

1 Visualización de Datos

Código cargar los datos y construir la gráfica 3D con los cafés e imprimir la matriz Y

```
> library ( FactoClass );
> data ( cafe );
> Y <- cafe [1:10 ,1:3];
> par ( las =1); # grafica ;
> Y3D <- scatterplot3d (Y, main ="Y",type ="h",color =" black ",box=FALSE ,las =1);
> Y3D $ points3d (Y, pch =1);
> addgrids3d (Y, grid = c("xy","xz","yz"));
> cord2d <-Y3D$xyz.convert (Y) # convertir coordenadas 3D a 2D;
> # poner etiquetas ;
> # text ( cord2d , labels = rownames (Y), cex =0.8 , col=" black ",pos =3);
> # xtable (Y, digits =c(0 ,0 ,1 ,0)) # para tabular de LaTeX ;
>
```

	Color	DA	EA
ExCl	298	385.1	25
C40M	361	481.3	41
C40C	321	422.6	40
C20M	335	444.3	33
C20C	314	368.7	32
ExOs	186	346.6	28
O40M	278	422.6	43
O40C	238	403.0	42
O20M	226	368.7	36
O20C	210	368.7	35

2 Calculo del Centro de Gravedad

Código para calcular y adicionar el centro de gravedad a la figura

```
> g <- colMeans (Y) # centro de gravedad ;
> Y3D$points3d (t(g), pch =19 , col=" darkgreen ",type = "h");
> text ( Y3D$xyz.convert (t(g)), labels ="g",pos =3, col=" black ", cex =1.3);
>
```

3 Centro de datos

Centrar los datos, graficarlos en 3D e imprimir la matriz Yc

```

> n <- 10
> par ( las =1);
> unos <-rep (1,n); # vector de n unos
> Yc <- Y - unos%*%t(g);
> # grafica de datos centrados
>
> Yc3D <- scatterplot3d (Yc , main ="Yc",type ="h",color =" black ", box =FALSE , las =1);
> Yc3D$points3d (Yc , pch =1);
> addgrids3d (Yc , grid =c("xy", "xz", "yz" ));
> text ( Yc3D$xyz.convert (Yc), labels = rownames (Yc),cex =0.8 , col =" black ",pos =3);
> Yc3D $ points3d (t(c(0 ,0 ,0)) , pch =19 , col =" black ",type = "h");
> text ( Yc3D$xyz.convert (t(c(0 ,0 ,0))) , labels ="0",pos =3, col =" black ",cex =1.3);
>
>

```

4 Distancia al centro de gravedad

```

> Y_dist <- round(as.dist(dist(Y)),0);
> Y_dist

      ExC1 C40M C40C C20M C20C Ex0s 040M 040C 020M
C40M   116
C40C    46    71
C20M    70    46    27
C20C    24   122    55    78
Ex0s   118   221   155   178   130
040M    46   102    43    62    66   120
040C    65   146    85   106    84    78    45
020M    75   176   109   133    88    46    75    37
020C    90   188   123   146   104    33    87    45    16

>

```

5 Calculo de matriz de varianzas

Multiplica la matriz de

```

> par ( las =1) # etiquetas de los dos ejes sean horizontales ;
> # Calculo de la matriz de Varianzas y covarianzas
>
> V <-t(Yc) %*% as.matrix (Yc)/n;
> V

```

```

      Color      DA      EA
Color 3105.810 1738.388 60.95

```

```
DA    1738.388 1560.188 129.36
EA     60.950 129.360 33.45
```

```
>
> # V = var (Y)*(n -1)/n; # Se usa porque R toma los datos como una muestra y no una poblaci
```

6 Calculo de la matriz diagonal

Toma lo valores de la diagonal de la matriz de varianzas

```
> # Diagonalización de la Matriz
>
> Dsigma <- diag ( sqrt ( diag (V ))) ;
> round (diag(Dsigma) ,1);
```

```
[1] 55.7 39.5 5.8
```

```
>
```

7 matriz normalizada X

```
> X <-as.matrix (Yc) %*% solve (Dsigma);
> colnames (X) <- colnames (Y);
> X3D <- scatterplot3d (X, main ="X",type ="h",box= FALSE );
> X3D$points3d (Yc , pch =1);
> addgrids3d (X, grid =c("xy","xz","yz" ));
> text ( X3D $ xyz.convert (X), labels = rownames (X),cex =0.8 , pos =3);
> X3D $ points3d (t(c(0 ,0 ,0)) , pch =19 , col=" black ",type ="h");
> # text ( X3D $ xyz.convert (t(c(0 ,0 ,0))) , labels ="0",pos =3, col=" black ",cex =0.8);
> # xtable (X, digits = rep (1 ,4)) # tabla para LaTeX ;
>
```

	Color	DA	EA
ExCl	0.4	-0.4	-1.8
C40M	1.5	2.0	1.0
C40C	0.8	0.5	0.8
C20M	1.0	1.1	-0.4
C20C	0.7	-0.8	-0.6
ExOs	-1.6	-1.4	-1.3
O40M	0.0	0.5	1.3
O40C	-0.7	0.0	1.1
O20M	-0.9	-0.8	0.1
O20C	-1.2	-0.8	-0.1

8 Distancias de los datos estandarizado

Distancias entre cafés cuando los datos están estandarizados(centrados y reducidos)

```
> X<-scale(Y);
> X_dist <- round(as.dist(dist(X)),1);
> X_dist
```

	ExC1	C40M	C40C	C20M	C20C	Ex0s	040M	040C	020M
C40M	3.7								
C40C	2.6	1.6							
C20M	2.0	1.6	1.3						
C20C	1.2	3.2	1.8	1.9					
Ex0s	2.2	4.9	3.5	3.6	2.3				
040M	3.1	2.0	0.9	2.0	2.3	3.4			
040C	3.0	2.8	1.5	2.4	2.2	2.8	0.8		
020M	2.2	3.6	2.2	2.6	1.6	1.6	1.9	1.3	
020C	2.3	3.9	2.4	2.8	1.8	1.3	2.2	1.5	0.3

9 Obtencion de los valores y vectores propios

```
> des <-eigen (V);
> des # calculo de valores y vectores propios
```

eigen() decomposition

\$values

```
[1] 4238.94326 444.23103 16.27412
```

\$vectors

	[,1]	[,2]	[,3]
[1,]	0.83785566	0.5409101	0.07358114
[2,]	0.54512571	-0.8219057	-0.16525428
[3,]	0.02891094	-0.1785702	0.98350233

```
> lambda <-des$values
> U <- des$vectors # matriz con vectores propios en columnas
> rownames(U) <- rownames (V)
> colnames(U) <- c(" Eje1 "," Eje2 "," Eje3 "); round (U ,3)
```

	Eje1	Eje2	Eje3
Color	0.838	0.541	0.074
DA	0.545	-0.822	-0.165
EA	0.029	-0.179	0.984

```
> lambda
```

```
[1] 4238.94326 444.23103 16.27412

> U

      Eje1      Eje2      Eje3
Color 0.83785566 0.5409101 0.07358114
DA    0.54512571 -0.8219057 -0.16525428
EA    0.02891094 -0.1785702 0.98350233

>
```

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```
> F <- X %*% U
> round ( sort (F[,1]) ,2)

Ex0s  020C  020M  040C  ExC1  C20C  040M  C40C  C20M  C40M
-2.04 -1.38 -1.15 -0.50  0.04  0.09  0.33  0.93  1.38  2.28

>
```

11 Código para obtener el primer plano factorial y la tabla

```
> F <- X %*% U;
> round (F ,2) # coordenadas sobre los nuevos ejes

      Eje1  Eje2  Eje3
ExC1  0.04  0.82 -1.60
C40M  2.28 -0.97  0.67
C40C  0.93 -0.15  0.70
C20M  1.38 -0.24 -0.50
C20C  0.09  1.09 -0.39
Ex0s -2.04  0.46 -1.11
040M  0.33 -0.63  1.13
040C -0.50 -0.58  0.99
020M -1.15  0.16  0.15
020C -1.38  0.04 -0.04

> plot (F[,1:2] , las =1, asp =1) # plano 12
> text (F[,1:2] , label = rownames (F), col=" black ",pos =2) # etiquetas
> abline (h=0,v=0, col =" darkgrey ") # ejes
> rowSums (F^2)-> d2;d2 # distancias

      ExC1      C40M      C40C      C20M      C20C      Ex0s      040M      040C
3.246622 6.578011 1.378697 2.226649 1.340566 5.614494 1.779107 1.572724
      020M      020C
1.359404 1.903726
```

```

> 1/n*F^2 %%%diag (1/ lambda )*100 -> cont # contribuciones
> F^2/d2*100 -> cos2 # cosenos cuadrados
> # tabla de ayudas para la interpretacion
> Ayu <-cbind ( dis2 =d2 ,F1=F[ ,1] , F2=F[ ,2] , cont1 = cont [,1] , cont2 =
+ cont [,2] , cos21 = cos2 [ ,1] , cos22 = cos2 [,2] ,
+ cosp = rowSums ( cos2 [ ,1:2]))
> round (Ayu ,2) # ayudas en consola

```

	dis2	F1	F2	cont1	cont2	cos21	cos22	cosp
ExCl	3.25	0.04	0.82	0.00	0.02	0.06	20.75	20.81
C40M	6.58	2.28	-0.97	0.01	0.02	78.87	14.21	93.08
C40C	1.38	0.93	-0.15	0.00	0.00	63.26	1.57	64.83
C20M	2.23	1.38	-0.24	0.00	0.00	86.08	2.62	88.70
C20C	1.34	0.09	1.09	0.00	0.03	0.61	88.10	88.71
ExOs	5.61	-2.04	0.46	0.01	0.00	74.38	3.79	78.17
O40M	1.78	0.33	-0.63	0.00	0.01	6.30	22.38	28.68
O40C	1.57	-0.50	-0.58	0.00	0.01	15.71	21.62	37.32
O20M	1.36	-1.15	0.16	0.00	0.00	96.57	1.87	98.43
O20C	1.90	-1.38	0.04	0.00	0.00	99.84	0.09	99.93

```

> #xtable (Ayu , digits = rep (2 ,9)) # salida para LaTeX
>

```

	dis2	F1	F2	cont1	cont2	cos21	cos22	cosp
ExCl	3.25	0.04	0.82	0.00	0.02	0.06	20.75	20.81
C40M	6.58	2.28	-0.97	0.01	0.02	78.87	14.21	93.08
C40C	1.38	0.93	-0.15	0.00	0.00	63.26	1.57	64.83
C20M	2.23	1.38	-0.24	0.00	0.00	86.08	2.62	88.70
C20C	1.34	0.09	1.09	0.00	0.03	0.61	88.10	88.71
ExOs	5.61	-2.04	0.46	0.01	0.00	74.38	3.79	78.17
O40M	1.78	0.33	-0.63	0.00	0.01	6.30	22.38	28.68
O40C	1.57	-0.50	-0.58	0.00	0.01	15.71	21.62	37.32
O20M	1.36	-1.15	0.16	0.00	0.00	96.57	1.87	98.43
O20C	1.90	-1.38	0.04	0.00	0.00	99.84	0.09	99.93

12 Calcular las coordenadas factoriales de los dos cafés comerciales y su proyección sobre el primer plano factorial

```

> comer <-as.matrix ( cafe [11:12 ,1:3]);
> comer

```

	Color	DA	EA
Com1	221	413.3	27
Com2	264	400.9	23

```

> comc <-comer - rep (1 ,2) %*%t(g);
> comc # centrado

      Color      DA      EA
Com1 -55.7 12.14  -8.5
Com2 -12.7 -0.26 -12.5

> comcr <- comc %*%solve ( Dsigma ) # reducido
> colnames ( comcr ) <- colnames ( comer ); comcr

      Color      DA      EA
Com1 -0.9994654  0.307347839 -1.469674
Com2 -0.2278853 -0.006582408 -2.161285

> Fsup <- comcr %*%U;
> Fsup

      Eje1      Eje2      Eje3
Com1 -0.7123542 -0.5307919 -1.569760
Com2 -0.2570080  0.2680857 -2.141309

> # primer plano factorial
> plot (F[,1:2] , las =1, asp =1)
> text (F[,1:2] , label = rownames (F), col=" black ",pos =1)
> abline (h=0,v=0, col=" darkgrey ")
> points (Fsup ,col =" black ",pch =20) # cafes comerciales
> text (Fsup , labels =c(" Com1 "," Com2 "), col=" darkgreen ",pos =2)

```

13 Código para calcular las coordenadas de las categorías de contaminación y proyectarlas sobre el primer plano factorial

```

> conta <-factor (c(" exce "," maiz "," ceba "," maiz "," ceba "," exce ",
+ " maiz "," ceba "," maiz "," ceba "))
> centroids (F, conta )$ centroids -> Fconta ; Fconta

      Eje1      Eje2      Eje3
ceba -0.2128594  0.09945118  0.3161817
exce -0.9999009  0.64113648 -1.3552319
maiz  0.7128099 -0.42001942  0.3614343

> points ( Fconta ,col =" brown ",pch =20)
> text ( Fconta , col=" brown ",labels = rownames ( Fconta ),pos =2)
>

```

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```

> G <- U %*% diag(sqrt(lambda));
> G <- G / G # G <- cor (Y,F)
> colnames (G) <-c("G1","G2","G3");
> G3D <- scatterplot3d (G, main ="G")
> coord <- G3D$xyz.convert(G)
> text (coord , labels = rownames (G), cex =0.8 , col=" black ",pos =4)
> G3D$ plane (0 ,0 ,0 , col =" darkgrey ")
> G3D$ points3d (t(c(0 ,0 ,0)) , pch =19 , col=" black ")
> cero <- G3D$xyz.convert (0, 0, 0)
> for (eje in 1:3) {
+ arrows ( cero $x, cero $y, coord $x[ eje ], coord $y[eje ], lwd = 2,
+ length = 0.1)
+ }
> # dev . print ( device =xfig , file =" cafeEspera .fig ")# grafica en xfig
>
> s.corcircle (G, clabel =2);
> # proyeccion de nota como variable ilustrativa
>
> Nota <- cafe [1:10 ,16]; Nota ;

[1] 7.46 6.24 6.12 6.04 6.22 7.40 5.90 6.94 6.90 7.16

> Fnota <- cor (Nota ,F); Fnota ;

           Eje1      Eje2      Eje3
[1,] -0.7328713 0.4366652 -0.5836551

> arrows (0,0 , Fnota [1] , Fnota [2] , col =" black ",angle =10 , lty =2);
> text (Fnota ," Nota ",col =" black ",pos =1, cex =2, font =3);
>
>
>

```