Mobile Phones Selling Price Report

Final report (MDSA Winter 2023)

Yongpeng Fu (10182778), Rudy Brown (10057171), Jose Palacios (30190988),
Stuart Finley(30191070), Andrii Voitkiv(30199373)

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Introduction

Mobile phones are everywhere, so are the prices. Despite still having the word "phone" in the name, a typical modern smartphone has much more features than just to make and receive calls. They are boasting a staggering range of applications like brand, memory, storage, camera, resolution, just to name a few. All these cutting edge technology and features packed in one little device does not come without a cost. A 2020 review of premium mobile phones shows a staggering *490%* rise in the last two decades.

With so many mobile phones on the market, it can be difficult to decide which one you want to buy. As a customer, we are particularly interested in finding some relation between all these features and its selling price. To this purpose, we collected the MobilePhone's dataset from Kaggle and apply a set of statistical analysis hoping to answer some guiding questions:

1. Can we estimate the average price for mobile phones?
2. What is the impact of each mobile phone's feature on the selling price?
3. Can a classification model to distinguish the selling price range?
4. Can we build a decent model to predict the selling price for a mobile phone?

Dataset and Cleanup

The initial dataset consists of 8 columns and 28,036 rows and no missing values. These 8 columns are:

- **Model**: categorical variables with sub-classes. These names include the color of the unit and its storage capacity. The latter being also listed as a separate column. - **Independent Variable**
- **Company**: categorical variable. Name of the phone's manufacturer. - **Independent Variable**
- **Price**: continuous variable. Units in Indian Rupees. - **Dependent Variable**
- **Rating**: continuous variable. - **Independent Variable**
- **Number of ratings**: discrete variable: a simple count. - **Independent Variable**
- **Total reviews**: discrete variable: a simple count. - **Independent Variable**
- **RAM size**: categorical variable. RAM specification of the phone. - **Independent Variable**
- **ROM size**: categorical variable. Storage (non-volatile memory) capacity of the phone. - **Independent Variable**

Some initial steps can be completed to clean the dataset and create new variables which can be used in our analysis. The initial steps for cleaning the dataset are as follows:

1. Remove any duplicates in the dataset;
2. Because **Model** column contains sub-class of a mobile phone, we decide to further break it down to *Model* and *Color*;
3. Convert all units from **RAM size** and **ROM size** measure to GB and then remove unit suffix;
4. Add additional column to segment the **Price** into 4 different levels;
5. Add additional column to determine if a phone has %G feature or not based on **Model** information.

```
mobile_dataset <- read.csv("./Updated_Mobile_Dataset.csv")
#Step 0: convert Model and Company letter to uppercase.
mobile_dataset$Model <- toupper(mobile_dataset$Model)
mobile_dataset$Company <- toupper(mobile_dataset$Company)
#Break down Model column into Model only and Color columns
#Step 1: remove the Company name from Model
Model_no_Company <- stringr::str_remove(mobile_dataset$Model,mobile_dataset$Company)
↪  %>% trimws(., which = c("both"))
#Step 2: remove anything after parentheses to get Model only info
mobile_dataset$Model_Only <- stringr::str_replace(Model_no_Company, "
↪  \\s*\\([^\\)]+\\)", "")
```

```r
#Step 3: Get the color information from inside the last ()
#Step 3.1: Get the parenthesis and what is inside from the last ()
Model_no_Company_parenthesis <- stringr::str_extract(Model_no_Company,
↪  "(?<=\\()([^()]*?)(?=\\)[^()]*$)")
#step 3.2: Get the color by just retaining the info before ,
mobile_dataset$Color <- gsub(",.*$", "", Model_no_Company_parenthesis)
#Step 4: Remove duplicated rows in the dataset
mobile_dataset <- mobile_dataset[!duplicated(mobile_dataset),]
#Step 5: cut the price based on the percentile into 4 different levels
mobile_dataset <- mobile_dataset %>% mutate(Price_Level = ntile(Price, n = 4))
#Step 5.1: map each number level to the character
from <- c(1,2,3,4)
to <- c("Low", "Medium", "High", "Very High")
mobile_dataset$Price_Level <- mapvalues(mobile_dataset$Price_Level, from = from, to
↪  = to)


#Step 6: Get the numeric part of RomSize (remove GB and MB, but convert MB to GB),
↪  discard any record that no numeric in RomSize
#Step 6.1: there are some data input errors for RamSize and RomSize. In the records
↪  where RomSize is "Not Known" are swapped with RamSize, so we need to correct
↪  that.
RamSize_temp <- ifelse(mobile_dataset$RomSize == "Not Known", "0 GB",
↪  mobile_dataset$RamSize)
mobile_dataset$RomSize <- ifelse(mobile_dataset$RomSize == "Not Known",
↪  mobile_dataset$RamSize, mobile_dataset$RomSize)
mobile_dataset$RamSize <- RamSize_temp
#Step 6.2: split RomSize into two columns with size number and unit, and convert MB
↪  to 1/1000GB, KB to 1/1000000GB
mobile_dataset$RamSize_Ori <- mobile_dataset$RamSize
mobile_dataset$RomSize_Ori <- mobile_dataset$RomSize
mobile_dataset <- mobile_dataset %>% separate(RomSize, c("RomSize_num",
↪  "RomSize_Unit")) %>% mutate(RomSize_Unit= mapvalues(.$RomSize_Unit, from =
↪  c("GB", "MB", "KB"), to = c(1, 1/1000, 1/1000000)))
```

```
## Warning: Expected 2 pieces. Additional pieces discarded in 1 rows [573].
```

```r
#step 6.3: remove any rows that are not numeric value for RomSize
mobile_dataset <- mobile_dataset[!is.na(as.numeric(mobile_dataset$RomSize_num)),]
```

```
## Warning in
## `[.data.frame`(mobile_dataset, !is.na(as.numeric(mobile_dataset$RomSize_num)), :
## NAs introduced by coercion
```

```r
mobile_dataset$RomSize_num <- as.numeric(mobile_dataset$RomSize_num)
mobile_dataset$RomSize_Unit <-
↪  ifelse(is.na(as.numeric(mobile_dataset$RomSize_Unit)), 0,
↪  as.numeric(mobile_dataset$RomSize_Unit))
#Step 6.4: generate the final column RomSize_inGB
mobile_dataset$RomSize_inGB <- mobile_dataset$RomSize_num *
↪  mobile_dataset$RomSize_Unit
```

```r
#Step 7: Get the numeric part of RamSize (remove GB and MB, but convert MB to GB),
↪  discard any record that no numeric in RamSize
#Step 7.1: split RamSize into two columns with size number and unit, and convert MB
↪  to 1/1000GB
mobile_dataset <- mobile_dataset %>% separate(RamSize, c("RamSize_num",
↪  "RamSize_Unit")) %>% mutate(RamSize_Unit= mapvalues(.$RamSize_Unit, from =
↪  c("GB", "MB"), to = c(1, 1/1000)))
#step 7.2: remove any rows that are not numeric value for RamSize
mobile_dataset <- mobile_dataset[!is.na(as.numeric(mobile_dataset$RamSize_num)),]
mobile_dataset$RamSize_num<- as.numeric(mobile_dataset$RamSize_num)
mobile_dataset$RamSize_Unit <- as.numeric(mobile_dataset$RamSize_Unit)
#Step 7.3: generate the final column RamSize_inGB
mobile_dataset$RamSize_inGB <- mobile_dataset$RamSize_num *
↪  mobile_dataset$RamSize_Unit


#Step 8: Create a new column to determine if the phone is 5G or not
mobile_dataset$Is_5G <- ifelse(str_detect(mobile_dataset$Model_Only, "5G"), "Yes",
↪  "No")
#Step 9: only keep the columns we need
column_names <- c("Model", "Company", "Price", "Rating", "No_of_ratings",
↪  "TotalReviwes", "Model_Only", "Color", "Price_Level", "RamSize_inGB",
↪  "RomSize_inGB", "RamSize_Ori", "RomSize_Ori", "Is_5G" )
mobile_dataset <- mobile_dataset[column_names]

# #Step 9: final check up. Convert all company name to uppercase and then do a final
↪  duplicated removal
# mobile_dataset$Company <- toupper(mobile_dataset$Company)
# mobile_dataset <- mobile_dataset[!duplicated(mobile_dataset),]
write.csv(mobile_dataset, file = './Cleaned_Mobile_Dataset.csv', row.names = F)
```

After cleaning and breaking down columns, the dataset now consists of 14 columns and 725 rows and no missing values. These 14 columns are:

- **Model**: categorical variables with sub-classes. These names include the color of the unit and its storage capacity. The latter being also listed as a separate column. - **Independent Variable**
- **Company**: categorical variable. Name of the phone's manufacturer. - **Independent Variable**
- **Price**: continuous variable. Units in Indian Rupees. - **Dependent Variable**
- **Rating**: continuous variable. - **Independent Variable**
- **Number of ratings**: discrete variable: a simple count. - **Independent Variable**
- **Total reviews**: discrete variable: a simple count. - **Independent Variable**
- **Model_Only**: categorical variable: only contains the model information of a mobile phone. - **Independent Variable**
- **Color**: categorical variable: color of a mobile phone. - **Independent Variable**
- **Price_Level**: The price level of a mobile phone, with levels of "Low", "Medium", "High", "Very High". - **Independent Variable**
- **RamSize_inGB**: continuous variable. RAM specification of the phone in GB. - **Independent Variable**
- **RomSize_inGB**: continuous variable. Storage (non-volatile memory) capacity of the phone in GB. - **Independent Variable**
- **RamSize_Ori**: categorical variable. RAM specification of the phone, original information. -

Independent Variable

- **RomSize_Ori**: categorical variable. Storage (non-volatile memory) capacity of the phone, original information. - **Independent Variable**
- **Is_5G**: categorical variable. If the phone has 5G service or not. - **Independent Variable**

```
mobile_dataset <- as_tibble(read.csv("./Cleaned_Mobile_Dataset.csv"))
#Specify the level for Price_Level column
mobile_dataset$Price_Level <- factor(mobile_dataset$Price_Level, levels = c("Low",
↪  "Medium", "High", "Very High"))
mobile_dataset %>% head(4)
```

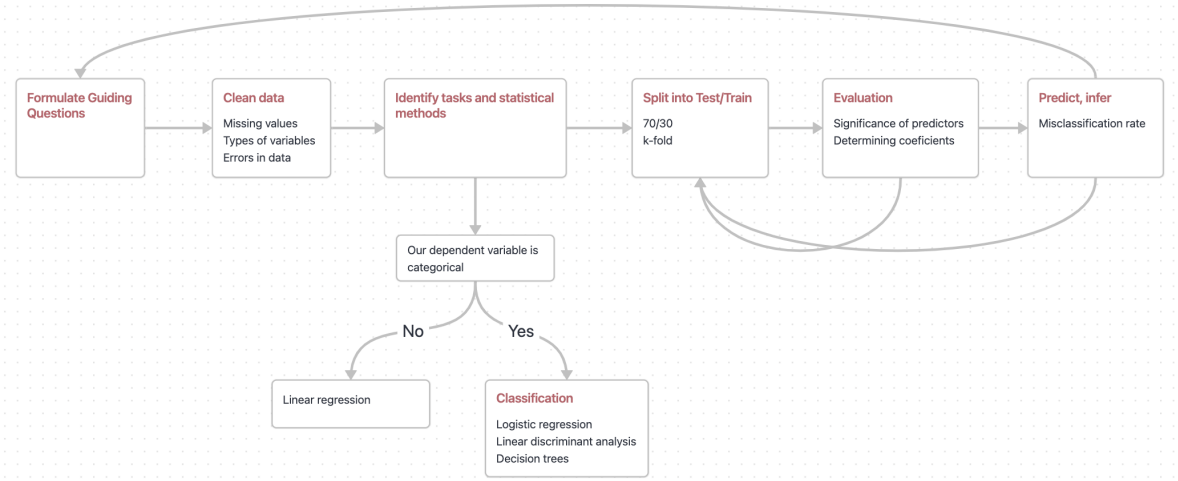
```
## # A tibble: 4 x 14
##   Model       Company Price Rating No_of~1 Total~2 Model~3 Color Price~4 RamSi~5
##   <chr>       <chr>   <int>  <dbl>   <int>   <int> <chr>   <chr> <fct>     <dbl>
## 1 INFINIX HO~ INFINIX  8199    4.3     505      52 HOT 20~ LUNA~ Medium        4
## 2 MOTOROLA E~ MOTORO~  7999    4.1   56085    5600 E40     CARB~ Medium        4
## 3 MOTOROLA E~ MOTORO~  7999    4.1   56085    5600 E40     PINK~ Medium        4
## 4 POCO C31 (~ POCO     7499    4.3  183688   11185 C31     SHAD~ Medium        4
## # ... with 4 more variables: RomSize_inGB <dbl>, RamSize_Ori <chr>,
## #   RomSize_Ori <chr>, Is_5G <chr>, and abbreviated variable names
## #   1: No_of_ratings, 2: TotalReviwes, 3: Model_Only, 4: Price_Level,
## #   5: RamSize_inGB
```

Table 1: The cleaned-up dataset for Mobile Phone

The dataset and detailed analysis can be found at this repository.

Scope of Analysis

Our team is finalizing what the full analysis of the dataset will look like, but a preliminary template and breakdown of work by team member has been included below. The different colors represent which components of the project different team members would take on. It is anticipated that all members will assist in the finalization of the report.



Chapter 4: Exploratory Data Analysis

4.1: A summary of the dataset

The dimension of the cleaned dataset is 726 rows and 14 columns. A summary of the data is as follows:

```
mobile_dataset <- as_tibble(read.csv("./Cleaned_Mobile_Dataset.csv"))
#Specify the level for Price_Level column
mobile_dataset$Price_Level <- factor(mobile_dataset$Price_Level, levels = c("Low",
↪  "Medium", "High", "Very High"))
mobile_dataset %>% summary()
```

```
##     Model             Company              Price            Rating
##  Length:725         Length:725         Min.   :   698   Min.   :2.700
##  Class :character   Class :character   1st Qu.:  7014   1st Qu.:4.100
##  Mode  :character   Mode  :character   Median : 12889   Median :4.200
##                                        Mean   : 15903   Mean   :4.227
##                                        3rd Qu.: 16999   3rd Qu.:4.300
##                                        Max.   :149900   Max.   :4.800
##  No_of_ratings     TotalReviwes    Model_Only           Color
##  Min.   :     3   Min.   :    0   Length:725         Length:725
##  1st Qu.:   874   1st Qu.:   80   Class :character   Class :character
##  Median :  7325   Median :  670   Mode  :character   Mode  :character
##  Mean   : 34522   Mean   : 2496
##  3rd Qu.: 37211   3rd Qu.: 2972
##  Max.   :575907   Max.   :33942
##     Price_Level   RamSize_inGB     RomSize_inGB    RamSize_Ori
##  Low      :171   Min.   : 0.000   Min.   :  0.00   Length:725
##  Medium   :185   1st Qu.: 0.064   1st Qu.: 32.00   Class :character
##  High     :185   Median : 4.000   Median : 64.00   Mode  :character
##  Very High:184   Mean   : 3.882   Mean   : 81.78
##                  3rd Qu.: 6.000   3rd Qu.:128.00
##                  Max.   :12.000   Max.   :512.00
##  RomSize_Ori           Is_5G
##  Length:725         Length:725
##  Class :character   Class :character
##  Mode  :character   Mode  :character
##
##
##
```

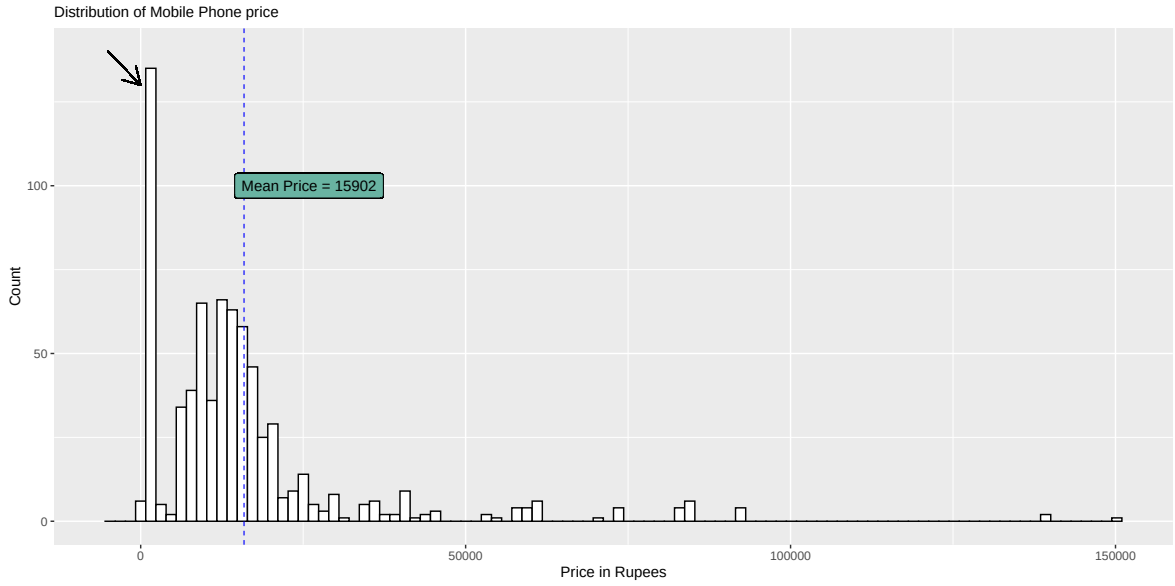
Table 2: A summary for Mobile Phone dataset

4.2: Exploratory Data Analysis

This section is focused on the exploration of relation between variables using various visualization techniques.

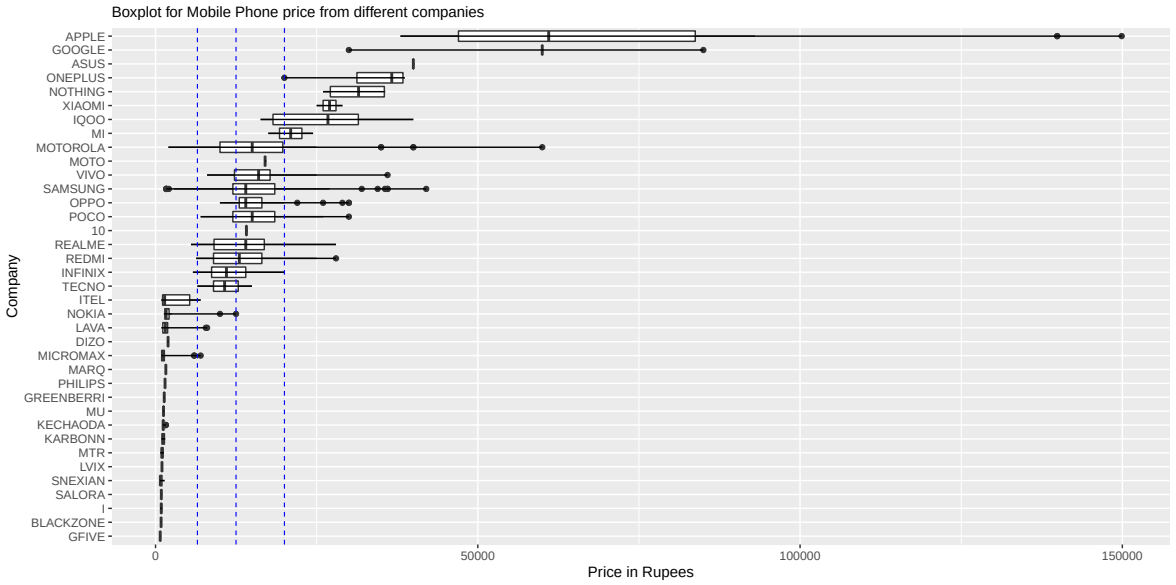
The main target is Price in the dataset. In the following visualization it shows the distribution of Mobile Phone price with long tail towards to the high end. The average price is 15902 Rupees. Most price falls in the range of 50000 Rupees. One really stands out price range (arrow indicated) is 1000-2000 Rupees with the highest frequency.

```
ggplot(data = mobile_dataset, mapping = aes(x=Price)) +
↪  geom_histogram(color="black", fill="white", bins = 100)+
  geom_vline(aes(xintercept=mean(Price)),
             color="blue", linetype="dashed", size=0.4) + geom_label(
    label="Mean Price = 15902",
    x= mean(mobile_dataset$Price) + 10000,
    y=100,
    label.padding = unit(0.35, "lines"),
    label.size = 0.25,
    color = "black",
    fill="#69b3a2"
  ) +  geom_segment(aes(x = -5000, y = 140, xend = 0, yend = 130),lineend =
↪  "round",linejoin = "round",
                  arrow = arrow(length = unit(0.5, "cm"))) + labs(y="Count",
                   ↪  x="Price in Rupees",
       subtitle="Distribution of Mobile Phone price")
```



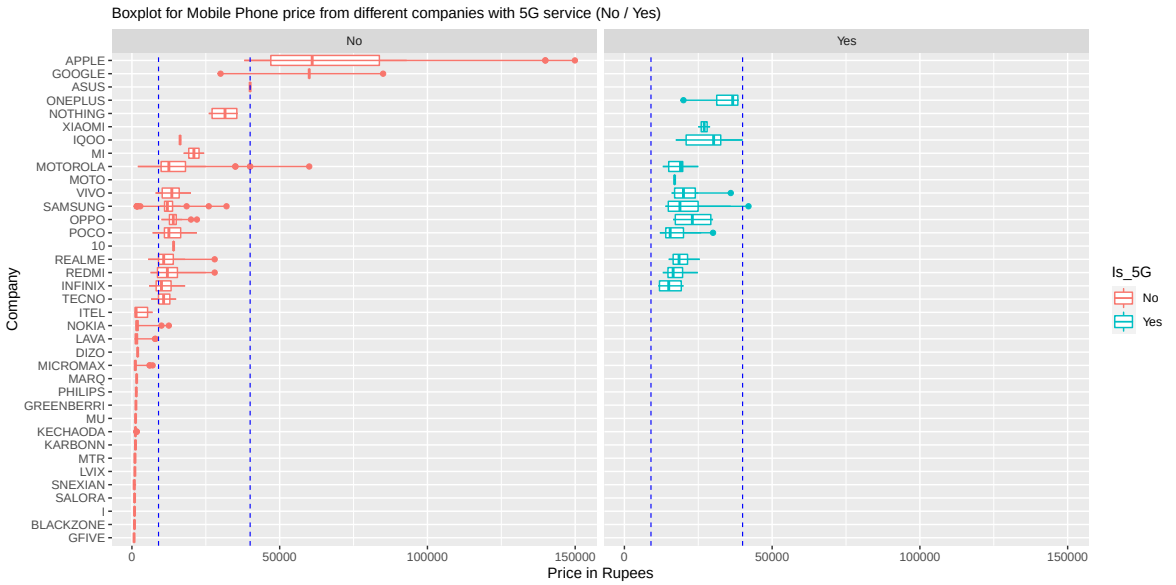
The following figure is to break down the Price by different phone-making companies. There are a total of 37 companies in the dataset. Iin consistent with previous figure about Price distribution, we see a big portion of Price falls between 9000 (left dash line) and 40000 (right dash line) Rupees. *Apple* alone contributes the most of high priced Mobile Phones, while companies like from *NOKIA* to *GFIVE* contribute to the low-priced ones.

```
ggplot(data = mobile_dataset, mapping = aes(y = reorder(Company, Price), x = Price))
↪  +geom_boxplot()+ geom_line() +
    sapply(c(6499, 12490, 20000), function(xint) geom_vline(aes(xintercept = xint),
    ↪  color="blue", linetype="dashed", size=0.4)) + labs(y="Company", x="Price in
    ↪  Rupees",
       subtitle="Boxplot for Mobile Phone price from different companies")
```



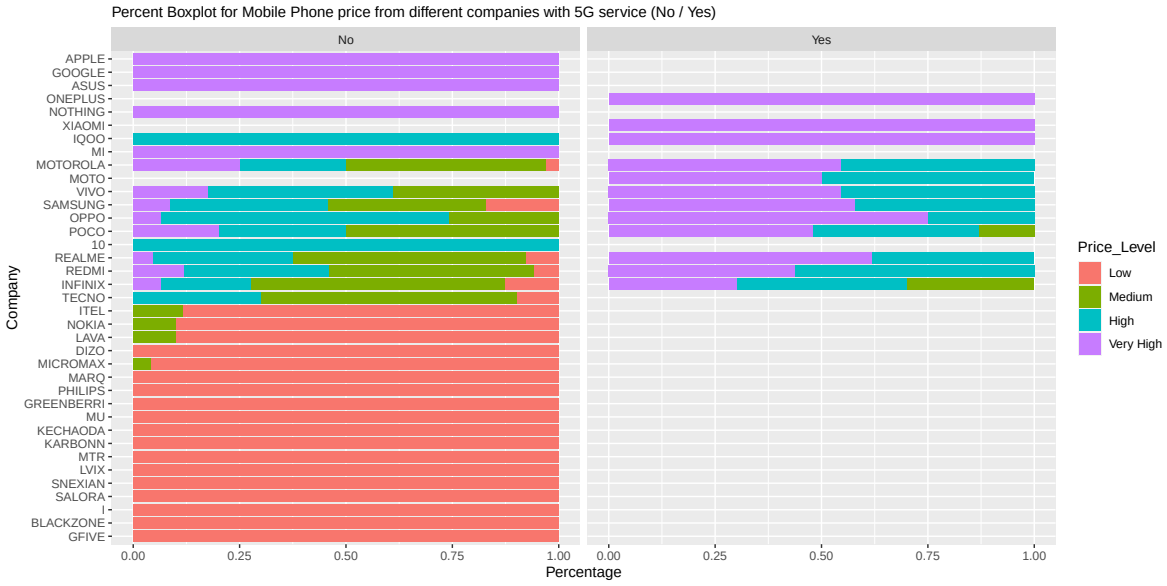
The Price is further broken down by their 5G services. Interestingly, neither high-priced nor low-priced Mobile Phones have equipped 5G service. In contrast, almost all middle-priced Mobile Phones have 5G service. Price for those with 5G service are slightly more expensive than those without. NOTE: the dashed line indicates the price between 9000 (left dash line) and 40000 (right dash line) Rupees.

```
ggplot(data = mobile_dataset, mapping = aes(y = reorder(Company, Price), x = Price,
↪  color = Is_5G)) +geom_boxplot(position=position_dodge(width = 0.8))+ geom_line()
↪  +
    sapply(c(9000, 40000), function(xint) geom_vline(aes(xintercept = xint),
    ↪  color="blue", linetype="dashed", size=0.4)) + labs(y="Company", x="Price in
    ↪  Rupees",
       subtitle="Boxplot for Mobile Phone price from different companies with 5G
       ↪  service (No / Yes)") + facet_wrap(~Is_5G)
```



The pattern is more obvious when we provide color for 4 different price level ("Low", "Medium", "High", "Very High"). Although mobile phones from companies like APPLE, GOOGLE, ASUS and NOTHING have no 5G service, their price are all very high. It is worth investigating if some other attributes like brand effect, Storage capacity (Rom Size), and calculation power (Ram Size) are playing roles. Most Mobile Phones (except MI) with 5G service, again, have a higher proportion falling in a Very High price level, compared to the counterparts without 5G service. Almost all the rest mobile phones without 5G service fall in a Low price level.

```
ggplot(data = mobile_dataset,mapping = aes(y =reorder(Company, Price), fill =
↪  Price_Level)) + geom_bar(stat = "count", position="fill") + labs(y="Company",
↪  x="Percentage",
      subtitle="Percent Boxplot for Mobile Phone price from different companies
       ↪  with 5G service (No / Yes)") + facet_wrap(~Is_5G)
```



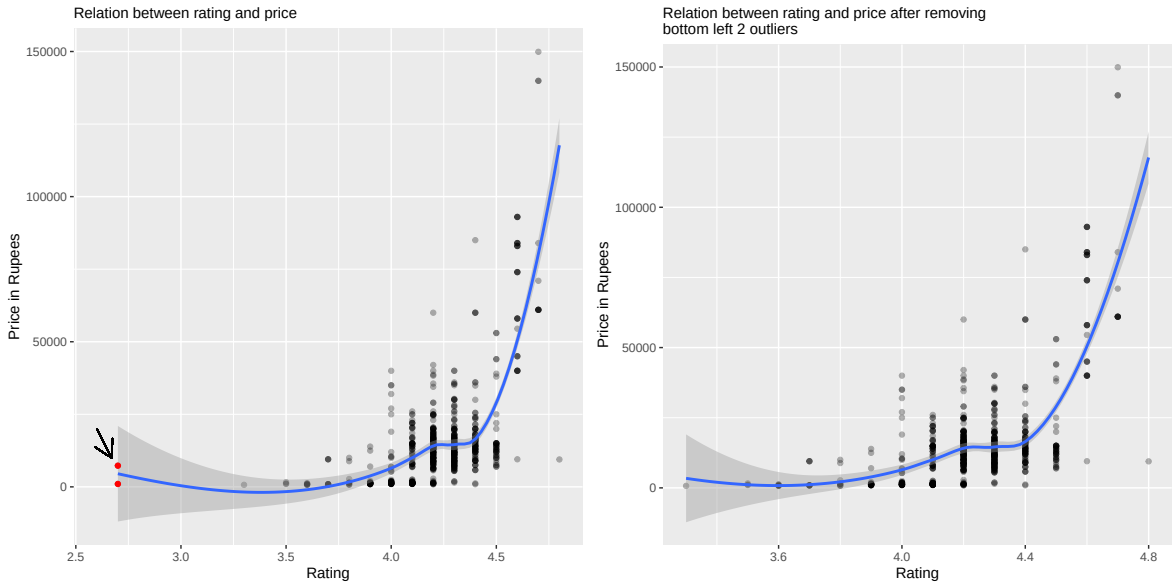
Next, we explored some quantitative features with respect to the Mobile Phone price. The first scatter plot shows an obvious positive relation between Rating and Price as the smooth line indicates. The higher the Rating, the higher the Price. And this holds when we remove those bottom left 2 outlier data points.

```
#The first plot is one with outlier
plot1 = ggplot(data = mobile_dataset,mapping = aes(x = Rating, y = Price)) +
↪  geom_point(alpha=0.3) + geom_smooth(se=T) +
  geom_segment(aes(x = 2.6, y = 20000, xend = 2.67, yend = 10000),lineend =
  ↪  "round",linejoin = "round",arrow = arrow(length = unit(0.5, "cm"))) +
  geom_point(data=mobile_dataset[mobile_dataset$Rating<3.0,], aes(x = Rating, y =
  ↪  Price), color='red') +
  labs(y="Price in Rupees", x="Rating", subtitle="Relation between rating and
  ↪  price")

#The first plot is a one with outliers removed
plot2 = ggplot(data = mobile_dataset[mobile_dataset$Rating>3.0, ],mapping = aes(x =
↪  Rating, y = Price)) + geom_point(alpha=0.3) + geom_smooth(se=T) +
  labs(y="Price in Rupees", x="Rating", subtitle="Relation between rating and price
  ↪  after removing \nbottom left 2 outliers")
```

```
grid.arrange(plot1, plot2, ncol=2)
```

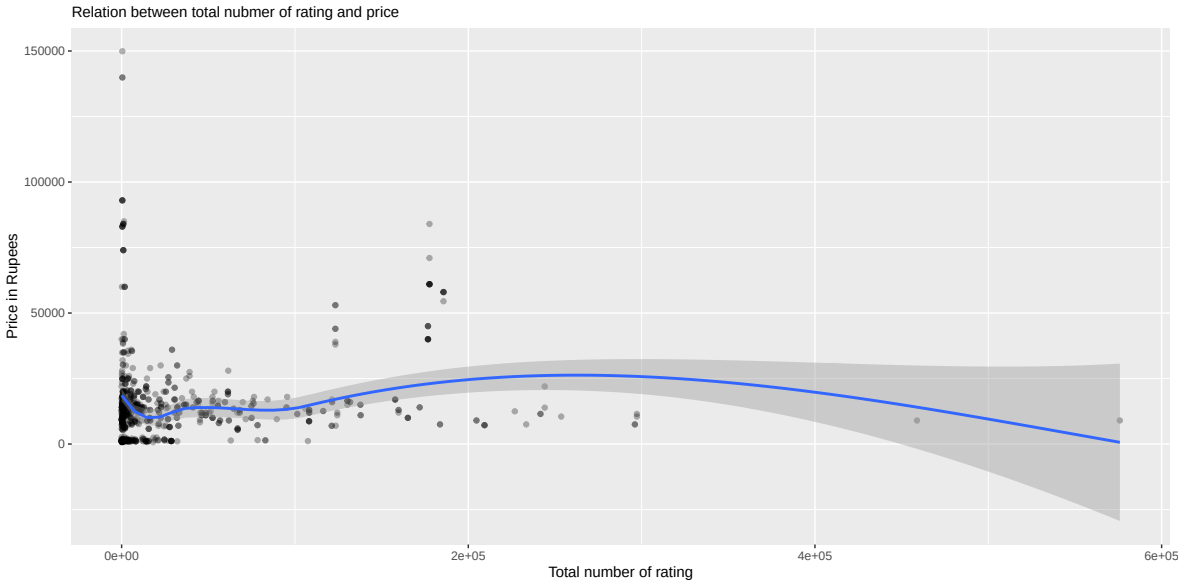
```
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```



The second scatter plot as follows shows the relation between Total number of rating and Price. As the smooth line indicates, there is no obvious correlation between them. The result holds even when we remove some seemingly outliers on the far right end.

```
ggplot(data = mobile_dataset,mapping = aes(x = No_of_ratings, y = Price)) +
↪  geom_point(alpha=0.3) + geom_smooth()+ labs(y="Price in Rupees", x="Total number
↪  of rating", subtitle="Relation between total nubmer of rating and price")
```

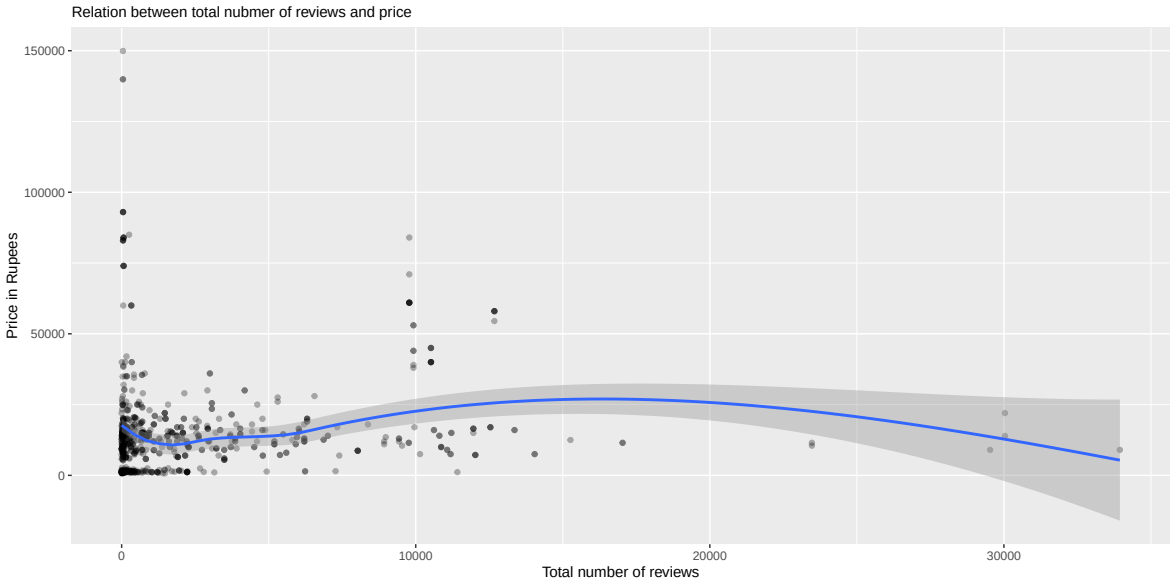
```
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```



The same pattern is also observed in the third scatter plot where relation between Total number of reviews and Price is plotted. As the smooth line indicates, there is no obvious correlation between them. The result holds even when we remove some seemingly outliers on the far right end.

```
ggplot(data = mobile_dataset,mapping = aes(x = TotalReviwes, y = Price)) +
↪  geom_point(alpha=0.3) + geom_smooth()+ labs(y="Price in Rupees", x="Total number
↪  of reviews", subtitle="Relation between total nubmer of reviews and price")
```

```
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```



In the fourth scatter plot, below, there seems a slight positive relation between Ram size (in GB) and the Price. Ram is normally associated with speed and performance of an operating system. The higher ram is, the better it is in speed and performance. It makes sense that a mobile phone with a larger Ram will charge more. However, because nowadays most mobile phones are very fast and stable, people wont tell too much difference, making the added on value from ram is only weekly associated with price.

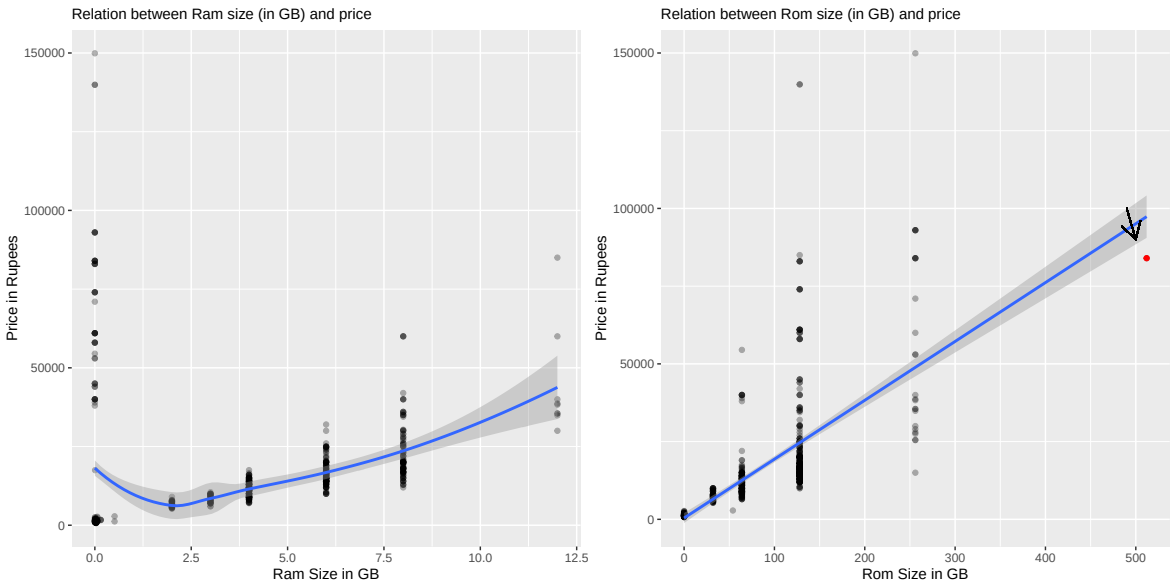
```
plot1 = ggplot(data = mobile_dataset,mapping = aes(x = RamSize_inGB, y = Price)) +
↪  geom_point(alpha=0.3) + geom_smooth(se=T)+ labs(y="Price in Rupees", x="Ram Size
↪  in GB", subtitle="Relation between Ram size (in GB) and price")

plot2 = ggplot(data = mobile_dataset,mapping = aes(x = RomSize_inGB, y = Price)) +
↪  geom_point(alpha=0.3) + geom_smooth(se=T, method = lm)+
  geom_segment(aes(x = 490, y = 100000, xend = 500, yend = 90000),lineend =
  ↪  "round",linejoin = "round",arrow = arrow(length = unit(0.5, "cm"))) +
  geom_point(data=mobile_dataset[mobile_dataset$RomSize_inGB>400,], aes(x =
  ↪  RomSize_inGB, y = Price), color='red') +
  labs(y="Price in Rupees", x="Rom Size in GB", subtitle="Relation between Rom size
  ↪  (in GB) and price")

grid.arrange(plot1, plot2, ncol=2)
```

```
## `geom_smooth()` using method = 'loess' and formula 'y ~ x'
```

```
## `geom_smooth()` using formula 'y ~ x'
```



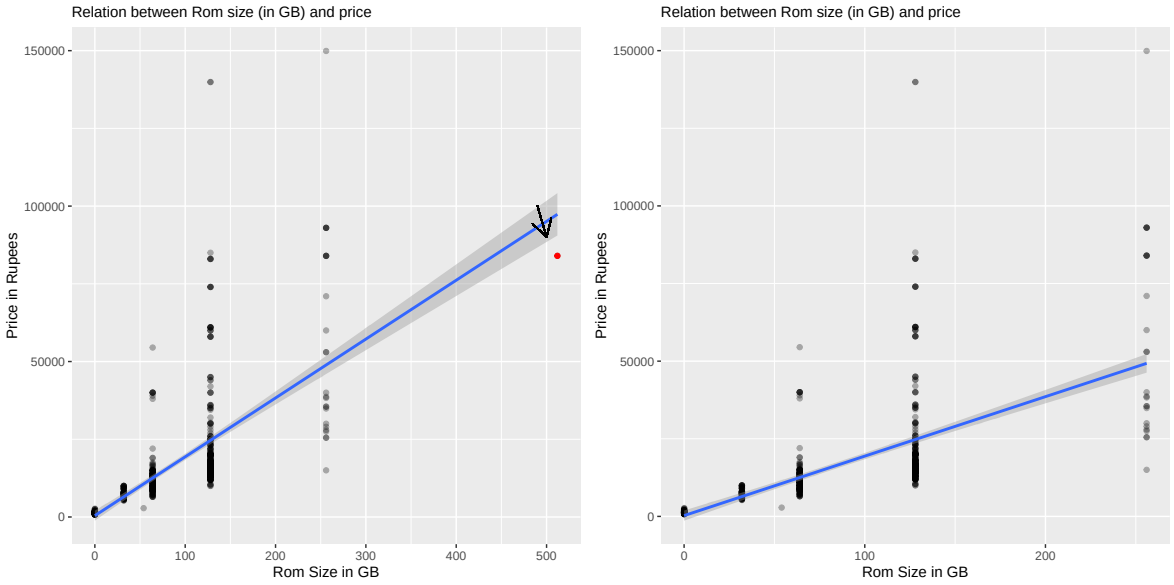
In the final scatter plot, again, we have two charts, one the original dataset, the other with outlier removed. Both cases tells the same story. In contrast to the previous scatter plot (Ram size (in GB) and the Price), there is a very obvious positive linear relation between Rom size (in GB) and the Price. This makes sense because often times a mobile phone is more limited by its non-volatile memory space than its speed & performance.

```
#The first plot is a one with outliers
plot1 = ggplot(data = mobile_dataset,mapping = aes(x = RomSize_inGB, y = Price)) +
↪  geom_point(alpha=0.3) + geom_smooth(se=T, method = lm)+
  geom_segment(aes(x = 490, y = 100000, xend = 500, yend = 90000),lineend =
  ↪  "round",linejoin = "round",arrow = arrow(length = unit(0.5, "cm"))) +
  geom_point(data=mobile_dataset[mobile_dataset$RomSize_inGB>400,], aes(x =
  ↪  RomSize_inGB, y = Price), color='red') +
  labs(y="Price in Rupees", x="Rom Size in GB", subtitle="Relation between Rom size
  ↪  (in GB) and price")
```

```
#The second plot is a one with outliers removed
plot2 = ggplot(data = mobile_dataset[mobile_dataset$RomSize_inGB<400, ],mapping =
↪  aes(x = RomSize_inGB, y = Price)) + geom_point(alpha=0.3) +
↪  geom_smooth(se=T,method = lm) +
  labs(y="Price in Rupees", x="Rom Size in GB", subtitle="Relation between Rom size
  ↪  (in GB) and price")

grid.arrange(plot1, plot2, ncol=2)
```

```
## `geom_smooth()` using formula 'y ~ x'
## `geom_smooth()` using formula 'y ~ x'
```



Chapter 5: Statistical Data Analysis

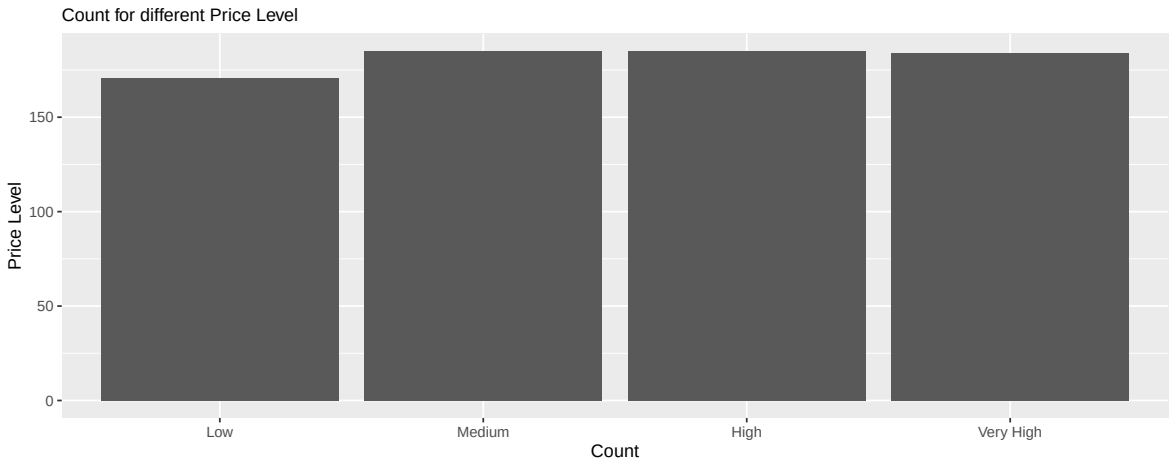
5.1: Prediction of Mobile Phone Price Level

In this section, we will use a range of statistical models to predict mobile phone price level: "Low", "Medium", "High", "Very High" based on some selected features.

- Linear Discriminant Analysis (LDA)
- Quadratic Discriminant Analysis (QDA)
- Decision Tree (Classification)
- Multinomial Regression

First, let use explore the distribution for difference price level. From the following bar plot, you can see it is very close to uniformly distributed across the dataset. Balanced dataset is important for us when we do the classification.

```
price_level_count <- table(mobile_dataset$Price_Level) %>% as.data.frame()
ggplot(data = price_level_count, mapping = aes(x = Var1, y = Freq)) + geom_bar(stat
↪  = "identity") +
  labs(y="Price Level", x="Count", subtitle="Count for different Price Level")
```



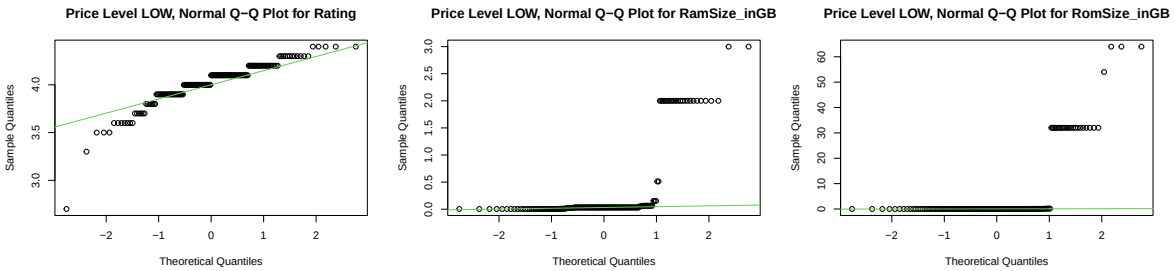
5.1.1 Quadratic Discriminant Analysis (LDA) We want to use LDA to classify our observations into mobile phone price level: "Low", "Medium", "High", "Very High". However, we know LDA has 2 assumptions:

- The distribution of the predictors is normally distributed within each group.
- The homogeneity of variance-covariance matrices

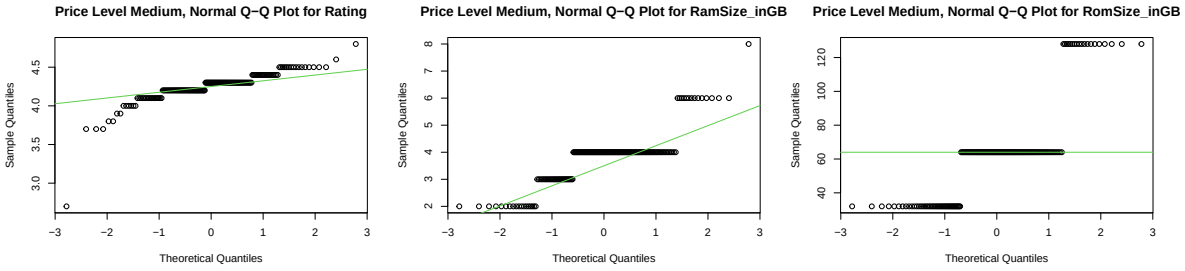
Based on EDA in section 4.2, we know three **numeric features** have a great impact on price level a mobile phone belongs to, which are *Rating*, *RamSize_inGB* and *RomSize_inGB*. As such, we will do a test for normal distribution for each predictor in each price level. Because we have 4 different price levels and 3 variables, the resulting normality check would be 4*3 = 12 comparison. We use Q-Q plot and Shapiro test for normality check.

```
#split the dataset based on the price level
mobile_dataset_low <- mobile_dataset[mobile_dataset$Price_Level == "Low", ]
mobile_dataset_medium <- mobile_dataset[mobile_dataset$Price_Level == "Medium", ]
mobile_dataset_high <- mobile_dataset[mobile_dataset$Price_Level == "High", ]
mobile_dataset_very_high <- mobile_dataset[mobile_dataset$Price_Level == "Very
↪  High", ]
```

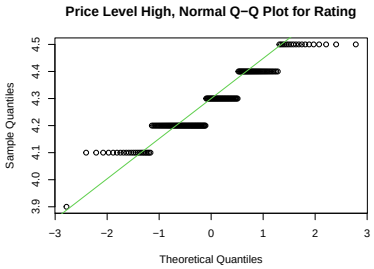
```r
#generate the QQ plot for each price level
variables <- c("Rating", "RamSize_inGB", "RomSize_inGB")
par(mfrow = c(1,3))
for (i in variables){
  qqnorm(mobile_dataset_low[[i]], main = paste("Price Level LOW, Normal Q-Q Plot
  ↪  for", i))
  qqline(mobile_dataset_low[[i]], col = 3)
}
```

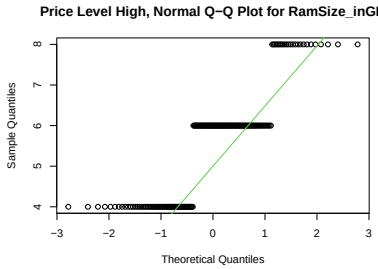


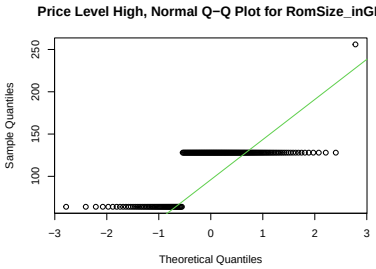

```r
par(mfrow = c(1,3))
for (i in variables){
  qqnorm(mobile_dataset_medium[[i]], main = paste("Price Level Medium, Normal Q-Q
  ↪  Plot for", i))
  qqline(mobile_dataset_medium[[i]], col = 3)
}
```



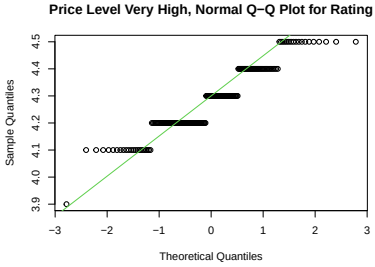

```r
par(mfrow = c(1,3))
for (i in variables){
  qqnorm(mobile_dataset_high[[i]], main = paste("Price Level High, Normal Q-Q Plot
  ↪  for", i))
  qqline(mobile_dataset_high[[i]], col = 3)
}
```

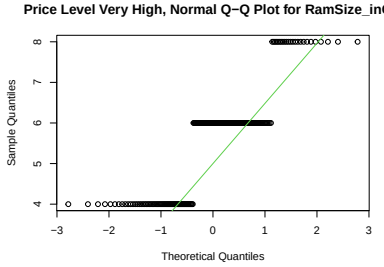


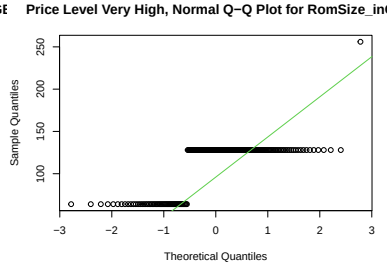





```
par(mfrow = c(1,3))
for (i in variables){
  qqnorm(mobile_dataset_high[[i]], main = paste("Price Level Very High, Normal Q-Q
  ↪  Plot for", i))
  qqline(mobile_dataset_high[[i]], col = 3)
}
```








```
#We also run the shapiro test to statistically conclude the result
p_value_rating <- c(shapiro.test(mobile_dataset_low$Rating)$p.value,
↪  shapiro.test(mobile_dataset_medium$Rating)$p.value,
                    shapiro.test(mobile_dataset_high$Rating)$p.value,
                    shapiro.test(mobile_dataset_very_high$Rating)$p.value)
p_value_RamSize_inGB <- c(shapiro.test(mobile_dataset_low$RamSize_inGB)$p.value,
↪  shapiro.test(mobile_dataset_medium$RamSize_inGB)$p.value,
                    shapiro.test(mobile_dataset_high$RamSize_inGB)$p.value,
                    shapiro.test(mobile_dataset_very_high$RamSize_inGB)$p.value)
p_value_rating_RomSize_inGB <-
↪  c(shapiro.test(mobile_dataset_low$RomSize_inGB)$p.value,
↪  shapiro.test(mobile_dataset_medium$RomSize_inGB)$p.value,
                    shapiro.test(mobile_dataset_high$RomSize_inGB)$p.value,
                    shapiro.test(mobile_dataset_very_high$RomSize_inGB)$p.value)
p_value_df <-
↪  data.frame(p_value_rating,p_value_RamSize_inGB,p_value_rating_RomSize_inGB)
rownames(p_value_df) <- c("Low", "Medium", "High", "Very High")
p_value_df
```

```
##           p_value_rating p_value_RamSize_inGB p_value_rating_RomSize_inGB
## Low         1.470349e-10        1.875399e-22               7.757042e-23
## Medium      6.944763e-16        6.976122e-16               2.960373e-18
## High        9.714119e-09        3.072293e-15               1.522047e-20
## Very High   1.078638e-07        5.203225e-15               1.132641e-21
```

Based on the Q-Q plots (dots not fall on the line) and Shapiro test (p value is $< 5\%$), we can conclude that all variables are not normal. Therefore, we will not preceded with LDA model. Although Quadratic Discriminant Analysis (QDA) also requires normality assumption, we still want to try QDA (in the next section) since it normally has less strict assumptions. NOTE, the above code is inspired by Pascal Schmidt from post Assumption Checking of LDA vs. QDA – R Tutorial Pima Indians Data Set.

5.1.2 Quadratic Discriminant Analysis (QDA)

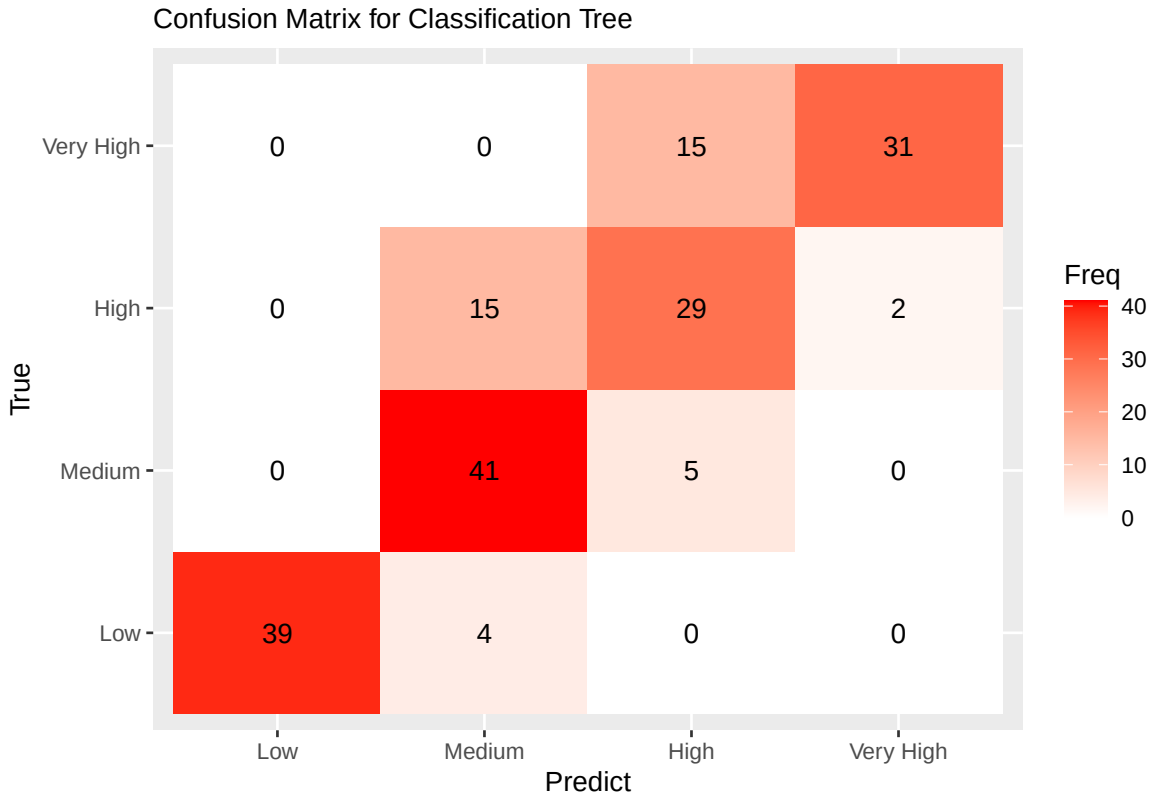
In consistent with LDA, we use the same three numeric features that have a great impact on price level a mobile phone belongs to, which are *Rating*, *RamSize_inGB* and *RomSize_inGB*. To that end, we split the dataset into 75% for training and 25% for testing purpose. We use each "Price_Level" as the stratum and the proportional allocation principle to get a stratified sample. Then we fit the data into Quadratic Discriminant Analysis (QDA) as follows:

```
set.seed(2023)
Ny <- round(table(mobile_dataset$Price_Level)[unique(mobile_dataset$Price_Level)]*
↪  0.75)
#Create the sample from the population
idx=sampling:::strata(mobile_dataset, stratanames=c("Price_Level"), size=Ny,
↪  method="srswor")
strata_sample <- getdata(mobile_dataset,idx)
train <- mobile_dataset[idx$ID_unit,]
test <- mobile_dataset[-idx$ID_unit,]
#Train the data using Quadratic Discriminant Analysis
Model.fit<-qda(Price_Level~Rating+RamSize_inGB+RomSize_inGB, data = train)
Model.fit
cat(rep("-", 50), "\n")
#This plot is showing that LD1 can do a really good to separate these species rather
↪  than LD2
# partimat(Price_Level~Rating+RamSize_inGB+RomSize_inGB, data = train, method="qda")
```

```
## Call:
## qda(Price_Level ~ Rating + RamSize_inGB + RomSize_inGB, data = train)
##
## Prior probabilities of groups:
##       Low    Medium      High Very High
## 0.2352941 0.2555147 0.2555147 0.2536765
##
## Group means:
##             Rating RamSize_inGB RomSize_inGB
## Low       4.012500    0.3342734     5.949688
## Medium    4.237410    3.8201439    62.848921
## High      4.276259    5.6258993   113.266187
## Very High 4.341304    5.5797536   142.376812
## - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - -
```

At last, we apply this model on the testing dataset, and calculate the misclassification rate.

```
Prob.predict<-predict(Model.fit,test,type="response")
ggplot(as.data.frame(table(Prob.predict$class,test$Price_Level)), aes(x = Var1, y =
↪  Var2, fill = Freq)) +geom_tile() + geom_text(aes(label = round(Freq, 1))) +
↪  scale_fill_gradient(low = "white", high = "red") + labs(y="True", x="Predict",
↪  subtitle="Confusion Matrix for Classification Tree")
```




```
cat(rep("-", 45), "\n")
cat("The misclassification rate for QDA is: ", mean(Prob.predict$class !=
↪  test$Price_Level))
```

```
## - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - -
## The misclassification rate for QDA is:  0.2265193
```

Conclusion: Quadratic Discriminant Analysis has a good performance to predict the mobile phone price level using only 3 variables (*Rating*, *RamSize_inGB* and *RomSize_inGB*), with a relatively high accuracy (77%).

5.1.3 Decision Tree (Classification)

To be consistent and comparable with QDA, we again use these three variables *Rating*, *RamSize_inGB* and *RomSize_inGB* to build the decision tree model. We split the dataset into 75% for training and 25% for testing purpose. We use each "Price_Level" as the stratum and the proportional allocation principle to get a stratified sample. Then we fit the data into Classification tree model as follows:

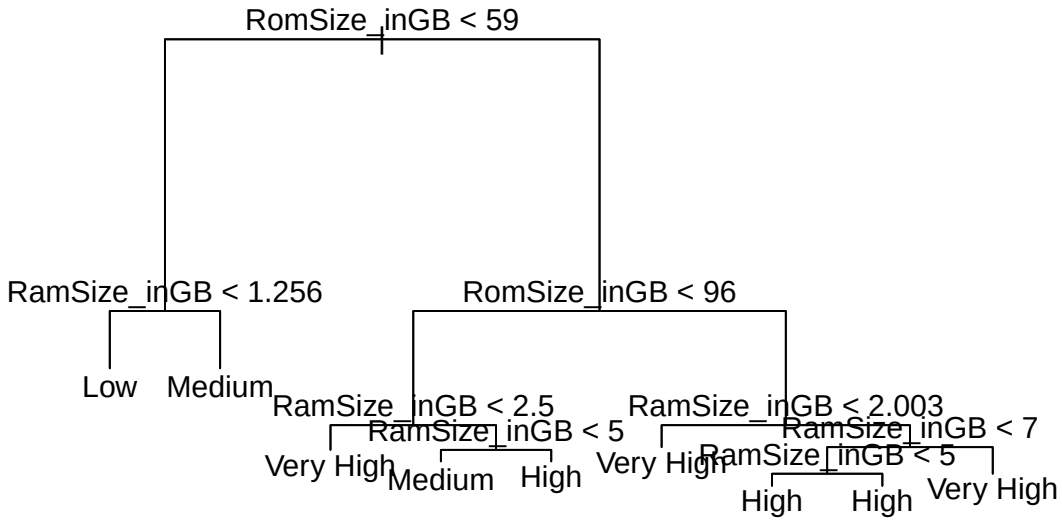
```
set.seed(2023)
Ny <- round(table(mobile_dataset$Price_Level)[unique(mobile_dataset$Price_Level)]*
↪  0.75)
#Create the sample from the population
idx=sampling:::strata(mobile_dataset, stratanames=c("Price_Level"), size=Ny,
↪  method="srswor")
strata_sample <- getdata(mobile_dataset,idx)
train <- mobile_dataset[idx$ID_unit,]
test <- mobile_dataset[-idx$ID_unit,]
```

```
#Fit the train data into the tree model
tree.class<-tree(factor(Price_Level)~Rating+RamSize_inGB+RomSize_inGB, train)
summary(tree.class)
```

```
##
## Classification tree:
## tree(formula = factor(Price_Level) ~ Rating + RamSize_inGB +
##     RomSize_inGB, data = train)
## Variables actually used in tree construction:
## [1] "RomSize_inGB" "RamSize_inGB"
## Number of terminal nodes:  9
## Residual mean deviance:  1.055 = 564.3 / 535
## Misclassification error rate: 0.2335 = 127 / 544
```

The tree is plotted without pruning as follows. There are a total of 9 terminal nodes in the tree.

```
#Let us plot the tree as well
plot(tree.class)
text(tree.class,pretty=0)
```

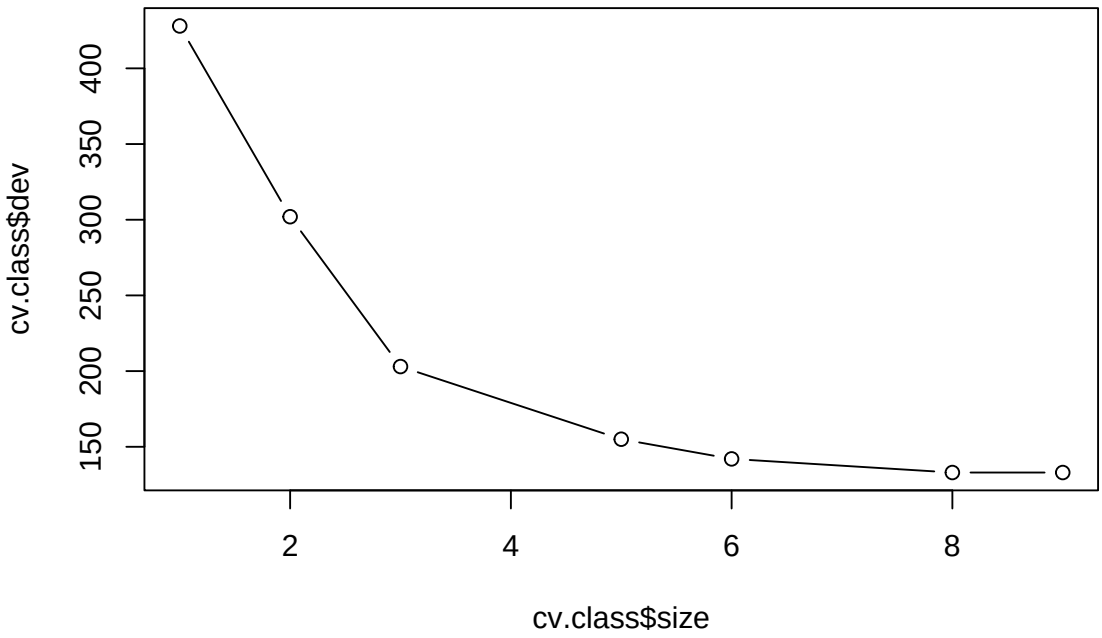



```
# rpart_fit <- rpart(factor(Price_Level)~Rating+RamSize_inGB+RomSize_inGB, train,
↪  method = 'class')
# rpart.plot(rpart_fit)
```

To find the best tree size, we used cross-validation to select the "best" number of tree size (the terminal nodes). Based on the following plot, it seems tree size 9 gives the smallest deviance. Just to demonstrate

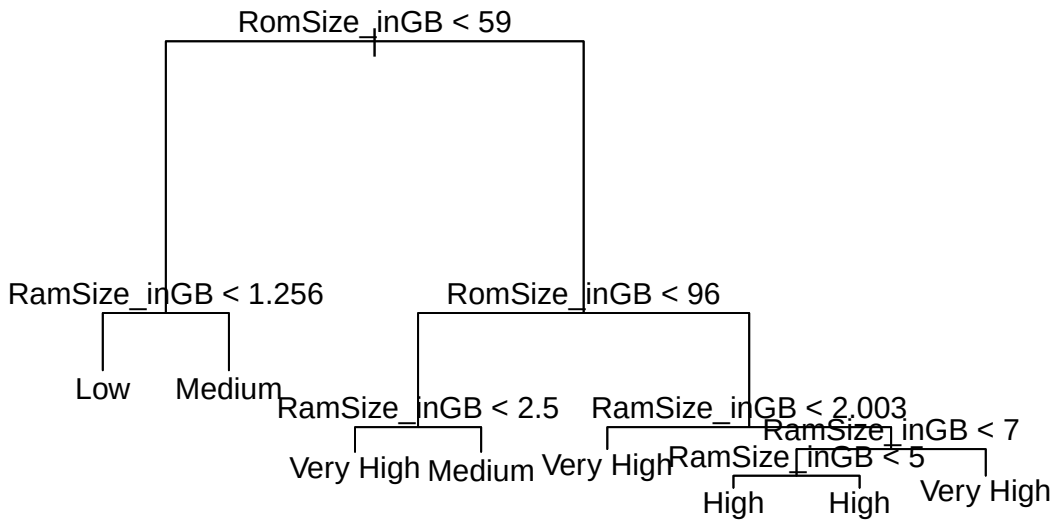
how prunned tree works and also reduce the complexity of tree, we decide to use 8 as the "best" tree size.

```
cv.class<-cv.tree(tree.class, FUN = prune.misclass)
plot(cv.class$size, cv.class$dev,type="b")
```



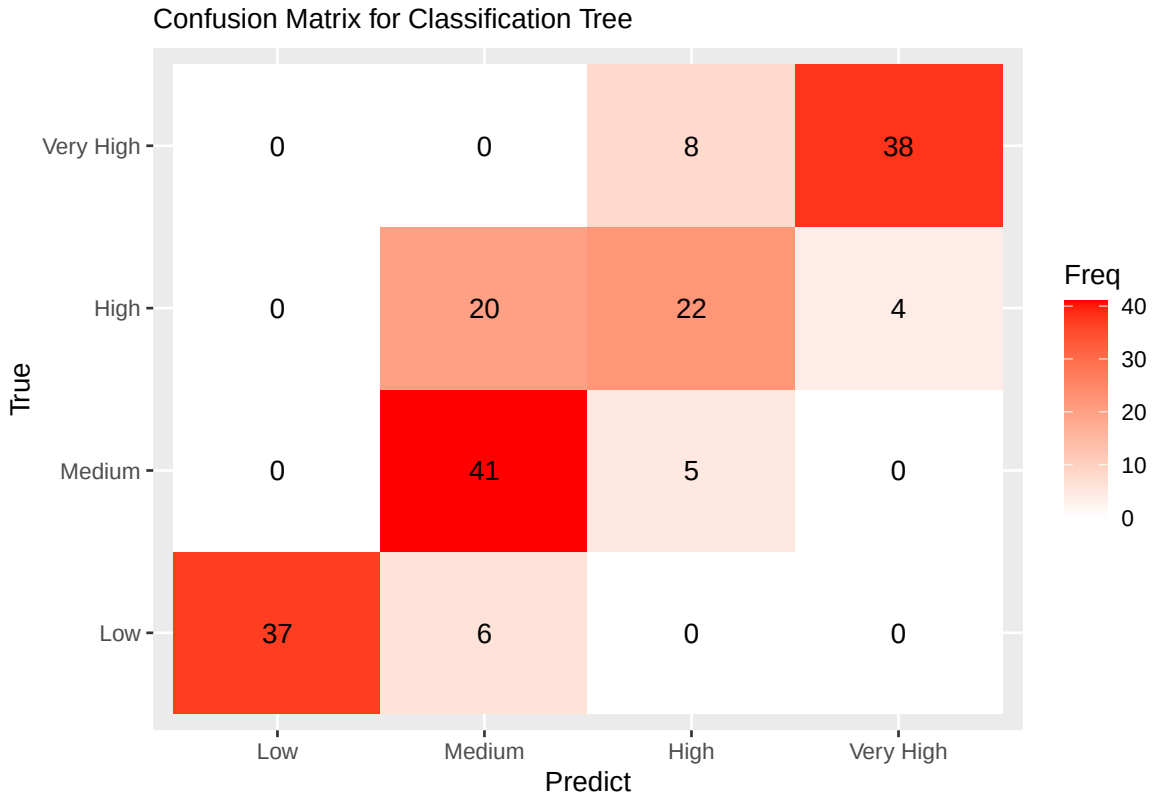
A tree after prunning is plotted as follows. There are a total of 8 terminal nodes in the tree.

```
prune.class=prune.tree(tree.class,best=8)
plot(prune.class)
text(prune.class,pretty=0)
```



Finally, we use the pruned tree to do prediction.

```
prune.pred=predict(prune.class,test,type="class")
ggplot(as.data.frame(table(prune.pred,test$Price_Level)), aes(x = prune.pred, y =
↪  Var2, fill = Freq)) +geom_tile() + geom_text(aes(label = round(Freq, 1))) +
↪  scale_fill_gradient(low = "white", high = "red") + labs(y="True", x="Predict",
↪  subtitle="Confusion Matrix for Classification Tree")
```




```
cat(rep("-", 45), "\n")
cat("The misclassification rate for regression tree is: ", mean(prune.pred !=
↪  test$Price_Level))
```

```
## - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - -
## The misclassification rate for regression tree is:  0.2375691
```

Conclusion: Decision Tree (Classification) has also a good performance to predict the mobile phone price level using only 3 variables (*Rating*, *RamSize_inGB* and *RomSize_inGB*), with a relatively high accuracy (76.2%).

5.1.4 Multinomial Regression

This is an experimental analysis. Based on EDA in section 4.2, we know that Company name (branding) also plays a big role in the price level. We also know that Rom size of a mobile phone matters a lot as well. We are curious to see if a combination of *Company* and *RomSize* can also be used to distinguish the price level.

Normally, we would split the dataset into 75% for training and 25% for testing purpose. However, because our sample size is small, not every Company has multiple records in our dataset. Therefore, in the following test, we use whole sample as the training and test purpose.

Then we fit the data into Multinomial Regression as follows. Note, because our response is ordinal, we use Cumulative logit model; also parallel = TRUE: means beta is the same, this is a simple model.

We also use Chi square test to test for the goodness-of-fit for this model.

H_0 : The Cumulative logit model fits the observations

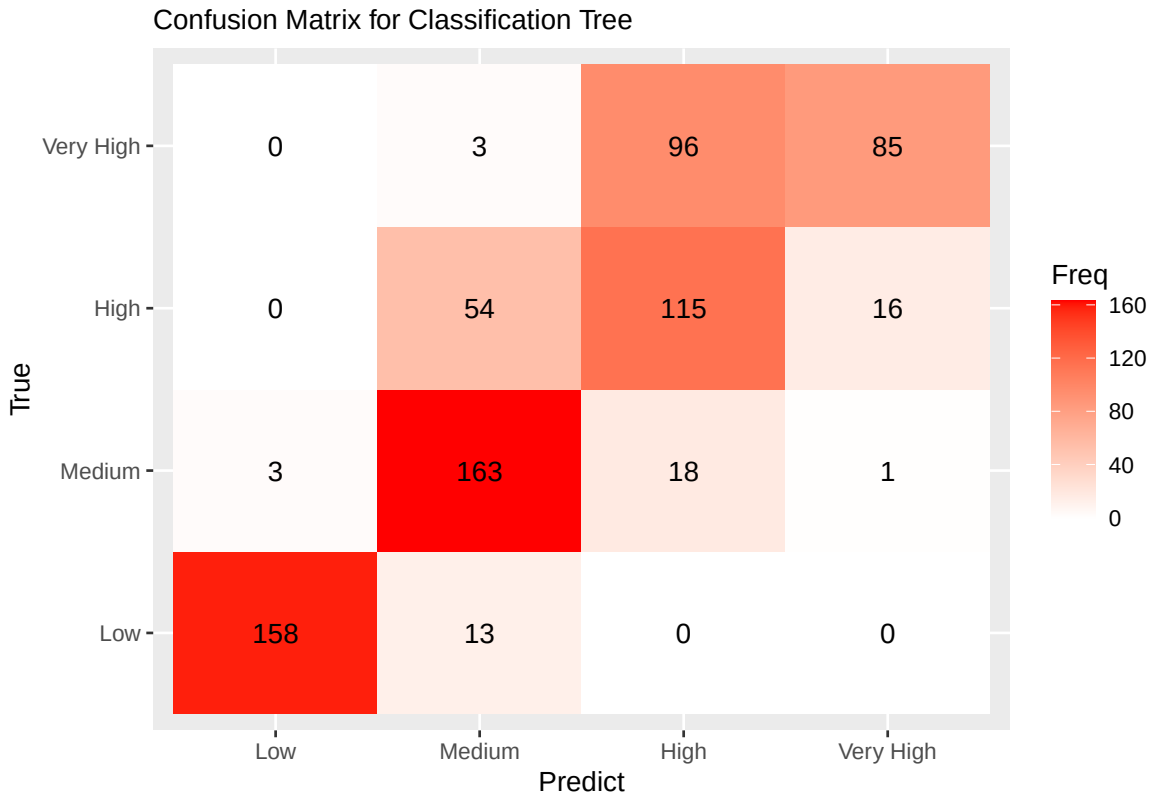
H_1 : The Cumulative logit model does not fit the observations

```
comany_rom_train <- mobile_dataset[c("Company", "RomSize_Ori", "Price_Level")]
multi_train_fit <- vglm(Price_Level~Company+RomSize_Ori,family=cumulative(parallel =
↪  TRUE),data=comany_rom_train)
cat("The p value for the chi test is: ",
↪  1-pchisq(deviance(multi_train_fit),df.residual(multi_train_fit)))
cat("\nThe p-value here is large = 1, so we cannot reject null hypothesis. Our model
↪  seems to be provide a good fit.")
```

```
## The p value for the chi test is:  1
## The p-value here is large = 1, so we cannot reject null hypothesis. Our model seems to be provide
```

Finally, we use this model to predict use the same training dataset, as a demonstration purpose.

```
pred_fit <- predict(multi_train_fit, type="response")
#Use the record that has the highest probability as the final predication for each
↪  row.
pred_fit_class <-factor(dimnames(pred_fit)[[2]][max.col(pred_fit, 'first')], levels
↪  = c("Low", "Medium", "High", "Very High"))
ggplot(as.data.frame(table(pred_fit_class, mobile_dataset$Price_Level)), aes(x =
↪  pred_fit_class, y = Var2, fill = Freq)) +geom_tile() + geom_text(aes(label =
↪  round(Freq, 1))) + scale_fill_gradient(low = "white", high = "red") +
↪  labs(y="True", x="Predict", subtitle="Confusion Matrix for Classification Tree")
```




```
cat(rep("-", 45), "\n")
cat("The misclassification rate for Multinomial Regression is: ",
↪  mean(pred_fit_class != mobile_dataset$Price_Level))
```

```
## - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - -
## The misclassification rate for Multinomial Regression is:  0.2813793
```

Conclusion: Multinomial Regression has also a good performance to predict the mobile phone price level using only 2 variables (*Company* and *RomSize*), with a relatively high accuracy (71.9%).

5.2: Cross-Validation

In section 5.1, we have compared three different models based on their misclassification rate: **Quadratic Discriminant Analysis (QDA)** = 0.2265193, **Decision Tree (Classification)** = 0.2375691, and **Multinomial Regression** = 0.2813793. In order to compare model performance, we decide to also use stratified 10-fold cross-validation to calculate the cross-validation errors of these 3 methods.

```
cat("\nFirst I am using the 10-fold cross validation for Quadratic Discriminant
↪  Analysis")
set.seed(2023)
#Create 10 folds
folds<-createFolds(mobile_dataset$Price_Level, k=10)
#Define a function to calculate the misclassification rate for each fold
misrate_fold<-function(idx){
  Train<-mobile_dataset[-idx,]
  Test<-mobile_dataset[idx,]
  fit <- qda(Price_Level~Rating+RamSize_inGB+RomSize_inGB, data = Train)
  pred<-predict(fit,Test)
  return(1- mean(pred$class == Test$Price_Level))
}
#Get the misclassification rate from each fold
type_misrate_fold=lapply(folds,misrate_fold)
#The average of misclassification rate  for 10 folds is:
cat("\nThe average of misclassification rate for 10 folds
    cross validation of Quadratic Discriminant Analysis is :",
    mean(as.numeric(type_misrate_fold)))
cat("\n")
cat(rep("-", 45), "\n")


cat("\nSecond I am using the 10-fold cross validation for Decision Tree
↪  (Classification)")
set.seed(2023)
#Create 10 folds
folds<-createFolds(mobile_dataset$Price_Level, k=10)
#Define a function to calculate the misclassification rate for each fold
misrate_fold<-function(idx){
  Train<-mobile_dataset[-idx,]
  Test<-mobile_dataset[idx,]
  fit <- tree(factor(Price_Level)~Rating+RamSize_inGB+RomSize_inGB, data = Train)
  pred<-predict(fit,Test, type = 'class')
  return(1- mean(pred == Test$Price_Level))
}

#Get the misclassification rate from each fold
```

```r
type_misrate_fold=lapply(folds,misrate_fold)
#The average of misclassification rate  for 10 folds is:
cat("\nThe average of misclassification rate for 10 folds cross
    validation of Decision Tree (Classification) is :",
↪  mean(as.numeric(type_misrate_fold)))
cat("\n")
cat(rep("-", 45), "\n")

cat("\nBecause our sample size is small, not every Company has multiple records in
↪  our dataset. \nTherefore, we are not able to perform cross-validation for
↪  Multinomial regression.")
```

```
##
## First I am using the 10-fold cross validation for Quadratic Discriminant Analysis
## The average of misclassification rate for 10 folds
##     cross validation of Quadratic Discriminant Analysis is : 0.2690109
## - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - -
##
## Second I am using the 10-fold cross validation for Decision Tree (Classification)
## The average of misclassification rate for 10 folds cross
##     validation of Decision Tree (Classification) is : 0.2314057
## - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - - -
##
## Because our sample size is small, not every Company has multiple records in our dataset.
## Therefore, we are not able to perform cross-validation for Multinomial regression.
```

5.3: Summary for Prediction of Mobile Phone Price Level

To summarize this part of analysis, we find some contradictory results. We used the balanced dataset trying to classify the Mobile Phone Price Level. In Section 5.1, we have the following misclassificaiton rate from each model:

- **Quadratic Discriminant Analysis (QDA)**: 0.2265193
- **Decision Tree (Classification)**: 0.2375691
- **Multinomial Regression**: 0.2813793

We can see Quadratic Discriminant Analysis (QDA) gives the lowest misclassification rate, making this model the best one. However, when we do the 10-folds cross validation, we have the following misclassificaiton rate from each model:

- **Quadratic Discriminant Analysis (QDA)**: 0.2690109
- **Decision Tree (Classification)**: 0.2314057
- **Multinomial Regression**: Not Available (see section 5.2 explanation)

From this result, Decision Tree (Classification) gives the lowest misclassification rate. Because cross-validation is averaging multiple misclassificaiton rate, we think this result is more reliable.

So our final conclusion is that Decision Tree (Classification) can best predict the Mobile Phone Price Level using only 3 variables (*Rating*, *RamSize_inGB* and *RomSize_inGB*), with a relatively high accuracy (76.9%).

Phone Company Categorization

The goal of this section is to look at categorization of phones that fall within the most expensive bracket. Among these phones are Apple, Google, Samgsung, Vivo and Iqoo. Initially, we wanted to look at categorizing Apple, Google and Samgsung, but the number of entries of Google in the dataset prevented us from using them (Unable to split Google into testing and training). For this reason, we included Vivo and Iqoo. For categorization, we chose to compare four different classification methods: LDA, QDA, Logistic Regression and an Bayesian Classifier and KNN.

Reading in the data

The first step prior to building the different classifiers was to read in the data into r.

```
cellphone = mobile_dataset
```

Manipulation of the dataframe prior to categorization

With the dataset in r, we are now able to reduce our dataframe to only contain the different companies which we want to perform classification on.

```
cellphone = cellphone[cellphone$Company %in% c("APPLE", "SAMSUNG", "VIVO", "IQOO"),
↪  ]
cellhone = cellphone %>% drop_na()
```

The next step is to chose which classifiers we want to use to perform analysis. Through playing around with the different attributes in the dataset, the rating, Price, number of ratings, total reviews and Rom Size were chosen as the variables used to classify company. Color was also considered, but since there are so many different unique colors, the test set would always contain a color not seen in training and the model would not function. With some possible exceptions, the color of the phone is likely not proprietary to the company and thus isn't crutial for categorization.

```
df2 <- cellphone[, (names(cellphone) %in%
↪  c("Rating","Price","No_of_ratings","TotalReviwes","RomSize_inGB", "Company"))]
```

In order to test some of the assumptions requried to use the aforementioned classification methods, the order of the columns is changed so that company, our dependant variable, appears in the last column of the data frame.

```
order<- df2[,c(6,2,3,4,5,1)]
order$Company <- as.factor(as.character(order$Company))
```

Testing Assumptions

First, we will test the assumption of homogeneity of covariance matrices. Homogeneity of covariance matrices is required to use LDA as a classification method. We can test for Homogeneity using the boxM test.

The hypotheses for the test are as follows:

H_0 : The observed covariance matrices for the dependent variables are equal across groups

H_a : The observed covariance matrices for the dependent variables are NOT equal across groups

```
library(heplots)
```

```
## Loading required package: car
```

```
## Loading required package: carData
```

```
##
## Attaching package: 'car'
```

```
## The following object is masked from 'package:dplyr':
##
##     recode
```

```
## The following object is masked from 'package:purrr':
##
##     some
```

```
## The following object is masked from 'package:VGAM':
##
##     logit
```

```
## Loading required package: broom
```

```
boxM(order[,1:5], order$Company)
```

```
##
##  Box's M-test for Homogeneity of Covariance Matrices
##
## data:  order[, 1:5]
## Chi-Sq (approx.) = 509.88, df = 45, p-value < 2.2e-16
```

We can see that since P is very small, we reject the null hypothesis in favor of the alternate hypothesis, indicating we have heterogeneity of covariance matrices. Our assumption of homogeneity of covariance matrices for LDA therefor is not met.

We can try to normalize the data to see if it has an impact on the result.

```
order2 <- order %>%
↪  mutate_at(c("Rating","Price","No_of_ratings","TotalReviwes","RomSize_inGB"),
↪  ~(scale(.) %>% as.vector))
order3 = order2
```

```
library(heplots)
boxM(order2[,1:5], order$Company)
```

```
##
##  Box's M-test for Homogeneity of Covariance Matrices
##
## data:  order2[, 1:5]
## Chi-Sq (approx.) = 509.88, df = 45, p-value < 2.2e-16
```

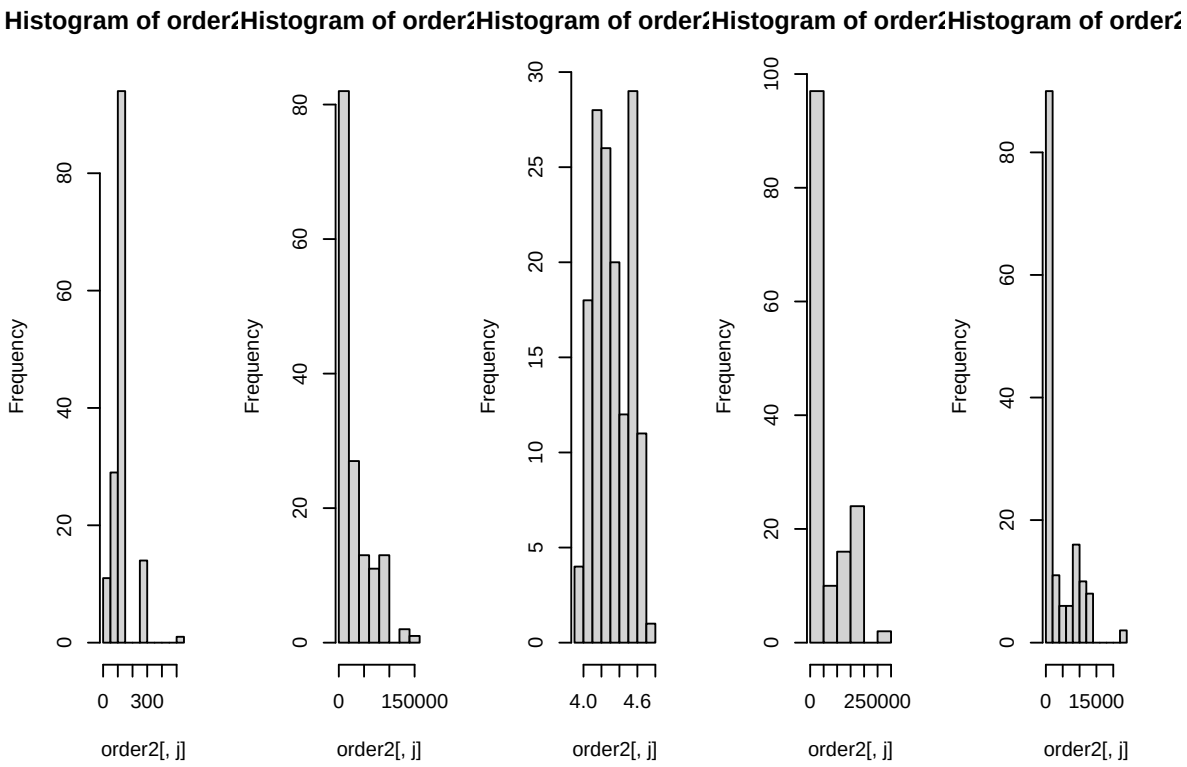
Normalization using the scale function has no effect on changing making the covariance matrices homogenous.

The covariance matrices do not need to be homogeneous to use QDA, but one of the assumtions of QDA is a gaussian distribution of the independant variables.

```
order2 = order[,1:5]
order2 <- as.matrix(order2[,1:5])
```

We are able to visualize the distribution of the indenpendant variable by using histograms of each of the data points.

```
par(mfrow = c(1, ncol(order2)))
for(j in 1:ncol(order2)){
  hist(order2[,j])}
```



From the histograms, Price, number of ratings and the total reviews do not appear to follow a normal distribution. We can use the Shapiro-Wilk normality test to validate these results.

Below is the null hypothesis for the test.

H_0 : The data follow a Gaussian distribution

H_a : The data does NOT follow a gaussian distribution

```
library(mvnormtest)
mshapiro.test(t(order2))
```

```
##
##  Shapiro-Wilk normality test
##
## data:  Z
## W = 0.83086, p-value = 7.943e-12
```

From p-value = 7.943e-12, we reject the null hypothesis in favor of the alternate hypothesis indicating that the independent variables do not follow a normal distribution.

We also need to test to see if multicollinearity is present in our predictors.

```
faraway::vif(order2)
```

```
##  RomSize_inGB         Price        Rating No_of_ratings  TotalReviwes
##      1.497726      3.018487      3.426773     31.038830     28.122784
```

It appears we need to remove number of ratings from our model because there is multicollinearity.

```
order3 <- order3[, -4]
order2 <- order2[, -4]

faraway::vif(order2)
```

```
## RomSize_inGB        Price       Rating TotalReviwes
##     1.495061     2.973678     2.915072     1.452722
```

Comparing Classifiers

LDA and QDA Classification While we have not met all the assumptions for LDA and QDA, we will try and do a classification using these methods regardless and look at the misclassification rates as a metric of their performance.

```
library(MASS)
library(ISLR)
set.seed(10)

sample <- sample(c(TRUE, FALSE), nrow(order2), replace=TRUE, prob=c(0.7,0.30))
train  <- order3[sample, ]
test   <- order3[-sample, ]

qda.fit<-qda(Company~Rating+Price+TotalReviwes+RomSize_inGB, data = train)
lda.fit<-lda(Company~Rating+Price+TotalReviwes+RomSize_inGB, data = train)
```

```
# Testing the LDA classifier with the test data
lda.pred=predict(lda.fit, test)
table(lda.pred$class, test$Company)
```

```
##
##            APPLE IQOO SAMSUNG VIVO
##   APPLE       46    0       0    0
##   IQOO         0    0       0    0
##   SAMSUNG      0    7      47   14
##   VIVO         0    1      13   20
```

```
mean(lda.pred$class != test$Company)
```

```
## [1] 0.2364865
```

The misclassification rate with Lda is 0.2364865.

```
#Testing the QDA classifier with the test data
qda.pred=predict(qda.fit, test)
```

```
table(qda.pred$class, test$Company)
```

```
##
##            APPLE IQOO SAMSUNG VIVO
##   APPLE       46    0       0    0
##   IQOO         0    5       1    0
##   SAMSUNG      0    3      40    9
##   VIVO         0    0      19   25
```

```
mean(qda.pred$class != test$Company)
```

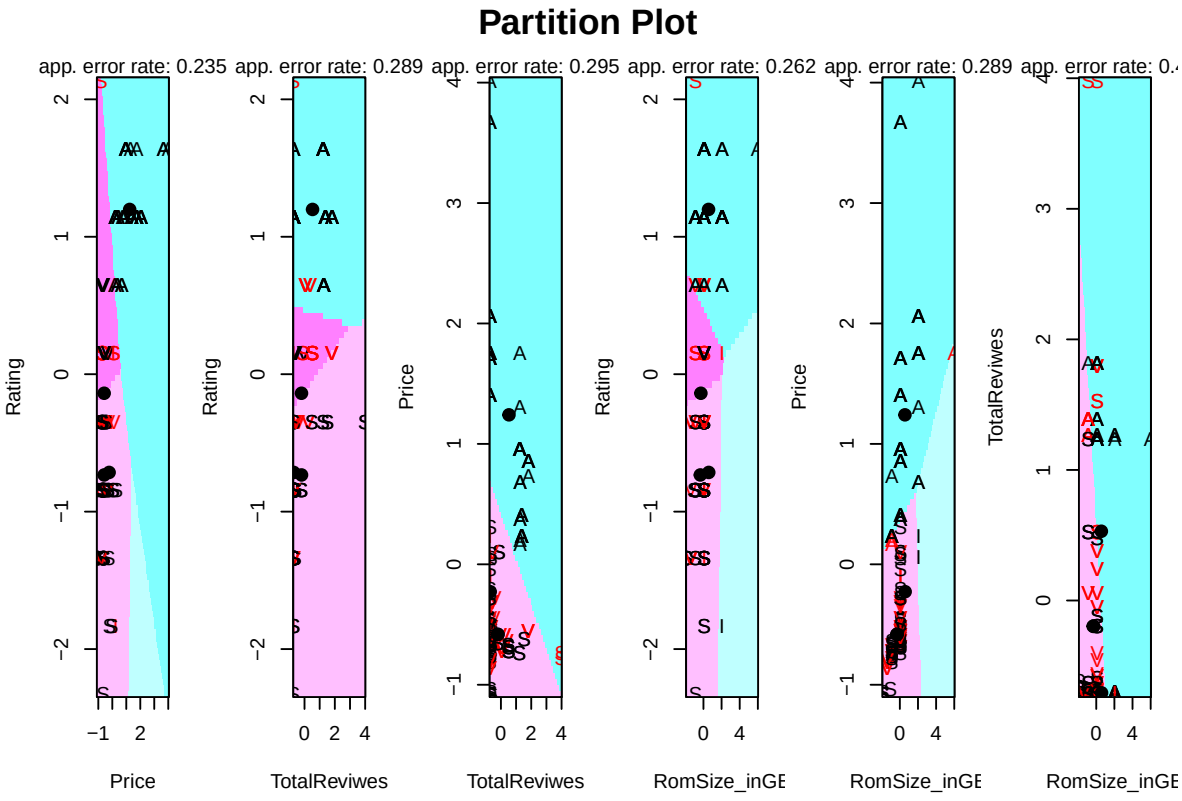
```
## [1] 0.2162162
```

The misclassification rate with qda is 0.2147651.

We are also able to visualize how LDA and QDA separate the data using klaR's partimat function. Using this tool it's possible to visualize how each of the different independent variables categorizes the company. It's also an important oberservation to notice how LDA makes distinctions with linear sections, where as the different sections of QDA are much more curved, hens 'quadratic'.

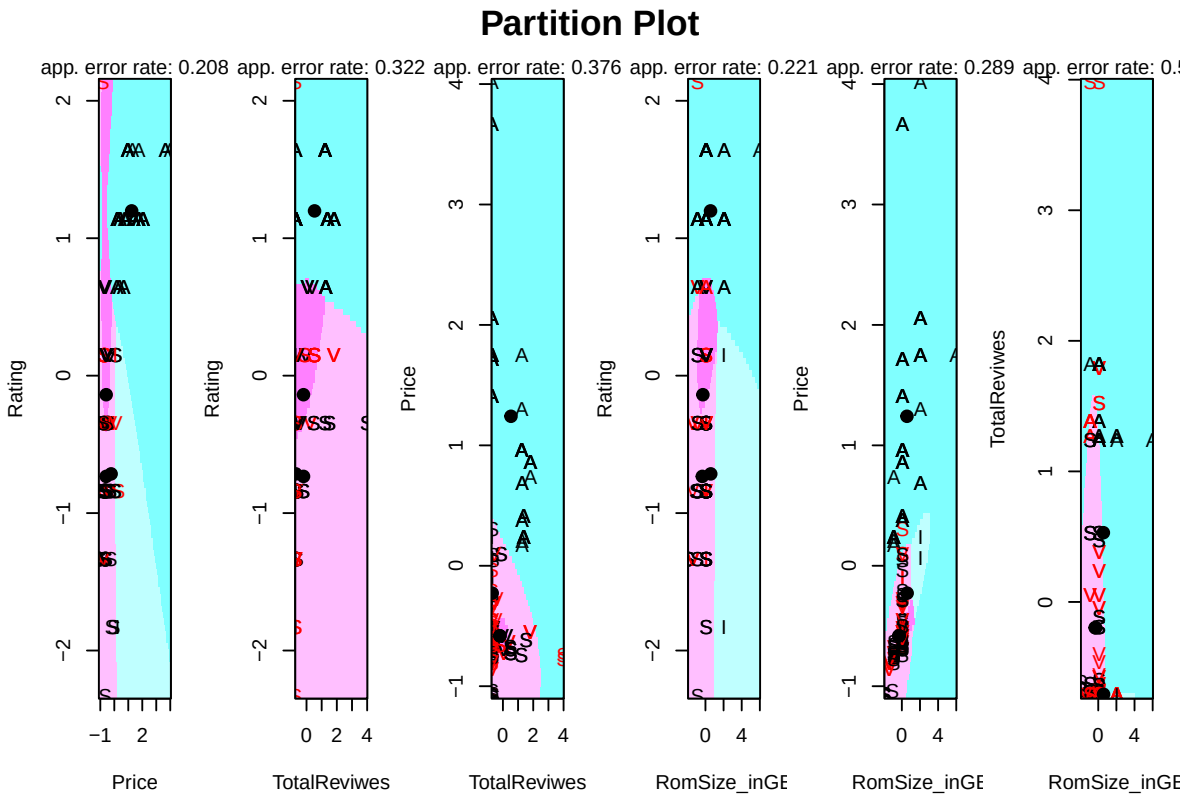
Below is the lDA partiton plot.

```
library(klaR)
partimat(Company ~ Rating+Price+TotalReviwes+RomSize_inGB, data = order3,
         method = "lda", nplots.vert = 1)
```



Below is the QDA partition plot.

```
partimat(Company ~ Rating+Price+TotalReviwes+RomSize_inGB, data = order3,
         method = "qda", nplots.vert = 1)
```



Recall that linearity was not achieve with price, number of ratings and total reviews, so QDA will be tested again after removing these predictors to see if the result is improved.

```
#removal of non-linear predictors
order4 <- order3[, (names(order3) %in% c("Rating","RomSize_inGB", "Company"))]
```

Building the training and test data for the QDA classifier with only rating and RomSize_inGB as independent variables.

```
set.seed(10)

sample <- sample(c(TRUE, FALSE), nrow(order4), replace=TRUE, prob=c(0.7,0.30))
trainQ  <- order4[sample, ]
testQ   <- order4[-sample, ]

qda.fit<-qda(Company~Rating+RomSize_inGB, data = trainQ)
```

Applying the QDA classification model to the test set.

```
qda.pred=predict(qda.fit, testQ)
table(qda.pred$class, test$Company)
```

```
##
##            APPLE IQOO SAMSUNG VIVO
```

```
##   APPLE      44    0       1    2
##   IQOO        0    1       0    0
##   SAMSUNG     0    7      48   13
##   VIVO        2    0      11   19
```

```
mean(qda.pred$class != test$Company)
```

```
## [1] 0.2432432
```

We can see that the misclassification rate has not changed significantly, and has increased to 0.2432432. Therefor, rating will not be removed from the predictors used in QDA.

Classification using Logistic Regression Moving from LDA and QDA, we can look to see whether a logistic regression classifier has improved classification accuracy. We will use the same predictors as LDA and QDA to have a fair comparison of misclassification rates.

```
require(foreign)
```

```
## Loading required package: foreign
```

```
require(nnet)
```

```
## Loading required package: nnet
```

```
require(ggplot2)
require(reshape2)
```

```
## Loading required package: reshape2
```

```
##
## Attaching package: 'reshape2'
```

```
## The following object is masked from 'package:tidyr':
##
##     smiths
```

```
library(VGAM)

Model.fit<-multinom(Company~Rating+Price+TotalReviwes+RomSize_inGB,  data = train)
```

```
## # weights:  24 (15 variable)
## initial  value 153.878674
## iter  10 value 50.014668
## iter  20 value 41.385169
## iter  30 value 39.045159
## iter  40 value 38.974093
## iter  50 value 38.974050
## iter  60 value 38.969317
## iter  60 value 38.969317
## iter  60 value 38.969317
## final  value 38.969317
## converged
```

```
Prob.predict<-predict(Model.fit, test)
```

```
Actual<-test$Company
table(Prob.predict, Actual)
```

```
##             Actual
## Prob.predict APPLE IQOO SAMSUNG VIVO
##      APPLE      46    0       0    0
##      IQOO        0    5       0    0
##      SAMSUNG     0    3      52   16
##      VIVO        0    0       8   18
```

```
mean(Prob.predict != Actual)
```

```
## [1] 0.1824324
```

We can see that logistic regression worked better than both LDA and QDA, with a misclassification rate of 0.1824324. This increased performance with logistic regression could be a result of the assumtion of homogenous covariance matrices not being met for LDA and doesn't assume the distribution of the data to be Gaussian like QDA.

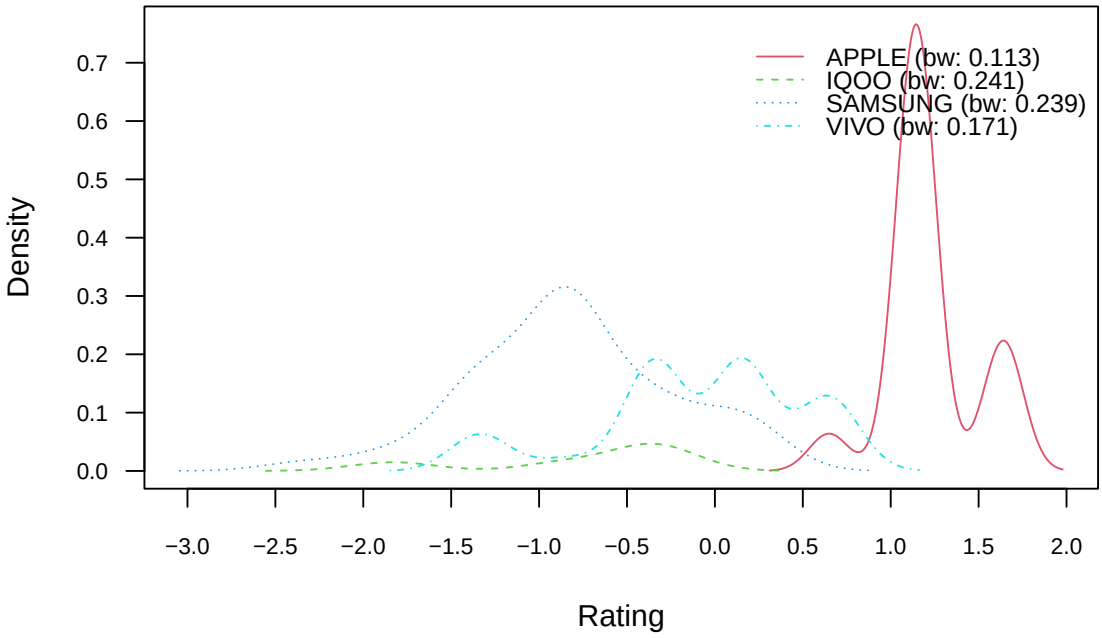
Naive Bayes Classification We will use Naive Bayes to see how it compares to LDA, QDA as well as logistic regression. Included below are the plots to show how the Naive Bayes Classifier works with the density of each of the different companies for a given variable.

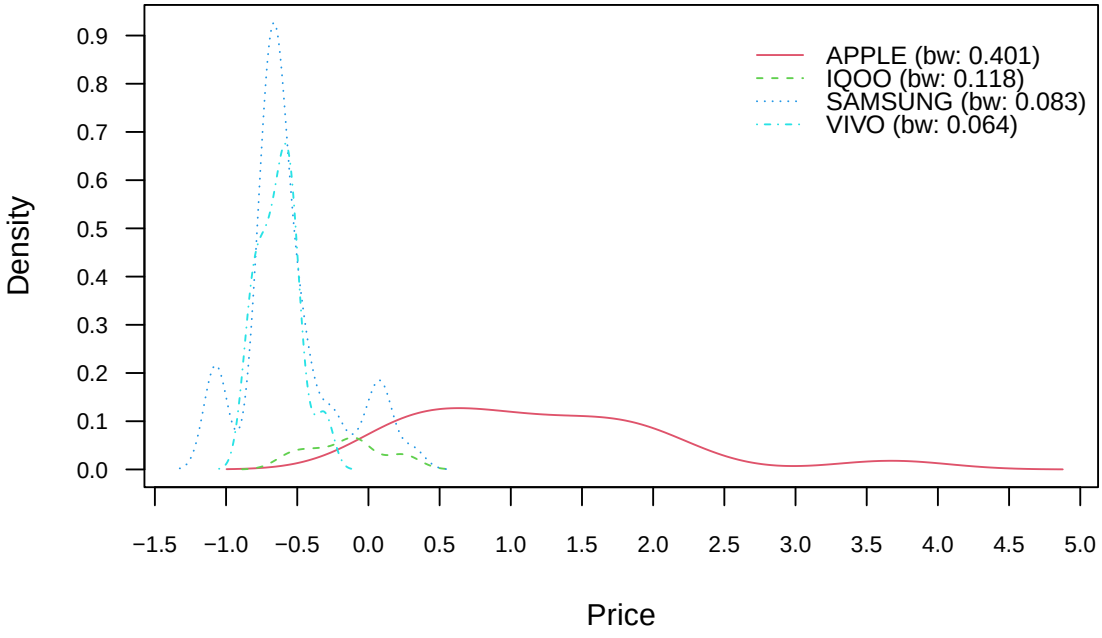
```
library(naivebayes)
```

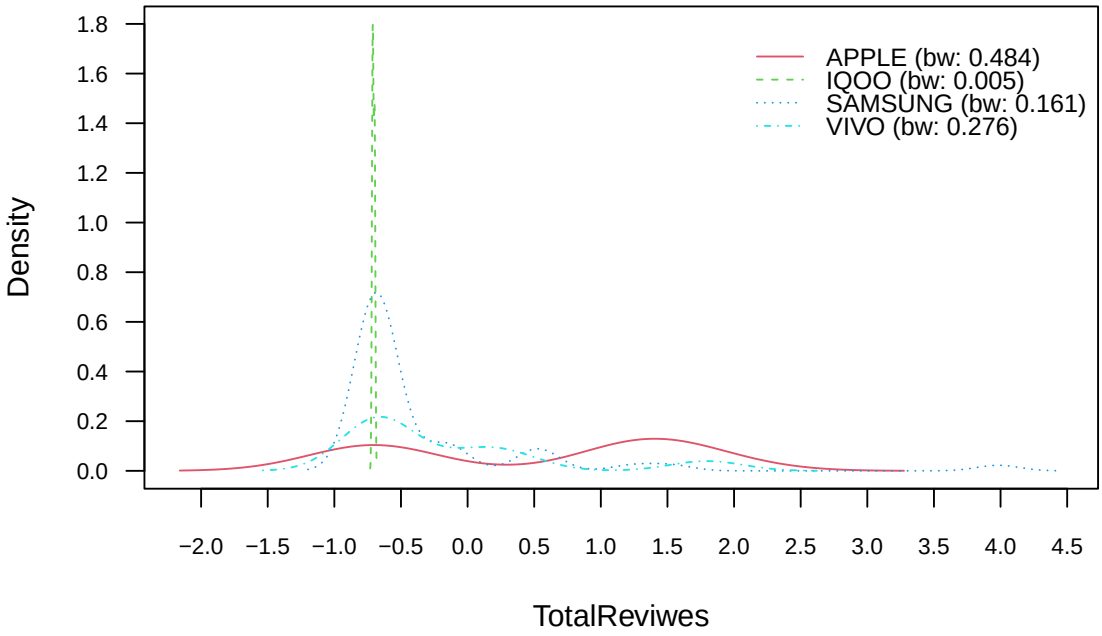
```
## naivebayes 0.9.7 loaded
```

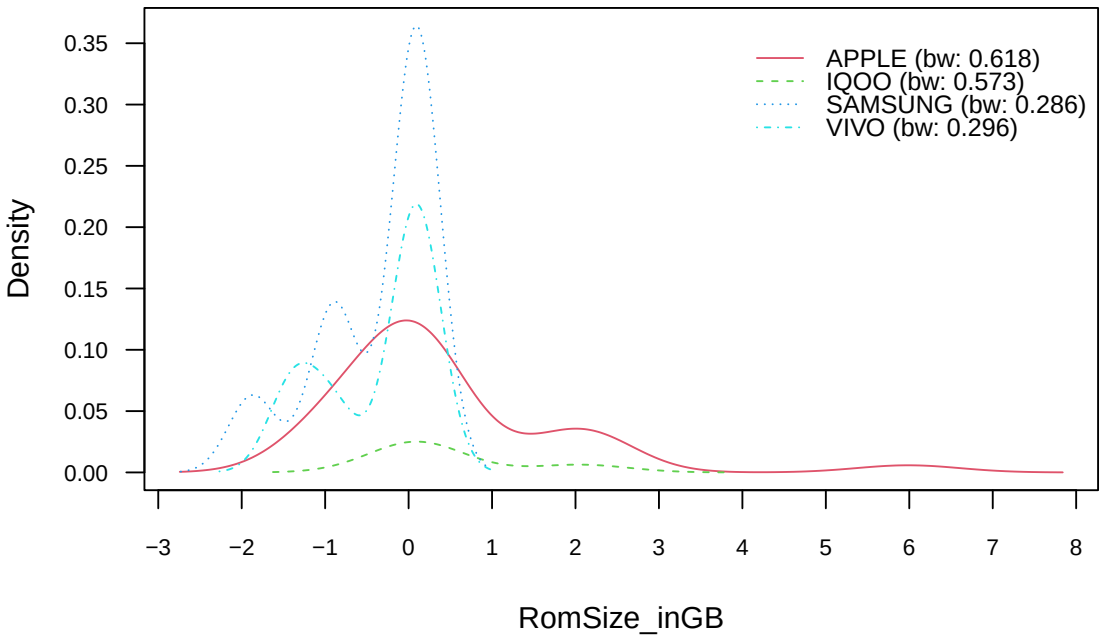
```
set.seed(10)
sample2 <- sample(c(TRUE, FALSE), nrow(order3), replace=TRUE, prob=c(0.7,0.30))
train2  <- order3[sample, ]
test2   <- order3[-sample, ]

modelbayes <- naive_bayes(Company~Rating+Price+TotalReviwes+RomSize_inGB, data =
↪  train2, usekernel = T)
plot(modelbayes)
```


APPLE (bw: 0.113)
IQOO (bw: 0.241)
SAMSUNG (bw: 0.239)
VIVO (bw: 0.171)
Density
Rating
0.0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
−3.0
−2.5
−2.0
−1.5
−1.0
−0.5
0.0
0.5
1.0
1.5
2.0


APPLE (bw: 0.401)
IQOO (bw: 0.118)
SAMSUNG (bw: 0.083)
VIVO (bw: 0.064)
Density
Price
0.0
0.1
0.2
0.3
0.4
0.5
0.6
0.7
0.8
0.9
−1.5
−1.0
−0.5
0.0
0.5
1.0
1.5
2.0
2.5
3.0
3.5
4.0
4.5
5.0


APPLE (bw: 0.484)
IQOO (bw: 0.005)
SAMSUNG (bw: 0.161)
VIVO (bw: 0.276)
Density
TotalReviwes


APPLE (bw: 0.618)
IQOO (bw: 0.573)
SAMSUNG (bw: 0.286)
VIVO (bw: 0.296)
Density
RomSize_inGB

Now to use naive bayes to predict

```
pred <- predict(modelbayes, test2)
```

```
## Warning: predict.naive_bayes(): more features in the newdata are provided as
## there are probability tables in the object. Calculation is performed based on
## features to be found in the tables.
```

```
(tab1 <- table(pred, test2$Company))
```

```
##
## pred      APPLE IQOO SAMSUNG VIVO
##   APPLE      46    0       0    0
##   IQOO        0    5       9    0
##   SAMSUNG     0    3      41    9
##   VIVO        0    0      10   25
```

```
mean(pred != test2$Company)
```

```
## [1] 0.2094595
```

We can see that the misclassification using Naive Bayes is 0.2094595 on the test set. This is less accurate than multinomial logistic regression but performed better than LDA and QDA.

Why did Naive bayes perform worse than multinomial logistic regression? One of the reasons may be the feature independence assumption. We can check the correlation between the variables.

```
print(cor(cellphone[, c('Rating','Price','TotalReviwes','RomSize_inGB')]))
```

```
##                  Rating      Price TotalReviwes RomSize_inGB
## Rating       1.0000000 0.70804693   0.42640871   0.37322466
## Price        0.7080469 1.00000000   0.04769482   0.57338900
## TotalReviwes 0.4264087 0.04769482   1.00000000   0.01339623
## RomSize_inGB 0.3732247 0.57338900   0.01339623   1.00000000
```

Clearly we have correlation between the independent variables used in the categorization of the phones. For this reason it may not be appropriate to use Naive Bayes for Classification.

We can try removing the rating out of the predictors since there is a high correlation with the others.

```
order5 <- order3[, (names(order3) %in% c('Price','TotalReviwes','RomSize_inGB',
↪  "Company"))]
```

```
set.seed(10)
sample3 <- sample(c(TRUE, FALSE), nrow(order5), replace=TRUE, prob=c(0.7,0.30))
train3  <- order5[sample, ]
test3   <- order5[-sample, ]

modelbayes2 <- naive_bayes(Company~Price+TotalReviwes+RomSize_inGB, data = train3,
↪  usekernel = T)
```

Now to use naive bayes to predict

```
pred2 <- predict(modelbayes2, test3)
```

```
## Warning: predict.naive_bayes(): more features in the newdata are provided as
## there are probability tables in the object. Calculation is performed based on
```

```
## features to be found in the tables.
```

```
(tab2 <- table(pred2, test3$Company))
```

```
##
## pred2     APPLE IQOO SAMSUNG VIVO
##   APPLE      43    0       0    0
##   IQOO        3    6      10    0
##   SAMSUNG     0    2      48   15
##   VIVO        0    0       2   19
```

```
mean(pred2 != test3$Company)
```

```
## [1] 0.2162162
```

The misclassification rate increased slightly when removing rating as one of the predictors. For this reason, we will leave rating in the classifier.

Evaluating the classification performance of KNN. We can also look at KNN, which is a non parametric classifier that does not make assumptions on the underlying distribution of the data.

We will perfome multiple runs of KNN, and varying the number of nearest neighbours k, in the classifier for each run to determine the most accurate classifier.

```
# Loading package
library(e1071)
library(caTools)
library(class)


# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],
                      test = test[,1:4],
                      cl = train$Company,
                      k = 11)


# Confusion Matrix
cm <- table(test$Company, classifier_knn)
cm
```

```
##          classifier_knn
##           APPLE IQOO SAMSUNG VIVO
##   APPLE      46    0       0    0
##   IQOO        0    0       7    1
##   SAMSUNG     2    0      45   13
##   VIVO        3    0      15   16
```

```
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)
misClassError
```

```
## [1] 0.277027
```

```r
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],
                      test = test[,1:4],
                      cl = train$Company,
                      k = 9)


# Confusion Matrix
cm <- table(test$Company, classifier_knn)
cm
```

```
##           classifier_knn
##            APPLE IQOO SAMSUNG VIVO
##   APPLE       46    0       0    0
##   IQOO         0    1       7    0
##   SAMSUNG      2    0      48   10
##   VIVO         0    0      16   18
```

```r
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)
misClassError
```

```
## [1] 0.2364865
```

```r
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],
                      test = test[,1:4],
                      cl = train$Company,
                      k = 7)


# Confusion Matrix
cm <- table(test$Company, classifier_knn)
cm
```

```
##           classifier_knn
##            APPLE IQOO SAMSUNG VIVO
##   APPLE       46    0       0    0
##   IQOO         0    1       7    0
##   SAMSUNG      1    0      53    6
##   VIVO         0    0      12   22
```

```r
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)
misClassError
```

```
## [1] 0.1756757
```

```r
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],
                      test = test[,1:4],
                      cl = train$Company,
                      k = 5)
```

```
# Confusion Matrix
cm <- table(test$Company, classifier_knn)
cm
```

```
##          classifier_knn
##           APPLE IQOO SAMSUNG VIVO
##   APPLE      46    0       0    0
##   IQOO        1    2       5    0
##   SAMSUNG     0    0      49   11
##   VIVO        0    1       7   26
```

```
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)
misClassError
```

```
## [1] 0.1689189
```

```
# Fitting the Knn Model
classifier_knn <- knn(train = train[,1:4],
                      test = test[,1:4],
                      cl = train$Company,
                      k = 3)


# Confusion Matrix
cm <- table(test$Company, classifier_knn)
cm
```

```
##          classifier_knn
##           APPLE IQOO SAMSUNG VIVO
##   APPLE      46    0       0    0
##   IQOO        1    2       5    0
##   SAMSUNG     0    0      49   11
##   VIVO        0    1       3   30
```

```
# Calculate out of Sample error
misClassError <- mean(classifier_knn != test$Company)
misClassError
```

```
## [1] 0.1418919
```

We can see from our results that the most accurate classifier is when k = 5.

Results from Classifier Predictions.

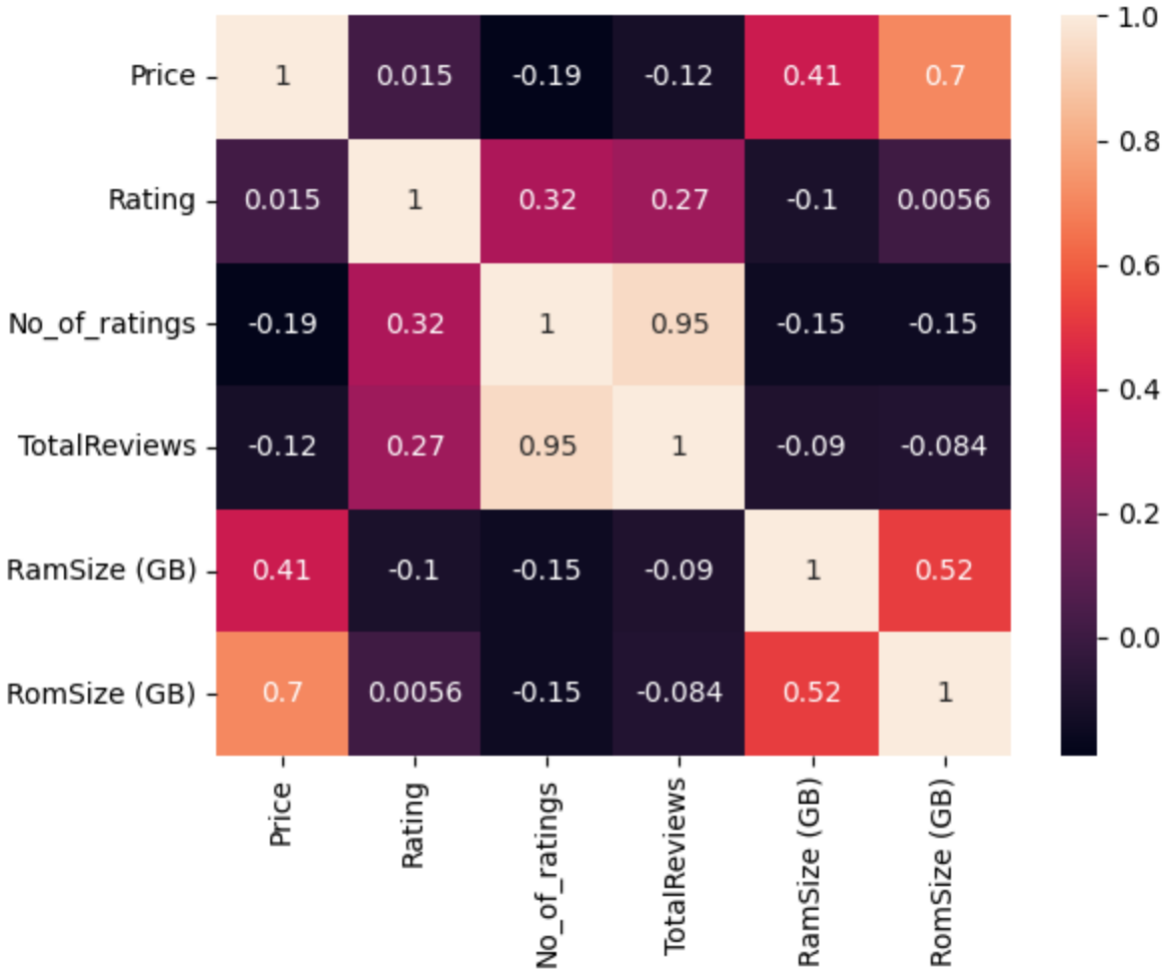
In conclusion, we have evaluated five different classifiers, including K-nearest neighbors (KNN), Naive Bayes, logistic regression, Quadratic Discriminant Analysis (QDA), and Linear Discriminant Analysis (LDA), on a dataset that did not follow a Gaussian distribution and had unequal covariance matrices as well as correlation between predictors. Our results show that KNN had the lowest misclassification rate of 0.16, followed by logistic regression at 0.18, QDA and Naive Bayes at 0.21, and LDA at 0.24. These findings suggest that KNN and logistic regression may be effective classifiers for non-Gaussian and non-equal covariance data, while QDA, Naive Bayes, and LDA may not perform as well.

Dimensionality reduction

We should emphasize that this part of the analysis is not particularly useful in a dataset with less than 10 predictors like ours. It was still carried for its value as a learning exercise. This point was brought up and addressed during our presentation. With that in mind let's go through the motions.

Principal component analysis

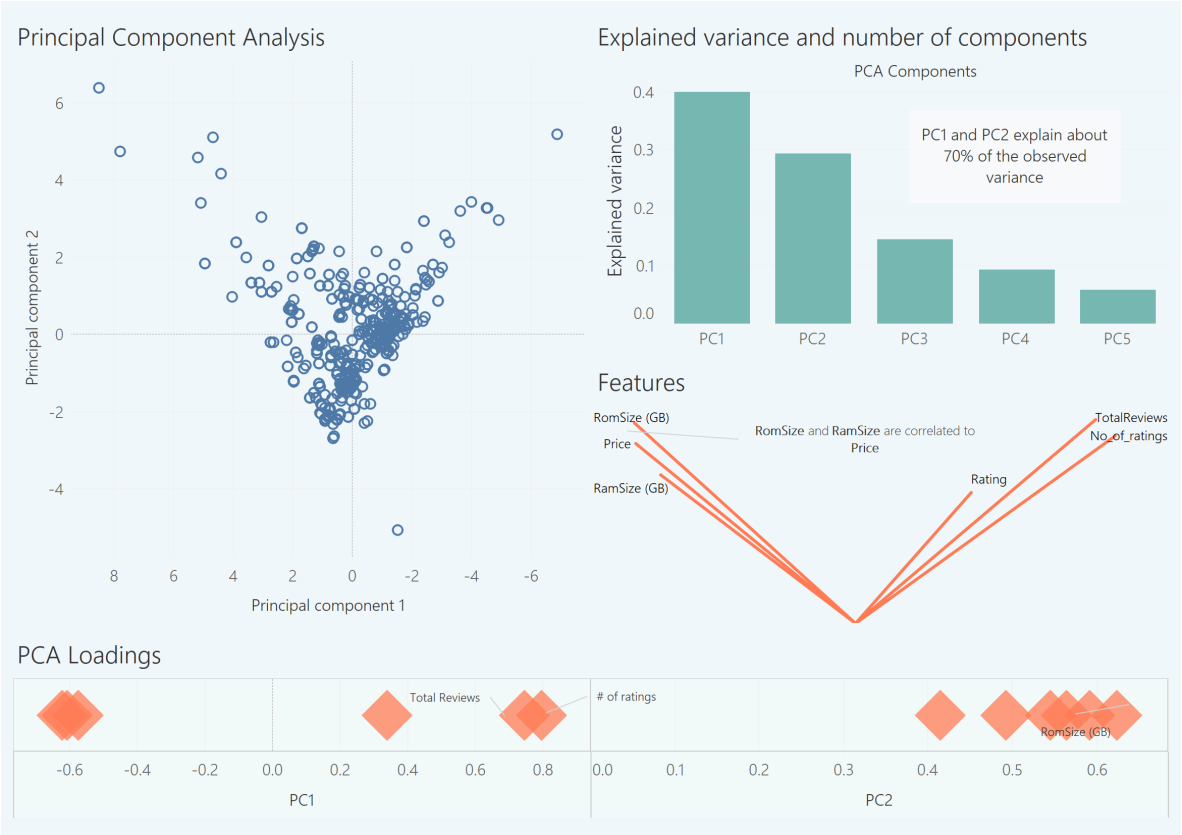
PCA is a tool that projects a collection of vectors into a a new vector space of fewer orthogonal dimensions. This projection can be simpler to fit using a linear model but much harder to interpret: the new predictors are going to be linear combinations of the original predictors and may not have a direct interpretation. To carry out a PCA one must have correlation among features,



PCA is sensitive to outliers and scale. This means that if our numerical predictors have different units or span different orders of magnitude we need to re-scale it. For every predictor, this is accomplished by simply subtracting the mean and dividing by its standard deviation. In python, the library *scikit learn* support different types of scaling out of the box. It can also perform PCA,

```
from sklearn.decomposition import PCA
pca = PCA(n_components = 2)
principal_components = pca.fit_transform(df_scaled)
```

The following figure summarizes the results,



We can see that about 70% of the variance can be explained by projecting onto a 2D space. To use this in a prediction scenario we'd have to setup a pipeline that follows this workflow,

1) Rescale
2) Map from the original predictor/response space to the new PC space using a a linear transformation
3) Apply the model (predict)
4) Rescale result
5) Map from PC to original predictor/response space

This is less of a hassle when dealing with many predictors and the gains from dimensionality reduction are tangible.

References

2020 review. "High-End Mobile Phones Price Have Soared 490% in 20 Years | This Is Money." This Is Money, This Is Money, 23 July 2020, https://www.thisismoney.co.uk/money/bills/article-8548235/High-end-mobile-phones-price-soared-490-20-years.html.

MobilePhone's dataset. "MobilePhone's Dataset | Kaggle." Kaggle: Your Machine Learning and Data Science Community, Kaggle, 20 Dec. 2022, https://www.kaggle.com/datasets/sudhanshuy17/mobilephone.

Pascal Schmidt. "Assumption Checking of LDA vs. QDA – R Tutorial Pima Indians Data Set", retrieved Feb 17 2023, https://thatdatatho.com/assumption-checking-lda-vs-qda-r-tutorial-2/.