

# Experimental investigation of forced convective heat transfer in cylindrical pipe flow

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## I. INTRODUCTION

Forced convective heat transfer in cylindrical pipe flow plays an important role in many technical cooling systems. These coolant technology is used wide variety of coolant applications such as electric devices, automotive, and plant factory. Considering heat transfer issues, heat transfer coefficient is one of the most important numbers.

Much remains to be studied for providing experimental data for high Prandtl number and laminar-to-turbulent transitional regime. In this paper, we focus on forced convective heat transfer in cylindrical pipe flow in particular high Prandtl number and transitional regime. A 50/50vol% mixture of water and glycole which is a typical liquid coolant in automotive applications were used as a operating fluid. This coolant liquid is normally used in low temperature. However, it's difficult to maintain the cylindrical pipe at low temperature. Therefore, as a 1st approach, we take a data for high temperature and then compared with Direct Numerical Simulation (DNS). If there is a good agreement between experimental data for high temperature and DNS, the result in a low temperature would be predicted by DNS. Moreover, the investigation shall also include the measurement of wall friction coefficient. The engineer is frequently interested in pressure drop which is related to determine pump or fan power equipments.

## II. THE PHENOMENA

Figure shows experimental setup which is already existing facilities by Christphan [?]. The experimental loop consists of heat exchanger, pump, coriolis mass flow rate, welder, reservoir, and test section basically. Heat exchanger keep thermal stationary condition in flow pipe. Mass flow rate is controlled by pump and bypass valve C which is located in a parallel. The pipe is thermal isolated, surrounded with glass wool.

Figure shows velocity and thermal boundary layer development vary with horizontal axis in a test section. Velocity and thermal profile are shown blue and red color, respectively. The test section is made of stainless steel (1.4301) with an inner diameter  $d_i=12\text{mm}$  and outer diameter  $d_o=15\text{mm}$ . Highly accurate resistance thermall probes (PT-100) are used to find

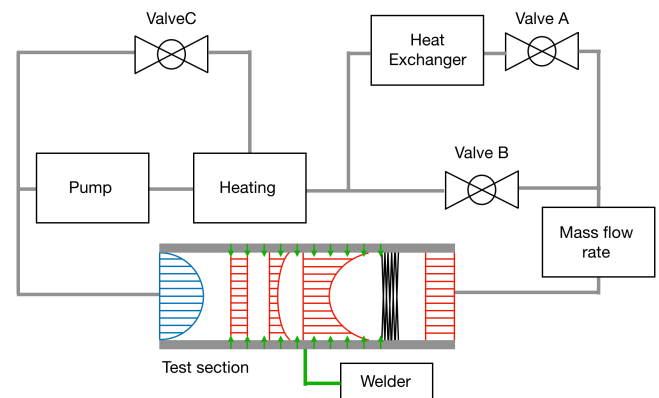


Fig. 1. Experimental loop.

out the inlet and outlet bulk temperature ( $T_{ib}$ ,  $T_{ob}$ ) and wall temperature  $T_w$ . Moreover, thermocouple 'Type-K' are used to take temperature gradient in flow direction. (See "science problems and interesting issue" section No.3.) However, those thermocouples aren't directly related to calculate four parameters. ( $Re$ ,  $Nu$ ,  $Pr$ ,  $C_f$ ) The test section consist of entrance, heated and thermal equalized part.

### 1) Entrance part

The first part of test section is 1.2[m] length entrance part which is sufficiently long to ensure dynamically developed flow condition at the exist. (See "science problems and interesting issue" section No.4.) The bulk temperature ( $T_{b0}$ ) at this section were measured by PT-100.

### 2) Heated part

The second part of test section is 2[m] length heated part which is sufficiently long to ensure thermal fully developed flow condition at the exist. The tube wall were heated electrically by welder which provide high current and low voltage to keep the uniform heat flux condition in a inner pipe flow. Convective heat transfer is independent with horizontal axis in fully developed flow, constant heat flux condition. The wall temperature ( $T_w$ ) at the exist of this section were measured by PT-100.

### 3) Thermal equalized part

The third part of test section is thermal equalized part which is including static mixture. Static mixture forms turbulent and vortex. Then, the thermal profile of heated exist mix together. At the end, the bulk temperature ( $T_{b1}$ ) are measured.

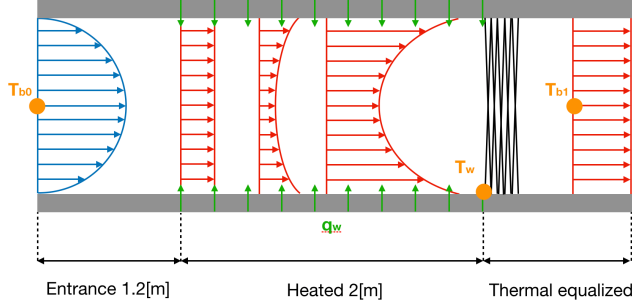


Fig. 2. Velocity (blue) and thermal (red) boundary layer development vary with horizontal axis in a test section.

There are 3 ways to control Re and Pr, the value which we need. It is hard to keep high Pr and low Re. Figure 3-8 shows material properties of Shell Heat Transfer Oil S2.

1) Cooling water

As opening valve A and closing valve B, decreasing flow temperature. Then, viscosity increase and Re decrease and Pr increase.

2) Bypass pipe

As opening bypass pipe C, decreasing mass flow rate then, Re decrease. As decreasing mass flow rate, Pr decrease because the number is related to heat transfer convection from the wall. (Heat is provided from the wall.) In order to decrease mass flow rate, controlling bypass pipe is stronger than pump machine.

3) Welder and mass pump machine

As decreasing mass flow rate (pump machine) and welder, Re decrease and Pr is kept nearly constant. Pr is proposonal to Nu which is, convection divided by conduction. Controlling both welder and mass flow rate, the ratio is maintained constant value.

Those method are in a unquantative way. (See "science problems and interesting issue" section No.1.2.)

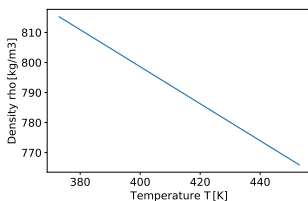


Fig. 3. Density rho, kg/m³

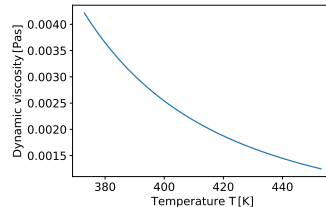


Fig. 4. Dynamic viscosity mu, Pas

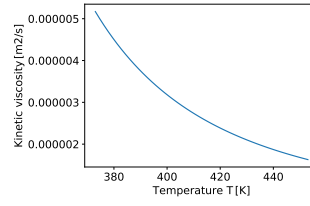


Fig. 5. Kinetic viscosity nu, m²/s

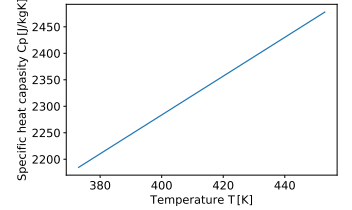


Fig. 6. Heat capacity Cp, J/kgK

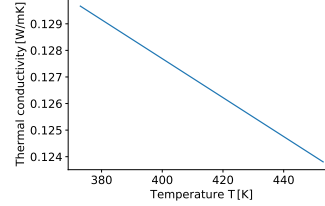


Fig. 7. Thermal conductivity, W/mk

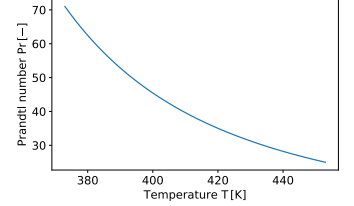


Fig. 8. Prandtl number Pr, -

### III. CALUCURATION FLOW

Material properties are temperature-dependent function. At first, material properties vary with temperature are taken. Next, we move to experimental facilities and measure temperature difference, pressure difference and mass flow rate. Finally, Nusselt, Prandtl, Reynolds numbers and friction coefficient are calculated by post-proccesing, MATLAB. In order to discuss the issue, experimental data are compared with next correlations.

### IV. CORRELATIONS

Skin friction coefficient for laminar flow is described following equation.

$$C_{f,lam} = \frac{16}{Re_b} \quad (1)$$

Konakov [?] showed skin friction coefficient for turbulent flow.

$$C_{f,turb} = 0.25(1.8 \log(Re_b) - 1.5)^{-2} \quad (2)$$

Note that these skin friction coefficient just suitable for no-heating condition, constant fluid properties. In this thesis, we provide heat to the pipe. Therefore, the fluid properties change depend on the temperature.

From general dimensional analysis, Nusselt number represents function of Reynolds number (Re) times Prandtl number (Pr) as following equation.

$$Nu = \alpha \cdot Re^{\pi\beta} \cdot Pr^{\pi\gamma} \quad (3)$$

Here, factors  $\alpha$ ,  $\beta$  and  $\gamma$  are constant value depend on flow regime and calculated from numerical experimental results. Gunienski [?] showed correlations for each flow regime laminar and turbulent, respectively. Gunienski [?] showed calculation method for laminar flow.

$$Nu_{lam} = (3.66^3 + 0.7^3 + (1.615(Re_b Pr_b \frac{d_i}{L})^{1/3})^3)^{1/3} \quad (4)$$

Gunienski [?] showed calculation method for turbulent flow.

$$Nu_{turb} = \frac{\frac{C_f}{2Re_b Pr_b}}{1 + 12.7 \sqrt{\frac{C_f}{2}} (Pr_b^{2/3} - 1)} \cdot \left(\frac{Pr_b}{Pr_w}\right)^{0.11} \quad (5)$$

The range is

$$0.1 \ll Pr_b \ll 1000, 10^4 \ll Re_b \ll 10^6. \quad (6)$$

He presented transitional flow as a liner interpolation between turbulent and laminar flow. (See "science problems and interesting issue" section No.12.)

$$Nu_m = (1 - r)Nu_{m,lam} + rNu_{m,turb} \quad (7)$$

$$r = \frac{Re_b - 2300}{10^4 - 2300} \quad (8)$$

## V. STATE-OF-THE-ART

The presentally considered oil is Shell Heat Transfer oil S2. The result show good agreement with correlations. We are going to use water-glycole as a operating liquid.

## VI. SCIENTIFIC PROBLEMS AND INTERESTS ISSUES

### 1) Quantative way

There are 3 valves, A, B and C in the experimental loop. The experimental condition Re and Pr are controlled by those 3 valves, pump and welder. The pump and welder can control in a quantative way. However, those 3 valves are controlled by human hand and those are no certain value. In this report, that's the reason why I just say INCREASE or DECREASE, unquantative way. Therefore, to contolle 3 valves in a quantative way are needed.

### 2) Fluid properties

Density, heat conductivity, specific heat transfer Cp, nu, mu, Pr are all varies with temperature shown as temperature dependance in figures 3-8. of fluid properties. It is difficult to reach high Prandtl number and transitional Reynolds number, which we really want. For example, as enhance cooling, temperature decrease, statics viscosity increase. As a result, Pr increase and Re decrease. There are 3 ways to contolle Pr and Re shown in "Experimental loop and Method" section. Pr and Re are related each other and it is difficult to maintain the value that we want to measure. This problem is related mere close to "quantative way" shown above. Therefore, we need to find solution which is able to reach the value in an optimal way, not rule-of-thumb.

### 3) Temperature calibration

There are two kinds of temperature measurement, PT-100 and thermocouples. Thermocouples are calibrated by PT-100 because PT-100 is more accurate than thermocouples. Here, there is a interesting issue. When we calibrate, thermocouples temperature of initial condition are always lower than PT-100. Figure.9 shows monitored thermocouples and PT-100 before calibration.

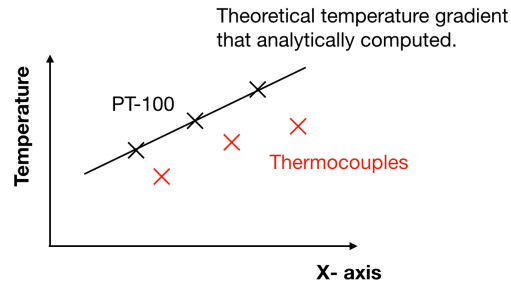


Fig. 9. Thermocouples are always located under PT-100 before temperature calibration

### 4) Fully developed length

In figure.2., the length of entrance part in the test-section is 1.2 [m]. To check the length of fully developed flow vary with Reynolds number wheather if there is a limitation of flow speed to do a experiment, or not.

### 5) Three parameters (Nu, Re, Pr)

Experimental data and correlations is compared. In a correlation, the Prandtl number is constant. However, experimental Prandtl number is not constant because the fluid properties vary with temperature. The aim is to set Prandtl number level and vary the Reynolds number. There are only two parameters can be descired on figures. The only choice is to take average Prandtl number and plot Nusselt and Reynolds number. Figure.10 shows only two parameter which are available to plot 2-D figures.

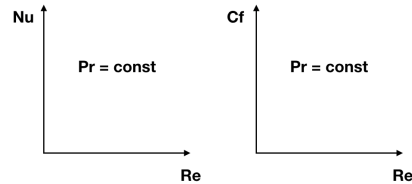


Fig. 10. Only two parameters "Nu and Re" and "Cf and Re" can be descired in figures.

### 6) The influence of enthalpy, changing with pump power

If we change pump power, not only flow speed but also heat transfer and enthalpy change. For example, as increasing pump power, increasing flow speed and decreasing Prandtl number vary with heat transfer rate. Calculating enthalpy, it would be easir to take Prandtl and Reynolds number which we wanted. Figure.11 shows many factors related in increasing pump.

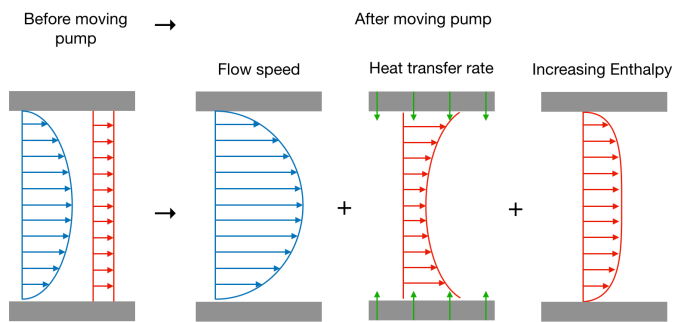


Fig. 11. Changing pump speed, vary with flow speed, heat transfer rate and enthalpy.

#### 7) Thermal contact resistant

To avoid any influence of electronic current used for heating pipe, temperature sensors are electronically isolated against stainless pipe in heated test-section. Calculating any influence of thermal contact resistant between those two materials.

#### 8) Property of operating liquid dependence with long period of time

It is unrealistic to change an operating liquid every experiments because it cost a lot and takes time. We need to use the same test liquid for long period of time. The fluid properties are taken at the beginning only one time. Fluid properties are really important issue in this research. Therefore, I want to search about fluid properties dependence on time.

#### 9) Low temperature cooling

In the heated part, the tube wall are heated electrically by welder. It is easy to make constant heat flux condition at high temperature. However, not so many ideas are available to maintain the 1[m] pipe low temperature.

#### 10) Applying turbulent intensity

#### 11) Applying Knudsen number

#### 12) Gnienski correlation

Gnienski showed transitional flow as a linear interpolation between turbulent and laminar flow. Propose in case of non-linear correspond.

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