

課題1

棒の全長は変化しないので

$$\left(\frac{R}{EA_1} + \alpha \Delta T\right)L_1 + \left(\frac{R}{EA_2} + \alpha \Delta T\right)L_2 = 0$$

$$\left(\frac{L_1}{A_1} + \frac{L_2}{A_2}\right) \frac{R}{E} = -(L_1 + L_2) \alpha \Delta T$$

$$R = - \frac{L_1 + L_2}{\frac{L_1}{A_1} + \frac{L_2}{A_2}} \cdot E \alpha \Delta T$$

$$= - \frac{L_1 + L_2}{A_2 L_1 + A_1 L_2} A_1 A_2 E \alpha \Delta T$$

したがって

$$G_1 = \frac{R}{A_1} = - \frac{L_1 + L_2}{A_2 L_1 + A_1 L_2} A_2 E \alpha \Delta T$$

$$G_2 = \frac{R}{A_2} = - \frac{L_1 + L_2}{A_2 L_1 + A_1 L_2} A_1 E \alpha \Delta T$$

それぞれの伸縮は

$$\delta_1 = \left(\frac{R}{EA_1} + \alpha \Delta T\right)L_1 = \left(1 - \frac{L_1 + L_2}{A_2 L_1 + A_1 L_2} A_2\right)L_1 \alpha \Delta T$$

$$\delta_2 = \left(\frac{R}{EA_2} + \alpha \Delta T\right)L_2 = \left(1 - \frac{L_1 + L_2}{A_2 L_1 + A_1 L_2} A_1\right)L_2 \alpha \Delta T$$