



for you !!

Wk 1 - Lec

- 10% weekly quizzes (wk 2)
 - 30% assignments (2 coding, 3 writing)
 - 60% final exam (in campus)
- ※ 노트 정리를 잘하고 교과서를 읽자!

Lecture - ask Qs thru mentimeter

Solve tut sheet before tutorials v

Lec 1

Algorithm Analysis

3 Abstractions

- Computational problem
 - defines the task ^{provided.}
 - what input is & what output should be
- Algorithm
 - step-by-step recipe to go from input to output ^{my job}
- Correctness & Complexity Analysis
 - proof that the algorithm solves the problem
 - analytical bound on resources used

Pseudocode : will resemble skeletal python code.

3. correctness:

ex)

1. Comp problem: return max of array

2. algorithm:

max $\leftarrow -\infty$

for $i \leftarrow 0$ to $n-1$ do

if $A[i] > \text{max}$:

max $\leftarrow A[i]$

return max

invariant: ~~after each iteration~~

After k^{th} iteration, max stores the maximum of the first k elements

build upon this invariant to prove the algorithm.

high-level English description

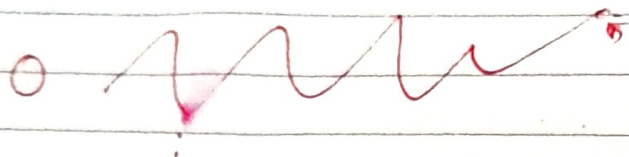
is mandatory?

~~is pseudocode?~~

pseudo \rightarrow concrete description?

ex computational problem #2

- daily fluctuations of a stock price in an Array A .
- find best single-trade outcome.



$$0 \leq i \leq j \leq n$$

buy sell

$$A = [3, -2, -5, -8, 3, 9, 15, -3, 9]$$

$$B = [0, 3, 1, -4, -12, 9, 0, 15, 12, 21]$$

$$A = [A_0, A_1, A_2, A_3, \dots, A_n]$$

$$B = \begin{cases} B[0] = 0 & \text{if } i = 0 \\ B[i] = A[i-1] + B[i-1] & \text{if } i > 0 \end{cases}$$

$$\therefore B = [0, A_0, A_0 + A_1, A_0 + A_1 + A_2, \dots]$$

$$A = [1, 2, 3]$$

$$B = [0, 1, 3, 6]$$

$$n = 3$$

$$i = 0 \quad j = 2$$

$$\text{profit} =$$

$$1 \quad \text{max-gap} \leftarrow 0$$

$$2 \quad \text{buy-sell-point} \leftarrow (\text{None}, \text{None}) \quad n = \text{size of } A$$

$$3 \quad B \leftarrow \text{new array of size } n+1$$

$$4 \quad B[0] \leftarrow 0$$

$$5 \quad \text{for } i \leftarrow 0 \text{ to } n-1 \text{ do}$$

$$6 \quad B[i+1] \leftarrow B[i] + A[i]$$

$$7 \quad \text{for } i \leftarrow 0 \text{ to } n-1 \text{ do}$$

$$8 \quad \text{for } j \leftarrow i+1 \text{ to } n \text{ do}$$

$$9 \quad \text{profit} \leftarrow B[j] - B[i]$$

$$10 \quad \text{if } \text{profit} > \text{max-gap:}$$

$$\text{max-gap} \leftarrow \text{profit}$$

$$\text{buy-sell-point} \leftarrow (i, j)$$

$$\text{for } j \leftarrow i \text{ to } n-1 \text{ do}$$

$$\text{profit} \leftarrow B[j+1] - B[i]$$

$$\text{if}$$

$$\Rightarrow //$$

$$\leftarrow (i, j+1)$$

shouldn't it be

Q efficiency?

bad: performs well on real-inputs.? who decides it? depends on hardware

bad: performs better than brute-force \leftarrow ill-defined

smaller

$$O(n)$$

$$\Omega(n)$$

$$\Theta(n)$$

equal

Good: Runs in polynomial time

\hookrightarrow should we count the exact steps? **No!**

\hookrightarrow what matters is the leading term: Asymptotic growth Analysis

"worst-case scenario"
Big-O notation

bigger