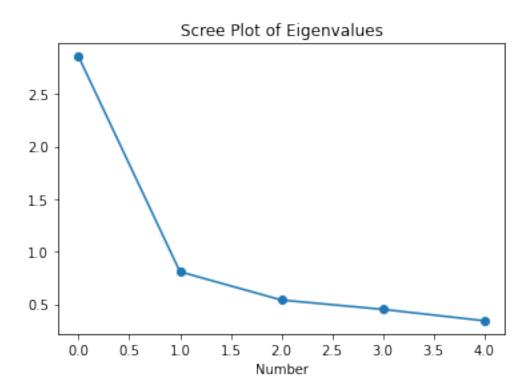
ESC21SUMMER_HW5_woohyunchoi

August 16, 2021

0.1 Factor Analysis on Stock data

```
[1]: import pandas as pd
    import numpy as np
    import matplotlib.pyplot as plt
[2]: import warnings
    warnings.filterwarnings('ignore')
[4]: # Data Import
    import ssl
    import pandas as pd
    ssl._create_default_https_context = ssl._create_unverified_context #Github
    stock = pd.read_csv('https://github.com/YonseiESC/ESC-21SUMMER/blob/main/week5/
     →stock.DAT?raw=True', header=None, delim_whitespace=True)
    stock.columns = ['X1', 'X2', 'X3', 'X4', 'X5']
    stock.corr()
[4]:
              Х1
                       Х2
                                 ХЗ
                                          Х4
                                                    Х5
    X1 1.000000 0.576924 0.508656 0.386721 0.462178
    X2 0.576924 1.000000 0.598384 0.389519 0.321953
    X3 0.508656 0.598384 1.000000 0.436101 0.425627
    X4 0.386721 0.389519 0.436101 1.000000 0.523529
    [5]: eigenValues, eigenVectors = np.linalg.eig(stock.corr())
    idx = eigenValues.argsort()[::-1]
    eigenValues = eigenValues[idx]
    eigenVectors = eigenVectors[:,idx]
[6]: # Case 0: p factors
    loadings_p = pd.DataFrame()
    loadings_p['Factor1'] = np.sqrt(eigenValues[0])*eigenVectors[:,0]
    loadings_p['Factor2'] = np.sqrt(eigenValues[1])*eigenVectors[:,1]
    loadings_p['Factor3'] = np.sqrt(eigenValues[2])*eigenVectors[:,2]
    loadings_p['Factor4'] = np.sqrt(eigenValues[3])*eigenVectors[:,3]
    loadings_p['Factor5'] = np.sqrt(eigenValues[4])*eigenVectors[:,4]
```

```
loadings_p.index = stock.columns
    np.round(loadings_p, 2)
[6]:
        Factor1 Factor2 Factor3 Factor4 Factor5
    Х1
           0.78
                    0.22
                             0.45
                                     -0.26
                                               0.27
    Х2
           0.77
                                     -0.14
                                              -0.40
                    0.46
                            -0.13
    ХЗ
           0.79
                    0.23
                            -0.25
                                      0.45
                                               0.23
                                               0.11
    Х4
           0.71
                   -0.47
                            -0.40
                                     -0.32
    Х5
           0.71
                   -0.52
                             0.32
                                      0.26
                                              -0.23
[7]: eigval = pd.DataFrame()
    eigval['Eigenvalue'] = eigenValues
    eigval['Proportion'] = eigval['Eigenvalue'] / len(eigval)
    eigval['Cumulative'] = eigval['Proportion'].cumsum(axis=0)
    eigval
[7]:
       Eigenvalue Proportion Cumulative
         2.856487
                      0.571297
                                 0.571297
    1
         0.809118
                     0.161824
                                 0.733121
    2
         0.540044
                     0.108009
                                 0.841130
                                 0.931399
    3
         0.451347
                     0.090269
         0.343004
                     0.068601
                                 1.000000
    4
[8]: plt.title('Scree Plot of Eigenvalues')
    plt.xlabel('Number')
    plt.plot(eigenValues, 'o-')
    plt.show()
```



0.1.1 Q. How many factors are required to describe adequately the space in which these data actually fall?

2 factors are required.

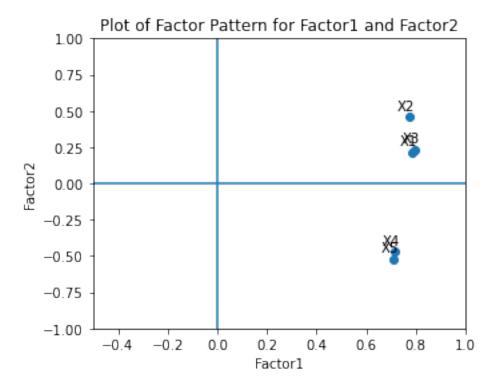
```
[9]: loadings2 = pd.DataFrame()
    loadings2['Factor1'] = np.sqrt(eigenValues[0])*eigenVectors[:,0]
    loadings2['Factor2'] = np.sqrt(eigenValues[1])*eigenVectors[:,1]
    loadings2.index = stock.columns
    np.round(loadings2, 2)
```

```
[9]:
         Factor1 Factor2
            0.78
                      0.22
     Х1
     Х2
            0.77
                      0.46
     ХЗ
            0.79
                      0.23
     Х4
            0.71
                     -0.47
     Х5
            0.71
                     -0.52
```

0.1.2 Q. Compute the communality of each variable.

```
[28]: com = []
for i in range(5):
    com.append(loadings2['Factor1'][i]**2 + loadings2['Factor2'][i]**2)
```

```
[29]: loadings2['communality'] = com
[30]: np.round(loadings2, 2)
[30]:
                   Factor2 communality
          Factor1
             0.78
                      0.22
                                   0.66
      X1
     Х2
             0.77
                      0.46
                                   0.81
      ХЗ
             0.79
                      0.23
                                   0.69
             0.71
                                   0.73
      Х4
                     -0.47
      Х5
             0.71
                     -0.52
                                   0.78
[10]: # Preplot(Before Rotation)
      x = loadings2.Factor1 ; y = loadings2.Factor2
      plt.figure(figsize = (5,4))
      plt.title('Plot of Factor Pattern for Factor1 and Factor2')
      plt.xlabel('Factor1') ; plt.ylabel('Factor2')
      plt.scatter(x,y)
      for i in range(len(loadings2)):
          plt.text(x[i]-0.05, y[i]+0.05, loadings2.index[i])
      plt.axvline(x = 0) ; plt.axhline(y = 0)
      plt.xlim(-0.5,1); plt.ylim(-1,1)
      plt.show()
```



0.1.3 Q. Compute the 2 x 2 matrix to rotate the Xi's 45 degrees anti-clockwise. Fill in a11, a12, a21, a22 on the following code.

```
[19]: A = pd.DataFrame([[1/np.sqrt(2), -1/np.sqrt(2)], [1/np.sqrt(2), 1/np.
      loadings_rotation = A.dot(loadings2.transpose()).transpose()
     loadings_rotation.columns = ('Factor1', 'Factor2')
     loadings_rotation
[19]:
          Factor1
                   Factor2
     X1 0.400781 0.707166
     X2 0.222435 0.870061
     X3 0.395929 0.727410
     X4 0.838037 0.169848
     X5 0.873861 0.133192
[31]: com1 = []
     for i in range(5):
         com1.append(loadings rotation['Factor1'][i]**2 +
      →loadings_rotation['Factor2'][i]**2)
     loadings_rotation['communality'] = com1
[32]: np.round(loadings_rotation, 2)
[32]:
         Factor1 Factor2 communality
            0.40
     Х1
                     0.71
                                 0.66
     Х2
            0.22
                     0.87
                                 0.81
     ХЗ
            0.40
                     0.73
                                 0.69
     Х4
            0.84
                     0.17
                                 0.73
     Х5
            0.87
                     0.13
                                 0.78
[20]: # Plot(After Rotation)
     x = loadings_rotation.Factor1 ; y = loadings_rotation.Factor2
     plt.figure(figsize = (5,4))
     plt.title('Plot of Factor Pattern for Factor1 and Factor2')
     plt.xlabel('Factor1'); plt.ylabel('Factor2')
     plt.scatter(x,y)
     for i in range(len(loadings_rotation)):
         plt.text(x[i]-0.05, y[i]+0.05, loadings_rotation.index[i])
     plt.axvline(x = 0) ; plt.axhline(y = 0)
     plt.xlim(-0.5,1); plt.ylim(-1,1)
     plt.show()
```

