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# 修 士 論 文

題目 : **Forced convective heat transfer in cylindrical pipe flows**

専攻                      理工学研究科（修士課程）  
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# Nomenclature

## Physics Constants

$c$	Speed of light in a vacuum inertial system	$299,792,458\text{ m/s}$
$h$	Plank Constant	$6.62607 \times 10^{-34}\text{ Js}$

## Material Properties

$T$	Temperature	$K$
$C_p$	Specific heat capacity	$J \cdot kg^{-1}K^{-1}$
$\lambda$	Thermal conductivity	$Wm^{-1}K^{-1}$
$\mu$	Dynamic viscosity	$Pa \cdot s$
$\rho$	Density	$kg/m^3$
$Pr$	Prandtl number	-

## Other Symbols

$\rho$	Friction Index
$V$	Constant Volume

## 第1章 Introduction

## 1.1 Study background

Forced convective heat transfer lies at the heart of many aspect of cooling technology and it is therefore desirable to understand its properties as well as possible. Effective cooling technology is constantly being required to wide variety of industrial engineering aplication. To achieve effective coolant system requires comprefensive research of heat transfer coefficient with a wide variety of flow condition. Although many reserchers have been focusing on experimental and computational research, heat transfer coefficient vary with Reynolds number is still unclear. To this end, many reserchers have been focusing on heat transfer from experimental and computational research aspect. However, heat transfer in transitional and turbulent flow is still very challenging task for both experimental and computational research.

1. Experimental research

2. Computational research

Direct numerical simuration In technology, flows regime and heat transfer plays an important role in considerting engineering issues. Navie-Stokes equations describe the relation of variable flows.

(1.1)

However, deterministic solution of the equations are only valid for small disturbances in the initial and boundary condition. In physically, it is hard to get initial and boundary conditions in infinite accurate. Turbulent has a large amount of fluctuations, i.e. turbulent is completely different kind of laminar flows. Direct Numerical Simuration (DNS) is one of the simulation way to predict flow forms. The object of the simuration is to solve the compelete set of equation of motion without using any model. From Kolmogorov lenght scale, total number of cumputations is derivered following equation (1.2). The DNS require large amount of total number of computations.

$$\mathcal{N} \times \mathcal{M} = \mathcal{O}(Re^{11/4}) \quad (1.2)$$

The equauation implies the limitation of the DNS and that is directly connected to computer technology. Normally, engineeres is interested in high Reynolds number such as aircraft or atmospheric boundary layer. However, such high Reynolds number requires huge amount of total number of computations and it's far from reality. Large eddy simulation

One attempt to improve our understanding of entanglement is the study of our ability to perform experimental investigation

These coolant technology is used wide variety of coolant applications such as electric devices, automotive, and plant factory. Considering heat transfer issues, heat transfer coefficients are one of the most important numbers. The Nusselt number (Nu) is a dimensionless number which represents the ratio of convective (h) and conductive heat transfer (k), as expressed in Equation.

## 1.2 Previous research

The equation implies the limitation of the DNS and that is directly connected to computer technology. Normally, engineers are interested in high Reynolds number such as aircraft or atmospheric boundary layer. However, such high Reynolds number requires huge amount of total number of computations and it's far from reality.

Therefore, it is necessary to get experimental data for correlations of heat transfer and flow condition and the Reynolds number.

Many studies have pointed out that a heat transfer coefficient varies depending on the type of flow: laminar, transition and turbulent. Gnienlinski[3][5] showed a calculation method about heat transfer coefficients for the laminar, transitional and turbulent flows. Bertsche et al.[1] focused on reliable prediction of the heat transfer coefficient for transitional flows. In their study, they showed experimental the heat transfer coefficients for the Reynolds number,  $500 < Re < 23000$ , and the Prandtl number,  $7 < Pr < 41$ .

However, not so many data is available for experimental data of laminar-to-turbulent transitional region. More studies should be conducted to obtain experimental data for high the Prandtl number and transitional flows. In this study, the author focused on forced convective heat transfer in flow of water and glycole in a cylindrical pipe. A 50/50vol% mixture of water and glycole, which is a typical liquid coolant in automotive applications, was used as an operating fluid. The experiment was carried out by considering a board range of Reynolds numbers, spanning from a laminar to fully turbulent flow. Moreover, the measurements of the wall friction coefficients was also performed in this study.

### 1.2.1 Skin friction coefficients

The skin friction coefficients for laminar flow is described following equation.

$$C_{f,lam} = \frac{16}{Re_b} \quad (1.3)$$

Konakov[4] showed the skin friction coefficients for turbulent flow.

$$C_{f,turb} = 0.25(1.8\log(Re_b) - 1.64)^{-2} \quad (1.4)$$

### 1.2.2 The heat transfer coefficients

Gunienski [2] showed correlations for each flow conditions: laminar, transitional and turbulent, respectively. Gunienski [2] showed calculation method for laminar flow.

$$Nu_{lam} = (3.66^3 + 0.7^3 + (1.615(Re_b Pr_b \frac{d_i}{L})^{1/3})^3)^{1/3} \quad (1.5)$$

He showed calculation method for turbulent flow.

$$Nu_{turb} = \frac{\frac{C_{f,turb}}{2Re \cdot Pr_b}}{1 + 12.7\sqrt{\frac{C_{f,turb}}{2}}(Pr_b^{2/3} - 1)} \cdot (\frac{Pr_b}{Pr_w})^{0.11} \quad (1.6)$$

The range is

$$0.1 \ll Pr_b \ll 1000, 10^4 \ll Re_b \ll 10^6 \quad (1.7)$$

He presented transitional flow as a liner interpolation between turbulent and laminar flow.

$$Nu_m = (1 - r)Nu_{m,lam} + rNu_{m,turb} \quad (1.8)$$

$$r = \frac{Re_b - 2300}{10^4 - 2300} \quad (1.9)$$



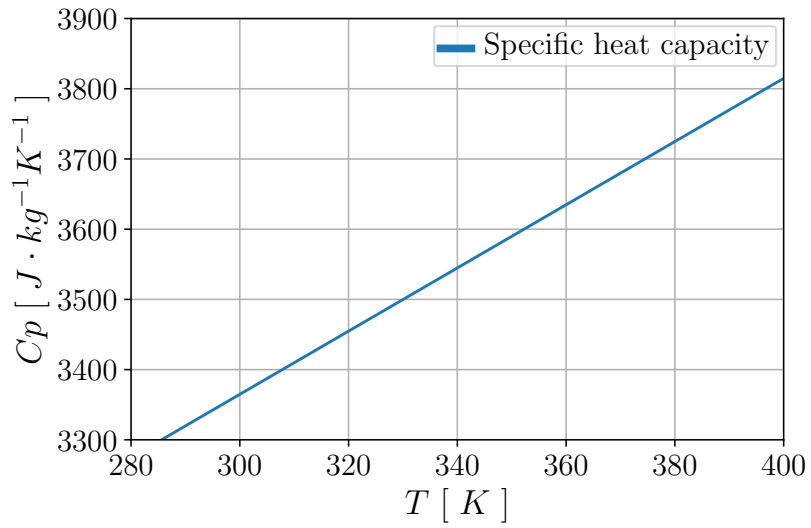
## 第2章 Methodology

## 2.1 Material properties

A 50/50vol% mixture of water and glycole which is a typical liquid coolant in automotive applications were used as a operating fluid. The material properties of the operationg fluid is temperature dependency. As bigger temperature difference between a pipe wall and the bulk, the material properties pronounced.

specific heat capacity

$$c_p = A_{c_p} + B_{c_p}T = 2.0148 + 4.50E - 3T \quad (2.1)$$



☒ 2.1: Specific heat capacity vary with temperature

thermal conductivity

$$\lambda = A_{\lambda} + B_{\lambda}T = 0.2134 + 6.071E - 4T \quad (2.2)$$

dynamic viscosity

$$\mu = A_{\mu} \cdot \exp\left(\frac{B_{\mu}}{T + C_{\mu}}\right) = 1.1001E - 4 \exp\left(\frac{325.85}{T - 207.30}\right) \quad (2.3)$$

density

$$\rho = A_{\rho} + B_{\rho}T = 1268.28 - 0.66T \quad (2.4)$$

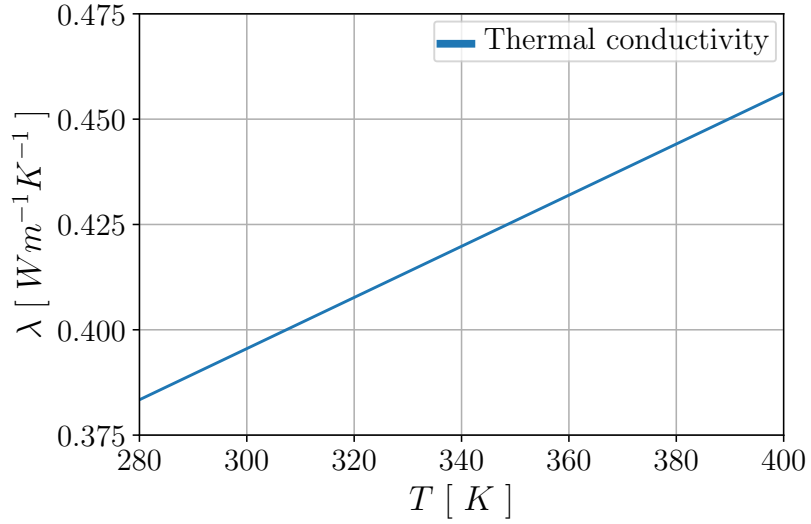


Fig 2.2: Thermal conductivity vary with temperature

prandtl number

$$Pr = \frac{\nu}{\alpha} = \frac{\mu \cdot c_p}{\lambda} \quad (2.5)$$

### 2.1.1 Effect of viscosity and density

Effect of viscosity 20% Effect of density 0.5%

### 2.1.2 Cooling and heating

Bertsche et al.[1] shows experimental investigation on heat transfer in cylindrical pipe flow by using a 50/50vol% mixture of water and glycole with cooling. The operationg fluid is the same as our study, however they measured the heat transfer by cooling the liquid. For cooling the liquid, the temperature at the wall is lower than bulk temperature. In other way, for heating the liquid, the temperature at the wall is higher that bulk temperature. As shown in material properties, the viscosity show strong temperature dependence and the curve isn't linear function. Thus, the heat transfer doesn't shows the same value with cooling and heating even though a Prandtl number is the same.

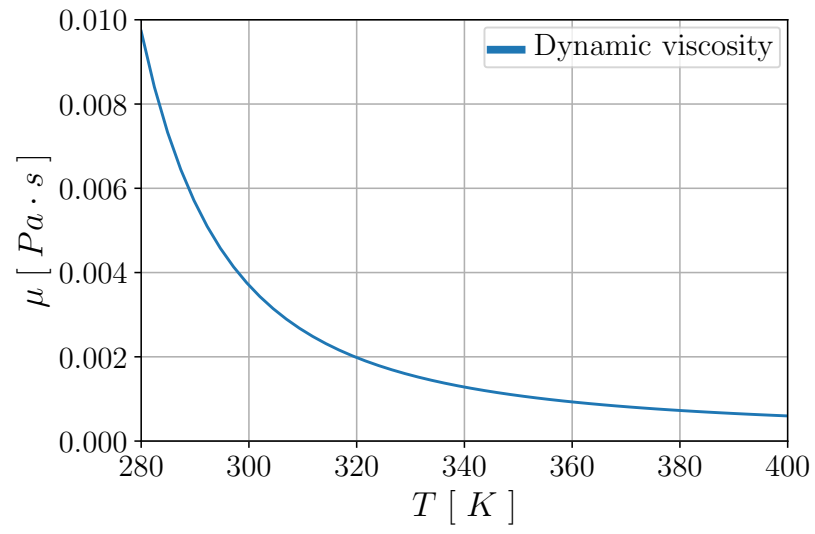


図 2.3: Dynamic viscosity vary with temperature

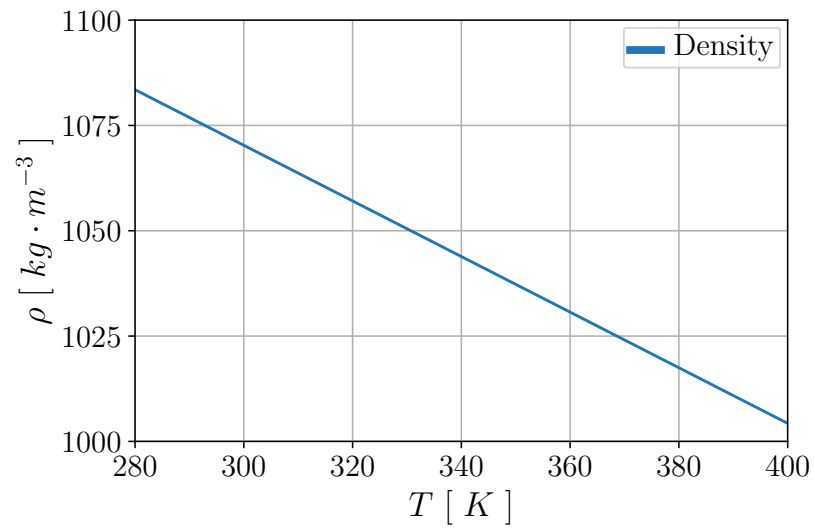


図 2.4: Density vary with temperature

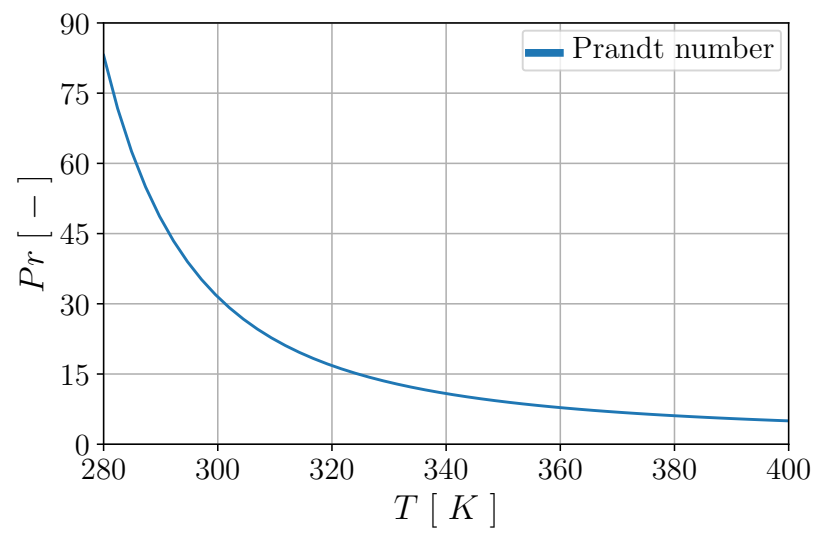


図 2.5: Prandtl number vary with temperature

## 2.2 Hydro and thermal boundary layer

## 第3章 Experimental facilities

- 3.1 Experimental loop**
- 3.2 Test section**
- 3.3 Wall temperature distribution**
- 3.4 Evaluation procedure**
- 3.5 Measurement Uncertainty**



## 第4章 Experiments

## 4.1 Validity of Experimental and evaluation procedure

## 4.2 Experimental result and variation

### 4.2.1 Validation of experimental result for $Pr_w = 7$

### 4.2.2 Validation of experimental result for $Pr_w = 10$

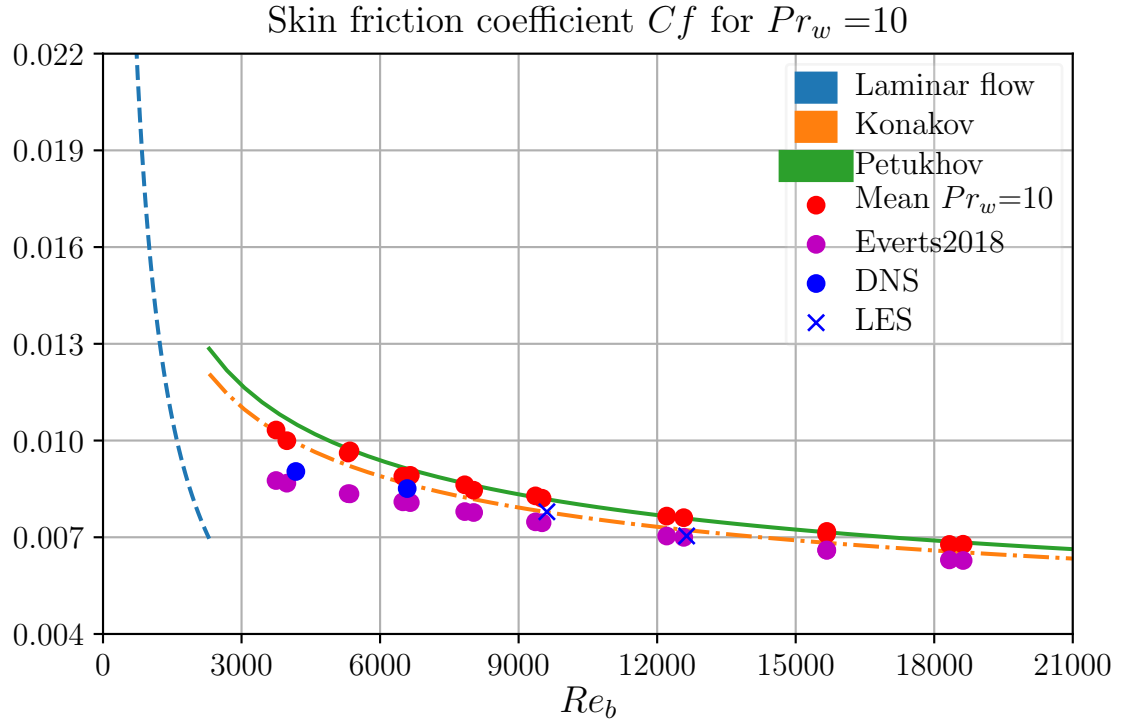


図 4.1: The comparison between skin friction coefficient  $C_f$  and bulk Reynolds number  $Re_b$  for  $Pr_w = 10$

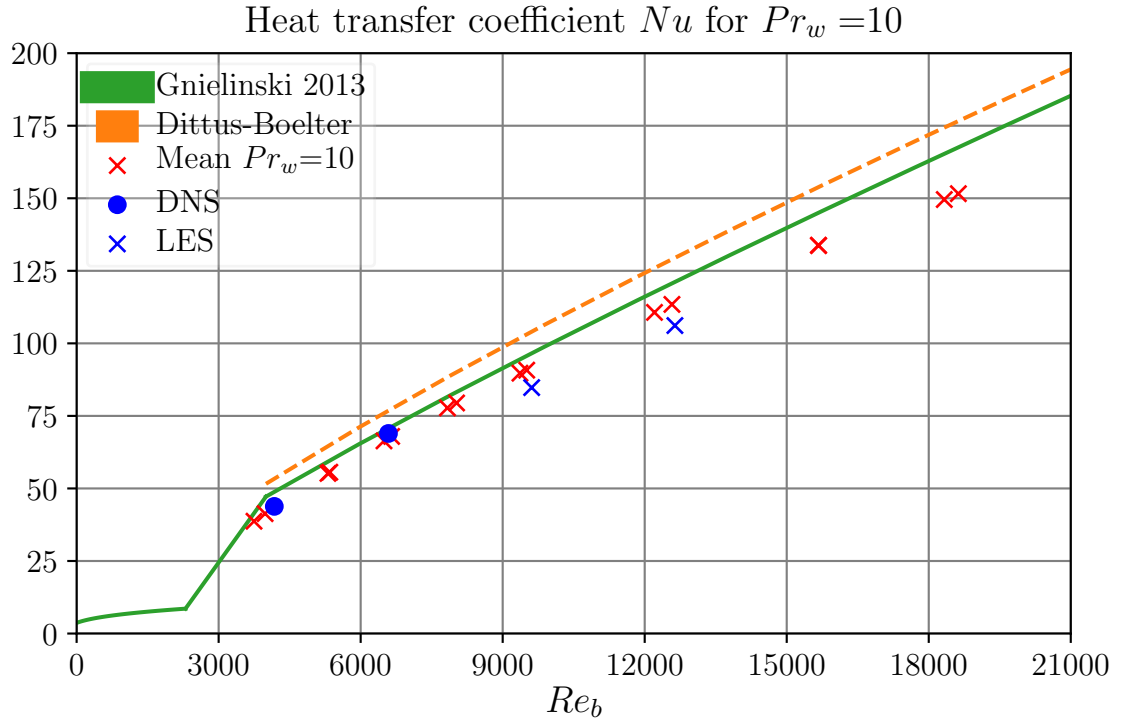


Figure 4.2: The comparison between heat transfer coefficient  $Nu$  and bulk Reynolds number  $Re_b$  for  $Pr_w = 10$

#### 4.2.3 Validation of experimental result for $Pr_w = 13$

#### 4.2.4 Validation of experimental result for $Pr_w = 13$

### 4.3 Discussion

#### 4.3.1 Reproducibility

#### 4.3.2 Secondary flow

#### 4.3.3 Influence of heat flux

#### 4.3.4 Scattering and probability density function

#### 4.3.5 Comparison with Bertsche

#### 4.3.6 Comparison with DNS and LES

#### 4.3.7 Effect of the pressure power

#### 4.3.8 Effect of material properties

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#### 4.3.9

表 4.1: Summary of the experimental parameters for  $Pr_w = 10$  and performance of the skin friction coefficient  $C_f$ , Nusselt number  $Nu$ .

$Pr_w$	$Re_b$	$C_f$	$Nu$	$T_w$ [ $^{\circ}C$ ]	$T_b$ [ $^{\circ}C$ ]	$\Delta T$ [ $^{\circ}C$ ]	$q_{el}$ [ $kW/m^2$ ]	$q_{hc}$ [ $kW/m^2$ ]
10.0	3981	0.00999	41.3	71.4	67.8	3.6	6.8	5.3
10.1	4047	0.00988	42.2	70.8	66.9	3.9	7.4	5.8
9.9	4128	0.00983	42.9	71.6	67.2	4.4	8.2	6.6
10.0	3981	0.00999	41.3	71.4	67.8	3.6	6.8	5.3
10.1	4047	0.00988	42.2	70.8	66.9	3.9	7.4	5.8
9.9	4128	0.00983	42.9	71.6	67.2	4.4	8.2	6.6
10.0	3981	0.00999	41.3	71.4	67.8	3.6	6.8	5.3
10.1	4047	0.00988	42.2	70.8	66.9	3.9	7.4	5.8

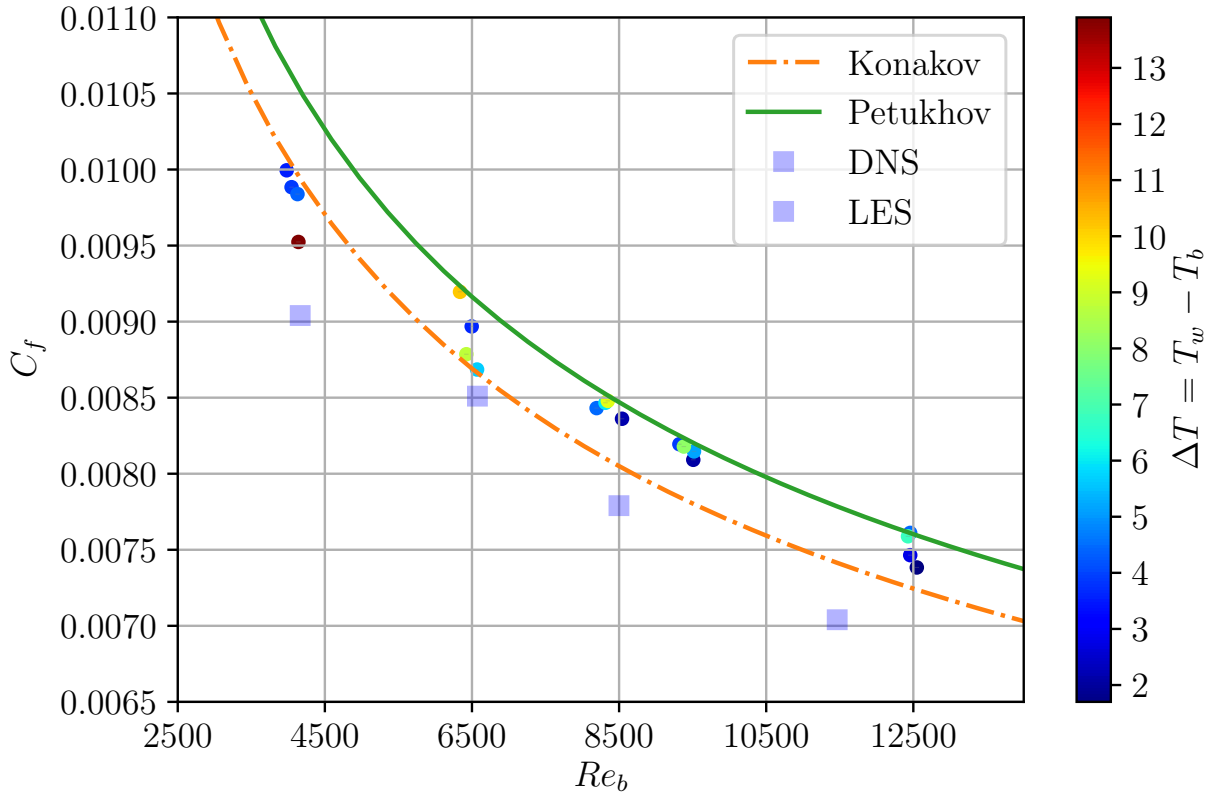


図 4.3: The comparison between skin friction coefficient  $C_f$  and bulk Reynolds number  $Re_b$  for  $Pr_w = 10$  vary with temperature difference  $\Delta T$  between a pipe wall  $T_w$  and the bulk  $T_b$ .

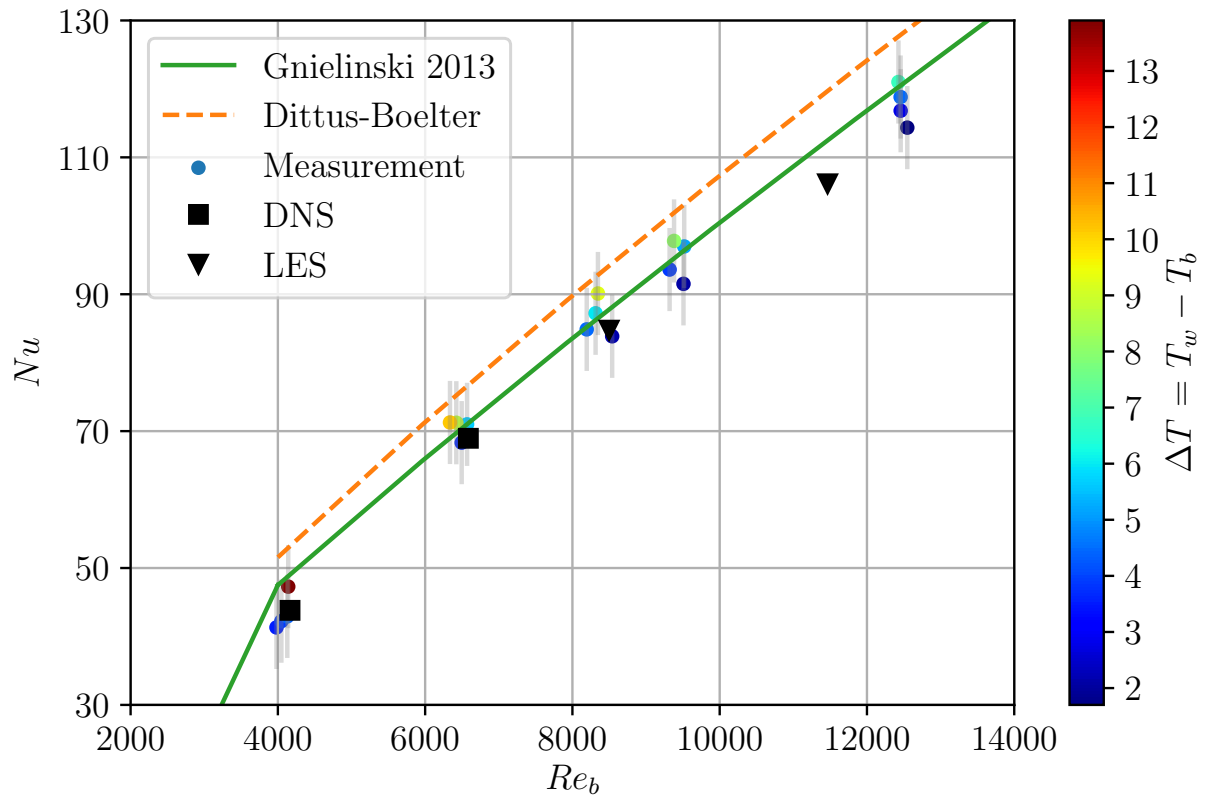


図 4.4: The comparison between heat transfer coefficient  $Nu$  and bulk Reynolds number  $Re_b$  for  $Pr_w = 10$  vary with temperature difference  $\Delta T$  between a pipe wall  $T_w$  and the bulk  $T_b$ .

表 4.2: Summary of the experimental parameters for  $Pr_w = 10$  and performance of the skin friction coefficient  $C_f$ , Nusselt number  $Nu$  and temperature defference  $\Delta T = T_w - T_b$ .

$Pr_w$	$Re_b$	$C_f$	$Nu$	$T_w$ [ $^{\circ}C$ ]	$T_b$ [ $^{\circ}C$ ]	$\Delta T$ [ $^{\circ}C$ ]	$q_{el}$ [ $kW/m^2$ ]	$q_{hc}$ [ $kW/m^2$ ]
10.0	3981	0.00999	41.3	71.4	67.8	3.6	6.8	5.3
10.1	4047	0.00988	42.2	70.8	66.9	3.9	7.4	5.8
9.9	4128	0.00983	42.9	71.6	67.2	4.4	8.2	6.6
9.9	4141	0.00952	47.3	71.8	57.9	14.0	26.7	23.1
10.0	6496	0.00897	68.3	71.5	67.8	3.7	11.1	8.9
10.0	6569	0.00869	71.0	71.3	65.6	5.7	16.8	14.1
9.9	6423	0.00879	71.2	71.5	62.8	8.8	25.7	22.0
10.0	6337	0.00920	71.3	71.4	61.1	10.2	30.0	25.6
10.0	8540	0.00836	83.9	71.5	69.2	2.2	8.7	6.6
10.0	8194	0.00843	84.9	71.4	66.9	4.5	16.3	13.4
10.0	8315	0.00847	87.2	71.4	65.4	6.0	21.9	18.5
10.0	8347	0.00848	90.1	71.4	62.1	9.3	34.1	29.6
9.9	9508	0.00809	91.5	71.5	69.5	2.1	8.8	6.6
10.0	9320	0.00819	93.6	71.4	67.5	3.9	15.6	12.8
10.0	9518	0.00815	97.0	71.3	66.1	5.2	21.2	17.8
9.9	9380	0.00818	97.8	71.7	63.6	8.1	32.4	27.8
10.0								
10.0								
10.0								
10.0								
10.0	12548	0.00738	114.3	71.4	69.7	1.7	8.9	6.7
10.0	12458	0.00746	116.8	71.4	68.6	2.8	14.6	11.7
9.9	12457	0.00761	118.8	71.6	67.1	4.5	22.6	19.0
9.9	12427	0.00759	121.0	71.6	64.7	6.8	33.6	29.1

表 4.3: Direct Numerical Simuration (DNS) and Large Eggy Simuration (LES) for  $Pr_w = 10$  vary with heat flux  $q_w = 20 [kW/m^2]$  and  $q_w = ? [kW/m^2]$

Type	$Pr_w$	$Re_\tau$	$Re_b$	$C_f$	$Nu$	$T_w [^\circ C]$	$T_b [^\circ C]$	$\Delta T [^\circ C]$	$q_w [kW/m^2]$
DNS	10.0	360	4165	0.00904	43.8	71.2	58.5	13.1	20.0
DNS	10.0	360	4165	?	?	71.2	?	?	40.0
DNS	10.0	500	6587	0.00851	69.0	71.2	63.3	8.3	20.0
DNS	10.0	500	6587	?	?	71.2	?	?	40.0
LES	10.0	600	8498	0.00779	84.8	71.2	64.8	6.8	20.0
LES	10.0	750	11465	0.00704	106.1	71.2	66.2	5.4	20.0

## 第5章 Conclusion



## 付 録A    Material properties

A 50/50vol% mixture of water and glycole which is a typical liquid coolant in automotive applications were used as a operating fluid.

## 付 録B    Post processing

[24]

# References

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