



Testing Techniques

# Classical Test Design Techniques

*Jan Tretmans*

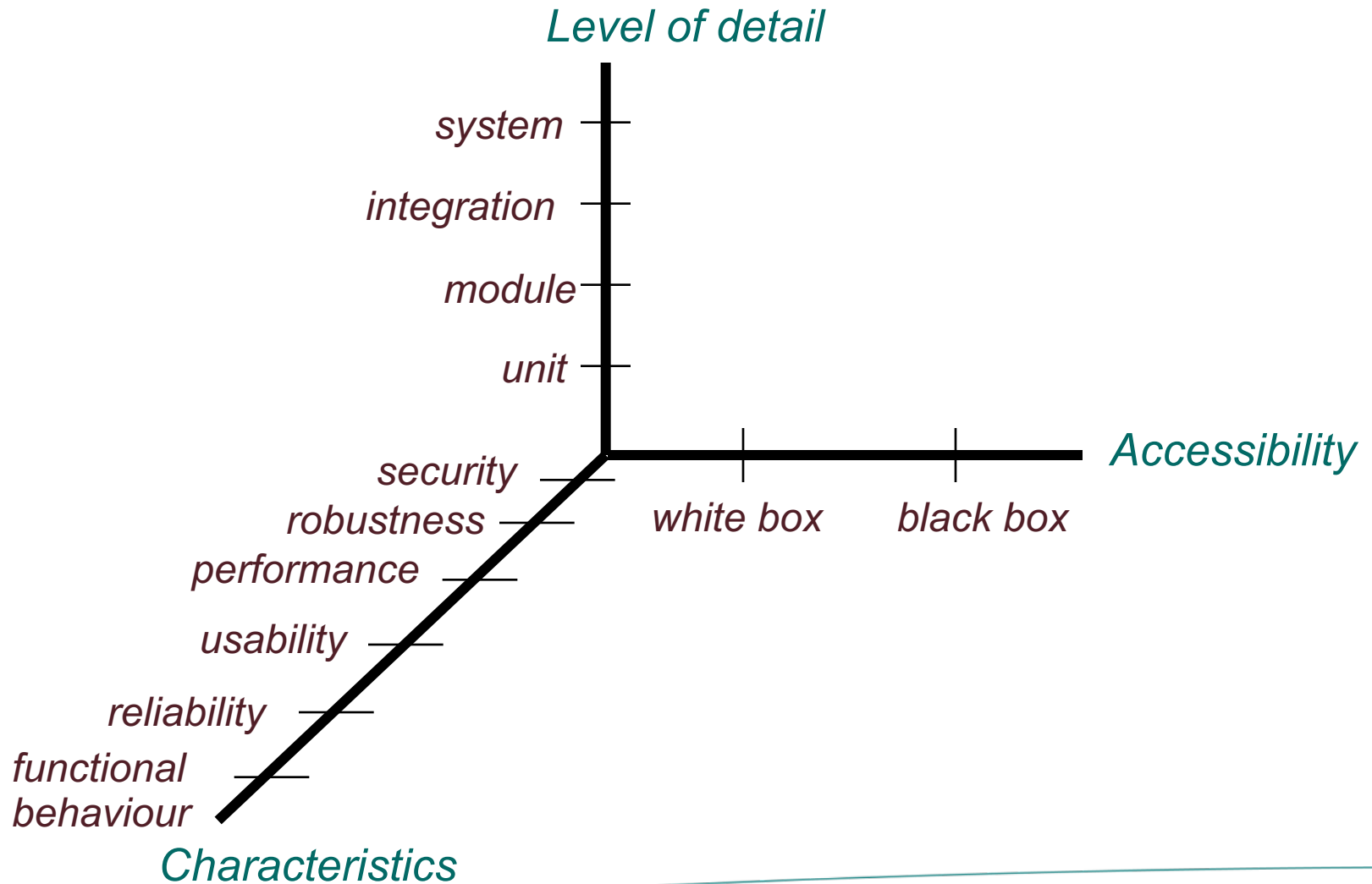
TNO – ESI  
Radboud University Nijmegen



# Some 'Classical' Test Design Techniques

- Black-box testing ( *functional testing* )
  - Equivalence partitioning
  - Boundary value analysis
  - Error guessing
- White-box testing ( *structural testing* )
  - Statement coverage
  - Decision / branch coverage
- Black-box and white-box test case design in combination
- Basics : heuristics and experience

# Types of Testing



# Development of Test Cases

Complete testing is in general impossible



Testing cannot guarantee the absence of faults



How to select subset of test cases from all possible test cases with a high chance of detecting most faults ?



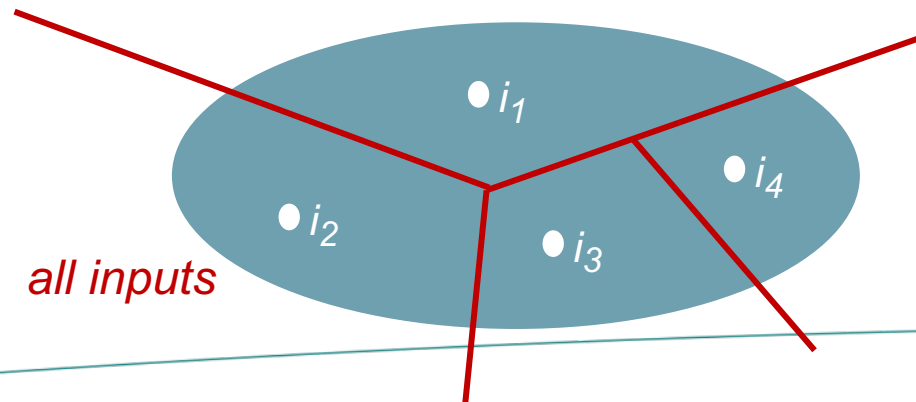
Test Case Design Strategies

Because : *if we have good test suite then we can have more confidence in the product that passes that test suite*

# Black-Box Testing : Equivalence Partitioning ( EP )

Divide all possible inputs into classes (partitions) such that :

- There is a finite number of input equivalence classes
- You may reasonably assume that
  - the program behaves analogously for inputs in the same class
  - one test with a representative value from a class is sufficient
  - if the representative detects a fault then other class members would detect the same fault



# Black-Box Testing : Equivalence Partitioning

## Strategy :

- Identify input equivalence classes
  - Based on conditions on inputs/outputs in specification/description
  - Both valid and invalid input equivalence classes
  - Based on heuristics and experience :
    - “input  $x$  in  $[1..10]$ ” → classes :  $x < 1$ ,  $1 \leq x \leq 10$ ,  $x > 10$
    - “enumeration  $A, B, C$ ” → classes :  $A, B, C$ ,  $\text{not}\{A,B,C\}$
    - “input integer  $n$ ” → classes :  $n$  not an integer,  
 $n < \text{min}$ ,  $\text{min} \leq n < 0$ ,  $0 \leq n \leq \text{max}$ ,  $n > \text{max}$
    - .....
- Define one/couple of test cases for each class
  - Test cases that cover valid classes
  - Test cases that cover at most one invalid class

# Example : Equivalence Partitioning

*Test a function for calculation of the absolute value of an integer x*

- Equivalence classes :

Condition	Valid eq. classes	Invalid eq. Classes
<i>nr of inputs</i>	1 <sup>(1)</sup>	0 <sup>(2)</sup> , > 1 <sup>(3)</sup>
<i>input type</i>	integer <sup>(4)</sup>	non-integer <sup>(5)</sup>
<i>particular abs</i>	< 0 <sup>(6)</sup> , >= 0 <sup>(7)</sup>	

*a type system can prevent these values*

- Test cases :

*x = -10* (1,4,6)

*x = -* (2)

*x = 10 20* (3)

*x = 100* (1,4,7)

*x = "XYZ"* (5)

# Triangle Program [Myers]

“A program reads three integer values. The three values are interpreted as representing the lengths of the sides of a triangle. The program prints a message that states whether the triangle is scalene, isosceles, or equilateral.”

*Write a set of test cases to test this program.*



# A Self-Assessment Test [Myers]

*Test cases for:*

1. valid scalene triangle ?
2. valid equilateral triangle ?
3. valid isosceles triangle ?
4. 3 permutations of previous ?
5. side = 0 ?
6. negative side ?
7. one side is sum of others ?
8. 3 permutations of previous ?
9. one side larger than sum of others ?
10. 3 permutations of previous ?
11. all sides = 0 ?
12. non-integer input ?
13. wrong number of values ?
14. for each test case: is expected output specified ?
15. check behaviour after output was produced ?

# Triangle Program [Myers]

*Test cases for:*

Valid cases:

1. valid scalene triangle ?
2. valid equilateral triangle ?
3. valid isosceles triangle ?

Invalid cases:

4. negative side ?
5. one side larger than sum of others ?
6. non-integer input ?
7. wrong number of values ?

# Example : Equivalence Partitioning

- Test a program that computes the sum of the first  $N$  integers as long as this sum is less than  $maxint$ . Otherwise an *error* should be reported. If  $N$  is negative, then it takes the absolute value  $N$ .
- *Formally:*

Given integer inputs  $N$  and  $maxint$  compute  $result$  :

$$result = \sum_{K=0}^{|N|} k \quad \text{if this} \leq maxint, \text{ error otherwise}$$

# Example : Equivalence Partitioning

- Equivalence classes :

<u>Condition</u>	<u>Valid eq. classes</u>	<u>Invalid eq. classes</u>
nr of inputs	2	< 2, > 2
type of input	int int	int no-int, no-int int
abs( <i>N</i> )	$N < 0, N \geq 0$	
<i>maxint</i>	$\sum k \leq \text{maxint}$ $\sum k > \text{maxint}$	

- Test Cases :

	<i>maxint</i>	<i>N</i>	<i>result</i>
<i>Valid</i>	100	10	55
	100	-10	55
	10	10	error
<i>Invalid</i>	10	-	error
	10 20	30	error
	"XYZ"	10	error
	100	9.1E4	error

# Black-Box Testing : Boundary Value Analysis ( BVA )

Based on experience / heuristics :

- Testing **boundary conditions** of eq. classes is more effective  
i.e. values directly on, above, and beneath edges of classes
- Choose input boundary values as tests in input classes  
instead of, or additional to arbitrary values
- Choose also inputs that invoke output boundary values  
( values on the boundary of output classes )
- Example strategy as extension of equivalence partitioning:
  - choose one (n) arbitrary value(s) in each eq. class
  - choose values exactly on lower and upper boundaries of eq. class
  - choose values immediately below and above each boundary  
( if applicable )

# Example : Boundary Value Analysis

*Test a function for calculation of the absolute value of an integer*

- Valid equivalence classes :

Condition	Valid eq. classes	Invalid eq. Classes
particular abs	$< 0$ , $\geq 0$	

- Test cases :

- class  $x < 0$ , arbitrary value:  $x = -10$
- class  $x \geq 0$ , arbitrary value  $x = 100$
- classes  $x < 0$ ,  $x \geq 0$ , on boundary :  $x = 0$
- classes  $x < 0$ ,  $x \geq 0$ , below and above:  $x = -1$ ,  $x = 1$

# A Self-Assessment Test [Myers]

*Test cases for:*

1. valid scalene triangle ?
2. valid equilateral triangle ?
3. valid isosceles triangle ?
4. 3 permutations of previous ?
5. side = 0 ?
6. negative side ?
7. one side is sum of others ?
8. 3 permutations of previous ?
9. one side larger than sum of others ?
10. 3 permutations of previous ?
11. all sides = 0 ?
12. non-integer input ?
13. wrong number of values ?
14. for each test case: is expected output specified ?
15. check behaviour after output was produced ?

# Example : Boundary Value Analysis

- Given inputs *maxint* and *N* compute *result* :

$$result = \sum_{K=0}^{|N|} k \quad \text{if this } \leq maxint, \text{ error otherwise}$$

- Valid equivalence classes :

<u>condition</u>	<u>valid eq. classes</u>
<i>abs(N)</i>	$N < 0, N \geq 0$
<i>maxint</i>	$\sum k \leq maxint, \sum k > maxint$

- Can be extended with *maxint* < 0, *maxint* >= 0, max integer, .....



# Example : Boundary Value Analysis

- Valid equivalence classes :

<u>condition</u>	<u>valid eq. classes</u>
$\text{abs}(N)$	$N < 0, N \geq 0$
$\text{maxint}$	$\sum k \leq \text{maxint}, \sum k > \text{maxint}$

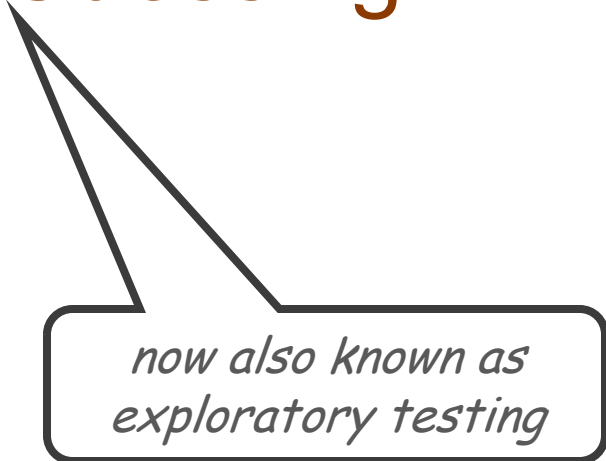
- Test Cases :

<u>maxint</u>	<u>N</u>	<u>result</u>	<u>maxint</u>	<u>N</u>	<u>result</u>
55	10	55	100	0	0
54	10	error	100	-1	1
56	10	55	100	1	1
0	0	0	...	...	...

- How to combine the boundary conditions of different inputs ?  
Take all possible boundary combinations ? This may blow up .....

# Black-Box Testing : Error Guessing

- Just 'guess' where the errors are .....
- Intuition and experience of tester
- Ad hoc, not really a technique
- But can be quite effective
- Strategy:
  - Make a list of possible errors or error-prone situations  
( may be related to boundary conditions )
  - Write test cases based on this list



*now also known as  
exploratory testing*

# Black-Box Testing : Error Guessing

- More sophisticated 'error guessing' : **Risk Analysis**
- Product risk analysis
  - functional : critical functionality or use of the product (e.g. safety)
  - structural : critical parts of the code ( high risk code sections )
    - parts with unclear specifications, . . . . .
    - complex algorithms or complex code
      - measure code complexity - tools available (McGabe, Logiscope,...)
- Process risk analysis
  - which phases of development were critical
    - e.g., requirements capturing, inexperienced development teams, . . . .
- High-risk code will be more thoroughly tested, or rewritten

# Black-Box Testing : Which One ?

- Black-box testing techniques :
  - Equivalence partitioning
  - Boundary value analysis
  - Cause-effect graphing
  - Decision tables
  - State transition testing
  - Error guessing
  - .....
- Which one to use ?
  - None of them are complete
  - All are based on some kind of heuristics
  - They are complementary

# Black-Box Testing : Which One ?

- Always use a combination of techniques
  - When a formal specification is available try to use it
  - Identify valid and invalid input equivalence classes
  - Identify output equivalence classes
  - Apply boundary value analysis on valid equivalence classes
  - Guess about possible errors
  - Cause-effect graphing for linking inputs and outputs

# White-Box Testing

- Testing based on the (internal) *structure* of the system under test
- For programs: testing based on program code  
hence, programming language dependent
- Extent to which (source) code is executed, i.e. covered
- Different kind of coverage :
  - path coverage
  - statement coverage
  - (multiple-) condition coverage
  - decision / branch coverage
  - . . . . .

# White-Box Testing : Path Testing

- Execute every possible path of a program,  
i.e., every possible sequence of statements
- Strongest white-box criterion
- Usually impossible: infinitely many paths ( in case of loops )
- So: not a realistic option
- But note: enormous reduction w.r.t. all possible test cases  
( each sequence of statements executed for only one value )

# Example Program

- Test a program that computes the sum of the first  $N$  integers as long as this sum is less than  $maxint$ . Otherwise an *error* should be reported. If  $N$  is negative, then it takes the absolute value  $N$ .

- Formally:

Given integer inputs  $N$  and  $maxint$  compute *result* :

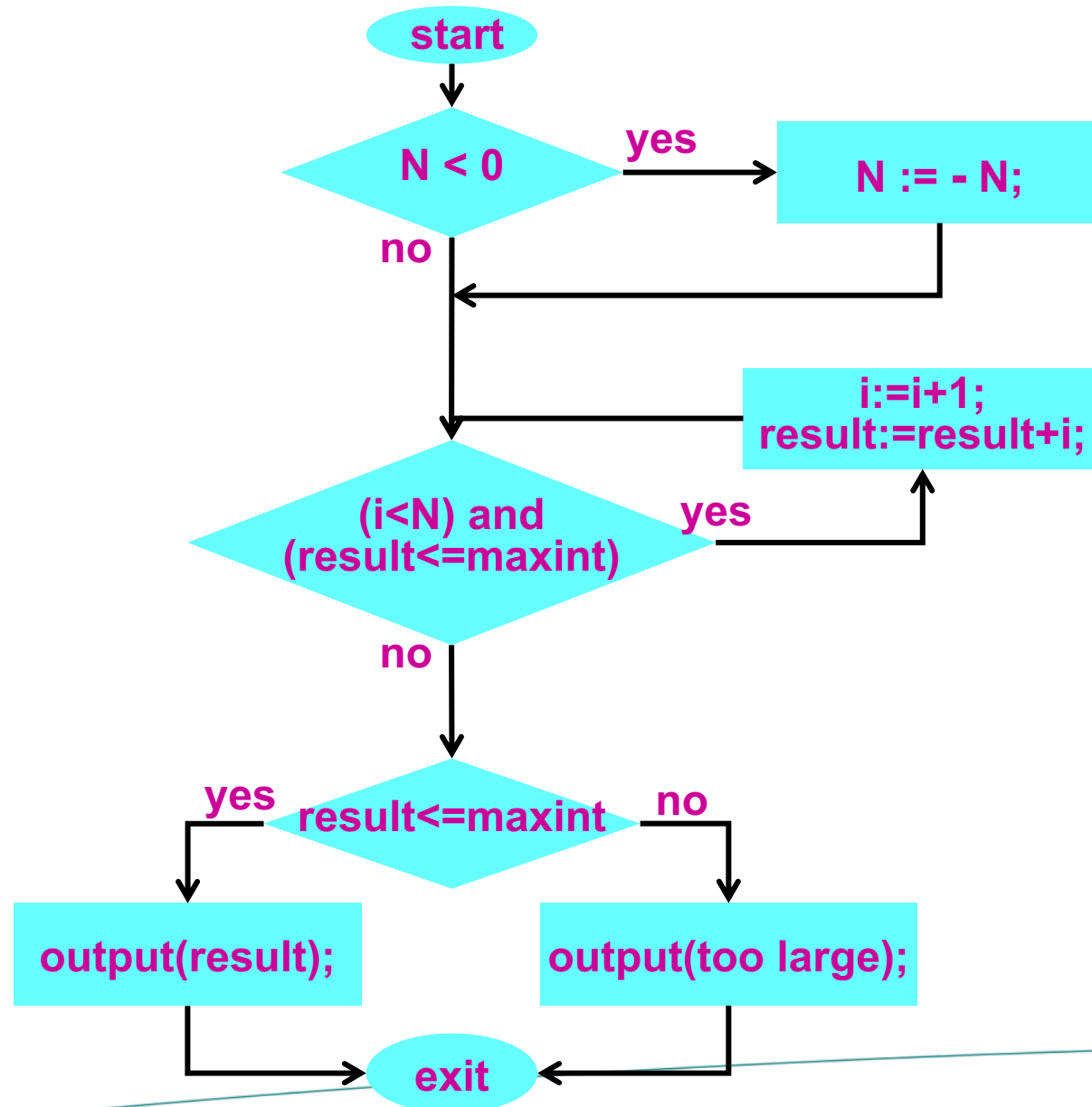
$$result = \sum_{K=0}^{|N|} k \quad \text{if this} \leq maxint, \quad error \text{ otherwise}$$



# Example Program

```
1      PROGRAM som ( maxint, N : INT )
2          INT  result := 0 ; i := 0 ;
3          IF  N < 0
4              THEN  N := - N ;
5              WHILE  ( i < N ) AND ( result <= maxint )
6                  DO      i := i + 1 ;
7                          result := result + i ;
8                  OD;
9              IF  result <= maxint
10                 THEN  OUTPUT ( result )
11                 ELSE  OUTPUT ( "too large" )
12             END.
```

# Example : Path Testing



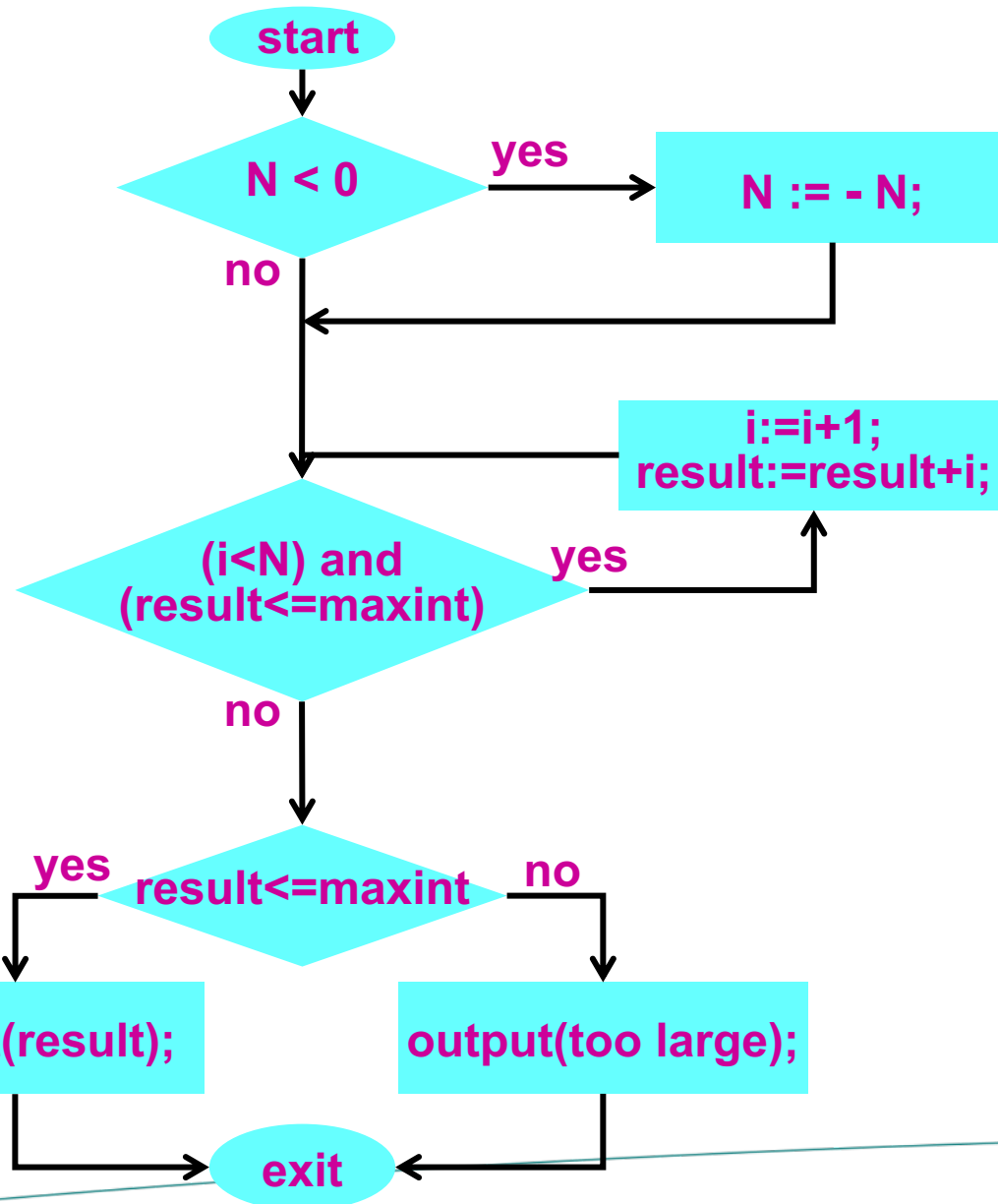
*Path:*

```
start
i:=i+1;
result:=result+i;
i:=i+1;
result:=result+i;
....
....
i:=i+1;
result:=result+i;
output(result);
exit
```

# White-Box Testing : Statement Coverage

- Execute every statement of a program
- Relatively weak criterion
- Weakest white-box criterion

# Example : Statement Coverage



Tests for complete statement coverage:

*maxint*    *N*

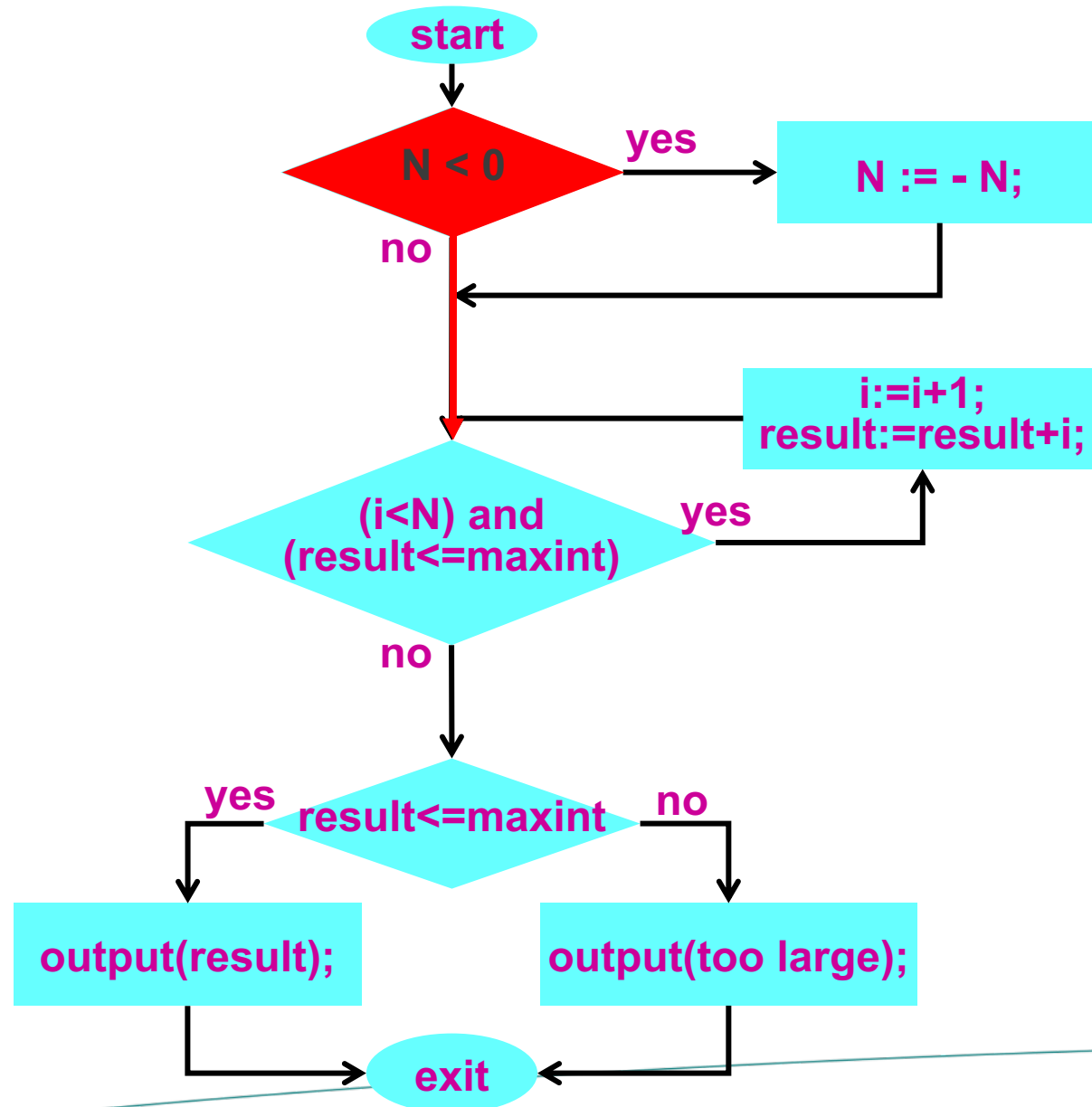
10        - 1

0         - 1

# White-Box Testing : Branch Coverage

- Branch coverage == decision coverage
- Execute every branch of a program :  
each possible outcome of each decision occurs at least once
- Example:
  - IF b THEN s1 ELSE s2
  - CASE x OF
    - 1 : ....
    - 2 : ....
    - 3 : ....

# Example : Branch Coverage



Tests for complete  
*statement coverage*:

*maxint*  $N$

10      - 1

0        - 1

are not sufficient for  
*branch coverage*;

Take:

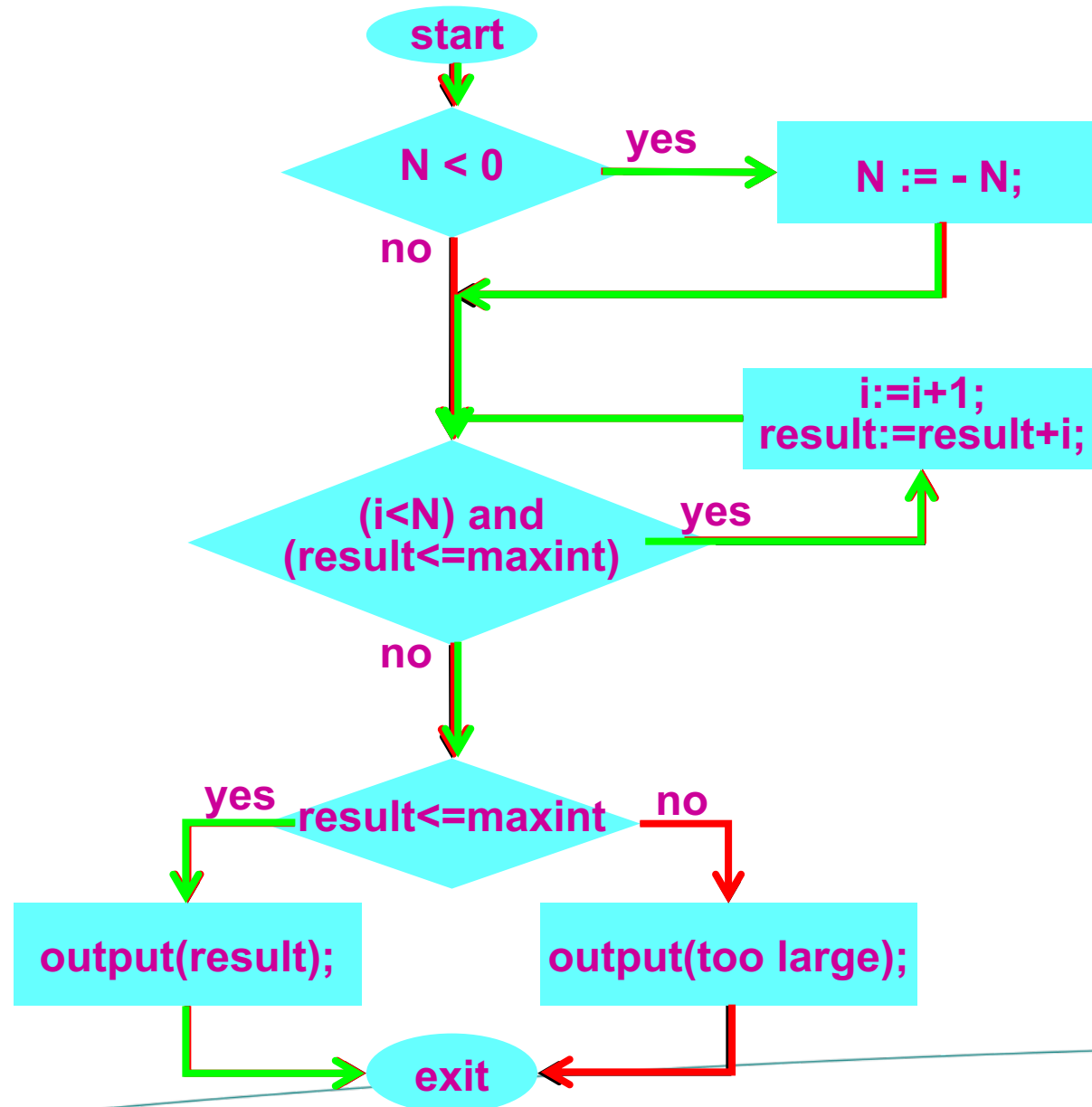
*maxint*  $N$

10        3

0        - 1

for complete  
*branch coverage*

# Example : Branch Coverage



*branch coverage*

guarantees that each decision outcome is taken at least once, but not all combinations of decisions!

*maxint* N

-1	-1
10	3

for *branch coverage*

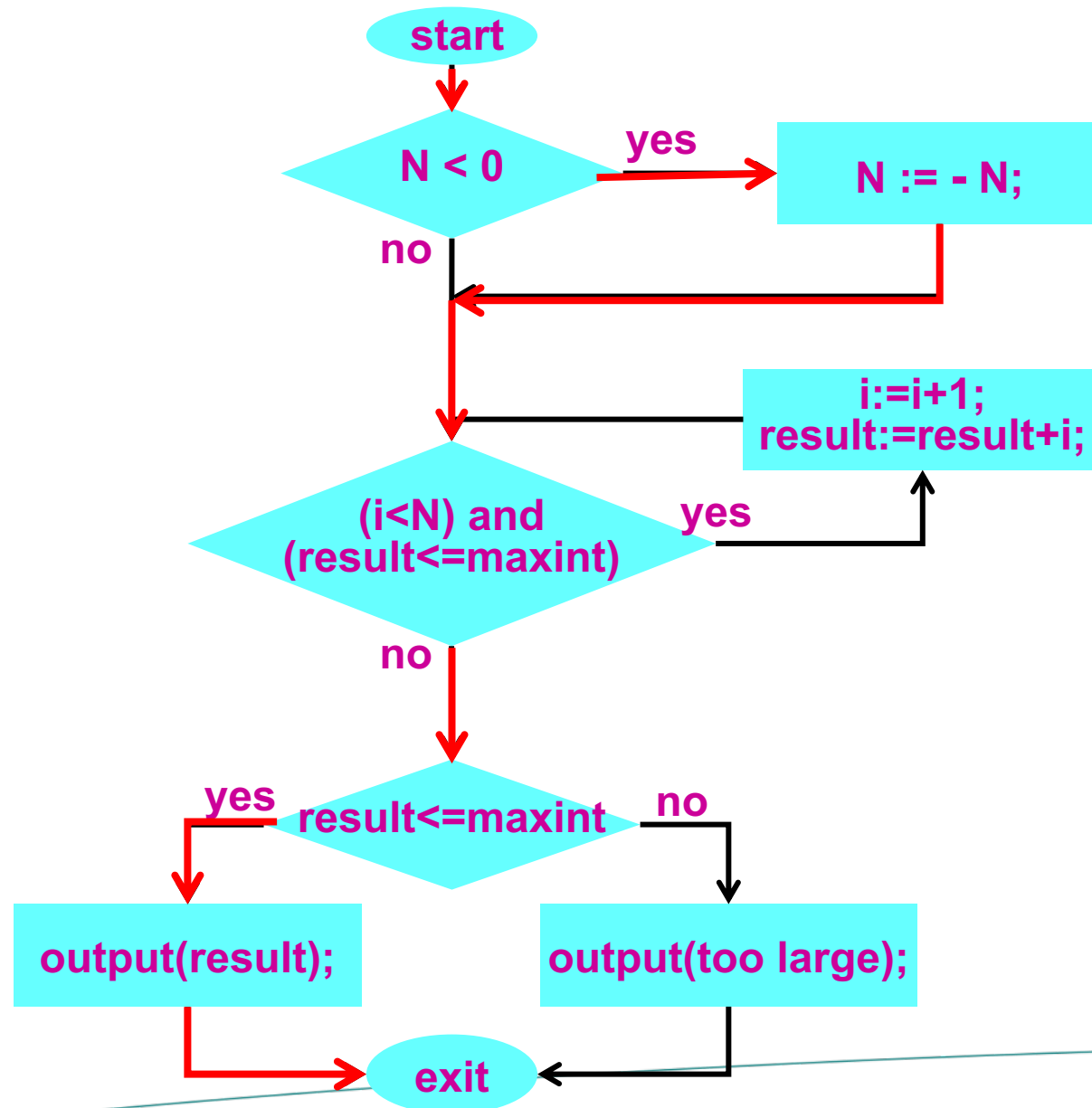
but no **green** path!

Needed :

combination of decisions

10	- 3
----	-----

# Example : Statement Coverage



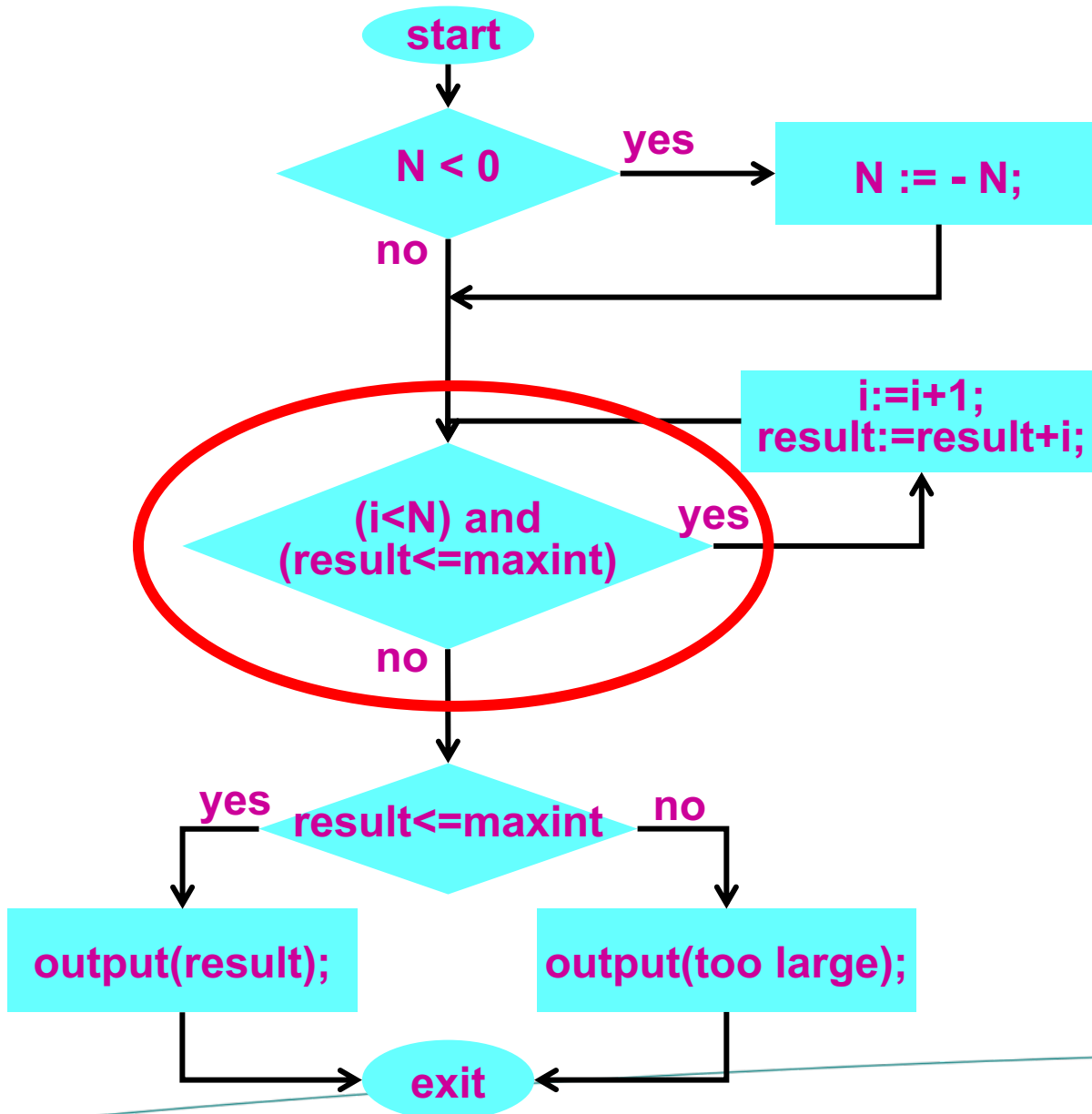
Sometimes there are *infeasible paths*  
( infeasible combinations of conditions )



# White-Box Testing : Condition Coverage

- Design test cases such that each possible outcome of each *condition* in each *decision* occurs at least once
- Example:
  - decision  $(i < N) \text{ AND } (result \leq maxint)$   
consists of two conditions :  $(i < value)$  and  $(result \leq maxint)$   
test cases should be designed such that each *condition* gets value *true* and *false* at least once

# Example : Statement Coverage



But  $(i = \text{result} = 0)$  :

$\text{maxint } N \quad i < N \quad \text{result} \leq \text{maxint}$

-1    1    true    false

1    0    false    true

gives *condition coverage*  
for all conditions

But it does not preserve  
*decision coverage*



always take care that  
*condition coverage*  
preserves *decision coverage*



*decision / condition coverage*

# White-Box testing : Multiple Condition Testing

- Design test cases for each combination of conditions
- Example:

$( i < N )$	$( result \leq maxint )$
false	false
false	true
true	false
true	true

- Implies *decision-*, *condition-*, *decision/condition coverage*
- But : exponential blow-up
- Again : some combinations may be infeasible

# White-Box testing : How to Apply ?

- Don't start with designing white-box test cases !
- Start with black-box test cases  
(equivalence partitioning, boundary value analysis, . . . . .)
- Check white-box coverage  
( statement-, branch-, condition-, . . . . . coverage )
- Use a **coverage tool**
- Design additional white-box test cases for not covered code

# A Coverage Tool

- Many coverage tools : commercial and open source  
tcov gcov Cobertura CodeCover Coverage.py EMMA, Jacoco, Jcov,  
PITest Clover Bullseye Jtest hpc VS Cantata, . . . . .
- Compile your program under test with a special option
- Run a number of test cases
- A listing indicates how often each statement/decision/. . . . . was executed  
and percentage of statements . . . . . executed