

* Dsp project :

IIR Filter : lowpass filter by Butterworth

instead we would use matlab built in func.

① First we get The function in S-domain and Then apply impulse invariance method

Butterworth

↓
impulse invariance

We need

$\omega_p \rightarrow$ passband edge freq.

$\omega_s \rightarrow$ Stopband edge frequency

$A_{max} \rightarrow$ Maximum allowable attenuation in passband

$A_{min} \rightarrow$ minimum allowable attenuation in Stopband

①

① Using rectangular window:

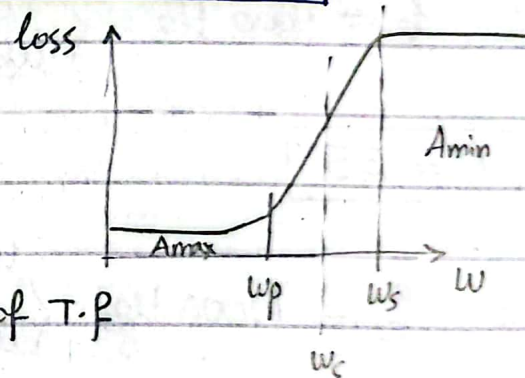
$$A_{max} = 0.7 \text{ dB} \quad A_{min} = 21 \text{ dB}$$

at $f_c = 2000 \text{ Hz}$

$$\therefore \omega_c = 2000 \times 2\pi \text{ rad/s}$$

$$\therefore \omega_p = 1500 \times 2\pi \text{ rad/s}$$

$$\therefore \omega_s = 2500 \times 2\pi \text{ rad/s}$$



$$n = \frac{\log \sqrt{\frac{10^{0.1 A_{min}}}{10^{0.1 A_{max}}}}}{\log \frac{\omega_s}{\omega_p}} = 6.4317 \approx \underline{\underline{7}} \text{ order of T.F.}$$

at $f_c = 4000 \text{ Hz}$

$$\omega_p = 3500 \times 2\pi \text{ rad/s}$$

$$\omega_s = 4500 \times 2\pi \text{ rad/s}$$

$n = 13 \rightarrow$ Not efficient

at $f_c = 10000 \text{ Hz}$

$$\omega_p = 9500 \times 2\pi \text{ rad/s}$$

$$\omega_s = 10500 \times 2\pi \text{ rad/s}$$

$n = 32 \rightarrow$ Not efficient

② Hamming window, $A_{\max} = 0.0194 \text{ dB}$ $A_{\min} = 53 \text{ dB}$

$$\text{at } f_c = 2000 \text{ Hz} \quad n = \frac{\log \left(\sqrt{\frac{10^{0.1 A_{\min}} - 1}{10^{0.1 A_{\max}} - 1}} \right)}{\log \left(\frac{\omega_s}{\omega_p} \right)}$$

$$\omega_s = 2500 \times 2\pi \text{ rad/sec} \quad \omega_p = 1500 \times 2\pi \text{ rad/sec}$$

$$\boxed{n = 17.2}$$

$$\text{at } f_c = 4000 \text{ Hz} \quad \begin{cases} \omega_p = 3500 \times 2\pi \text{ rad/sec} \\ \omega_s = 4500 \times 2\pi \text{ rad/sec} \end{cases}$$

$$\boxed{n = 35}$$

$$\text{at } f_c = 10000 \text{ Hz} \quad \begin{cases} \omega_p = 9500 \times 2\pi \text{ rad/sec} \\ \omega_s = 10500 \times 2\pi \text{ rad/sec} \end{cases} \quad \boxed{n = 87.98} \Rightarrow 88$$

③ Blackman $A_{\max} = 0.0017 \text{ dB}$ $A_{\min} = 74 \text{ dB}$

$$\text{at } f_c = 2000 \text{ Hz} \quad \underline{n = 25}$$

$$\text{at } f_c = 4000 \text{ Hz} \quad \underline{n = 50}$$

$$\text{at } f_c = 10000 \text{ Hz} \quad \boxed{n = 124.319}$$

The design of These orders will be very complex

as we have seen The order is very high that's because of the narrow transition region we might want to increase the transition region a bit

We will choose arbitrary values for w_p, w_s

① Rectangular window:

$$\text{at } f_c = 2000 \text{ Hz} \quad \begin{cases} w_p = 1800 \times 2\pi \text{ rad/s} \\ w_s = 3500 \times 2\pi \text{ rad/s} \end{cases} \quad n = 5$$

$$\text{at } f_c = 4000 \text{ Hz} \quad \begin{cases} w_p = 3800 \times 2\pi \text{ rad/s} \\ w_s = 5500 \times 2\pi \text{ rad/s} \end{cases} \quad n = 9$$

$$\text{at } f_c = 10000 \text{ Hz} \quad \begin{cases} w_p = 9800 \times 2\pi \text{ rad/s} \\ w_s = 11500 \times 2\pi \text{ rad/s} \end{cases} \quad n = 201$$

$$\begin{aligned} \text{② Hamming} \quad & \text{at } f_c = 2000 \text{ Hz} \quad n = 8 \\ & \text{at } f_c = 4000 \text{ Hz} \quad n = 15 \\ & \text{at } f_c = 10000 \text{ Hz} \quad n = 32 \end{aligned}$$

$$f_p = f_c - 500 ;$$

$$f_s = f_c + 2500 ;$$

$$\text{③ Blackman,} \quad \text{at } f_c = 2000 \text{ Hz} \quad n = 12$$

$$\text{at } f_c = 4000 \text{ Hz} \quad n = 21$$

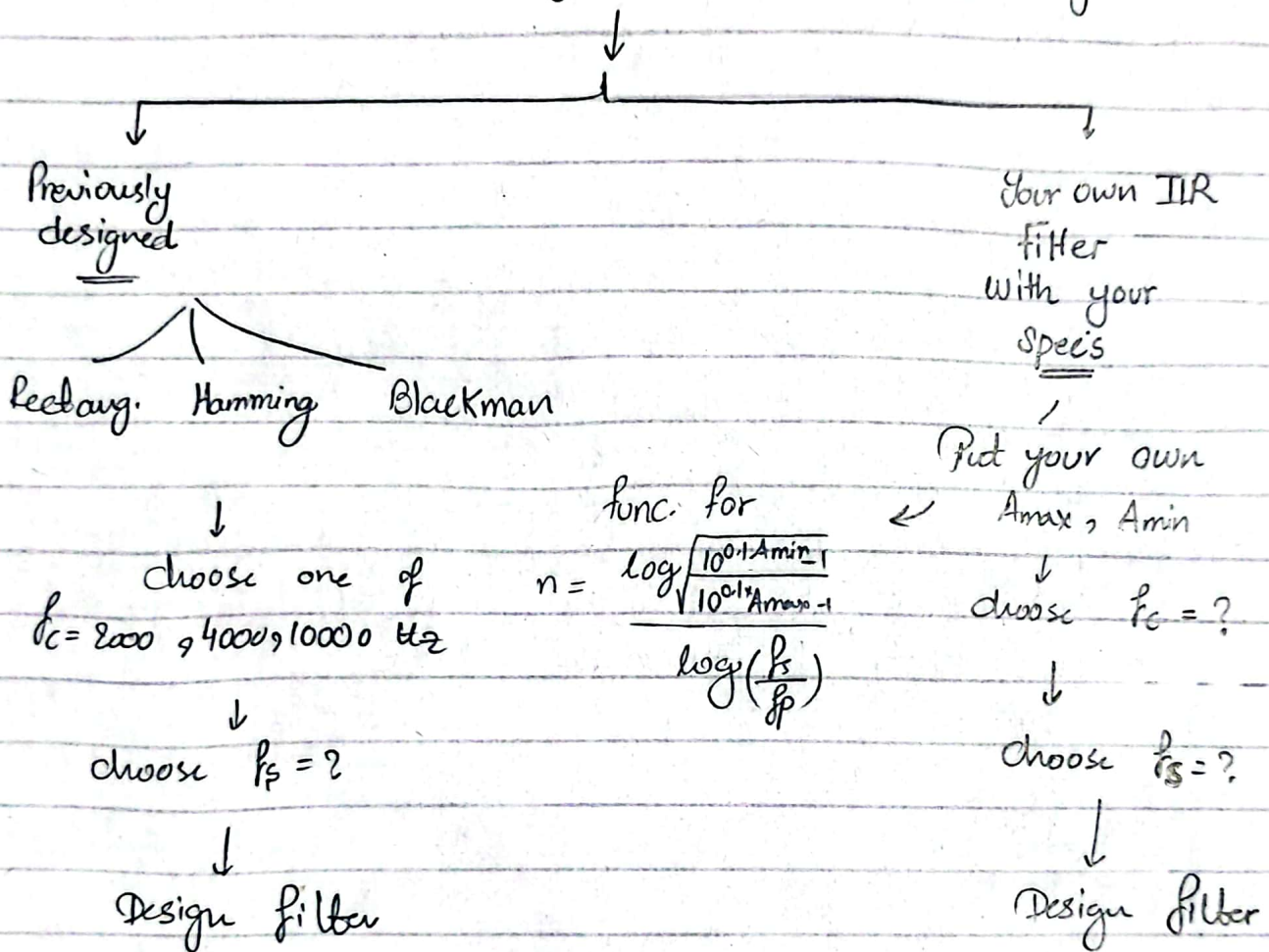
$$\text{at } f_c = 10000 \text{ Hz} \quad n = 467$$

$$f_p = f_c - 500 ;$$

$$f_s = f_c + 2500 ;$$

Program Design IIR

* We Saw That to achieve The low transition region with max. , and min attenuation required by the windows it would take us a large func. with many (high order)



func. for

$$n = \frac{\log \sqrt{\frac{10^{0.1 A_{min}} - 1}{10^{0.1 A_{max}} - 1}}}{\log \left(\frac{f_s}{f_p} \right)}$$

Plot filter

Plot Previous and after \Rightarrow sound

compare both