

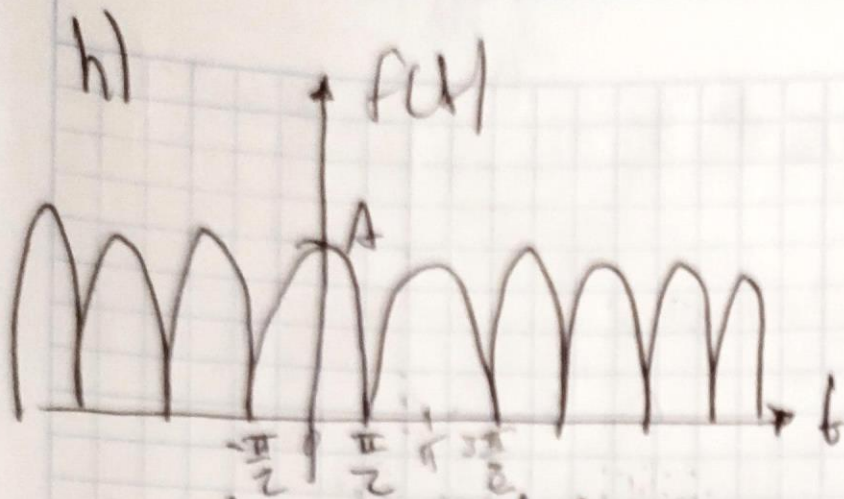
$$\mathcal{F}\left\{\frac{d^2}{dt^2} f(t)\right\} = \mathcal{F}\left\{4 \frac{d}{dt} \delta(t+0)\right\} - \mathcal{F}\{48\delta(t-10)\} + \mathcal{F}\{48\delta(t-11)\} + \mathcal{F}\{4 \frac{d}{dt} \delta(t-12)\} - \mathcal{F}\{48\delta(t-14)\} - \mathcal{F}\{48\delta(t-18)\}$$

$$(i\omega)^2 F(\omega) = i\omega 4 \frac{d}{d\omega} e^{i\omega 0} - 48 e^{i\omega 10} + 48 e^{i\omega 11} + i\omega 4 \frac{d}{d\omega} e^{i\omega 12} - 48 e^{i\omega 14} - 48 e^{i\omega 18}$$

$$F(\omega) = \left\{ \frac{-1}{\omega^2} \left[ -4 e^{i\omega 0} + 4 e^{i\omega 12} \right] - 48 e^{i\omega 10} + 48 e^{i\omega 11} - 48 e^{i\omega 14} - 48 e^{i\omega 18} \right\}$$

$$\pm 8\pi \delta(\omega) \pm 2\pi [\delta(\omega - 100) - \delta(\omega - 100)] \begin{cases} 0 & -7 < t < 2 \\ 0 & 2 < t < 7 \end{cases}$$





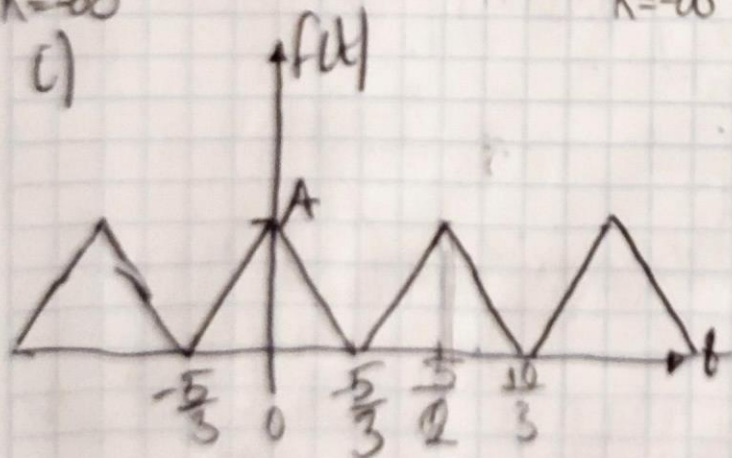
$$f(t) = \begin{cases} A \cos t & -\frac{\pi}{2} < t < \frac{\pi}{2} \\ f(t + \pi) \end{cases}$$

Usando resultado de (b)

$$A \cos t G_{\pi}(t) \leftrightarrow \frac{A\pi}{2} \left[ \text{Sa}\left(\frac{\omega\pi}{2} + 1\right) + \text{Sa}\left(\frac{\omega\pi}{2} - 1\right) \right]$$

$$A \cos t G_{\pi}(t + K\pi) \leftrightarrow \frac{A\pi}{2} \left[ \text{Sa}\left(\frac{\omega\pi}{2} + 1\right) + \text{Sa}\left(\frac{\omega\pi}{2} - 1\right) \right] e^{iK\pi}$$

$$\sum_{K=-\infty}^{\infty} A \cos t G_{\pi}(t + K\pi) \leftrightarrow \sum_{K=-\infty}^{\infty} \frac{A\pi}{2} \left[ \text{Sa}\left(\frac{\omega\pi}{2} + 1\right) + \text{Sa}\left(\frac{\omega\pi}{2} - 1\right) \right] e^{iK\pi}$$



$$A\left(\frac{t}{d}\right) \leftrightarrow \frac{Ad}{2} \text{Sa}^2 \frac{\omega d}{4}$$

$$d = \frac{10}{3}$$

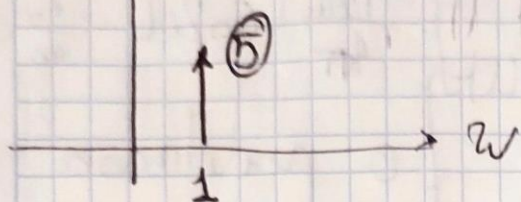
$$\Lambda\left(\frac{3t}{10}\right) \leftrightarrow \frac{A10}{6} \text{Sa}^2 \frac{\omega 10}{12}$$

$$\Lambda\left(\frac{3}{10}\left(t + \frac{K5}{2}\right)\right) \leftrightarrow \frac{A10}{6} \text{Sa}^2 \frac{\omega 10}{12} e^{iK\pi}$$

$$\sum_{K=-\infty}^{\infty} \Lambda\left(\frac{3}{10}\left(t + \frac{K5}{2}\right)\right) \leftrightarrow \sum_{K=-\infty}^{\infty} \frac{A10}{6} \text{Sa}^2 \frac{\omega 10}{12} e^{iK\pi}$$



j)  $F(\omega)$



$$F(\omega) = 5\delta(\omega - 1)$$

Calculando transformadas

$$\delta(t) \leftrightarrow 1$$

$$\delta(t-1) \leftrightarrow e^{-i\omega}$$

$$5\delta(t-1) \leftrightarrow 5e^{-i\omega}$$

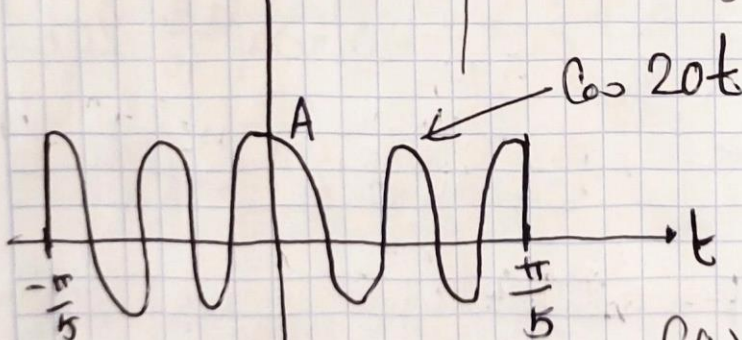
$$5e^{-i\omega} \leftrightarrow 2\pi 5\delta(\omega - 1)$$

$$f(t) = \frac{5e^{-i\omega}}{2\pi} \leftarrow \text{Inversa } F(\omega) \quad \frac{5e^{-i\omega}}{2\pi} \leftrightarrow 5\delta(\omega - 1)$$

$$F(\omega) = 5e^{-i\omega} \quad \text{Transformada Fourier de } F(\omega)$$

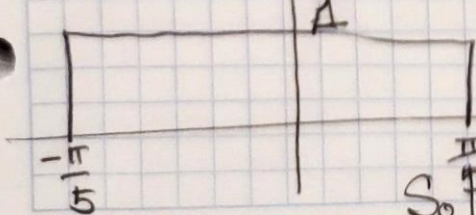
**Problema 12** Aplicando el teorema de modulación encontrar la transformada de cada una de las señales moduladas que mostramos

a)  $f(t) = A \cos 20t \quad -\frac{\pi}{5} < t < \frac{\pi}{5}$



$$\frac{1}{2} = \frac{\pi}{5}$$

$g(t) = \begin{cases} 1 & -\frac{\pi}{5} < t < \frac{\pi}{5} \\ 0 & \text{elsewhere} \end{cases}$



$$f(t) \times g(t) = A \cos 20t \cdot \begin{cases} 1 & -\frac{\pi}{5} < t < \frac{\pi}{5} \\ 0 & \text{elsewhere} \end{cases}$$

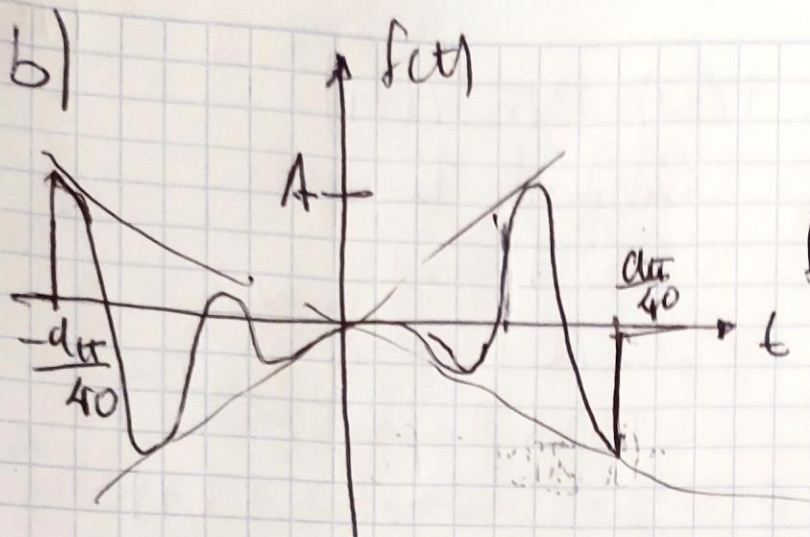
$$\begin{cases} 1 & -\frac{\pi}{5} < t < \frac{\pi}{5} \\ 0 & \text{elsewhere} \end{cases} \leftrightarrow \frac{\pi}{5} \text{Sa} \left( \frac{\omega\pi}{5} \right)$$

$$\begin{cases} 1 & -\frac{\pi}{5} < t < \frac{\pi}{5} \\ 0 & \text{elsewhere} \end{cases} \cos(20t) \leftrightarrow \frac{\pi}{5} \left[ \text{Sa} \left( \frac{\omega\pi}{5} + 20 \right) + \text{Sa} \left( \frac{\omega\pi}{5} - 20 \right) \right]$$

Sol.  $A \begin{cases} 1 & -\frac{\pi}{5} < t < \frac{\pi}{5} \\ 0 & \text{elsewhere} \end{cases} \cos(20t) \leftrightarrow \frac{A\pi}{5} \left[ \text{Sa} \left( \frac{\omega\pi}{5} + 20 \right) + \text{Sa} \left( \frac{\omega\pi}{5} - 20 \right) \right]$

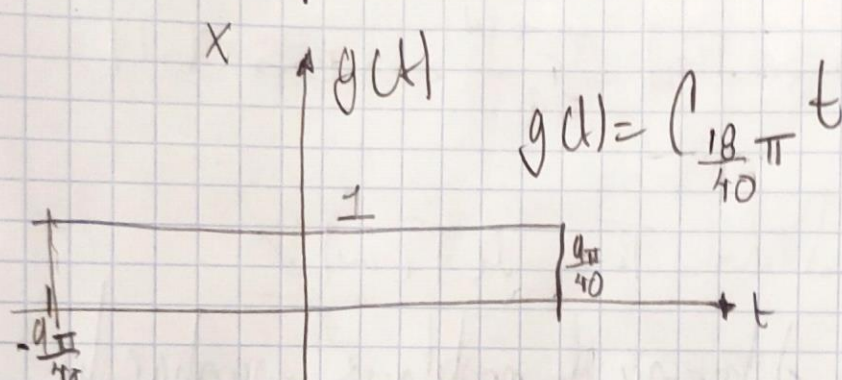


b)



$$f(t) = \frac{-40A}{40\pi} t \cos 20t \quad -\frac{40\pi}{40} \leq t \leq \frac{40\pi}{40}$$

o para otros casos



$$g(t) = \left( \frac{18\pi}{40} \right) t$$

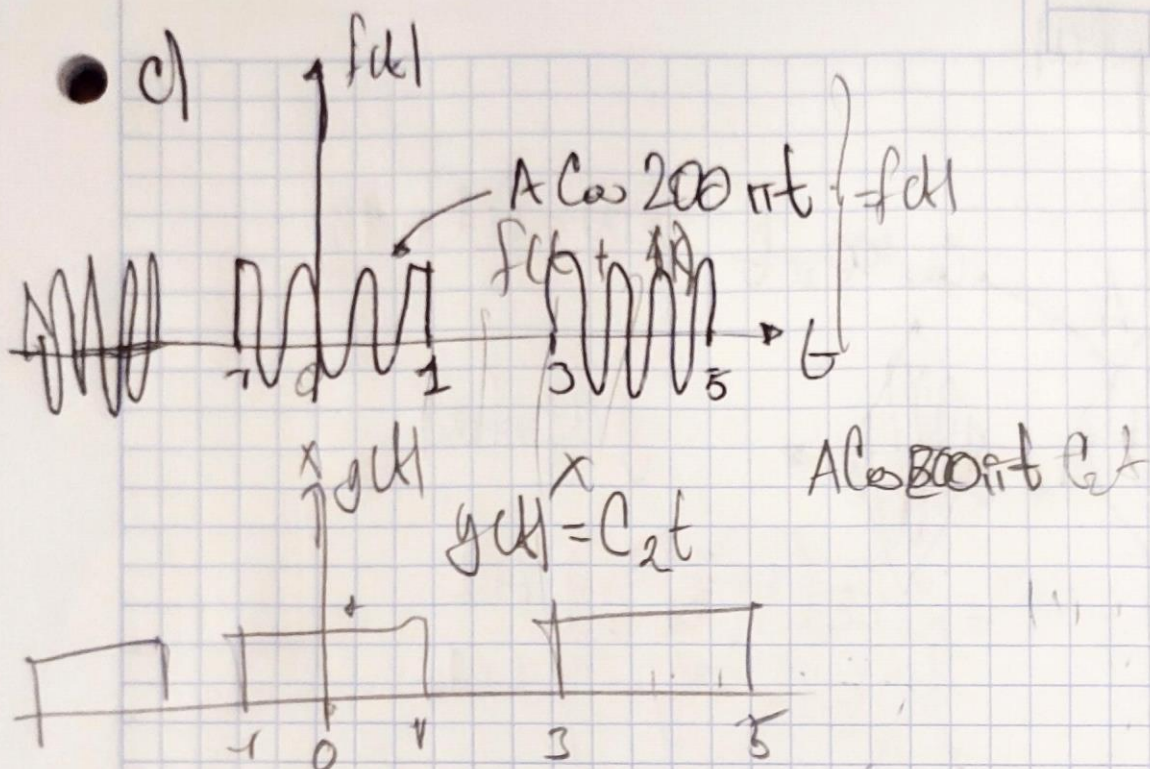
$$\left( \frac{18\pi}{40} \right) t \longleftrightarrow \frac{18\pi}{40} \text{Sa} \left( \frac{w 40}{40} \right)$$

$$\left( \frac{18\pi}{40} \right) t \cos 20t \longleftrightarrow \frac{18\pi}{40} \left[ \text{Sa} \left( \frac{w 40}{40} + 20 \right) + \text{Sa} \left( \frac{w 40}{40} - 20 \right) \right]$$

$$(-it) \left( \frac{18\pi}{40} \right) t \cos 20t \longleftrightarrow \frac{d}{dw} \left\{ \frac{18\pi}{40} \left[ \text{Sa} \left( \frac{w 40}{40} + 20 \right) + \text{Sa} \left( \frac{w 40}{40} - 20 \right) \right] \right\}$$

$$\frac{-40A}{40\pi} t \cos 20t \left( \frac{18\pi}{40} \right) t \longleftrightarrow 2\pi A \frac{d}{dw} \left\{ \text{Sa} \left( \frac{w 40}{40} + 20 \right) + \text{Sa} \left( \frac{w 40}{40} - 20 \right) \right\}$$





$$C_2 t \leftrightarrow 2 \text{Sa } \omega$$

$$C_2 t \cos 200\pi t \leftrightarrow \text{Sa}(\omega + 200\pi) + \text{Sa}(\omega - 200\pi)$$

$$A C_2 t \cos 200\pi t \leftrightarrow A \text{Sa}(\omega + 200\pi) + A \text{Sa}(\omega - 200\pi)$$

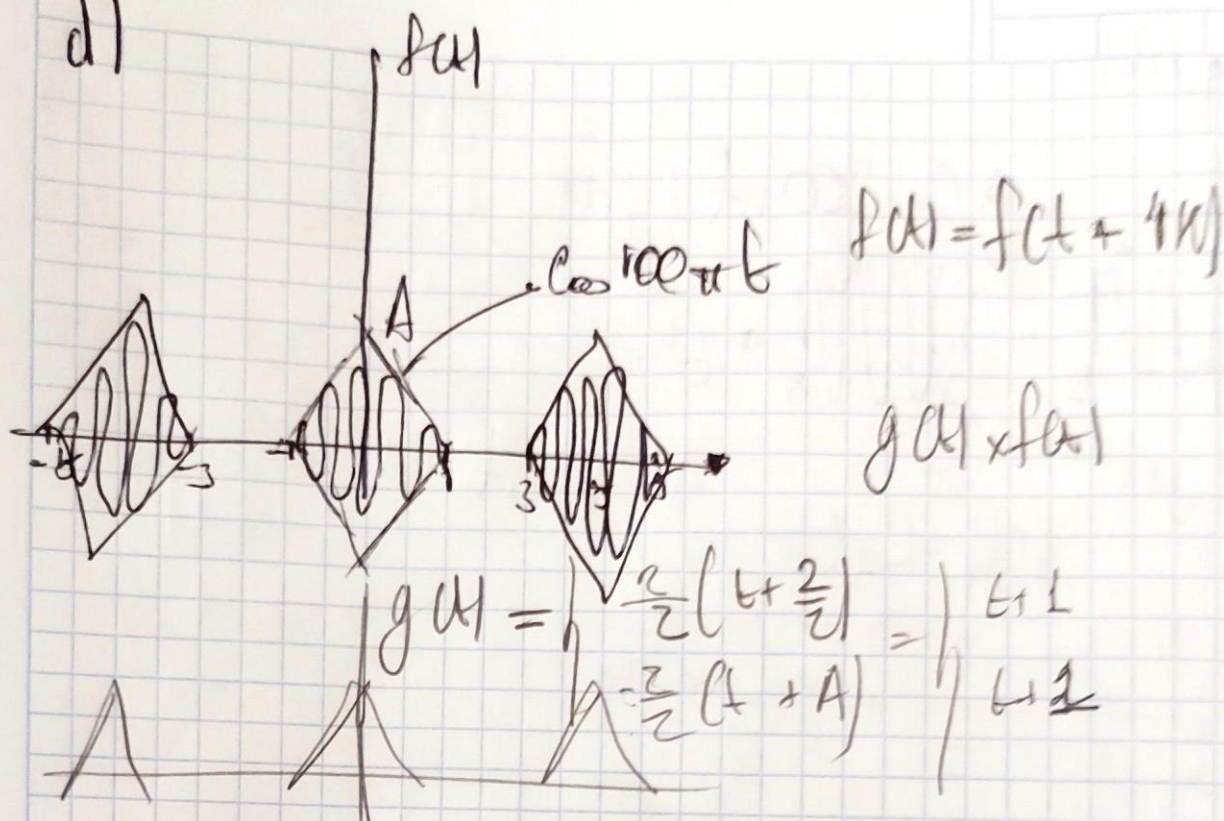
$t = t + 4K$

$$A C_2(t + 4K) \cos(200\pi(t + 4K)) \leftrightarrow A \text{Sa}(\omega + 200\pi) + A \text{Sa}(\omega - 200\pi) e^{j4K\omega}$$

$$\sum_{K=-\infty}^{\infty} A C_2(t + 4K) \cos(200\pi(t + 4K)) \leftrightarrow \sum_{K=-\infty}^{\infty} A [\text{Sa}(\omega + 200\pi) + \text{Sa}(\omega - 200\pi)] e^{j4K\omega}$$



d)



$$g(t) \longleftrightarrow \text{Sa}^2\left(\frac{\omega}{2}\right)$$

$$g(t) \cos(100\pi t) \longleftrightarrow \frac{1}{2} \text{Sa}\left(\frac{\omega}{2} + 100\pi\right) + \text{Sa}\left(\frac{\omega}{2} - 100\pi\right)$$

$$g(t) A \cos(100\pi t) \longleftrightarrow \frac{A}{2} \left[ \text{Sa}\left(\frac{\omega}{2} + 100\pi\right) + \text{Sa}\left(\frac{\omega}{2} - 100\pi\right) \right]$$

$t + 4k$

$$\sum_{n=-\infty}^{\infty} g(t + 4k) A \cos(100\pi(t + 4k)) \longleftrightarrow \sum_{n=-\infty}^{\infty} \frac{A}{2} \left[ \text{Sa}\left(\frac{\omega}{2} + 100\pi\right) + \text{Sa}\left(\frac{\omega}{2} - 100\pi\right) \right] e^{j4k\omega}$$

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