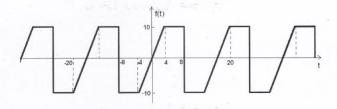
INSTITUTO POLITECNICO NACIONAL ESCUELA SUPERIOR DE COMPUTO Teoría de Comunicaciones y Señales

1er. Exámen departamental

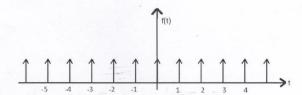
NOMBRE:	TIPO: B
GRIDO:	

Problema 1. Encuentre la Serie Trigonométrica de Fourier de x(t)



Problema 2. A partir de la serie obtenida en el problema anterior, encuentra la Serie Exponencial de Fourier.

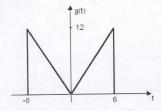
Problema 3. Encuentre la transformada de Fourier de la siguiente función periódica:



Problema 4. Usando propiedades, encuentre la transformada inversa de Fourier de:

?
$$\leftrightarrow 6\delta(3\omega - 10)cos(15\omega) + \frac{1}{3 - j\omega}\omega^2 + e^{j4\omega}(\omega - 1)$$

Problema 5. Usando Propiedades de la transformada de Fourier encuentre la transformada de f(t)



1er Examen Departamental TIPO B

$$T=16$$

$$\omega_{o}=\frac{217}{16}=\frac{17}{8}$$
esimpar:

 $Q_0 = Q_n = Q$

$$D_{n} = \frac{4}{T} \int_{0}^{T} f(t) \operatorname{Sen nwot} dt$$

$$D_{n} = \frac{4}{16} \int_{0}^{8} f(t) \operatorname{Sen nm} t dt$$

$$D_{n} = \frac{4}{16} \int_{0}^{8} f(t) \operatorname{Sen nm} t dt$$

$$D_{n} = \frac{4}{4} \int_{0}^{4} \frac{5}{2} t \operatorname{Sen nm} t dt + \frac{1}{4} \int_{4}^{8} \operatorname{IoSen nm} t dt$$

$$U = t dv = \operatorname{sen nm} t dt$$

$$V = -\frac{8}{nU} \cos \frac{n\pi}{2} t$$

$$V = -\frac{8}{nU} \cos \frac{n\pi}{2} t$$

$$f(t) = \int \frac{40}{n^2 \pi^2} \int e^{n \pi t} \frac{20}{n \pi} f(t)^{n/2} \int e^{n \frac{\pi t}{8}} e^{n \frac{\pi t}{8}} \frac{1}{n \pi} \int e^{n \frac{\pi t}{8}} e^{n \frac{\pi t}{8}} e^{n \frac{\pi t}{8}}$$

 $b_n = \frac{40}{n^2 \pi^2} \text{ Sen } \frac{n\pi}{2} - \frac{20}{n\pi} (-1)^n$

$$b_{n} = \frac{5}{8} \left\{ \frac{-8}{n\pi} + \cos \frac{n\pi}{8} t \right\}_{0}^{4} + \frac{8}{n\pi} \int_{0}^{4} \cos \frac{n\pi}{8} t \, dt$$

$$+ \left(\frac{5}{2}\right) \left(-\frac{8}{n\pi}\right) \cos \frac{n\pi}{8} t \, dt$$

$$D_{n} = \frac{5}{8} \left[\frac{-32}{n\pi} \cos \frac{n\pi}{2} + \phi + \frac{64}{n^{2}\pi^{2}} \sin \frac{n\pi}{8} t \right]_{0}^{4} - \frac{20}{n\pi} \cos \frac{n\pi}{8} t \Big|_{0}^{8}$$

$$D_{n} = -\frac{20}{n\pi} \cos \frac{n\pi}{2} + \frac{40}{n^{2}\pi^{2}} \left[\sin \frac{n\pi}{2} - \phi \right] - \frac{20}{n\pi} \left[\cos n\pi - \cos \frac{n\pi}{2} \right]$$

$$= -\frac{20}{n\pi} \cos \frac{n\pi}{2} + \frac{40}{n^{2}\pi^{2}} \sin \frac{n\pi}{2} - \frac{20}{n\pi} \cos n\pi + \frac{20}{n\pi} \cos \frac{n\pi}{2} \right]$$

Problema 2 (1.5 pts)

Si
$$f(t) = \sum_{n=1}^{\infty} \left[\frac{40}{n^2 \pi^2} \operatorname{sen} \frac{n\pi}{2} - \frac{20}{n\pi} (-1)^n \right] \cdot \operatorname{Sen} \frac{n\pi}{8} t$$

Entonces, so serie exponencial, está dada por: $f(t) = \sum_{n=\infty}^{\infty} (n e^{i\frac{n\pi}{2}t} con C_n = \frac{1}{2}(0n-ibn)$ Pero como 0n=0

$$C_{n} = -\frac{1}{2}b_{n} = -i\left[\frac{20}{n^{2}\pi^{2}} \operatorname{sen} \frac{n\pi}{2} - \frac{10}{n\pi} (-1)^{n}\right]$$

$$C_{n} = i\left[\frac{10}{n\pi} (-1)^{n} - \frac{20}{n^{2}\pi^{2}} \operatorname{sen} \frac{n\pi}{2}\right]$$

Finalmente:

$$f(t) = \sum_{n=-\infty}^{\infty} j \left[\frac{10}{n\pi} (-1)^n - \frac{20}{n^2 \pi^2} \operatorname{Sen} \frac{n\pi}{2} \right] \cdot C^{\frac{1}{8}t}$$

$$f(t) = \sum_{n=-\infty}^{\infty} j \frac{10}{n\pi} \left[(-1)^n - \frac{2}{n\pi} \operatorname{Sen} \frac{n\pi}{2} \right] C^{\frac{10}{8}t}$$

$$1.5$$

Problema 3

$$2 \quad C_n = \frac{1}{7} \int_{-L}^{\frac{T}{2}} f(t) e^{-\ln w \cdot t} dt$$

$$C_{n} = \int_{\frac{1}{2}}^{\frac{1}{2}} \int_{-i2\pi nt}^{-i2\pi nt} dt$$

$$C_{n} = \int_{0}^{0+} \frac{1}{\delta(t)} e^{-i2\pi nt} dt$$

$$C_{n} = \int_{0}^{0+} \frac{1}{\delta(t)} e^{-i2\pi nt} dt$$

$$C_n = \int_0^{0+} \delta(t) e^{-i2\pi nt} dt$$

De la Propiedad de muestreo de $\delta(4)$

$$C_n = C^\circ = 1$$

Finalmente:

$$\mathcal{J}_{1}\left\{f(t)\right\} = 2\Pi \sum_{n=-\infty}^{\infty} \delta\left(\omega - 2\Pi n\right) \begin{cases}
2.0 \text{ pts}
\end{cases}$$

Problema 4 (2,5 pts)



?
$$\longleftrightarrow$$
 68 (3W-10). Cos 15W+ \coprod $\overset{i4w}{U}$ $\overset{i4w}{U}$

Solvaión:

$$\begin{array}{c}
\widehat{I} & 5i & \delta(t) \leftrightarrow I \\
\frac{1}{2\pi} & \sim \delta(-\omega) \\
\frac{1}{2\pi} & \epsilon^{100} \leftrightarrow \delta(\omega - 10) \\
\frac{1}{2\pi} & \epsilon^{100} \leftrightarrow \epsilon^{100} & \epsilon^{100} & \epsilon^{100} \\
\frac{1}{2\pi} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} \\
\frac{1}{3\pi} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} & \epsilon^{100} \\
\end{array}$$

$$\frac{1}{2\pi}e^{i\frac{\omega}{3}} \longrightarrow 3\delta(3\omega-10)$$

$$\frac{1}{\pi}e^{i\frac{\omega}{3}} \longrightarrow 6\delta(3\omega-10)$$

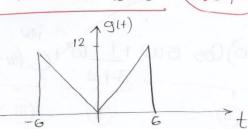
$$-\frac{d^{2}}{d^{2}+}\left[e^{+3t}u(+)\right] \longleftrightarrow \frac{w^{2}}{3-iw}$$

$$(w-1) = \frac{1}{\frac{d}{dt}} \frac{\delta(t)}{\delta(t)} \Leftrightarrow i\omega$$

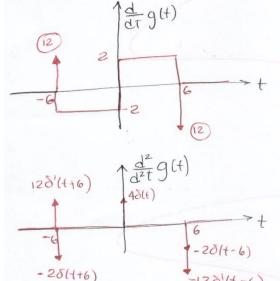
$$-j = \frac{1}{\frac{d}{dt}} \frac{\delta(t)}{\delta(t)} e^{jt} \Leftrightarrow (w-1)$$

$$-i = \frac{1}{\frac{d}{dt}} \frac{\delta(t+4)}{\delta(t+4)} \Leftrightarrow (w-1) = \frac{1}{\frac{d}$$

Problema 5



SOLUCION;



 $\frac{d^{2}}{(2+g(t))} = -2\delta(t+6) + (2\delta'(t+6) + 4\delta(t)) - 2\delta(t-6) - (2\delta'(t-6))$

$$\begin{aligned} & \left[\int_{1}^{2} \frac{d^{2}}{d^{2}t} g(t) \right] = -2 \int_{1}^{2} \int_{0}^{2} \delta(t+6) \\ & + 12 \int_{1}^{2} \int_{0}^{2} \left[(t+6) \right] + 4 \int_{1}^{2} \int_{0}^{2} (t+1) \\ & - 2 \int_{1}^{2} \int_{0}^{2} \left[(t+6) \right] - 12 \int_{1}^{2} \int_{0}^{2} \left[(t-6) \right] \end{aligned}$$

$$\left| \mathcal{F}_{1} \left| \frac{d^{2}}{d^{2}t} g(t) \right| = -2 e^{i\omega t} + 12i\omega e^{i\omega t} + 4 \\
-2 e^{-i\omega t} - 12i\omega e^{-i\omega t}$$

$$\frac{d^2}{d^2}g(t) \longrightarrow 8 \operatorname{Sen}^2 3w - 24w \operatorname{Sen} 6w$$

Si glt)
$$\longrightarrow$$
 G(w)
$$\frac{d^2}{d^2t}g(t) \longleftarrow (|w|)^2G(w)$$

Finalmente

Finalmente
$$(Jw)^2G(w) = 85en^23w - 24 wSen6w$$

$$G(w) = -\frac{1}{w^2} [8 \sin^2 3w - 24w \text{Sen6w}]$$

$$G(\omega) = \frac{24}{\omega} \operatorname{Sen} 6\omega - \frac{8}{\omega^2} \operatorname{sen}^2 3\omega$$