                     include fix test initialValue parm
## 1 same gender_sim TRUE FALSE FALSE
                                                   0
```

```
frndeff2 sim <- includeEffects(frndeff2 sim, sameX,</pre>
interaction1="smokebeh sim", name="fr4wav sim")# Add the "sameX" effect for
smokebeh sim
##
     effectName
                      include fix test initialValue parm
## 1 same smokebeh_sim TRUE FALSE FALSE
frndeff2 sim# Show the effects
#frndeff_sim2 <- includeEffects(frndeff_sim2,egoX,interaction1="smokebeh_s
im",name="fr4wav_sim", include = FALSE)
#frndeff_sim2 <- includeEffects(frndeff_sim2,altX,interaction1="smokebeh_s
im",name="fr4wav_sim", include = FALSE)
#frndeff_sim2 <- includeEffects(frndeff_sim2,avSim,interaction1="fr4wav_si
m",name="smokebeh_sim", include = FALSE)
#frndeff_sim2 <- includeEffects(frndeff_sim2,totSim,interaction1="fr4wav_s</pre>
im",name="smokebeh_sim", include = FALSE)
#frndeff_sim2 <- includeEffects(frndeff_sim2,recip,transTrip,name="fr4wav_</pre>
sim", include = FALSE)
#frndeff_sim2 <- includeEffects(frndeff_sim2,egoX,interaction1="gender_sim
",name="fr4wav_sim", include = FALSE)
#frndeff_sim2 <- includeEffects(frndeff_sim2,altX,interaction1="gender_sim
",name="fr4wav_sim", include = FALSE)
```

Estimation

mdoel 1

```
myalgorithm1 <- sienaAlgorithmCreate(
    projname='coevol_sim1',seed = 999)# Create the algorithm and set seed =
999

RSmod1_sim <- siena07(myalgorithm1,data = friend_sim,
    effects = frndeff_sim,
    batch=TRUE,
    verbose=FALSE,useCluster=TRUE,
    initC=TRUE,nbrNodes=3,
    returnDeps=TRUE)# Run the model</pre>
```

```
summary(RSmod1_sim)# SHow the results of fitting
```

model 2

```
myalgorithm2 <- sienaAlgorithmCreate(
    projname='coevol_sim2',seed =999)# Create the akgorithm and set the seed =999

RSmod2_sim <- siena07(myalgorithm2,data = friend_sim,
    effects = frndeff2_sim,
    batch=TRUE,
    verbose=FALSE,useCluster=TRUE,
    initC=TRUE,nbrNodes=3,
    returnDeps=TRUE)# Etimate the model

summary(RSmod2_sim)# SHow the results of fitting</pre>
```