Mobile Phones Selling Price Report

Final report (MDSA Winter 2023)

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Introduction

Mobile phones are everywhere, so are the prices. Despite still having the word "phone" in the name, a typical modern smartphone has much more features than just to make and receive calls. They are boasting a staggering range of applications like brand, memory, storage, camera, resolution, just to name a few. All these cutting edge technology and features packed in one little device does not come without a cost. A 2020 review of premium mobile phones shows a staggering 490% rise in the last two decades.

With so many mobile phones on the market, it can be difficult to decide which one you want to buy. As a customer, we are particularly interested in finding some relation between all these features and its selling price. To this purpose, we collected the MobilePhone's dataset from Kaggle and apply a set of statistical analysis hoping to answer some guiding questions:

- 1. Can we estimate the average price for mobile phones?
- 2. What is the impact of each mobile phone's feature on the selling price?
- 3. Can a classification model to distinguish the selling price range?
- 4. Can we build a decent model to predict the selling price for a mobile phone?

Dataset and Cleanup

The initial dataset consists of 8 columns and 28,036 rows and no missing values. These 8 columns are:

- Model: categorical variables with sub-classes. These names include the color of the unit and its storage capacity. The latter being also listed as a separate column. Independent Variable
- Company: categorical variable. Name of the phone's manufacturer. Independent Variable
- Price: continuous variable. Units in Indian Rupees. Dependent Variable
- Rating: continuous variable. Independent Variable
- Number of ratings: discrete variable: a simple count. Independent Variable
- Total reviews: discrete variable: a simple count. Independent Variable
- RAM size: categorical variable. RAM specification of the phone. Independent Variable
- ROM size: categorical variable. Storage (non-volatile memory) capacity of the phone. Independent Variable

Some initial steps can be completed to clean the dataset and create new variables which can be used in our analysis. The initial steps for cleaning the dataset are as follows:

- 1. Remove any duplicates in the dataset;
- 2. Because **Model** column contains sub-class of a mobile phone, we decide to further break it down to *Model* and *Color*;
- 3. Convert all units from RAM size and ROM size measure to GB and then remove unit suffix;
- 4. Add additional column to segment the **Price** into 4 different levels;
- 5. Add additional column to determine if a phone has %G feature or not based on Model information.

```
#Step 3: Get the color information from inside the last ()
#Step 3.1: Get the parenthesis and what is inside from the last ()
Model_no_Company_parenthesis <- stringr::str_extract(Model_no_Company,</pre>
→ "(?<=\\()([^()]*?)(?=\\)[^()]*$)")</pre>
#step 3.2: Get the color by just retaining the info before,
mobile_dataset$Color <- gsub(",.*$", "", Model_no_Company_parenthesis)</pre>
#Step 4: Remove duplicated rows in the dataset
mobile_dataset <- mobile_dataset[!duplicated(mobile_dataset),]</pre>
#Step 5: cut the price based on the percentile into 4 different levels
mobile_dataset <- mobile_dataset %>% mutate(Price_Level = ntile(Price, n = 4))
#Step 5.1: map each number level to the character
from <-c(1,2,3,4)
to <- c("Low", "Medium", "High", "Very High")
mobile_dataset$Price_Level <- mapvalues(mobile_dataset$Price_Level, from = from, to
\rightarrow = to)
#Step 6: Get the numeric part of RomSize (remove GB and MB, but convert MB to GB),
→ discard any record that no numeric in RomSize
#Step 6.1: there are some data input errors for RamSize and RomSize. In the records
→ where RomSize is "Not Known" are swapped with RamSize, so we need to correct
\rightarrow that.
RamSize_temp <- ifelse(mobile_dataset$RomSize == "Not Known", "O GB",</pre>

→ mobile_dataset$RamSize)
mobile_dataset$RomSize <- ifelse(mobile_dataset$RomSize == "Not Known",
→ mobile_dataset$RamSize, mobile_dataset$RomSize)
mobile_dataset$RamSize <- RamSize_temp</pre>
#Step 6.2: split RomSize into two columns with size number and unit, and convert MB
→ to 1/1000GB, KB to 1/1000000GB
mobile_dataset$RamSize_Ori <- mobile_dataset$RamSize</pre>
mobile_dataset$RomSize_Ori <- mobile_dataset$RomSize</pre>
mobile_dataset <- mobile_dataset %>% separate(RomSize, c("RomSize_num",
- "RomSize_Unit")) %>% mutate(RomSize_Unit= mapvalues(.$RomSize_Unit, from =
\rightarrow c("GB", "MB", "KB"), to = c(1, 1/1000, 1/1000000)))
#step 6.3: remove any rows that are not numeric value for RomSize
mobile_dataset <- mobile_dataset[!is.na(as.numeric(mobile_dataset$RomSize_num)),]</pre>
mobile_dataset$RomSize_num <- as.numeric(mobile_dataset$RomSize_num)</pre>
mobile_dataset$RomSize_Unit <-</pre>

    ifelse(is.na(as.numeric(mobile_dataset$RomSize_Unit)), 0,
→ as.numeric(mobile_dataset$RomSize_Unit))
#Step 6.4: generate the final column RomSize_inGB
mobile_dataset$RomSize_inGB <- mobile_dataset$RomSize_num *</pre>

→ mobile_dataset$RomSize_Unit

#Step 7: Get the numeric part of RamSize (remove GB and MB, but convert MB to GB),
\rightarrow discard any record that no numeric in RamSize
#Step 7.1: split RamSize into two columns with size number and unit, and convert MB
→ to 1/1000GB
mobile_dataset <- mobile_dataset %% separate(RamSize, c("RamSize_num",
"RamSize_Unit")) %>% mutate(RamSize_Unit= mapvalues(.$RamSize_Unit, from =
\rightarrow c("GB", "MB"), to = c(1, 1/1000)))
#step 7.2: remove any rows that are not numeric value for RamSize
mobile dataset <- mobile dataset[!is.na(as.numeric(mobile dataset$RamSize num)),]</pre>
mobile_dataset$RamSize_num<- as.numeric(mobile_dataset$RamSize_num)</pre>
```

```
mobile dataset$RamSize Unit <- as.numeric(mobile dataset$RamSize Unit)</pre>
#Step 7.3: generate the final column RamSize_inGB
mobile_dataset$RamSize_inGB <- mobile_dataset$RamSize_num *

→ mobile_dataset$RamSize_Unit

#Step 8: Create a new column to determine if the phone is 5G or not
mobile_dataset$Is_5G <- ifelse(str_detect(mobile_dataset$Model_Only, "5G"), "Yes",</pre>
→ "No")
#Step 9: only keep the columns we need
column_names <- c("Model", "Company", "Price", "Rating", "No_of_ratings",
    "TotalReviwes", "Model_Only", "Color", "Price_Level", "RamSize_inGB",
    "RomSize_inGB", "RamSize_Ori", "RomSize_Ori", "Is_5G" )
mobile_dataset <- mobile_dataset[column_names]</pre>
# #Step 9: final check up. Convert all company name to uppercase and then do a final
\rightarrow duplicated removal
# mobile_dataset$Company <- toupper(mobile_dataset$Company)</pre>
# mobile dataset <- mobile dataset[!duplicated(mobile dataset),]</pre>
write.csv(mobile_dataset, file = './Cleaned_Mobile_Dataset.csv', row.names = F)
```

After cleaning and breaking down columns, the dataset now consists of 14 columns and 725 rows and no missing values. These 14 columns are:

- Model: categorical variables with sub-classes. These names include the color of the unit and its storage capacity. The latter being also listed as a separate column. Independent Variable
- Company: categorical variable. Name of the phone's manufacturer. Independent Variable
- Price: continuous variable. Units in Indian Rupees. Dependent Variable
- Rating: continuous variable. Independent Variable
- Number of ratings: discrete variable: a simple count. Independent Variable
- Total reviews: discrete variable: a simple count. Independent Variable
- Model_Only: categorical variable: only contains the model information of a mobile phone. Independent Variable
- Color: categorical variable: color of a mobile phone. Independent Variable
- **Price_Level**: The price level of a mobile phone, with levels of "Low", "Medium", "High", "Very High". **Independent Variable**
- RamSize_inGB: continuous variable. RAM specification of the phone in GB. Independent Variable
- RomSize_inGB: continuous variable. Storage (non-volatile memory) capacity of the phone in GB. Independent Variable
- RamSize_Ori: categorical variable. RAM specification of the phone, original information. Independent Variable
- RomSize_Ori: categorical variable. Storage (non-volatile memory) capacity of the phone, original information. Independent Variable
- Is_5G: categorical variable. If the phone has 5G service or not. Independent Variable

```
## Model Company Price Rating No_of_ratings
## 1 INFINIX HOT 20 PLAY (LUNA BLUE, 64 GB) INFINIX 8199 4.3 505
## 2 MOTOROLA E40 (CARBON GRAY, 64 GB) MOTOROLA 7999 4.1 56085
```

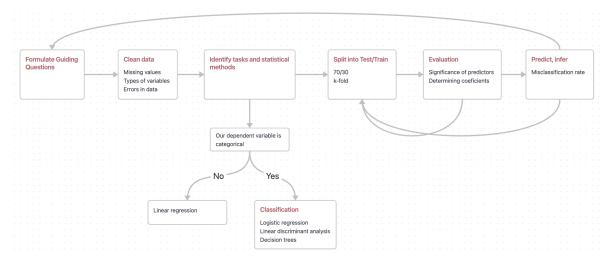
```
## 3
            MOTOROLA E40 (PINK CLAY, 64 GB) MOTOROLA
                                                          7999
                                                                   4.1
                                                                                56085
## 4
              POCO C31 (SHADOW GRAY, 64 GB)
                                                    POCO
                                                          7499
                                                                   4.3
                                                                               183688
##
     TotalReviwes
                    Model_Only
                                       Color Price_Level RamSize_inGB RomSize_inGB
## 1
                52 HOT 20 PLAY
                                                                      4
                                  LUNA BLUE
                                                  Medium
                                                                                   64
## 2
              5600
                            E40 CARBON GRAY
                                                  Medium
                                                                      4
                                                                                   64
  3
              5600
##
                                  PINK CLAY
                                                  Medium
                                                                      4
                                                                                   64
                            E40
## 4
            11185
                            C31 SHADOW GRAY
                                                  Medium
                                                                      4
                                                                                   64
##
     RamSize_Ori RomSize_Ori Is_5G
## 1
            4 GB
                        64 GB
                                  No
  2
            4 GB
                        64 GB
##
                                  No
##
  3
            4 GB
                        64 GB
                                  No
## 4
            4 GB
                        64 GB
                                  No
```

Table 1: The cleaned-up dataset for Mobile Phone

The dataset and detailed analysis can be found at this repository.

Scope of Analysis

Our team is finalizing what the full analysis of the dataset will look like, but a preliminary template and breakdown of work by team member has been included below. The different colors represent which components of the project different team members would take on. It is anticipated that all members will assist in the finalization of the report.



Chapter 1: Exploratory Data Analysis

1.1: A summary of the dataset

The dimension of the cleaned dataset is 726 rows and 14 columns. A summary of the data is as follows:

```
##
       Model
                          Company
                                                 Price
                                                                   Rating
    Length:725
##
                        Length:725
                                                         698
                                                                       :2.700
                                            Min.
                                                               Min.
##
    Class : character
                        Class : character
                                             1st Qu.:
                                                       7014
                                                               1st Qu.:4.100
##
    Mode :character
                        Mode :character
                                            Median: 12889
                                                               Median :4.200
##
                                             Mean
                                                    : 15903
                                                               Mean
                                                                       :4.227
                                                               3rd Qu.:4.300
##
                                             3rd Qu.: 16999
##
                                            Max.
                                                    :149900
                                                               Max.
                                                                       :4.800
##
                                        Model_Only
                                                               Color
    No_of_ratings
                       TotalReviwes
                  3
                                       Length:725
##
    Min.
                      Min.
                                                            Length:725
                      1st Qu.:
    1st Qu.:
                874
                                  80
                                       Class :character
##
                                                            Class : character
##
    Median :
              7325
                      Median :
                                 670
                                       Mode :character
                                                            Mode : character
##
    Mean
            : 34522
                      Mean
                              : 2496
##
    3rd Qu.: 37211
                      3rd Qu.: 2972
            :575907
                              :33942
##
    Max.
                      Max.
##
       Price_Level
                      RamSize_inGB
                                        {\tt RomSize\_inGB}
                                                          RamSize_Ori
##
    Low
              :171
                     Min.
                             : 0.000
                                       Min.
                                               : 0.00
                                                          Length:725
##
    Medium
              :185
                     1st Qu.: 0.064
                                       1st Qu.: 32.00
                                                          Class : character
##
    High
              :185
                     Median : 4.000
                                       Median : 64.00
                                                         Mode :character
    Very High: 184
                            : 3.882
                                               : 81.78
##
                     Mean
                                       Mean
##
                     3rd Qu.: 6.000
                                       3rd Qu.:128.00
##
                             :12.000
                                               :512.00
                     Max.
                                       Max.
##
    RomSize Ori
                            Is 5G
##
    Length:725
                        Length:725
    Class : character
                        Class : character
    Mode :character
                        Mode :character
##
##
##
```

 Table 2: A summary for Mobile Phone dataset

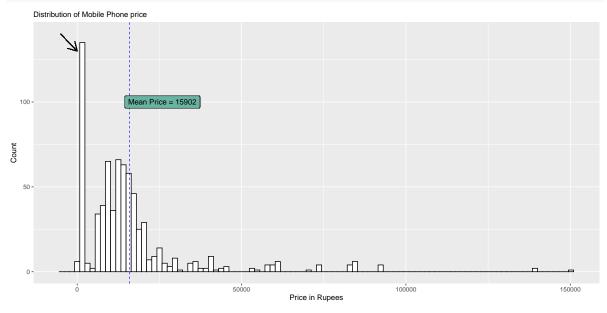
1.2: Exploratory Data Analysis

This section is focused on the exploration of relation between variables using various visualization techniques.

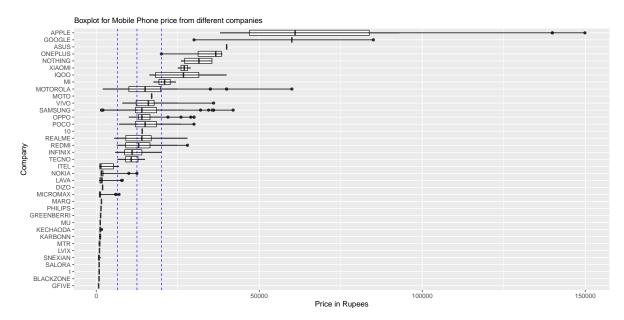
The main target is Price in the dataset. In the following visualization it shows the distribution of Mobile Phone price with long tail towards to the high end. The average price is 15902 Rupees. Most price falls in the range of 50000 Rupees. One really stands out price range (arrow indicated) is 1000-2000 Rupees with the highest frequency.

```
ggplot(data = mobile_dataset, mapping = aes(x=Price)) +

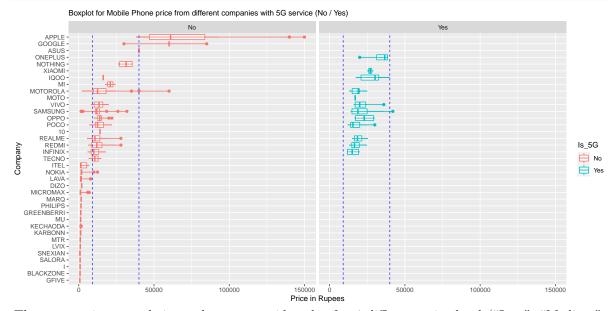
→ geom_histogram(color="black", fill="white", bins = 100)+
 geom_vline(aes(xintercept=mean(Price)),
           color="blue", linetype="dashed", size=0.4) + geom_label(
   label="Mean Price = 15902",
   x= mean(mobile_dataset$Price) + 10000,
   v = 100.
   label.padding = unit(0.35, "lines"),
   label.size = 0.25,
   color = "black",
    fill="#69b3a2"
 ) + geom_segment(aes(x = -5000, y = 140, xend = 0, yend = 130), lineend =
    "round",linejoin = "round",
                 arrow = arrow(length = unit(0.5, "cm"))) + labs(y="Count",
                  subtitle="Distribution of Mobile Phone price")
```



The following figure is to break down the Price by different phone-making companies. There are a total of 37 companies in the dataset. Iin consistent with previous figure about Price distribution, we see a big portion of Price falls between 9000 (left dash line) and 40000 (right dash line) Rupees. Apple alone contributes the most of high priced Mobile Phones, while companies like from NOKIA to GFIVE contribute to the low-priced ones.

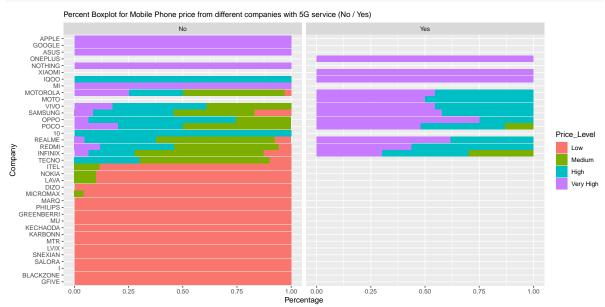


The Price is further broken down by their 5G services. Interestingly, neither high-priced nor low-priced Mobile Phones have equipped 5G service. In contrast, almost all middle-priced Mobile Phones have 5G service. Price for those with 5G service are slightly more expensive than those without. NOTE: the dashed line indicates the price between 9000 (left dash line) and 40000 (right dash line) Rupees.



The pattern is more obvious when we provide color for 4 different price level ("Low", "Medium",

"High", "Very High"). Although mobile phones from companies like APPLE, GOOGLE, ASUS and NOTHING have no 5G service, their price are all very high. It is worth investigating if some other attributes like brand effect, Storage capacity (Rom Size), and calculation power (Ram Size) are playing roles. Most Mobile Phones (except MI) with 5G service, again, have a higher proportion falling in a Very High price level, compared to the counterparts without 5G service. Almost all the rest mobile phones without 5G service fall in a Low price level.



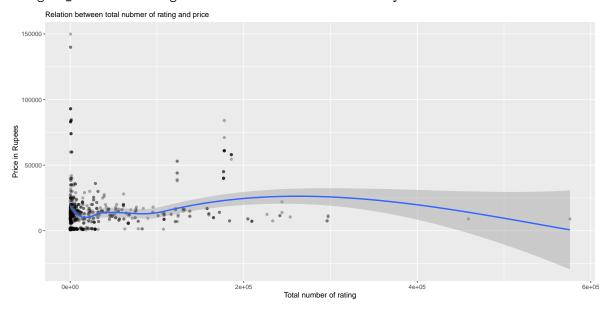
Next, we explored some quantitative features with respect to the Mobile Phone price. The first scatter plot shows an obvious positive relation between Rating and Price as the smooth line indicates. The higher the Rating, the higher the Price. And this holds when we remove those bottom left 2 outlier data points.

`geom_smooth()` using method = 'loess' and formula 'y ~ x' ## `geom_smooth()` using method = 'loess' and formula 'y ~ x' Relation between rating and price Relation between rating and price after removing bottom left 2 outliers 150000 1000000100000100000100000010000010000010000010000010

The second scatter plot as follows shows the relation between Total number of rating and Price. As the smooth line indicates, there is no obvious correlation between them. The result holds even when we remove some seemingly outliers on the far right end.

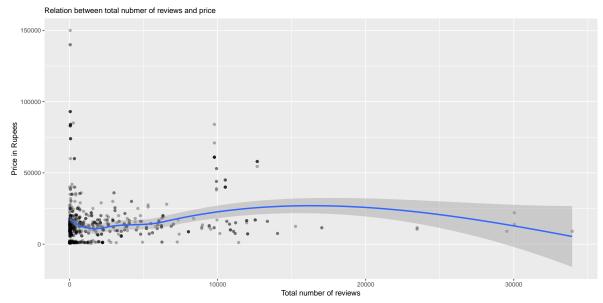
4.0 Rating

`geom_smooth()` using method = 'loess' and formula 'y ~ x'



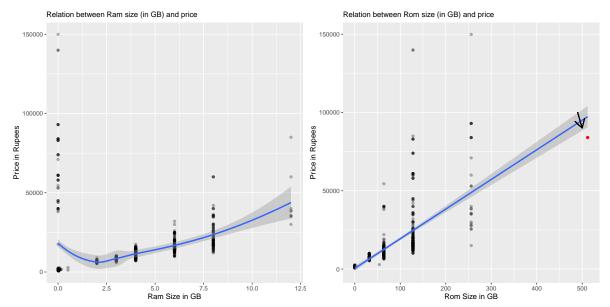
The same pattern is also observed in the third scatter plot where relation between Total number of reviews and Price is plotted. As the smooth line indicates, there is no obvious correlation between them. The result holds even when we remove some seemingly outliers on the far right end.

$geom_smooth()$ using method = 'loess' and formula 'y ~ x'



In the fourth scatter plot, below, there seems a slight positive relation between Ram size (in GB) and the Price. Ram is normally associated with speed and performance of an operating system. The higher ram is, the better it is in speed and performance. It makes sense that a mobile phone with a larger Ram will charge more. However, because nowadays most mobile phones are very fast and stable, people wont tell too much difference, making the added on value from ram is only weekly associated with price.

```
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
## `geom_smooth()` using formula 'y ~ x'
```



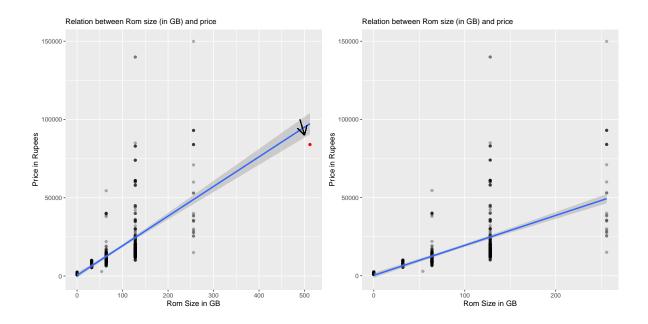
In the final scatter plot, again, we have two charts, one the original dataset, the other with outlier removed. Both cases tells the same story. In contrast to the previous scatter plot (Ram size (in GB) and the Price), there is a very obvious positive linear relation between Rom size (in GB) and the Price. This makes sense because often times a mobile phone is more limited by its non-volatile memory space than its speed & performance.

```
#The first plot is a one with outliers
plot1 = ggplot(data = mobile_dataset,mapping = aes(x = RomSize_inGB, y = Price)) +

→ geom_point(alpha=0.3) + geom_smooth(se=T, method = lm)+
  geom\_segment(aes(x = 490, y = 100000, xend = 500, yend = 90000), lineend =
→ "round",linejoin = "round",arrow = arrow(length = unit(0.5, "cm"))) +
  geom_point(data=mobile_dataset[mobile_dataset$RomSize_inGB>400,], aes(x =
→ RomSize_inGB, y = Price), color='red') +
  labs(y="Price in Rupees", x="Rom Size in GB", subtitle="Relation between Rom size
    (in GB) and price")
#The second plot is a one with outliers removed
plot2 = ggplot(data = mobile_dataset[mobile_dataset$RomSize_inGB<400, ],mapping =</pre>
→ aes(x = RomSize_inGB, y = Price)) + geom_point(alpha=0.3) +

    geom_smooth(se=T,method = lm) +

  labs(y="Price in Rupees", x="Rom Size in GB", subtitle="Relation between Rom size
    (in GB) and price")
grid.arrange(plot1, plot2, ncol=2)
## `geom_smooth()` using formula 'y ~ x'
## `geom_smooth()` using formula 'y ~ x'
```



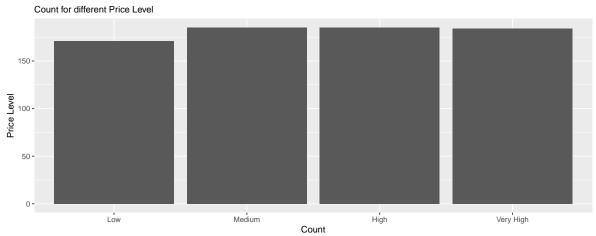
Chapter 2: Predicting the Mobile Phone Price Level

2.1: Prediction of Mobile Phone Price Level

In this section, we will use a range of statistical models to predict mobile phone price level: "Low", "Medium", "High", "Very High" based on some selected features.

- Linear Discriminant Analysis (LDA)
- Quadratic Discriminant Analysis (QDA)
- Decision Tree (Classification)
- Multinomial Regression

First, let use explore the distribution for difference price level. From the following bar plot, you can see it is very close to uniformly distributed across the dataset. Balanced dataset is important for us when we do the classification.



2.1.1 Quadratic Discriminant Analysis (LDA) We want to use LDA to classify our observations into mobile phone price level: "Low", "Medium", "High", "Very High". However, we know LDA has 2 assumptions:

- The distribution of the predictors is normally distributed within each group.
- The homogeneity of variance-covariance matrices

Based on EDA in section 4.2, we know three **numeric features** have a great impact on price level a mobile phone belongs to, which are Rating, $RamSize_inGB$ and $RomSize_inGB$. As such, we will do a test for normal distribution for each predictor in each price level. Because we have 4 different price levels and 3 variables, the resulting normality check would be 4*3 = 12 comparison. We use Q-Q plot and Shapiro test for normality check.

```
variables <- c("Rating", "RamSize_inGB", "RomSize_inGB")</pre>
par(mfrow = c(1,3))
for (i in variables){
   qqnorm(mobile_dataset_low[[i]], main = paste("Price Level LOW, Normal Q-Q Plot

  for", i))

   qqline(mobile_dataset_low[[i]], col = 3)
}
       Price Level LOW, Normal Q-Q Plot for Rating
                                               Price Level LOW, Normal Q-Q Plot for RamSize_inGB
                                                                                          Price Level LOW, Normal Q-Q Plot for RomSize_inGB
                                              2.5
Sample Quantiles
                                           Sample Quantiles
                                                                                       Sample Quantiles
                                              2.0
                                                                                         40
                                             1.0 1.5
  3.5
                                                                                         30
                                                                                         20
   3.0
                                              0.5
                                              0.0
                                                            Theoretical Quantiles
                                                                                                       Theoretical Quantiles
par(mfrow = c(1,3))
for (i in variables){
   qqnorm(mobile_dataset_medium[[i]], main = paste("Price Level Medium, Normal Q-Q
    → Plot for", i))
   qqline(mobile_dataset_medium[[i]], col = 3)
}
      Price Level Medium, Normal Q-Q Plot for Rating
                                             Price Level Medium, Normal Q-Q Plot for RamSize_inGB
                                                                                        Price Level Medium, Normal Q-Q Plot for RomSize_inGB
   4.5
                                                                                      Quantiles
                                                                                        9
                                           Sample Quantiles
Sample Quantiles
                                             9
  4.0
                                                                                        80
  3.5
                                                                                      Sample
                                                                                        9
   3.0
                                                                                                       Theoretical Quantiles
par(mfrow = c(1,3))
for (i in variables){
   qqnorm(mobile_dataset_high[[i]], main = paste("Price Level High, Normal Q-Q Plot

  for", i))

   qqline(mobile_dataset_high[[i]], col = 3)
}
       Price Level High, Normal Q-Q Plot for Rating
                                               Price Level High, Normal Q-Q Plot for RamSize_inGB
                                                                                          Price Level High, Normal Q-Q Plot for RomSize_inGB
                                                                                         250
   4.4
                                                                                         200
Sample Quantiles
  4.2 4.3
                                                                                      Sample Quantiles
                                           Sample Quantiles
                                                                                         150
   4.0 4.1
                                                                                         8
par(mfrow = c(1,3))
for (i in variables){
```

```
qqnorm(mobile_dataset_high[[i]], main = paste("Price Level Very High, Normal Q-Q
  → Plot for", i))
  qqline(mobile_dataset_high[[i]], col = 3)
}
   Price Level Very High, Normal Q-Q Plot for Rating
                                 Price Level Very High, Normal Q-Q Plot for RamSize inGE Price Level Very High, Normal Q-Q Plot for RomSize inGE
                                                                   250
  4.4
                                                                   200
                                                                Sample Quantiles
Sample Quantiles
                                Sample Quantiles
  4.3
  4.2
                                                                   150
  4.
                                                                   90
  4.0
#We also run the shapiro test to statistically conclude the result
p_value_rating <- c(shapiro.test(mobile_dataset_low$Rating)$p.value,</pre>
    shapiro.test(mobile_dataset_medium$Rating)$p.value,
                       shapiro.test(mobile dataset high$Rating)$p.value,
                       shapiro.test(mobile_dataset_very_high$Rating)$p.value)
p_value_RamSize_inGB <- c(shapiro.test(mobile_dataset_low$RamSize_inGB)$p.value,
    shapiro.test(mobile_dataset_medium$RamSize_inGB)$p.value,
                       shapiro.test(mobile_dataset_high$RamSize_inGB)$p.value,
                       shapiro.test(mobile_dataset_very_high$RamSize_inGB)$p.value)
p_value_rating_RomSize_inGB <-</pre>
    c(shapiro.test(mobile_dataset_low$RomSize_inGB)$p.value,
    shapiro.test(mobile_dataset_medium$RomSize_inGB)$p.value,
                       shapiro.test(mobile_dataset_high$RomSize_inGB)$p.value,
                       shapiro.test(mobile_dataset_very_high$RomSize_inGB)$p.value)
p_value_df <-

→ data.frame(p_value_rating,p_value_RamSize_inGB,p_value_rating_RomSize_inGB)

rownames(p_value_df) <- c("Low", "Medium", "High", "Very High")</pre>
p_value_df
##
               p_value_rating p_value_RamSize_inGB p_value_rating_RomSize_inGB
## Low
                 1.470349e-10
                                         1.875399e-22
                                                                         7.757042e-23
```

Based on the Q-Q plots (dots not fall on the line) and Shapiro test (p value is < 5%), we can conclude that all variables are not normal. Therefore, we will not preceded with LDA model. Although Quadratic Discriminant Analysis (QDA) also requires normality assumption, we still want to try QDA (in the next section) since it normally has less strict assumptions. NOTE, the above code is inspired by Pascal Schmidt from post Assumption Checking of LDA vs. QDA – R Tutorial Pima Indians Data Set.

2.1.2 Quadratic Discriminant Analysis (QDA)

In consistent with LDA, we use the same three numeric features that have a great impact on price level a mobile phone belongs to, which are *Rating*, *RamSize_inGB* and *RomSize_inGB*. To that end, we split the dataset into 75% for training and 25% for testing purpose. We use each "Price_Level" as the stratum and the proportional allocation principle to get a stratified sample. Then we fit the data into Quadratic Discriminant Analysis (QDA) as follows:

```
set.seed(2023)
Ny <- round(table(mobile_dataset$Price_Level)[unique(mobile_dataset$Price_Level)]*
#Create the sample from the population
idx=sampling:::strata(mobile_dataset, stratanames=c("Price_Level"), size=Ny,

→ method="srswor")

strata_sample <- getdata(mobile_dataset,idx)</pre>
train <- mobile_dataset[idx$ID_unit,]</pre>
test <- mobile_dataset[-idx$ID_unit,]</pre>
#Train the data using Quadratic Discriminant Analysis
Model.fit<-qda(Price Level~Rating+RamSize inGB+RomSize inGB, data = train)
Model.fit
cat(rep("-", 50), "\n")
#This plot is showing that LD1 can do a really good to separate these species rather
\rightarrow than LD2
# partimat(Price Level~Rating+RamSize inGB+RomSize inGB, data = train, method="qda")
## Call:
## qda(Price_Level ~ Rating + RamSize_inGB + RomSize_inGB, data = train)
## Prior probabilities of groups:
                Medium
                            High Very High
##
         Low
## 0.2352941 0.2555147 0.2555147 0.2536765
##
## Group means:
##
               Rating RamSize_inGB RomSize_inGB
## Low
             4.012500 0.3342734 5.949688
             4.237410
                          3.8201439
                                       62.848921
## Medium
## High
             4.276259
                         5.6258993
                                    113.266187
## Very High 4.341304
                          5.5797536
                                      142.376812
At last, we apply this model on the testing dataset, and calculate the misclassification rate.
Prob.predict<-predict(Model.fit,test,type="response")</pre>
ggplot(as.data.frame(table(Prob.predict$class,test$Price_Level)), aes(x = Var1, y =
```

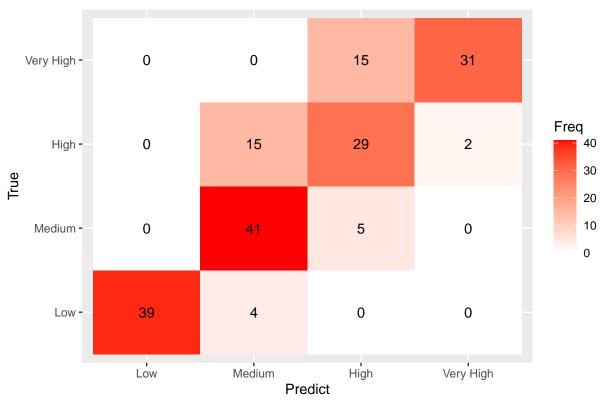
```
Prob.predict<-predict(Model.fit,test,type="response")
ggplot(as.data.frame(table(Prob.predict$class,test$Price_Level)), aes(x = Var1, y =

\( \to Var2, \) fill = Freq)) +geom_tile() + geom_text(aes(label = round(Freq, 1))) +

\( \to \) scale_fill_gradient(low = "white", high = "red") + labs(y="True", x="Predict",

\( \to \) subtitle="Confusion Matrix for Classification Tree")
```

Confusion Matrix for Classification Tree



```
cat(rep("-", 45), "\n")
cat("The misclassification rate for QDA is: ", mean(Prob.predict$class !=

    test$Price_Level))
```

The misclassification rate for QDA is: 0.2265193

Conclusion: Quadratic Discriminant Analysis has a good performance to predict the mobile phone price level using only 3 variables (Rating, RamSize_inGB and RomSize_inGB), with a relatively high accuracy (77%).

2.1.3 Decision Tree (Classification)

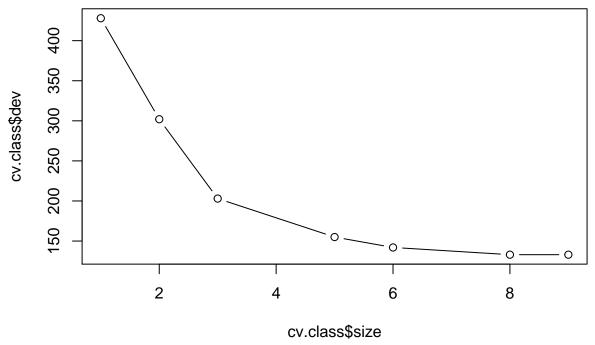
To be consistent and comparable with QDA, we again use these three variables Rating, $RamSize_inGB$ and $RomSize_inGB$ to build the decision tree model. We split the dataset into 75% for training and 25% for testing purpose. We use each "Price_Level" as the stratum and the proportional allocation principle to get a stratified sample. Then we fit the data into Classification tree model as follows:

```
#Fit the train data into the tree model
tree.class<-tree(factor(Price_Level)~Rating+RamSize_inGB+RomSize_inGB, train)</pre>
summary(tree.class)
##
## Classification tree:
## tree(formula = factor(Price_Level) ~ Rating + RamSize_inGB +
       RomSize_inGB, data = train)
## Variables actually used in tree construction:
## [1] "RomSize inGB" "RamSize inGB"
## Number of terminal nodes: 9
## Residual mean deviance: 1.055 = 564.3 / 535
## Misclassification error rate: 0.2335 = 127 / 544
The tree is plotted without pruning as follows. There are a total of 9 terminal nodes in the tree.
#Let us plot the tree as well
plot(tree.class)
text(tree.class,pretty=0)
RamSize inGB < 1.256
                                     RomSize linGB < 96
            Medium RamSize_inGB < 2.5 RamSize_inGB < 2.003 RamSize_inGB < 7 Very High Medium High Very High High Very High
# rpart_fit <- rpart(factor(Price_Level)~Rating+RamSize_inGB+RomSize_inGB, train,
```

To find the best tree size, we used cross-validation to select the "best" number of tree size (the terminal nodes). Based on the following plot, it seems tree size 9 gives the smallest deviance. Just to demonstrate how prunned tree works and also reduce the complexity of tree, we decide to use 8 as the "best" tree size.

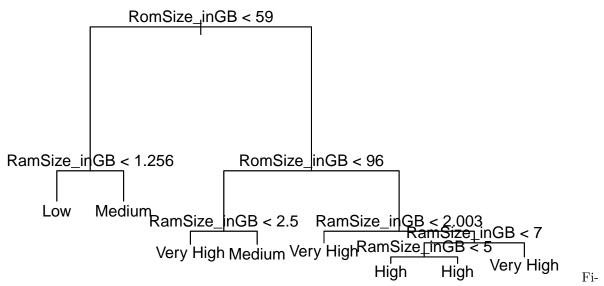
→ method = 'class')
rpart.plot(rpart fit)

```
cv.class<-cv.tree(tree.class, FUN = prune.misclass)
plot(cv.class$size, cv.class$dev,type="b")</pre>
```



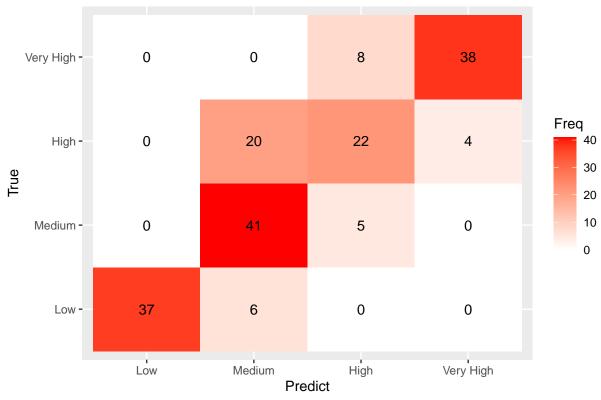
A tree after prunning is plotted as follows. There are a total of 8 terminal nodes in the tree.

```
prune.class=prune.tree(tree.class,best=8)
plot(prune.class)
text(prune.class,pretty=0)
```



nally, we use the pruned tree to do prediction.

Confusion Matrix for Classification Tree



```
cat(rep("-", 45), "\n")
cat("The misclassification rate for regression tree is: ", mean(prune.pred !=
    test$Price_Level))
```

The misclassification rate for regression tree is: 0.2375691

Conclusion: Decision Tree (Classification) has also a good performance to predict the mobile phone price level using only 3 variables (*Rating*, *RamSize_inGB* and *RomSize_inGB*), with a relatively high accuracy (76.2%).

2.1.4 Multinomial Regression

This is an experimental analysis. Based on EDA in section 4.2, we know that Company name (branding) also plays a big role in the price level. We also know that Rom size of a mobile phone matters a lot as well. We are curious to see if a combination of *Company* and *RomSize* can also be used to distinguish the price level.

Normally, we would split the dataset into 75% for training and 25% for testing purpose. However, because our sample size is small, not every Company has multiple records in our dataset. Therefore, in the following test, we use whole sample as the training and test purpose.

Then we fit the data into Multinomial Regression as follows. Note, because our response is ordinal, we use Cumulative logit model; also parallel = TRUE: means beta is the same, this is a simple model.

We also use Chi square test to test for the goodness-of-fit for this model.

 H_0 : The Cumulative logit model fits the observations

H_1 : The Cumulative logit model does not fit the observations

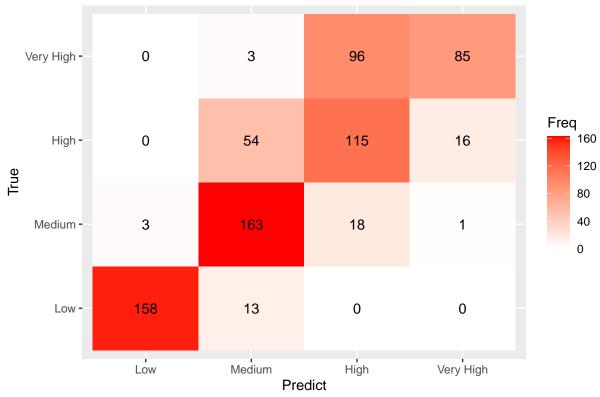
The p value for the chi test is: 1

The p-value here is large = 1, so we cannot reject null hypothesis. Our model seems to be provide

Finally, we use this model to predict use the same training dataset, as a demonstration purpose.

```
pred_fit <- predict(multi_train_fit, type="response")
#Use the record that has the highest probability as the final predication for each
    row.
pred_fit_class <-factor(dimnames(pred_fit)[[2]][max.col(pred_fit, 'first')], levels
    = c("Low", "Medium", "High", "Very High"))
ggplot(as.data.frame(table(pred_fit_class, mobile_dataset$Price_Level)), aes(x =
    pred_fit_class, y = Var2, fill = Freq)) +geom_tile() + geom_text(aes(label =
    round(Freq, 1))) + scale_fill_gradient(low = "white", high = "red") +
    labs(y="True", x="Predict", subtitle="Confusion Matrix for Classification Tree")</pre>
```

Confusion Matrix for Classification Tree



Conclusion: Multinomial Regression has also a good performance to predict the mobile phone price level using only 2 variables (*Company* and *RomSize*), with a relatively high accuracy (71.9%).

2.2: Cross-Validation

In section 2.1, we have compared three different models based on their misclassification rate: **Quadratic Discriminant Analysis** (**QDA**) = 0.2265193, **Decision Tree** (**Classification**) = 0.2375691, and **Multinomial Regression** = 0.2813793. In order to compare model performance, we decide to also use stratified 10-fold cross-validation to calculate the cross-validation errors of these 3 methods.

```
cat("\nFirst I am using the 10-fold cross validation for Quadratic Discriminant
→ Analysis")
set.seed(2023)
#Create 10 folds
folds<-createFolds(mobile_dataset$Price_Level, k=10)</pre>
#Define a function to calculate the misclassification rate for each fold
misrate_fold<-function(idx){</pre>
  Train<-mobile_dataset[-idx,]</pre>
  Test<-mobile_dataset[idx,]</pre>
  fit <- qda(Price_Level~Rating+RamSize_inGB+RomSize_inGB, data = Train)</pre>
  pred<-predict(fit,Test)</pre>
  return(1- mean(pred$class == Test$Price_Level))
}
#Get the misclassification rate from each fold
type_misrate_fold=lapply(folds,misrate_fold)
#The average of misclassification rate for 10 folds is:
cat("\nThe average of misclassification rate for 10 folds
    cross validation of Quadratic Discriminant Analysis is :",
    mean(as.numeric(type_misrate_fold)))
cat("\n")
cat(rep("-", 45), "\n")
cat("\nSecond I am using the 10-fold cross validation for Decision Tree
set.seed(2023)
#Create 10 folds
folds<-createFolds(mobile_dataset$Price_Level, k=10)</pre>
#Define a function to calculate the misclassification rate for each fold
misrate_fold<-function(idx){</pre>
  Train<-mobile_dataset[-idx,]</pre>
  Test<-mobile_dataset[idx,]</pre>
  fit <- tree(factor(Price Level)~Rating+RamSize inGB+RomSize inGB, data = Train)
  pred<-predict(fit,Test, type = 'class')</pre>
  return(1- mean(pred == Test$Price_Level))
}
#Get the misclassification rate from each fold
```

```
type misrate fold=lapply(folds, misrate fold)
#The average of misclassification rate for 10 folds is:
cat("\nThe average of misclassification rate for 10 folds cross
    validation of Decision Tree (Classification) is :",
  mean(as.numeric(type_misrate_fold)))
cat("\n")
cat(rep("-", 45), "\n")
cat("\nBecause our sample size is small, not every Company has multiple records in
\hookrightarrow our dataset. \nTherefore, we are not able to perform cross-validation for
   Multinomial regression.")
##
## First I am using the 10-fold cross validation for Quadratic Discriminant Analysis
## The average of misclassification rate for 10 folds
       cross validation of Quadratic Discriminant Analysis is: 0.2690109
## - -
##
## Second I am using the 10-fold cross validation for Decision Tree (Classification)
## The average of misclassification rate for 10 folds cross
##
       validation of Decision Tree (Classification) is: 0.2314057
## - -
##
## Because our sample size is small, not every Company has multiple records in our dataset.
## Therefore, we are not able to perform cross-validation for Multinomial regression.
```

2.3: Summary for Prediction of Mobile Phone Price Level

To summarize this part of analysis, we find some contradictory results. We used the balanced dataset trying to classify the Mobile Phone Price Level. In Section 2.1, we have the following misclassification rate from each model:

- Quadratic Discriminant Analysis (QDA): 0.2265193
- Decision Tree (Classification): 0.2375691
- Multinomial Regression: 0.2813793

We can see Quadratic Discriminant Analysis (QDA) gives the lowest misclassification rate, making this model the best one. However, when we do the 10-folds cross validation, we have the following misclassification rate from each model:

- Quadratic Discriminant Analysis (QDA): 0.2690109
- Decision Tree (Classification): 0.2314057
- Multinomial Regression: Not Available (see section 2.2 explanation)

From this result, Decision Tree (Classification) gives the lowest misclassification rate. Because cross-validation is averaging multiple misclassification rate, we think this result is more reliable.

So our final conclusion is that Decision Tree (Classification) can best predict the Mobile Phone Price Level using only 3 variables (Rating, RamSize_inGB and RomSize_inGB), with a relatively high accuracy (76.9%).

Chapter 3: Phone Company Categorization

The goal of this section is to look at categorization of phones that fall within the most expensive bracket. Among these phones are Apple, Google, Samgsung, Vivo and Iqoo. Initially, we wanted to look at categorizing Apple, Google and Samgsung, but the number of entries of Google in the dataset prevented us from using them (Unable to split Google into testing and training). For this reason, we included Vivo and Iqoo. For categorization, we chose to compare four different classification methods: LDA, QDA, Logistic Regression and an Bayesian Classifier and KNN.

The first step prior to building the different classifiers was to read in the data into r.

```
cellphone = mobile_dataset
```

3.1: Manipulation of the dataframe prior to categorization

With the dataset in r, we are now able to reduce our dataframe to only contain the different companies which we want to perform classification on.

The next step is to chose which classifiers we want to use to perform analysis. Through playing around with the different attributes in the dataset, the rating, Price, number of ratings, total reviews and Rom Size were chosen as the variables used to classify company. Color was also considered, but since there are so many different unique colors, the test set would always contain a color not seen in training and the model would not function. With some possible exceptions, the color of the phone is likely not proprietary to the company and thus isn't crucial for categorization.

In order to test some of the assumptions required to use the aforementioned classification methods, the order of the columns is changed so that company, our dependant variable, appears in the last column of the data frame.

```
order<- df2[,c(6,2,3,4,5,1)]
order$Company <- as.factor(as.character(order$Company))</pre>
```

3.2: Testing Assumptions

First, we will test the assumption of homogeneity of covariance matrices. Homogeneity of covariance matrices is required to use LDA as a classification method. We can test for Homogeneity using the boxM test.

The hypotheses for the test are as follows:

 H_0 : The observed covariance matrices for the dependent variables are equal across groups

 H_a : The observed covariance matrices for the dependent variables are NOT equal across groups

```
library(heplots)
```

```
## Loading required package: car
```

```
## Loading required package: carData
##
## Attaching package: 'car'
## The following object is masked from 'package:dplyr':
##
##
       recode
## The following object is masked from 'package:purrr':
##
##
## The following object is masked from 'package: VGAM':
##
##
## Loading required package: broom
boxM(order[,1:5], order$Company)
##
##
    Box's M-test for Homogeneity of Covariance Matrices
##
## data: order[, 1:5]
## Chi-Sq (approx.) = 509.88, df = 45, p-value < 2.2e-16
```

We can see that since P is very small, we reject the null hypothesis in favor of the alternate hypothesis, indicating we have heterogeneity of covariance matrices. Our assumption of homogeneity of covariance matrices for LDA therefor is not met.

We can try to normalize the data to see if it has an impact on the result.

Normalization using the scale function has no effect on changing making the covariance matrices homogeneous.

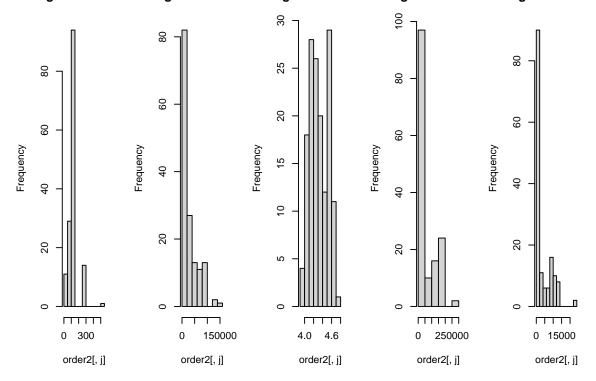
The covariance matrices do not need to be homogeneous to use QDA, but one of the assumptions of QDA is a Gaussian distribution of the independent variables.

```
order2 = order[,1:5]
order2 <- as.matrix(order2[,1:5])</pre>
```

We are able to visualize the distribution of the independent variable by using histograms of each of the data points.

```
par(mfrow = c(1, ncol(order2)))
for(j in 1:ncol(order2)){
  hist(order2[,j])}
```

Histogram of order:Histogram of order:Histogram of order:Histogram of order:



From the histograms, Price, number of ratings and the total reviews do not appear to follow a normal distribution. We can use the Shapiro-Wilk normality test to validate these results.

Below is the null hypothesis for the test.

 H_0 : The data follow a Gaussian distribution H_a : The data does NOT follow a gaussian distribution

```
library(mvnormtest)
mshapiro.test(t(order2))
```

```
##
## Shapiro-Wilk normality test
##
## data: Z
## W = 0.83086, p-value = 7.943e-12
```

From p-value = 7.943e-12, we reject the null hypothesis in favor of the alternate hypothesis indicating that the independent variables do not follow a normal distribution.

We also need to test to see if multicollinearity is present in our predictors.

```
faraway::vif(order2)

## RomSize_inGB Price Rating No_of_ratings TotalReviwes
```

```
## 1.497726 3.018487 3.426773 31.038830 28.122784
```

It appears we need to remove number of ratings from our model because there is multicollinearity.

3.3: Comparing Classifiers

##

##

##

APPLE

IQOO

3.3.1: LDA and QDA Classification

While we have not met all the assumptions for LDA and QDA, we will try and do a classification using these methods regardless and look at the misclassification rates as a metric of their performance.

```
library (MASS)
library(ISLR)
set.seed(10)
sample <- sample(c(TRUE, FALSE), nrow(order2), replace=TRUE, prob=c(0.7,0.30))</pre>
train <- order3[sample, ]</pre>
       <- order3[-sample, ]
test
qda.fit<-qda(Company~Rating+Price+TotalReviwes+RomSize_inGB, data = train)
lda.fit<-lda(Company~Rating+Price+TotalReviwes+RomSize_inGB, data = train)</pre>
# Testing the LDA classifier with the test data
lda.pred=predict(lda.fit, test)
table(lda.pred$class, test$Company)
##
             APPLE IQOO SAMSUNG VIVO
##
##
     APPLE
                 46
                       0
                               0
                                     0
##
     IQOO
                  0
                       0
                                0
                                     0
##
     SAMSUNG
                  0
                       7
                               47
                                    14
##
     VIVO
                  0
                       1
                                    20
mean(lda.pred$class != test$Company)
## [1] 0.2364865
The misclassification rate with Lda is 0.2364865.
#Testing the QDA classifier with the test data
qda.pred=predict(qda.fit, test)
table(qda.pred$class, test$Company)
##
```

APPLE IQOO SAMSUNG VIVO

0

0

0

5

46

0

```
## SAMSUNG 0 3 40 9
## VIVO 0 0 19 25
mean(qda.pred$class != test$Company)
```

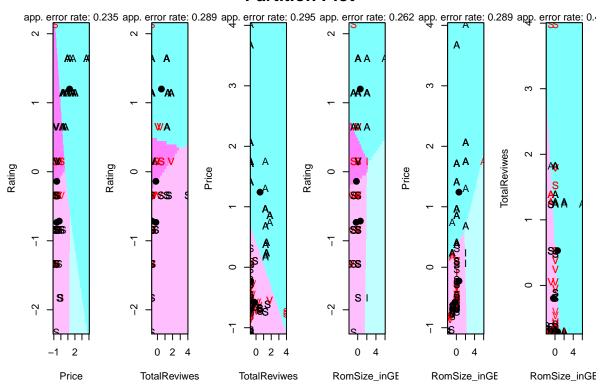
[1] 0.2162162

The misclassification rate with qda is 0.2162162.

We are also able to visualize how LDA and QDA separate the data using klaR's partimat function. Using this tool it's possible to visualize how each of the different independent variables categorizes the company. It's also an important observation to notice how LDA makes distinctions with linear sections, where as the different sections of QDA are much more curved, hens 'quadratic'.

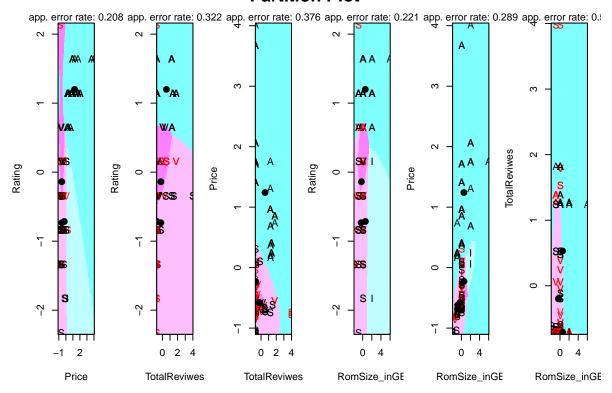
Below is the lDA partiton plot.

Partition Plot



Below is the QDA partition plot.

Partition Plot



Recall that linearity was not achieve with price, number of ratings and total reviews, so QDA will be tested again after removing these predictors to see if the result is improved.

```
#removal of non-linear predictors
order4 <- order3[, (names(order3) %in% c("Rating", "RomSize_inGB", "Company"))]</pre>
```

Building the training and test data for the QDA classifier with only rating and RomSize_inGB as independent variables.

```
set.seed(10)

sample <- sample(c(TRUE, FALSE), nrow(order4), replace=TRUE, prob=c(0.7,0.30))
trainQ <- order4[sample, ]
testQ <- order4[-sample, ]

qda.fit<-qda(Company~Rating+RomSize_inGB, data = trainQ)</pre>
```

Applying the QDA classification model to the test set.

```
qda.pred=predict(qda.fit, testQ)
table(qda.pred$class, test$Company)
```

```
##
               APPLE IQOO SAMSUNG VIVO
##
     APPLE
                  44
                                         2
##
                         0
                                   1
                                   0
                                         0
##
     IQOO
                   0
                         1
                         7
                   0
                                        13
##
     SAMSUNG
                                  48
##
     VIVO
                   2
                         0
                                        19
                                  11
```

```
mean(qda.pred$class != test$Company)
```

```
## [1] 0.2432432
```

We can see that the misclassification rate has not changed significantly, and has increased to 0.2432432. Therefor, rating will not be removed from the predictors used in QDA.

3.3.2: Classification using Logistic Regression

Moving from LDA and QDA, we can look to see whether a logistic regression classifier has improved classification accuracy. We will use the same predictors as LDA and QDA to have a fair comparison of misclassification rates.

```
misclassification rates.
require(foreign)
## Loading required package: foreign
require(nnet)
## Loading required package: nnet
require(ggplot2)
require(reshape2)
## Loading required package: reshape2
## Attaching package: 'reshape2'
## The following object is masked from 'package:tidyr':
##
##
       smiths
library(VGAM)
Model.fit<-multinom(Company~Rating+Price+TotalReviwes+RomSize_inGB, data = train)</pre>
## # weights: 24 (15 variable)
## initial value 153.878674
## iter 10 value 50.014668
## iter 20 value 41.385169
## iter 30 value 39.045159
## iter 40 value 38.974093
## iter 50 value 38.974050
## iter 60 value 38.969317
## iter 60 value 38.969317
## iter 60 value 38.969317
## final value 38.969317
## converged
Prob.predict<-predict(Model.fit, test)</pre>
Actual<-test$Company</pre>
table(Prob.predict, Actual)
```

Actual

```
## Prob.predict APPLE IQOO SAMSUNG VIVO
##
        APPLE
                     46
                           0
                                    0
                                          0
##
        IQOO
                      0
                           5
                                    0
                                          0
##
        SAMSUNG
                      0
                           3
                                   52
                                        16
##
        OVIV
                      0
                           0
                                        18
mean(Prob.predict != Actual)
```

```
## [1] 0.1824324
```

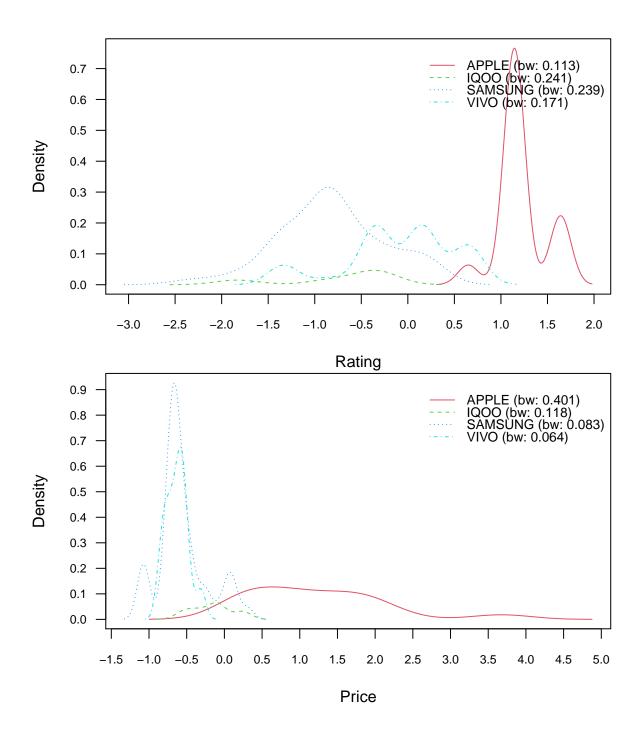
We can see that logistic regression worked better than both LDA and QDA, with a misclassification rate of 0.1824324. This increased performance with logistic regression could be a result of the assumtion of homogenous covariance matrices not being met for LDA and doesn't assume the distribution of the data to be Gaussian like QDA.

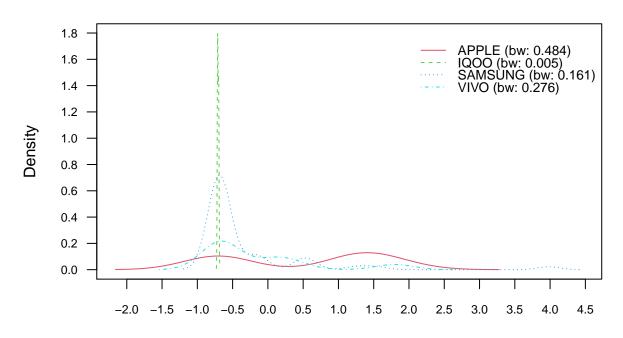
3.3.3: Naive Bayes Classification

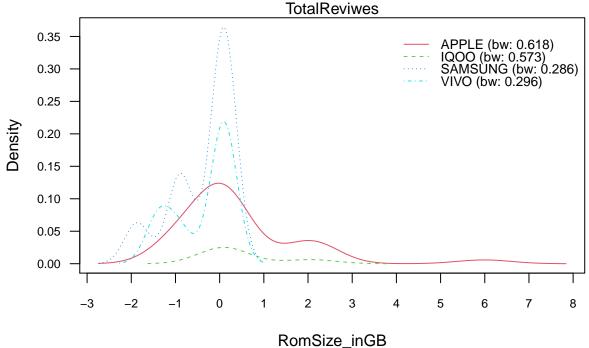
We will use Naive Bayes to see how it compares to LDA, QDA as well as logistic regression. Included below are the plots to show how the Naive Bayes Classifier works with the density of each of the different companies for a given variable.

```
library(naivebayes)
```

```
## naivebayes 0.9.7 loaded
```







Now to use naive bayes to predict

```
pred <- predict(modelbayes, test2)</pre>
```

Warning: predict.naive_bayes(): more features in the newdata are provided as
there are probability tables in the object. Calculation is performed based on
features to be found in the tables.

(tab1 <- table(pred, test2\$Company))</pre>

```
##
              APPLE IQOO SAMSUNG VIVO
## pred
##
     APPLE
                  46
                        0
                                 0
                        5
                                 9
                                       0
##
     IQOO
                   0
##
     SAMSUNG
                   0
                         3
                                41
                                       9
     VIVO
                         0
                                      25
##
                   0
                                10
mean(pred != test2$Company)
```

```
## [1] 0.2094595
```

We can see that the misclassification using Naive Bayes is 0.2094595 on the test set. This is less accurate than multinomial logistic regression but performed better than LDA and QDA.

Why did Naive bayes perform worse than multinomial logistic regression? One of the reasons may be the feature independence assumption. We can check the correlation between the variables.

```
print(cor(cellphone[, c('Rating','Price','TotalReviwes','RomSize_inGB')]))
```

```
##
                   Rating
                               Price TotalReviwes RomSize_inGB
## Rating
                1.0000000 0.70804693
                                       0.42640871
                                                     0.37322466
## Price
                0.7080469 1.00000000
                                       0.04769482
                                                     0.57338900
## TotalReviwes 0.4264087 0.04769482
                                        1.0000000
                                                     0.01339623
## RomSize_inGB 0.3732247 0.57338900
                                       0.01339623
                                                     1.0000000
```

Clearly we have correlation between the independent variables used in the categorization of the phones. For this reason it may not be appropriate to use Naive Bayes for Classification.

We can try removing the rating out of the predictors since there is a high correlation with the others.

Now to use naive bayes to predict

```
pred2 <- predict(modelbayes2, test3)</pre>
```

```
## Warning: predict.naive_bayes(): more features in the newdata are provided as
## there are probability tables in the object. Calculation is performed based on
## features to be found in the tables.
```

```
(tab2 <- table(pred2, test3$Company))</pre>
```

```
##
## pred2
              APPLE IQOO SAMSUNG VIVO
                  43
                        0
                                 0
                                       0
##
     APPLE
##
     IQ00
                   3
                        6
                                10
                                       0
                        2
     SAMSUNG
                   0
##
                                48
                                      15
```

```
##
     VIVO
                               2
                                   19
mean(pred2 != test3$Company)
```

```
## [1] 0.2162162
```

The misclassification rate increased slightly when removing rating as one of the predictors. For this reason, we will leave rating in the classifier.

3.3.4: Evaluating the classification performance of KNN.

We can also look at KNN, which is a non parametric classifier that does not make assumptions on the underlying distribution of the data.

We will perfome multiple runs of KNN, and varying the number of nearest neighbours k, in the classifier

```
for each run to determine the most accurate classifier.
# Loading package
library(e1071)
library(caTools)
library(class)
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],</pre>
                       test = test[,1:4],
                       cl = train$Company,
                       k = 11)
# Confusion Matrix
cm <- table(test$Company, classifier_knn)</pre>
cm
##
             classifier_knn
##
             APPLE IQOO SAMSUNG VIVO
##
     APPLE
                 46
                     0
                                0
                                     0
                                7
##
     IQOO
                  0
                       0
                                     1
##
                  2
                       0
     SAMSUNG
                               45
                                    13
##
     OVIV
                  3
                       0
                               15
                                    16
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)</pre>
misClassError
## [1] 0.277027
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],</pre>
                       test = test[,1:4],
                       cl = train$Company,
                       k = 9)
# Confusion Matrix
```

```
cm <- table(test$Company, classifier_knn)</pre>
cm
##
            classifier_knn
##
            APPLE IQOO SAMSUNG VIVO
             46
##
    APPLE
                   0 0
##
    IQOO
                0
                   1
                             7
                                  0
               2 0
##
    SAMSUNG
                            48
                               10
    VIVO
                0
                                 18
##
                     0
                            16
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)</pre>
misClassError
## [1] 0.2364865
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],</pre>
                     test = test[,1:4],
                     cl = train$Company,
                     k = 7)
# Confusion Matrix
cm <- table(test$Company, classifier_knn)</pre>
           classifier knn
##
           APPLE IQOO SAMSUNG VIVO
##
## APPLE
             46 0 0
## IQ00
                0 1
                            7
                                  0
##
    SAMSUNG
               1 0
                            53
##
   VIVO
                0
                     0
                            12
                                 22
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)</pre>
misClassError
## [1] 0.1756757
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],</pre>
                     test = test[,1:4],
                     cl = train$Company,
                     k = 5)
# Confusion Matrix
cm <- table(test$Company, classifier_knn)</pre>
cm
##
            classifier_knn
            APPLE IQOO SAMSUNG VIVO
##
   APPLE
              46 0
                            0
##
```

```
##
     IQOO
                        2
                                      0
##
     SAMSUNG
                  0
                        0
                               49
                                     11
##
     VIVO
                  0
                        1
                                     26
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)
misClassError
## [1] 0.1689189
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],</pre>
                        test = test[,1:4],
                        cl = train$Company,
                       k = 3
# Confusion Matrix
   <- table(test$Company, classifier_knn)</pre>
cm
##
             classifier_knn
##
              APPLE IQOO SAMSUNG VIVO
##
     APPLE
                 46
                        0
                                0
                                      0
##
     IQOO
                  1
                        2
                                5
                                      0
##
     SAMSUNG
                  0
                        0
                               49
                                     11
     OVIV
                  0
                        1
                                3
                                     30
##
# Calculate out of Sample error
misClassError <- mean(classifier knn != test$Company)
misClassError
```

[1] 0.1418919

We can see from our results that the most accurate classifier is when k = 5.

3.4: Results from Classifier Predictions.

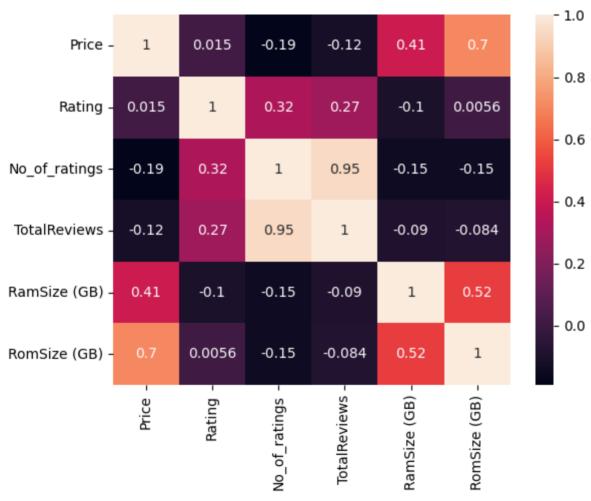
In conclusion, we have evaluated five different classifiers, including K-nearest neighbors (KNN), Naive Bayes, logistic regression, Quadratic Discriminant Analysis (QDA), and Linear Discriminant Analysis (LDA), on a dataset that did not follow a Gaussian distribution and had unequal covariance matrices as well as correlation between predictors. Our results show that KNN had the lowest misclassification rate of 0.16, followed by logistic regression at 0.18, QDA and Naive Bayes at 0.21, and LDA at 0.24. These findings suggest that KNN and logistic regression may be effective classifiers for non-Gaussian and non-equal covariance data, while QDA, Naive Bayes, and LDA may not perform as well.

Chapter 4: Dimensionality Reduction

We should emphasize that this part of the analysis is not particularly useful in a dataset with less than 10 predictors like ours. It was still carried for its value as a learning exercise. This point was brought up and addressed during our presentation. With that in mind let's go through the motions.

4.1: Principal component analysis

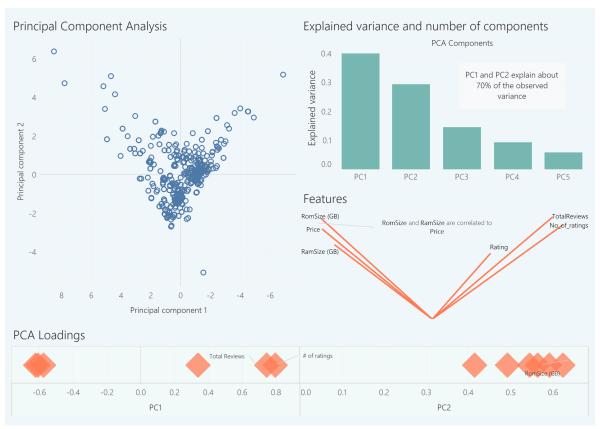
PCA is a tool that projects a collection of vectors into a a new vector space of fewer orthogonal dimensions. This projection can be simpler to fit using a linear model but much harder to interpret: the new predictors are going to be linear combinations of the original predictors and may not have a direct interpretation. To carry out a PCA one must have correlation among features,



PCA is sensitive to outliers and scale. This means that if our numerical predictors have different units or span different orders of magnitude we need to re-scale it. For every predictor, this is accomplished by simply subtracting the mean and dividing by its standard deviation. In python, the library *scikit learn* support different types of scaling out of the box. It can also perform PCA,

```
from sklearn.decomposition import PCA
pca = PCA(n_components = 2)
principal_components = pca.fit_transform(df_scaled)
```

The following figure summarizes the results,



We can see that about 70% of the variance can be explained by projecting onto a 2D space. To use this in a prediction scenario we'd have to setup a pipeline that follows this workflow,

- 1) Rescale
- 2) Map from the original predictor/response space to the new PC space using a a linear transformation
- 3) Apply the model (predict)
- 4) Rescale result
- 5) Map from PC to original predictor/response space

This is less of a hassle when dealing with many predictors and the gains from dimensionality reduction are tangible.

Chapter 5: Predicting the Selling Price of Mobile Phones

Now, after we have a better understanding of the data, we can start building a model to predict the price of a mobile phone. First, we will build a Multiple Linear Regression model to predict the price of a mobile phone to see if there are linear relationships between Price and dependent variables. Before we start, here are some steps we will take: 1. Split the data into training and test sets. 2. Explore collinearity between the variables. 3. Build a base valid model. 4. If there is noticable pattern in the residual plot, introduce interaction terms and higher order terms. 5. Check the assumptions of the model. 6. If any of the assumptions are violated, try to fix them with transformations and outliers removal.

At each stage of the model building process, we will check the performance of the model using the test set.

In case the multiple linear regression model does not perform well, or the relationship is non-linear we will build a Regression Tree that can model more complex relationships between the variables.

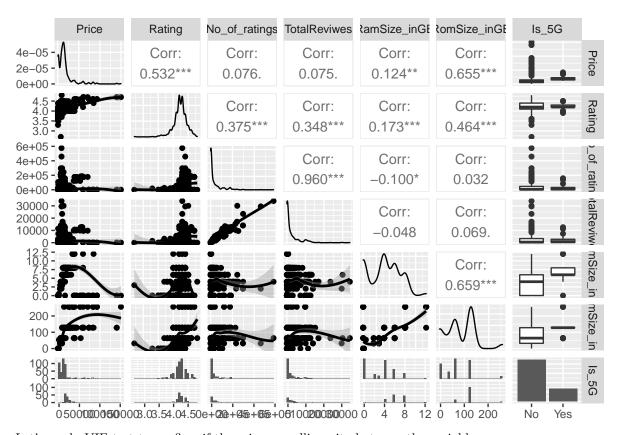
5.1: Multiple Linear Regression

5.1.1: Building a base model

As our initial step, we will use the following variables as predictors: Rating, No_of_ratings, TotalReviwes, RamSize_inGB, RomSize_inGB, Is_5G. We will not use Company as a predictor because it is a categorical variable with many levels and it will make the model more complex. We will use Price as the response variable. Again, we will use train data set to build the model and test data set to evaluate the model.

```
# Split the data into training and test sets
set.seed(2023)
train_index <- sample(1:nrow(mobile_dataset_mlr), 0.8 * nrow(mobile_dataset_mlr))
train_data <- mobile_dataset_mlr[train_index, ]
test_data <- mobile_dataset_mlr[-train_index, ]</pre>
```

Let's explore the relationship between the variables using the correlation matrix.



Let's apply VIF test to confirm if there is any collinearity between the variables.

```
# Check the "variance inflation factor" for each coefficient using imediag function
→ from the package "regclass"
library(regclass)
VIF(mlr_full_model)
##
          Rating No_of_ratings
                                 TotalReviwes
                                                {\tt RamSize\_inGB}
                                                               RomSize_inGB
##
        1.585407
                      14.057267
                                     13.412710
                                                     2.065303
                                                                   2.328033
## factor(Is_5G)
##
        1.320028
```

From the VIF values, we can see that two variables are collinear. And form the correlation matrix the relationship between the variables is also high (96%). So, we will remove the variable with the highest VIF value, that is No_of_ratings.

Then we update the model by removing No_of_ratings and check significance of the variables.

```
## Residuals:
##
     Min
             1Q Median
                           3Q
                                 Max
  -34720 -4432 -1312
                         2274
                               88499
##
##
## Coefficients:
##
                     Estimate Std. Error t value Pr(>|t|)
                   -7.894e+04 1.064e+04 -7.421 4.21e-13 ***
## (Intercept)
## Rating
                    2.052e+04 2.600e+03
                                          7.890 1.54e-14 ***
## TotalReviwes
                                         -3.464 0.000572 ***
                   -4.146e-01 1.197e-01
## RamSize inGB
                   -3.154e+03 2.252e+02 -14.006 < 2e-16 ***
## RomSize inGB
                    2.650e+02 1.154e+01 22.965 < 2e-16 ***
## factor(Is 5G)Yes 2.773e+02 1.239e+03
                                         0.224 0.822978
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10990 on 574 degrees of freedom
## Multiple R-squared: 0.6359, Adjusted R-squared: 0.6327
## F-statistic: 200.5 on 5 and 574 DF, p-value: < 2.2e-16
```

From the individual t-test, we can see that the variable Is_5G is not significant with p-value 82%. Therefore, we will remove it from the model.

The adjusted R-squared value is 0.6333551, which means that the model explains 63.335511% of the variance in the data.

Now, all the variables are significant. Therefore, the model is valid and can be used for prediction.

```
# Predict the price of the test data

test_data$predicted_price_mlr_base <- predict(mlr_updated_model, test_data)

# Negative values are not possible for the price of a mobile phone. Therefore, we

will replace the negative values with 0.

test_data$predicted_price_mlr_base[test_data$predicted_price_mlr_base < 0] <- 0

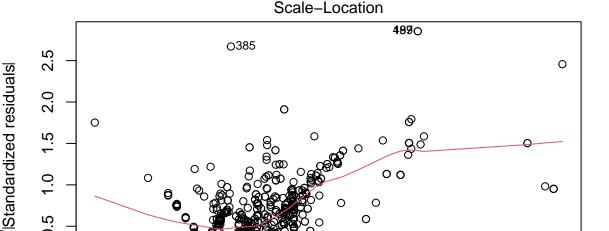
# Calculate the mean square error

rmse1 <- sqrt(mean((test_data$Price - test_data$predicted_price_mlr_base)^2))
```

The RMSE value is 1.0681819×10^4 . The RMSE value is high. Therefore, we will try to improve the model by introducing interaction terms and higher order terms.

Let's plot the predicted values vs actual values to see how well the model fits the data.

```
# Check assumptions of the model
# Plot the residuals vs fitted values
plot(mlr_updated_model, which = 3)
```



Fitted values Im(Price ~ Rating + TotalReviwes + RamSize_inGB + RomSize_inGB)

0

0

60000

0

80000

0

40000

8 0

The residual plot shows that the model is not a good fit for the data. The residuals are not randomly distributed around the horizontal axis. There is a pattern in the residual plot. Therefore, we will try to improve the model by introducing interaction terms and higher order terms.

20000

5.1.2: Improving the model by introducing interaction terms and higher order terms

Let's improve the model by trying interaction terms.

0

-20000

S

Ö.

0

```
# Build a multiple linear regression model with interaction terms
mlr_interaction_model <- lm(Price ~ Rating + TotalReviwes + RamSize_inGB +
    RomSize_inGB + Rating:TotalReviwes + Rating:RamSize_inGB + Rating:RomSize_inGB +
    TotalReviwes:RamSize_inGB + TotalReviwes:RomSize_inGB +
    RamSize inGB:RomSize inGB, data = train data)
summary(mlr_interaction_model)
##
## Call:
   lm(formula = Price ~ Rating + TotalReviwes + RamSize_inGB + RomSize_inGB +
##
       Rating:TotalReviwes + Rating:RamSize_inGB + Rating:RomSize_inGB +
##
       TotalReviwes:RamSize_inGB + TotalReviwes:RomSize_inGB + RamSize_inGB:RomSize_inGB,
##
       data = train_data)
##
## Residuals:
##
      Min
              1Q Median
                            3Q
                                   Max
##
   -37220
           -3142
                   -859
                                67354
                           1480
## Coefficients:
##
                                Estimate Std. Error t value Pr(>|t|)
```

```
## (Intercept)
                             -8.099e+04 1.243e+04 -6.513 1.62e-10 ***
## Rating
                             2.070e+04 3.099e+03
                                                    6.678 5.76e-11 ***
## TotalReviwes
                             -1.671e+00
                                        3.310e+00
                                                   -0.505
                                                            0.6138
## RamSize_inGB
                             9.065e+04 5.214e+03
                                                  17.386 < 2e-16 ***
## RomSize_inGB
                             -4.480e+03 2.510e+02 -17.844 < 2e-16 ***
## Rating:TotalReviwes
                             4.452e-01 7.479e-01
                                                    0.595
                                                            0.5519
## Rating:RamSize_inGB
                             -2.109e+04
                                        1.202e+03 -17.547
                                                           < 2e-16 ***
## Rating:RomSize_inGB
                                                    19.029
                              1.048e+03
                                        5.508e+01
                                                           < 2e-16 ***
## TotalReviwes:RamSize_inGB 8.202e-02 4.804e-02
                                                    1.707
                                                            0.0884 .
## TotalReviwes:RomSize inGB -1.059e-02 2.020e-03
                                                   -5.242 2.24e-07 ***
## RamSize inGB:RomSize inGB 1.056e+01 2.061e+00
                                                    5.124 4.09e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 8150 on 569 degrees of freedom
## Multiple R-squared: 0.8016, Adjusted R-squared: 0.7981
## F-statistic: 229.9 on 10 and 569 DF, p-value: < 2.2e-16
```

Let's remove the interaction terms with insignificant p-values and build the model again. As TotalReviwes has the p-value higher than 0.05, we still want to keep in the model, as it is a part of the significant interaction term TotalReviwes:RomSize_inGB.

```
# Update the model by removing the variable with the insignificant p-value
mlr_interaction_updated_model <- lm(Price ~ Rating + TotalReviwes + RamSize_inGB +
    RomSize_inGB + Rating:RamSize_inGB + Rating:RomSize_inGB +
    TotalReviwes:RomSize_inGB + RamSize_inGB:RomSize_inGB, data = train_data)
```

The adjusted R-squared value is 0.7977683, which means that the model explains 79.7768343% of the variance in the data.

Now, all the variables are significant. Therefore, the model is valid and can be used for prediction.

[1] "RMSE: 11615.5191247919"

We can see that the RMSE value is higher than the base model. This is because the model is overfitting the data. Let's try to improve the model by adding polynomial terms.

We start by adding a polynomial term to the most highly correlated variable with the target variable, that is Rating. We start with a quadratic term and then try higher orders. We stop when some of the terms become insignificant. It turned out that the cubic term is the best fit for the model. Here is the summary of the model.

```
# Build polynomial regression model

mlr_poly_model <- lm(Price ~ poly(Rating, 3) + TotalReviwes + RamSize_inGB +

RomSize_inGB + Rating:RamSize_inGB + Rating:RomSize_inGB +

TotalReviwes:RomSize_inGB + RamSize_inGB:RomSize_inGB, data = train_data)
```

The adjusted R-squared value is 0.8160948, which means that the model explains 81.6094801% of the variance in the data. It is a very good fit for the data. But let's apply the model to the test data and see how well it performs.

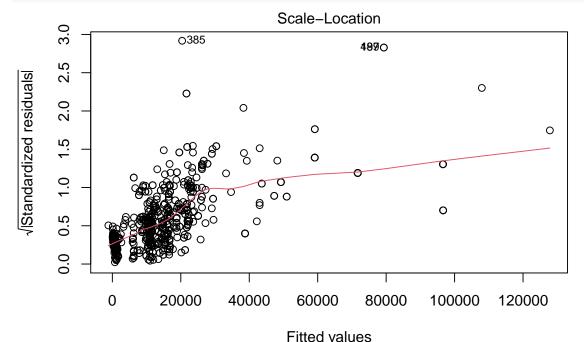
```
# Predict the price of the test data
test_data$predicted_price_mlr_poly <- predict(mlr_poly_model, test_data)
# Negative values are not possible for the price of a mobile phone. Therefore, we
    will replace the negative values with 0.
test_data$predicted_price_mlr_poly[test_data$predicted_price_mlr_poly < 0] <- 0
# Calculate the mean square error
rmse3 <- sqrt(mean((test_data$Price - test_data$predicted_price_mlr_poly)^2))</pre>
```

The RMSE values (1.0145555×10^4) slightly improved compared to the base model. Let's check the assumptions of the model.

5.1.3: Checking the assumptions of the model

Homoscedasticity - constant variance of the residuals. The residuals should be randomly distributed around the horizontal axis.

```
# Check assumptions of the model
# Plot the residuals vs fitted values
plot(mlr_poly_model, which = 3)
```



Im(Price ~ poly(Rating, 3) + TotalReviwes + RamSize inGB + RomSize inGB + R...

The residuals are not randomly distributed around the horizontal axis. There is a pattern in the residual

plot. Therefore, we will try to improve the model by transforming the target variable. But first, let's cross-check homoskedasticity with the Breusch-Pagan test. And later check the other assumptions of the model as well.

```
library(lmtest)
bptest(mlr_poly_model)
```

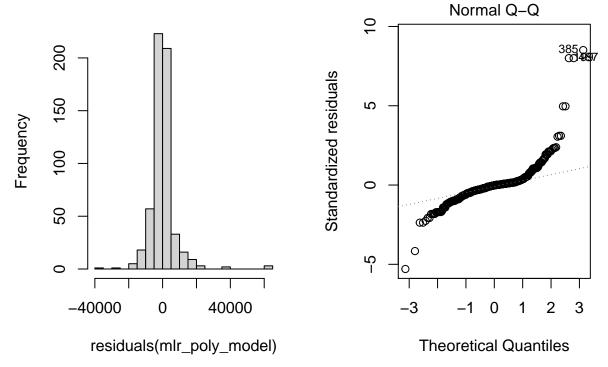
```
##
## studentized Breusch-Pagan test
##
## data: mlr_poly_model
## BP = 106.01, df = 10, p-value < 2.2e-16</pre>
```

The output displays the Breusch-Pagan test that results from the MLR polynomial model. The p-value = 0 < 0.05, indicating that we reject the null hypothesis. Therefore, the test provides evidence to suggest that heteroscedasticity is present - non-constant variance.

Normality - the residuals should be normally distributed.

```
# Normality test
par(mfrow=c(1,2))
hist(residuals(mlr_poly_model), breaks = 24)
plot(mlr_poly_model, which=2) #a Normal plot
```

Histogram of residuals(mlr_poly_me



The residuals are not normally distributed. QQ-plot demonstrates significant deviations from the "normal" line. Let's cross-check the normality of the residuals with the Shapiro-Wilk test.

H0: the sample data are significantly normally distributed Ha: the sample data are not significantly normally distributed

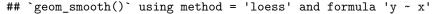
shapiro.test(residuals(mlr_poly_model))

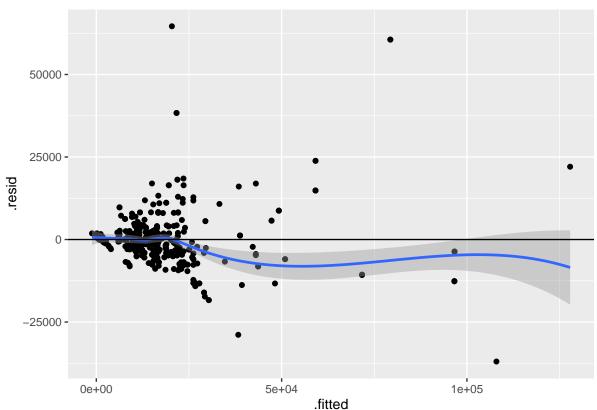
```
##
## Shapiro-Wilk normality test
##
## data: residuals(mlr_poly_model)
## W = 0.7283, p-value < 2.2e-16</pre>
```

The p-value(2.2e-16) is much lower than 0.05, which confirms that the residuals are not normally distributed (reject null hypothesis).

Linearity - the relationship between the independent variables and the dependent variable should be linear.

```
ggplot(mlr_poly_model, aes(x=.fitted, y=.resid)) +
    geom_point() + geom_smooth()+
    geom_hline(yintercept = 0)
```

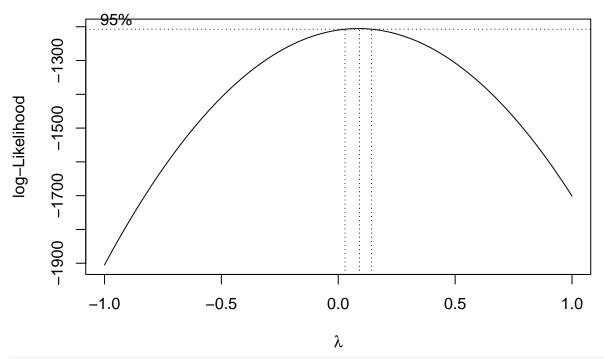




The residuals deviate more and more from the horizontal axis as the fitted values increase. Therefore, the relationship between the independent variables and the dependent variable is not linear.

Therefore, we will try to fix the assumptions by transforming the target variable. We will use the Box-Cox transformation. ### 5.1.4: Box-Cox transformation

```
library("MASS")
bc = boxcox(mlr_poly_model,lambda=seq(-1,1))
```



After the transformation and removing the outliers, we still weren't able to fix the assumptions of the model (code is not provided in the sake of brevity). Even though the adjusted R-squared value is 0.8160948 we can't use the model for prediction.

All steps of the model building process are summarized in the following diagram.

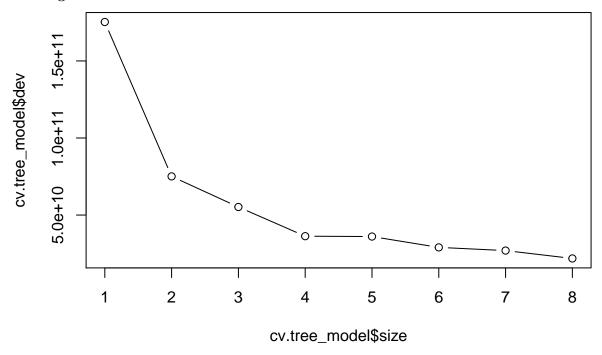
Therefore, we will try Regression Tree to model more complex relationships between the variables. And as our final step in this chapter, we will compare the RMSE values of the models using cross-validation.

5.2: Regression tree

```
# Fit a regression tree to the data
library(tree)
tree_model <- tree(Price ~ ., data = train_data)</pre>
## Warning in tree(Price ~ ., data = train_data): NAs introduced by coercion
summary(tree_model)
##
## Regression tree:
## tree(formula = Price ~ ., data = train_data)
## Variables actually used in tree construction:
## [1] "RamSize_inGB" "No_of_ratings" "RomSize_inGB"
## Number of terminal nodes: 8
## Residual mean deviance: 38980000 = 1.945e+10 / 499
## Distribution of residuals:
       Min. 1st Qu.
                       Median
                                  Mean 3rd Qu.
                                                     Max.
## -26340.0 -2831.0
                      -207.4
                                   0.0
                                        1589.0 40560.0
Our initial tree has 8 terminal nodes.
# Plot the tree
plot(tree_model)
text(tree_model, pretty = 0)
      No_of_ratings < 62153.5
                                            RamSize_inGB < 5
                           RomSize_in&B < 16.0765
             80660
                                  1302
                                           10410
                                                                        45980
                                                     16830
                                                              23880
# Apply the tree to the test set
tree_pred <- predict(tree_model, test_data)</pre>
# Calculate the RMSE
rmse5 <- sqrt(mean((tree_pred - test_data$Price)^2))</pre>
```

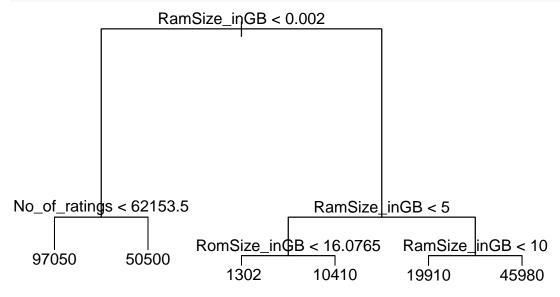
The RMSE value is 5573.7100824. Let's prune the tree. To do that, we will first check the plot between the cross-valiation error and the size of the tree.

Pruning the tree



We will use 4 as the best number of terminal nodes. Let's prune the tree and calculate the RMSE.

```
# Prune the tree
pruned_tree_model <- prune.tree(tree_model, best = 6)
# Plot the pruned tree
plot(pruned_tree_model)
text(pruned_tree_model, pretty = 0)</pre>
```



The RMSE after pruning is 6104.2294325.

5.3: Cross-validation

Let's create 10 folds and calculate the cross-validation error for both models.

Cross-validation error for our best linear regression model is 7679.4340007.

Cross-validation error for our best linear regression model is 6433.6142975.

5.4: Conclusions

In this chapter, we have built a linear regression model and a regression tree model to predict the price of a mobile phone. We have used the RMSE value and cross-validation method to compare the models. The RMSE value for the linear regression model is 1.0145555×10^4 and the RMSE value for the regression tree model is 6104.2294325. Therefore, the regression tree model is better than the linear regression model. Besides, the Multiple Linear Regression model doesn't meet the assumptions. Comparing to the Regression Tree model, it doesn't have such assumptions. Therefore, we recommend using the Regression Tree model for prediction.

Chapter 6: Using Regression to Determine if a Phone is Apple

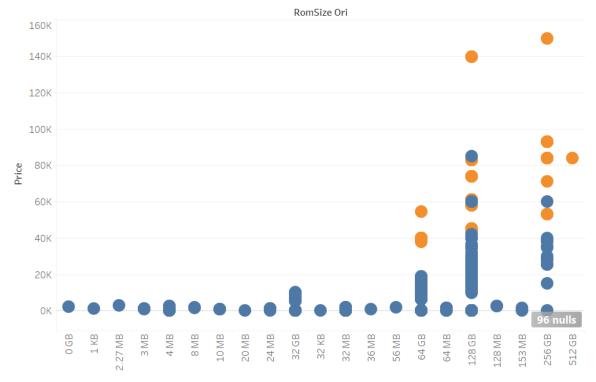
```
mobil_df <- mobile_dataset
mobil_df$Apple = mobil_df$Company=='APPLE'</pre>
```

6.1: Assessing Apple Phones in the Dataset

Then the dataset was checked for possible values of technical specs for Apple phones.

Apple customers paid more for the same amount of Rom than non-Apple customers





However, for phones with the same amount of Rom, Apple customers gave their phones a higher rating than non-Apple customers

Apple phones had higher ratings than other phones but Apple customers paid more money for their phone with an equivalent rating.

6.2: Comparison of Price Regression between Datasets with and without Apple Phones

To compare the price dependence of Apple and non-Apple phones on rating and RomSize, we set out to perform two different regression analysis of price on Apple and non-Apple phones.

First, the dataset was trimmed to compare only phones that had RomSizes in which existed in Apple and non-Apple phones.

```
mobil_df <- mobil_df[mobil_df$RomSize_Ori %in% c('64 GB','128 GB',"256 GB"),]</pre>
```

Then, two new datasets were created, one containing only apple phones and one containing only phones that were not apple.

```
apple_df <- mobil_df[mobil_df$Apple==TRUE,]
notapple_df <- mobil_df[mobil_df$Apple==FALSE,]</pre>
```

6.2.1: The Apple Dataset

Simple Random Sampling was used to create a regression fit for Apple phone price with RomSize and Rating as predictors.

Rating and Rom Size for Apple and Non-Apple Phones

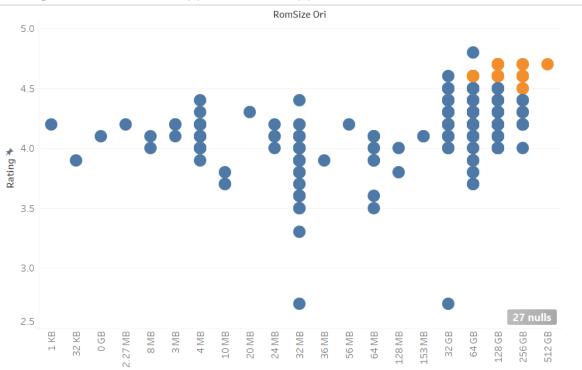


Figure 1: Apple vs. Rating

Rating and Price for Apple and Non-Apple Phones

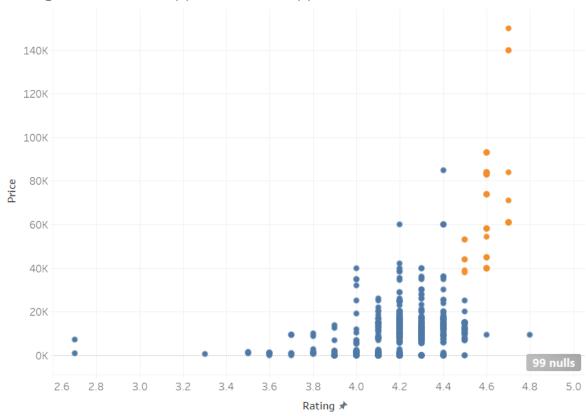


Figure 2: Apple vs. Rating

```
set.seed(12)
idx = sample(dim(apple_df)[1], dim(apple_df)[1]*0.75)
Train=apple_df[idx,]
Test=apple_df[-idx,]
apple_mod <- glm(Price~factor(RomSize_Ori) + Rating , data = Train)
predapple_mod <- predict(apple_mod, Test, type = 'response')</pre>
apple_mod
##
## Call: glm(formula = Price ~ factor(RomSize_Ori) + Rating, data = Train)
##
## Coefficients:
                  (Intercept) factor(RomSize_Ori)256 GB
##
##
                      -964059
                                                     20059
   factor(RomSize_Ori)64 GB
                                                    Rating
                       -22668
                                                    224286
##
##
## Degrees of Freedom: 32 Total (i.e. Null); 29 Residual
## Null Deviance:
                         2.769e+10
## Residual Deviance: 1.359e+10
                                      AIC: 758.2
The price regression of Apple phones had a RomSize coefficients of 20059 when the RomSize was 256GB
and -22668 when the RomSize was 64GB. The Rating coefficient was 224286.
1-mean(abs((Test$Price-predapple_mod)/Test$Price))
## [1] 0.7376318
The price accuracy of the Apple model was around 74% against the test set.
6.2.2 The Non-Apple Dataset
The same strategy was employed for the non-Apple dataset.
set.seed(12)
idx = sample(dim(notapple_df)[1], dim(apple_df)[1]*0.75)
Train=notapple_df[idx,]
Test=notapple_df[-idx,]
notapple_mod <- glm(Price~factor(RomSize_Ori) + Rating , data = Train)</pre>
prednotapple_mod <- predict(notapple_mod, Test, type = 'response')</pre>
notapple_mod
##
## Call: glm(formula = Price ~ factor(RomSize_Ori) + Rating, data = Train)
##
## Coefficients:
##
                  (Intercept) factor(RomSize_Ori)256 GB
```

13465

Rating

11442

-28770

-8726

Degrees of Freedom: 32 Total (i.e. Null); 29 Residual

factor(RomSize_Ori)64 GB

##

##

##

##

Null Deviance: 2.26e+09

Residual Deviance: 1.181e+09 AIC: 677.6

The price regression of non-Apple phones had a RomSize coefficients of 13465 when the RomSize was 256GB and -8726 when the RomSize was 64GB. The Rating coefficient was 11442.

```
1-mean(abs((Test$Price-prednotapple_mod)/Test$Price))
```

[1] 0.7332917

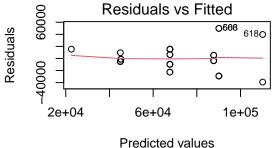
The price accuracy of the model was around 73% against the test set.

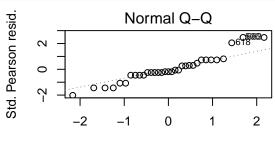
The price of Apple phones is affected much more by the RomSize and the Rating than non-Apple phones. The Apple phones had RomSize coefficients that doubled those of non-Apple phones and the Rating coefficient for Apple phones was roughly 20x higher than that of non-Apple phones. This suggests that while a customer may be paying more for the same amount of Rom with Apple phones, the generally high cost of Apple is mostly dependent on the high ratings that Apple phones typically receive.

6.2.3 Linear Regression Assumptions

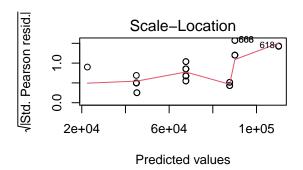
We wanted to verify the assumptions of our linear regression

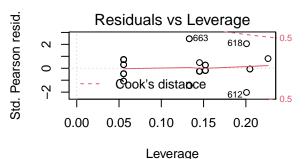
```
par(mfrow=c(2,2)) # init 4 charts in 1 panel
plot(apple_mod)
```





Theoretical Quantiles





The apple dataset was quite small.

shapiro.test(apple_df\$Price)

##

Shapiro-Wilk normality test

```
##
## data: apple_df$Price
## W = 0.86263, p-value = 7.868e-05
```

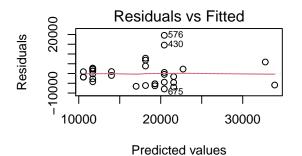
The prices of Apple phones are not normally distributed and the condition of normality is not met. However, from the normal Q-Q plot, it is apparent that the phones in the middle range of the dataset are more normally distributed than the tails.

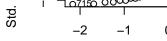
```
bptest(apple_mod)
```

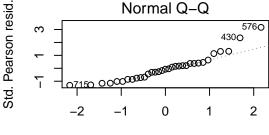
```
##
##
    studentized Breusch-Pagan test
##
## data:
          apple_mod
## BP = 18.727, df = 3, p-value = 0.0003113
```

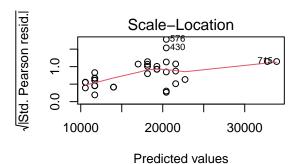
The rejection of the null hypothesis that homoscedasticity is not present means that the data is heteroscedastic and our condition is not met.

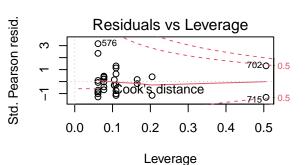
```
par(mfrow=c(2,2)) # init 4 charts in 1 panel
plot(notapple_mod)
```











Theoretical Quantiles

The prices for non-Apple phones are not normally distributed and that condition is not met.

shapiro.test(notapple_df\$Price)

```
##
##
   Shapiro-Wilk normality test
##
## data: notapple_df$Price
## W = 0.73903, p-value < 2.2e-16
```

bptest(notapple_mod)

```
##
## studentized Breusch-Pagan test
##
## data: notapple_mod
## BP = 4.2836, df = 3, p-value = 0.2324
```

However, the non-Apple phone dataset does have homoscedasticity.

We continue with our analysis despite the failure to meet the assumptions.

6.3: Logistic Regression of Apple Phones from non-Apple Phones

We sought to evaluate our ability to differentiate Apple phones from non-Apple phones using logistic regression.

Despite Apple phones being generally more expensive, the best logistic regression model determines whether a phone is Apple or non-Apple primarily by Rating and RomSize.

```
summary(log_apple_mod)
```

```
##
## Call:
## glm(formula = Apple ~ factor(RomSize_Ori) + Price + Rating, family = binomial,
      data = Train)
##
##
## Deviance Residuals:
       Min
                  1Q
                        Median
                                      3Q
##
                                               Max
                                           1.55529
## -2.13162 -0.04370 -0.01410 -0.00532
##
## Coefficients:
##
                              Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                            -1.054e+02 3.147e+01 -3.348 0.000814 ***
## factor(RomSize_Ori)256 GB 1.433e+00 2.153e+00 0.666 0.505631
                             6.911e-01 1.598e+00 0.432 0.665427
## factor(RomSize_Ori)64 GB
## Price
                             1.257e-04 3.946e-05 3.186 0.001441 **
                             2.201e+01 6.995e+00 3.146 0.001656 **
## Rating
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 215.291 on 382
                                      degrees of freedom
## Residual deviance: 20.998 on 378
                                      degrees of freedom
## AIC: 30.998
```

[1] 0.08806262

Apple phones comprised 9% of dataset and the logistic regression model was able to correctly classify Apple phones 99.2% of the time.

6.4: Summary

The approach of dividing the dataset into two to apply two linear price regressions to the dataset of Apple phones and the dataset of non-Apple phones illustrated how Romsize and Rating affected Apple phone prices differently than non-Apple phones. The logistic regression of Apple phones proved that it's effective to use logistic regression to determine if a phone is an Apple phone or not using the phone's price, rating and RomSize.

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