SCIGMA

User's Manual and Reference

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External Software Packages

Besides Loki, SCIGMA includes (subsets of) the following external packages: AntTweakBar, GLFW, GLEW, zlib, libpng (all available under the zlib/libpng license), ODESSA and LAPACK (available under the modified BSD license). The AntTweakBar, GLFW and libpng sources have been slightly modified.

Contact

SCIGMA is a code in evolution. Especially, it has not yet been tested on a wide variety of machines, which makes it susceptible to the occasional OpenGL malfunction and missing shared library. Therefore, bug reports as well as comments and feedback to scigma.contact@gmail.com are very much appreciated!

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1 Setting up SCIGMA

1.1 Prerequisites

SCIGMA runs under Windows, Linux and Mac OS X. It needs graphics hardware that supports at least OpenGL 2.1 (any desktop computer or laptop bought after 2008 should be fine). The Python programming language (version>=2.7) must be installed on the system. Python is part of OS X and comes preinstalled with most Linux flavors. If you do not have Python installed on Linux, you can always install it using the package manager of your distribution. If you are using Windows and don't have Python installed, have a look at http://portablepython.com. It's a conveniently self-contained version of Python that does not require admin privileges to install.

1.2 Obtaining the Python package

There are precompiled binary packages for Windows and Mac OS X available at https://github.com/scigma/scigma/releases.

Note that the 32-bit Windows binaries have been compiled with sjlj exception handling, while the 64-bit binaries have been compiled with seh exception handling. If you are going to use software compiled with MinGW and a different type of exception handling together with SCIGMA, you will run into trouble. In that case, you will have to build SCIGMA yourself, with your own version of MinGW.

For Linux, there is currently no binary package and you need to build SCIGMA yourself as well (see section 1.4 below).

1.3 Installation and first start

Create a folder for SCIGMA-related work (e.g \$HOME/myodes and drop the scigma folder into it. Now, open a Python session in the folder you just created (i.e. \$HOME/myodes should be the current working directory). At the Python prompt type:

>>> import scigma

After a few seconds, the SCIGMA graphics window should appear.

If you are using Portable Python in Windows, the fastest way to get things running is to drop the "scigma" folder into the "Portable Python ..." folder, double-click on Python-Portable.exe and type

>>> import scigma

in the console that opens.

1.4 Building SCIGMA from source

1.4.1 Obtaining the sources

You can either download the source archive at https://github.com/scigma/scigma/releases or, if you are familiar with git, clone the git repository directly from https://github.com/scigma/scigma.

In principle, you should be able to build SCIGMA with a combination of any working C++ compiler, any working Fortran compiler and CMake on your system (if CMake can deal with the compilers). However, the instructions below are the recommended way to build things, while other ways are untested.

1.4.2 Building under Linux

You will need to have g++, gfortran and cmake installed, as well as the X11 and OpenGL header packages (how these are called may vary depending on your distro; for Debian and its derivatives, like Ubuntu, install the xorg-dev and libglu1-mesa-dev packages). To build SCIGMA, open a terminal and change into the build directory of the top level folder. Now configure with

\$ cmake ../source

and build with

\$ make

Now, build should contain the shared library libscigma.so.

\$ cp libscigma.so ../scigma

copies this library into the scigma subdirectory, which now contains the complete Python package. See section 1.3 on how to use the package.

1.4.3 Building under Windows

You will need both MinGW (with the g++, gfortran and msys packages) and CMake to compile SCIGMA.

If you do not have MinGW, download 'mingw-get-setup.exe' from http://sourceforge.net/projects/mingw/files and start the installation manager. Mark the packages mingw32-base, mingw32-gcc-gfortran, mingw32-gcc-g++ and msys-base for installation and apply the changes. Finally, add mingw/bin and mingw/msys/1.0/bin to the system path.

If you do not have CMake, download and run the installer from http://www.cmake.org/download. Now you are ready to build SCIGMA:

Start the CMake gui and specify the source and build subdirectories of the top level folder as source directory and binary directory, respectively. Push the Configure-button. When CMake asks you for the build type, choose MSYS Makefiles, with native compilers. After the configuration is done, press Generate. Now, the build folder contains the Makefiles and you are done with CMake.

Start the msys terminal (in the MinGW installation folder under msys\1.0\bin\msys.bat) and change into the build directory. If your build directory is C:\scigma-0.9.1\build, for example,

\$ cd /c/scigma-0.9.1/build

as command in the msys console. Finally, enter

\$ make

to build the package. If everything runs smoothly, the shared library libscigma.dll will appear in the build folder. Copy this file into the scigma subdirectory with

\$ cp libscigma.dll ../scigma

The scigma folder now contains the complete Python package and can be used as described in section 1.3.

1.4.4 Building under Mac OS X

The recommended way to obtain all three prerequisites (C++, Fortran and CMake) is to first install MacPorts (if you have another package manager like homebrew or fink already installed that should work as well). Installation instructions and the program itself can be found at https://www.macports.org/install.php. Once you are done with installing MacPorts, you will have g++ already available as part of the Xcode Command Line Tools. You can then proceed to install gfortran with

\$ sudo port install gfortran

as well as CMake with

\$ sudo port install cmake

To build SCIGMA, open a terminal and change into the build directory of the top level folder of SCIGMA's source distribution. Configure with

\$ cmake ../source

and build with

\$ make

Now, build should contain the shared library libscigma.dylib.

\$ cp libscigma.dylib ../scigma

copies this library into the scigma subdirectory, which now contains the complete Python package. See section 1.3 on how to use the package.

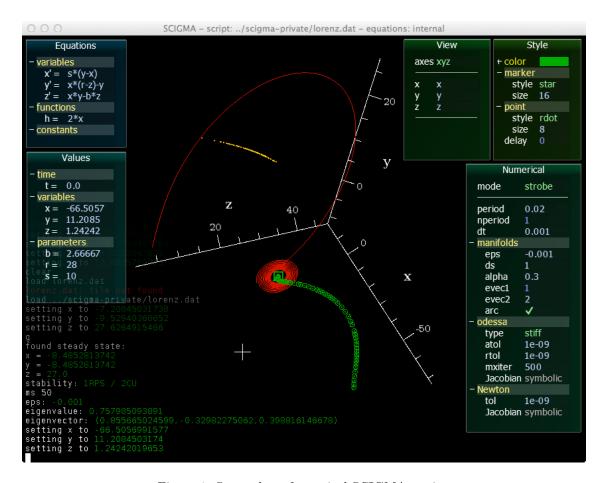


Figure 1: Screenshot of a typical SCIGMA session

2 Overview

SCIGMA is a Python package that allows you to

- specify a set of ordinary differential equations
- visualize the phase and/or parameter space
- select initial conditions and parameters interactively
- plot trajectories
- find stationary states
- examine the stability of those states
- plot invariant manifolds of those states
- do all of the above for iterated maps, as well as Poincaré maps and stroboscopic maps of ordinary differential equations
- automate these tasks with a simple scripting language or directly from Python
- read the results back into your own Python programs

Figure 1 shows SCIGMA's user interface. The largest part of the window is taken up by a diagram of the phase space and/or parameter space. On the sides, there are some panels that give you information about the current equation system, as well as all kinds of numerical and graphic settings. In the bottom left corner, there is a console at which you can enter equations and

commands, as well as adjust and query the settings.

The first thing you have to do when working with SCIGMA is to let the program know which equations you want to look at. There are several ways to do that, which are all described in section 3. Once you have done that, you will be ready to produce some nice graphics. Most of SCIGMA's work is done by a handful of commands, namely

- plot, which plots orbits of maps and trajectories of differential equations,
- guess, which finds stationary states of trajectories and differential equations,
- and mstable/munstable, which trace out invariant manifolds.

These commands, together with some more bookkeeping and visual commands are described in section 4. Some other commands that you might find useful include

- fit, which scales the currently visible viewing area/volume such that objects fit onto the screen,
- clear, which deletes all objects in the graphics window,
- and reset, which, on top of clearing the graphics window, also deletes the current equation system.

Of course there are a lot of options and settings that modify the behavior of SCIGMA's commands, the most important one being the mode setting. mode governs whether SCIGMA considers the system as a discrete map or as a differential equation, as well as whether it turns a set of differential equations into a stroboscopic map or Poincaré map. This and other settings are described in section 5.

Finally, section 6 describes how to navigate the viewing area (or viewing volume in three-dimensional projection) with the mouse, as well as how to interactively select objects and pick initial conditions for the numerical commands.

3 Specifying the equations

In SCIGMA, there are three ways of encoding equations, namely

- directly at the command line in the graphics window, or from a script file (best suited for the explorative investigation of smaller systems);
- by specifying a set of equations in a Python script Python is more expressive (e.g. loops and arrays are available), but you will have to specify the Jacobian yourself.
- as a precompiled shared library (fastest, but less convenient than both of the above).

The next three sections describe all of these possibilities.

Before we dive into the specifics, let us discuss what all three approaches have in common: SCIGMA distinguishes between three types of user defined symbols in equations: variables, parameters and functions. The number of variables determines the dimension of the phase space for an ODE or a map. Parameters are values that are constant in time and may be used for bifurcation analysis (... coming soon ...). Functions are quantities that depend on variables, or parameters, or both, which are not strictly necessary to describe the problem, but might be convenient as auxiliary functions or otherwise interesting. For illustration, look at these equations for an harmonic oscillator:

$$\dot{x} = -y
\dot{y} = \omega^2 x
\omega = \sqrt{\frac{k}{m}}$$
(1)

Here, x and y are variables, k and m are parameters and ω is a (constant) function. Regardless of how the equations are specified, you can always set the value of a variable or a parameter like this

x=1 k=2

at the SCIGMA console, or in the Values panel.

3.1 At the SCIGMA console

Variables

To define a variable for an ODE system, all you have to do is provide its time derivative. x' = x-1

defines a variable x with $\dot{x} = x - 1$. The initial condition / current value for x is set like this: x = 0.5

For an iterated map, the syntax to define a variable by providing the iterative equation, is the same:

n' = n*2+1

How your equations are interpreted depends on whether the mode option of the program is set to 'ode', 'strobe' or 'Poincare' (interpretation as ODE) or to 'map' (interpretation as iterated map).

Parameters

If you assign a value to a new symbol a = 2,

supported mathematical operations

```
+, -, *, /, **, sqrt, exp, ln, log10, sin, cos, tan, asin, acos, atan, atan2, sinh, cosh, tanh, asinh, acosh, atanh, pow, sigmoid, pulse, abs, sign, step, mod
```

Table 1: List of mathematical operations understood by SCIGMA's internal parser. ** stands for exponentiation, as in FORTRAN or Python. sigmoid takes two arguments x and β and is defined as $s = (1 + \exp(-x/\beta))^{-1}$; pulse also takes two arguments: $p = \exp(x/\beta)/(\beta \exp(x/\beta) + \beta)$, which is the derivative of the sigmoid function. Therefore, the area under the pulse is always equal to 1. The step function behaves like its GLSL equivalent, taking two parameters as well, where the second parameter is the position of the step. mod is equivalent to the C function fmod

this defines a new parameter. Parameters are also created implicitly when a symbol appears in an expression for the first time (see below).

Functions

If the right hand side of your equation contains at least one symbol like $x,\,n,$ and a, you create a function rather than a parameter:

```
xSquare = x**2
```

Note that xSquare keeps track of the changes in x and updates itself accordingly, not only if x changes its value, but even if it is completely redefined; as another example, consider this definition for the time derivative of y:

```
y' = x**2 + a**b
```

Here, a is an already known parameter with value 2, while b is implicitly initialized as a new parameter with value 0, which happens whenever you enter an equation with a symbol that is not yet defined. x is of course a variable since our first definition. For the moment, we have $\dot{y} = x^2 + 2^0$. Note that instead of the last line, you could also have written

```
y' = xSquare + a**b.
```

When you redefine a variable, parameter or function, this affects all other functions depending on it. For example after

```
b = x+y,
```

the time derivative of y becomes $\dot{y} = x^2 + 2^{x+y}$. Because previous definitions are updated, the order in which you enter a set of equations does not matter; SCIGMA takes care that the equations remain consistent.

Evaluation operator

If you do want to extract the current value of a function instead of the function itself, use the \$-operator:

```
$(a**2)
```

prints out 4, for example. Do NOT use this operator on the right hand of equations, this will erratically change the value of the left hand side function.

Builtin mathematical functions

There is a number of builtin mathematical operations understood by SCIGMA's parser that can be used in expressions. Please see table 1 for the full list.

command	effect	
x' = value expression	define variable x	
x = expression	define function \mathbf{x}	
x = value	define parameter x / set value of variable x	
\$expression	replace expression by its current value	
!x	delete symbol x	
!x'	turn variable x into parameter	

Table 2: List of different command types understood by SCIGMA's internal parser. *value* is any expression that evaluates to a constant, i.e. either a number, or a builtin function of just numbers like sin(3.14)**2. *expression* is any expression that depends on at least one other defined symbol like sin(2*a) or f*g+1.

Deleting variables, parameters and functions

To delete all information pertaining to a symbol x, use

This deletes function definitions, map and ODE definitions and the symbol itself (unless there are symbols that depend on x; in this case, these have to be deleted first). You can also do this !x',

which takes the variable x out of the dynamical system, but keeps it available as parameter.

Example

Table 2 shows a summary of the available commands of SCIGMA's internal equation parser. With these commands, we are now ready to specify equations (1) from the beginning of this chapter:

```
x'=-y
y'=omega**2*x
omega=sqrt(k/m)
```

Before observing the dynamics, we must also assign sensible values to the parameters ${\tt k}$ and ${\tt m},$ for example

k=1 m=2

Now the system can be used with SCIGMA. Note again that the order in which the five equations above are entered does not matter.

Instead of entering the equations step by step at runtime you can also collect them in a file and use the load command. Either way, the equations will also be mirrored in the Equations panel, which can be used to modify the equations as well.

3.2 In a Python script

You can load a set of equations from a Python file at runtime with the equations command. SCIGMA scans this script for the following symbols:

```
v_names is a list of variable names:
    v_names = ['x','y','z']
```

v_values is a list of initial values for the variables:

```
v_{values} = [0,0,0]
```

If v_values is defined, it must have the same length as v_names. If it is not defined the variables are not initialized on equation loading.

p_names is a list of parameter names:

```
p_names = ['a','b','c']
```

If p_names is not defined, SCIGMA assumes that there are no parameters.

p_values is a list of initial values for the parameters:

```
p_{values} = [1,2,3]
```

If p_values is defined, it must have the same length as p_names. If it is not defined the parameters are not initialized on equation loading.

f is a function defining the right hand side of the dynamical system. f can have one of these signatures:

SCIGMA decides on the type of system by looking at the number of arguments and the name of the first argument. Therefore, the first argument must always be t for non-autonomous systems. SCIGMA will pass the variables in the first argument (autonomous systems) or second argument (non-autonomous systems) and the parameters in the second or third argument. The right hand side must be written to the third (autonomous systems) or the fourth argument (non-autonomous systems). Note that x, p and xdot are raw pointers to memory, so you are responsible to not access them beyond their limits, which are given by the length of the v_names and p_names lists, respectively (the example below shows how the arguments are used).

dfdx is a function defining the jacobian of the dynamical system. If dfdx is defined, it must have the same signature as f, for example

SCIGMA expects the Jacobian in column major ordering, i.e. if there are N variables, the first N entries of jac contain the partial derivatives of the right hand side with respect to the first variable, the next N entries the partial derivatives with respect to the second variable and so on (compare also the example below). You do not need to provide zero elements of the Jacobian.

f_names is a list of additional function names:

```
f_names = ['f,'g','h']
```

If defined, these are some additional functions of interest which are computed and stored along with the variables. They are evaluated by calling

func, which, must again have the same signature as f:

func must be defined if f_names is defined and has at least one entry.

Example

The Python script describing the example equations (1) would look like this:

```
import math
```

```
v_names=['x','y']
p_names=['k','m']
p_values=[1,2]
f_names=['omega']

def f(x,p,xdot):
        xdot[0]=-x[1]
        xdot[1]=p[0]/p[1]*x[0]

def dfdx(x,p,jac):
        jac[1]=p[0]/p[1]
        jac[2]=-1

def func(x,p,values):
        values[0]=math.sqrt(p[0]/p[1])
```

Please note that you cannot use the additional functions inside the body of $\tt f$ or $\tt dfdx$ (this is because internally, $\tt func$ is not evaluated for every single call of $\tt f$ and $\tt dfdx$).

3.3 In a Shared Library

 \dots coming soon \dots

4 Commands

In the list of commands below, mandatory arguments are written like <this>, optional arguments are written like [this]. If there are two or more distinct possibilities for an argument, they will be denoted like|this> [or|like|this]. Most commands have abbreviations, which are given at the end of the description of the command.

4.1 General

equations ['internal'|filename]

specifies the source of the dynamical equations. You can provide the equations either internally at the command line (this is the standard setting, to which you can return by giving 'internal' as argument), or in a Python script file specified by filename. See sections 3.1 and 3.2 for details on the format of internal equations and of the Python file, respectively. If neither 'internal', nor any filename is given as an argument, the command opens a file dialog. This command may be abbreviated by eq.

load [filename]

loads and runs a the script file specified in filename. If filename is not given, the command opens a file dialog. This command may be abbreviated by 1.

select <name>

makes the object specified by name the currently selected object. This command may be abbreviated by sel.

delete <name>

deletes the orbit, manifold or special point specified by name from memory, including all of the data. This command may be abbreviated by del.

clear

Deletes all orbits, manifolds and special points. This command may be abbreviated by cl.

reset

Deletes all orbits, manifolds and special points, deletes the current set of equations and resets the view to a two-dimensional plot of x vs y between (-1, -1) and (1, 1). This command may be abbreviated by res.

quit

closes the current window and frees the associated resources (i.e. makes them available to Python's garbage collector). This command may be abbreviated by q.

4.2 Numerical

You will notice that some of the commands below come in two versions, namely with and without an appended asterisk (*). For these commands, the version with the asterisk shows *all* iterates if nperiod is not 1, while the command without the asterisk just shows the *nperiod-th* iterates.

plot [n] [name] / plot* [n] [name]

takes the current state as initial condition and plots n steps of the resulting orbit or trajectory. The orbit will be assigned name as identifier for further reference. If n is not given, only one step will be taken. A negative n will reverse the direction of the iteration/integration. If name is not given, a unique name of the form 'trN' will be generated.

The behavior of this command depends on the current setting of the mode option:

If mode is map, the program iterates the map and plots every nperiod-th point.

If mode is ode, the program integrates the differential equations for n time steps dt and plots the trajectory.

If mode is strobe, the program will plot every nperiod-th point of the stroboscopic map of

the differential equations with a time interval period (this is effectively the same behavior as for ode, with period×nperiod as time step instead of dt).

If mode is Poincare, the program constructs a Poincare map for the intersection of the secvar=secval plane, iterates it and plots every nperiod-th point. maxtime determines how far the program should integrate before giving up on finding an intersection. secdir determines whether the value of secvar should be increasing or decreasing at the intersection.

The appearance of the resulting trajectory in depends on the current values of color, marker.style, marker.size, point.style, point.size and delay. This command may be abbreviated by p / p*.

guess [name] / guess* [name]

takes the current state as starting point and tries to find a stationary state or the current map or ode by Newton iteration. If a stationary state is found, it will be assigned name as identifier for further reference. If name is not given, a unique name of the form 'fpN' ('fixed point', for differential equations) or 'ppN' ('periodic point', for maps) will be generated. If mode is not ode, the program will look for a stationary state of the nperiod-th iterate of the map. Stationary states of differential equations will be marked with a circle, if they are unstable, and with circles with a dot in the center, if they are stable. Stationary states of maps will be marked with an empty square, if they are unstable, and with a square with a dot in the center, if they are stable. The further appearance depends on the current values of color, and marker.size. This command may be abbreviated by g / g*.

evals [name]

prints the eigenvalues of the object specified by name. If name is not given, the currently selected object is used.

evecs [name]

prints the eigenvectors of the object specified by name. If name is not given, the currently selected object is used.

mstable [n] [origin] [name] / mstable* [n] [origin] [name]

takes a stationary state (the 'origin') previously found with guess and plots n steps of the 1-dimensional unstable manifold of the origin along an unstable eigenvector, which is determined by the value of evec1. name will be assigned to the manifold as identifier for further reference. If n is not given, just the initial segment is created. If origin is not given, the currently selected object is used. If name is not given, a unique name of the form 'mfN' will be generated. If mode is ode, one step will correspond to an integration of $\pm dt$. Otherwise, the manifold for the nperiod-th iterate of the map will be constructed, with an arc length step of (roughly) ds. The accuracy of the manifold stepping algorithm for maps can be adjusted with alpha. The appearance of the manifold depends on the current values of color, marker.style, marker.size, point.style, point.size and delay. This command may be abbreviated by ms / ms*.

munstable [n] [origin] [name] / munstable* [n] [origin] [name] works analog to mstable. This command may be abbreviated by mu / mu*.

rtime [name]

If name denotes an orbit or stationary state of a stroboscopic map or Poincare map, this prints the return time. If name is not given, rtime prints the return time of the currently selected object. This command may be abbreviated by rt.

circle <diameter> [n]

takes the current position as center and places n initial conditions equally spaced on the circle with the specified diameter. diameter is given in units of the currently visible portion of phase space. If n is not given, 100 is used. This command may be abbreviated by cir.

4.3 View and style

hide <name>

hides the orbit, manifold or special point specified by name if it is currently on display, but keeps it in memory.

show <name>

displays the orbit, manifold or special point specified by name if it is currently hidden.

2d

changes to two-dimensional projection.

34

changes to three-dimensional projection.

xrange <min> <max>

adjusts the range of the x dimension. min must be smaller than max.

yrange <min> <max>

adjusts the range of the y dimension. min must be smaller than max.

zrange <min> <max>

adjusts the range of the z dimension. \min must be smaller than \max .

crange <min> <max>

adjusts the range of the color dimension. min must be smaller than max.

fit

adjusts the viewing volume to include all visible objects. This command may be abbreviated by ${\tt f}$.

5 Settings

Settings can be changed on the command line with the syntax given below. If only the name of an option is entered, SCIGMA prints its value on the console. Instead of using the command line, you can also access all settings using the Numerical, View and Style panels.

5.1 Numerical

mode <'m[ap]'|'o[de]'|'s[trobe]'|'P[oincare]'>

specifies which type of dynamical problem is investigated. If mode is set to map, the equations are interpreted as a discrete map, otherwise they are interpreted as system of ordinary differential equations. The behavior of most numerical commands, as well as the availability and relevance of other numerical options depends on the value of mode. The default value is ode.

period <value>

sets the return time for stroboscopic maps (mode is strobe). If equations are internal, value can be any expression that evaluates to a constant (value in the sense of table 2), for example \$(2*pi/omega). If equations are not internal, value must either be a number, or the value of a symbol defined in the equation system, prefixed with the \$-operator, for example \$T. The default value is 1.0.

nperiod <value>

sets the number of periods for the iteration of maps. value must be an integer. All algorithms (basically plot, guess and the manifold commands) acting on maps (regular, stroboscopic and Poincaré), will use the nperiod-th iterate of the map. The default value is 1.

dt <value>

sets the time step for the integrator. This is relevant for all settings of mode except the map setting. dt must be positive real number. If you want to plot backwards in time, use a negative step size. The default value is 0.001.

secvar <varname>

sets the variable of the Poincaré section. varname must be a variable that is part of the current equation system. The default value is 'x'.

secval <value>

sets the variable value of the Poincaré section. value must be a positive real number, the default value is 0.0.

secdir <'+'|'-'>

sets the direction in which crossings of Poincaré section are detected. If '+', crossings with increasing value of secvar are detected, if '-', crossings with decreasing value of secvar are detected. The default value is '+'.

maxtime <value>

determines, until which value of t SCIGMA integrates to find a section of the Poincaré plane, before throwing the towel. value must be a positive real number, the default value is 100.0.

eps <value>

sets the distance of the initial segment of invariant manifolds from a stationary state. value must be a non-zero real number. By changing the sign, you can plot the two parts of one-dimensional manifolds. The default value is 0.0001.

ds <value>

sets the arc length step for invariant manifolds of maps (not used if mode is ode). value must be a positive real number, the default is 0.01.

alpha <value>

sets the maximum accepted angle for consecutive line segments on invariant manifolds of maps (not used if mode is ode). value must be a positive angle in rad. Internally, SCIGMA uses an adapted step size algorithm to approximate invariant manifolds of maps. If two consecutive line segments have an angle of more than alpha, the internal step size is reduced. The default value is 0.3.

evec1 <value>

sets the first eigenvector that is used when computing invariant manifolds. value must be a positive integer, no larger then the number of dimensions in the current equations system. The eigenvalues of any stationary state are sorted according to stability (i.e. with ascending real value for ODEs, with ascending modulus for maps). For a stable (unstable) manifold the evec1-th most stable (unstable) eigenvalue is selected. The default value is 1, for the selection of the most stable (unstable) eigenvalue.

Newton.tol <value>

sets the tolerance of the Newton-Raphson algorithm that is used for finding stationary states, and also to converge onto Poincaré planes. value must be a positive real number, the default is 1e-9.

atol stol stol

sets the absolute tolerance of the ODESSA integration algorithm. value must be a positive real number, the default is 1e-9.

rtol <value>

sets the relative tolerance of the ODESSA integration algorithm. value must be a positive real number, the default is 1e-9.

type <'non-stiff'|'stiff'> sets whether the ODESSA integrator should use an algorithm for non-stiff or stiff equations. The default value is 'stiff'.

mxiter <value>

sets the number of internal steps before the ODESSA integrator bails out if it does not converge. value must be a positive integer, the default is 500. switches between

5.2 View and style

axes <'xy','xyz','xyc','xyzc'>

sets the whether the current view is 2D ('xy'), 2D with a color map ('xyc'), 3D ('xyz') or 3D with a color map ('xyzc'). The default is 'xy'.

color <name|r g b [a]|index>

sets the drawing color for new objects. There are three ways of specifying the color:

- using the name, e.g. color green; available names are 'red', 'green', 'blue', 'yellow', 'pink', 'lime', 'azure', 'orange', 'brown', 'forest', 'navy', 'teal', 'rose', 'aqua', 'sky', 'beige', 'black', 'dark_gray', 'gray', 'light_gray', 'white', 'cyan' and 'magenta'.
- using rgb (and potentially alpha) values, e.g. color 1 0 1 [1] for magenta; all values must be real numbers between 0.0 and 1.0, alpha values are optional.
- using an index, e.g. color 6 for orange; the index must be an integer from 0-22 which points into the list of colors given above.

The default value is color red = color 0.75 0 0 = color 0.

delay <value>

sets the artificial plotting delay. value must be a non-negative real number. If not zero, SCIGMA waits for delay seconds before plotting the next step of an orbit or manifold that is currently computed. This can be used to better observe the evolution of a state in

phase space over time. Also, if marker.style is not none, the current point of the orbit or trajectory is marked with a small graphic, which is easier to track. Plotting with delay only works correctly, however, if a single step can be computed faster than delay, otherwise the speed of the integration/manifold plotting algorithm determines how fast things are plotted. The default value is 0.0.

marker.style

sets the marker style for plotting with delay. Possible values are 'dot', 'plus', 'ring', 'rdot', 'rplus', 'rcross', 'quad', 'qdot', 'qplus', 'qcross', 'hash', 'star' and 'none'. The default value is 'star'.

marker.size

sets the marker size for plotting with delay and for marking stationary states. value must be a positive real number (values larger than 64.0 may not be supported by the OpenGL implementation). The default value is 16.0.

point.style

sets the point style for plotting orbits, trajectories and one-dimensional manifolds. Possible values are 'dot', 'plus', 'ring', 'rdot', 'rplus', 'rcross', 'quad', 'qdot', 'qplus', 'qcross', 'hash', 'star' and 'none'. The default value is 'none' (in this case, the points are connected by line segments).

point.size

sets the point size for plotting orbits, trajectories and one-dimensional manifolds. value must be a positive real number (values larger than 64.0 may not be supported by the OpenGL implementation). The default value is 8.0.

6 Mouse navigation

6.1 Rotating

If the current projection is three-dimensional (see axes option and the 2d/3d commands), you can rotate the viewing volume by pressing the left mouse button somewhere over an empty region of the graphics window and dragging the mouse.

6.2 Shifting

You can shift the viewing area/volume along the horizontal and vertical axes of the screen by pressing the left mouse button somewhere over an empty region of the graphics window and dragging the mouse while also pressing the shift key. Alternatively, if you let the cursor hover over one of the axes, such that it is highlighted, you can shift along this axes by pressing the left mouse button and dragging the mouse.

6.3 Zooming

You can change the scale of the viewing area/volume by scrolling with the mouse wheel, while the cursor is over an empty region of the graphics window. This zooms in and out equally for all axes. Alternatively, if you let the cursor hover over one of the axes, such that it is highlighted, you can scale just this axis by scrolling with the mouse wheel.

6.4 Picking points

If the projection is two-dimensional, double clicking somewhere in the graphics window will make the two coordinates of this point current. You will also see a white crosshair shape marking the point. In three-dimensional projection, the first double click will define a line of sight. If you rotate the viewing volume, you will see the line of sight as it runs through the viewing volume. On it, there is a white crosshair shape that follows the movement of the mouse. If you are satisfied with the position of the crosshair, double click again, and the three coordinates of the point will be made current. Also, the point is marked by the crosshair.

Both in two and three dimensions you can pick more than one point. To do so, press the control key while performing the steps above multiple times. As a result, you will get a number of crosshair shapes, marking your set of newly picked initial conditions. Commands like plot will now act simultaneously on all of these.

6.5 Picking objects

Whenever the mouse hovers over an object like a trajectory in the graphics window, the object is highlighted. If you now double click, this will select the object under the cursor as current object. The current object is used by commands like munstable, if no object is explicitly given as an argument. Also, the coordinates of the object (in case of orbits and trajectories: the last point) are made current.

7 The Python layer

 \dots coming soon \dots

8 The C++ layer

 \dots coming soon \dots

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