Functional Programming

Lecture 13: Parser combinators

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Outline

Parser combinators

Parsing expressions

Recall the datatype of expressions

Front-end is missing: parser that turns input string (concrete syntax) into expression tree (abstract syntax)

```
>>> parse "4 + 7 * 11"

Just (Add (Lit 4) (Mul (Lit 7) (Lit 11)))

>>> parse "(4 + 7) * 11"

Just (Add (Mul (Lit 4) (Lit 7)) (Lit 11))
```

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```
type Parser = String → (Expr, String)
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Similarly, a parser may fail

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```
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```

can return any unconsumed part of the argument string

Similarly, a parser may fail

```
type Parser = String \rightarrow Maybe (Expr. String)
```

Finally, different parsers will likely return different types of values

```
type Parser a = String \rightarrow Maybe (a, String)
```

Ad hoc parsing

Suppose we have a parser for natural numbers

```
parseNat :: Parser Int
we can use this parser to build a parser for a non-empty list of natural numbers
  parseNatList :: Parser [Int] — = String \rightarrow Maybe ([Int], String)
  parseNatList ('): (s_0) = case parseNat cs_0 of
       Nothing → Nothing
      Just (n, cs_1) \rightarrow case parseNats cs_1 of
                             \mathsf{Just} \ (\mathsf{ns}, \mathsf{'}]\mathsf{'}: \mathsf{cs}_2)] \to \mathsf{Just} \ (\mathsf{n}: \mathsf{ns}, \mathsf{cs}_2)
                             Nothing
                                      → Nothing
    where
    parseNats "" = Just ([]."")
    parseNats (', ': cs_1) = case parseNat cs_1 of
         Nothing \rightarrow Nothing
         Just (n, cs_2) \rightarrow case parseNats cs_2 of
                               Nothing → Nothing
                               Just (ns, cs_3) \rightarrow Just (n:ns, cs_3)
    parseNats cs = Just ([], cs)
  parseNatList _ = Nothing
```



Parser combinators

Idea: provide some basic parsers and some combinators to glue them together

Parsing a single character

```
>>> (char '0') "01"
Just ('0', "1")
>>> (char '1') "01"
Nothing
```

Returning "semantic" values

```
>>> (char '0' *> pure 0) "01"
Just (0,"1")
```

Parsing alternative choices

```
\gg let bit = (char '0' *> pure 0)
          <|> (char '1' *> pure 1)
>>> bit "01"
Just (0,"1")
>>> bit "10"
Just (1,"0")
```

The Parser type

We want the parser type to be made into an instance of type classes.

```
type Parser a = String \rightarrow Maybe (a, String)
Can't make type synonyms an instance, so, introduce a new type:

newtype Parser a = P { parse :: String \rightarrow Maybe (a, String) }
Reminder: this is the same as

newtype Parser a = P (String \rightarrow Maybe (a, String))

parse :: Parser a \rightarrow String \rightarrow Maybe (a, String)

parse (P pf) = pf
```

Note: Parser combines state with failure.

Parser instances

We will use the operations of classes Functor, Applicative and Monad (and more) as combinators.

So, we want the parser type to be made into instances of these type classes

```
{-# LANGUAGE DeriveFunctor #-}
newtype Parser a = P { parse :: String → Maybe (a, String) }
deriving (Functor)
```

A simple parsing primitive

```
\begin{array}{ll} \text{item} & :: \ \mathsf{Parser} \ \mathsf{Char} \\ \text{item} & = \mathsf{P} \ (\setminus \mathsf{input} \ \to \ \mathsf{case} \ \mathsf{input} \ \mathsf{of} \\ & [] & \to \ \mathsf{Nothing} \\ & (\mathsf{x} \colon \mathsf{xs}) & \to \ \mathsf{Just} \ (\mathsf{x}, \mathsf{xs})) \end{array}
```

Examples

```
>>> parse item ""
Nothing
>>> parse item "abc"
Just ('a',"bc")
>>> parse (fmap toUpper item) "abc"
Just ('A',"bc")
>>> parse (fmap toUpper item) ""
Nothing
```

```
\begin{array}{ll} \textbf{newtype} \ \ \mathsf{Parser} \ \ \mathsf{a} = \mathsf{P} \\ \{ \ \mathsf{parse} \ :: \ \mathsf{String} \ \to \ \mathsf{Maybe} \ (\mathsf{a}, \mathsf{String}) \ \} \end{array}
```

More instances

We make the parser type into an Applicative

```
instance Applicative Parser where  \begin{array}{l} \text{pure} :: a \to \mathsf{Parser} \ a \\ \text{pure} \ x = \mathsf{P} \ ( \setminus \mathsf{inp} \to \mathsf{Just} \ (\mathsf{x}, \mathsf{inp}) ) \\ <\!\!\! *\!\!\! :: \mathsf{Parser} \ (a \to b) \to \mathsf{Parser} \ a \to \mathsf{Parser} \ b \\ \mathsf{fp} <\!\!\! *\!\!\! > \mathsf{xp} = \mathsf{P} \ ( \setminus \mathsf{inp}_1 \to \mathsf{case} \ \mathsf{parse} \ \mathsf{fp} \ \mathsf{inp}_1 \ \mathsf{of} \\ & \quad \mathsf{Nothing} \quad \to \mathsf{Nothing} \\ & \quad \mathsf{Just} \ (\mathsf{f}, \mathsf{inp}_2) \to \mathsf{case} \ \mathsf{parse} \ \mathsf{xp} \ \mathsf{inp}_1 \ \mathsf{of} \\ & \quad \mathsf{Nothing} \quad \to \mathsf{Nothing} \\ & \quad \mathsf{Just} \ (\mathsf{x}, \mathsf{inp}_3) \to \mathsf{Just} \ (\mathsf{f} \ \mathsf{x}, \ \mathsf{inp}_3) ) \\ \end{array}
```

More instances

We make the parser type into an Applicative

```
instance Applicative Parser where

pure :: a \rightarrow Parser a

pure x = P(\langle inp \rightarrow Just(x, inp))

<*> :: Parser (a \rightarrow b) \rightarrow Parser a \rightarrow Parser b

fp < > xp = P(\langle inp_1 \rightarrow do - Maybe monad)

(f, inp_2) \leftarrow parse fp inp_1

(x, inp_3) \leftarrow parse xp inp_2

pure (f, x, inp_3)
```

Note: Ghc can derive Functor, but not Applicative

Examples

```
Trivial parser
 >>> parse (pure 1) "abc"
  Just (1, "abc")
Parser consuming three characters, discarding the second
  three :: Parser (Char, Char)
  three = pure (\x \y z \rightarrow (x,z)) \ll item \ll item \ll item
then
  >>> parse three "abcdef"
  Just (('a','c'),"def")
  >>> parse three "ab"
  Nothing
```

Convenience combinators

Let's (re)introduce

```
(\langle \$ \rangle) :: (Functor f) \Rightarrow b \rightarrow f a \rightarrow f b
(<*) :: (Applicative f) \Rightarrow f b \rightarrow f a \rightarrow f b
(*>) :: (Applicative f) \Rightarrow f a \rightarrow f b \rightarrow f b
x \ll p = (\setminus \rightarrow x) \ll p
p \ll q = (\x \rightarrow x) \ll p \ll q
p *> q = (\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ ) < > p < *> q
```

We can now write

```
three :: Parser (Char, Char)
three = (,) < $> item < * item < * item
```

Mnemonic: operators without > ignore the result of the parser after it.

Monad instance

```
instance Monad Parser where
    (>>=) :: Parser a \rightarrow (a \rightarrow Parser b) \rightarrow Parser b
    p \gg f = P (\ln p_1 \rightarrow do - Maybe monad)
                          (x, inp_2) \leftarrow parse p inp_1
                          parse (f x) inp_2
Now we can use the do notation.
  three' :: Parser (Char, Char)
  three' = do x \leftarrow item
                 item
                 y \leftarrow item
                 pure (x,y)
```

Making choices

Applicative and Monad operators combine parsers in sequence

- output string from each parser in the sequence becomes input string for the next
- if one parser fails, the sequence fails

We can also combine parsers in parallel

- all parsers get the same input
- if one parser succeeds, the combintation succeeds

Making choices

Use the choice operator from class Alternative

```
class (Applicative f) \Rightarrow Alternative f where
empty :: f a
(<|>) :: f a \rightarrow f a \rightarrow f a
```

The operation <|> is associative, and has empty as identity element

Alternative instance for Maybe

```
instance Alternative Maybe where
  empty :: Maybe a
  empty = Nothing
(<|>) :: Maybe a → Maybe a → Maybe a
  Nothing <|> my = my
  Just x <|> _ = Just x
```

Examples

```
\begin{array}{ll} \textbf{newtype} \ \ \mathsf{Parser} \ \ \mathsf{a} = \mathsf{P} \\ \{ \ \mathsf{parse} \ :: \ \mathsf{String} \ \to \ \mathsf{Maybe} \ (\mathsf{a}, \mathsf{String}) \ \} \end{array}
```

A choice for Parser

```
\begin{array}{lll} \textbf{instance} & \textbf{Alternative Parser where} \\ & \textbf{empty} :: \textbf{Parser a} \\ & \textbf{empty} = \textbf{P} \; \big( \big| \textbf{inp} \; \rightarrow \; \textbf{Nothing} \big) \\ & (< \mid >) \; :: \; \textbf{Parser a} \; \rightarrow \; \textbf{Parser a} \; \rightarrow \; \textbf{Parser a} \\ & \textbf{p}_1 < \mid > \; \textbf{p}_2 = \textbf{P} \; \big( \big| \textbf{inp} \; \rightarrow \; \textbf{case} \; \textbf{parse} \; \textbf{p}_1 \; \textbf{inp} \; \textbf{of} \\ & & \textbf{Nothing} \quad \rightarrow \; \textbf{parse} \; \textbf{p}_2 \; \textbf{inp} \\ & & \textbf{Just result}_1 \; \rightarrow \; \textbf{Just result}_1 \big) \end{array}
```

A choice for Parser

```
instance Alternative Parser where empty :: Parser a empty = P (\inp \rightarrow empty) (\langle | \rangle) :: Parser a \rightarrow Parser a \rightarrow Parser a p_1 < | > p_2 = P (\inp \rightarrow parse p_1 inp < | > parse p_2 inp)
```

A choice for Parser

```
instance Alternative Parser where
    empty :: Parser a
    emptv = P ( \setminus inp \rightarrow emptv)
    (<|>) :: Parser a \rightarrow Parser a \rightarrow Parser a
    p_1 < p_2 = P (\inf \rightarrow parse p_1 inp < parse p_2 inp)
Examples
  >>> parse empty "abc"
  Nothing
  >>> parse (item <|> pure 'd') "abc"
  Just ('a', "bc")
  >>> parse (empty <|> pure 'd') "abc"
  Just ('d'."abc")
```

Derived primitives

Checking for characters that satisfy predicate p

```
sat :: (Char \rightarrow Bool) \rightarrow Parser Char sat p = do x \leftarrow item

if p x then pure x else empty
```

More primitives

```
\begin{array}{lll} \text{digit} & :: & \text{Parser Char} & \text{upper} & :: & \text{Parser Char} \\ \text{digit} & = & \text{sat isDigit} & \text{upper} & = & \text{sat isUpper} \\ \text{letter} & :: & \text{Parser Char} & \text{lower} & :: & \text{Parser Char} \\ \text{letter} & = & \text{sat isAlpha} & \text{lower} & = & \text{sat isLower} \\ \text{alphanum} & :: & \text{Parser Char} & \text{char} & :: & \text{Char} & \rightarrow & \text{Parser Char} \\ \text{alphanum} & = & \text{sat isAlphaNum} & \text{char} & x & = & \text{sat} & (== x) \\ \end{array}
```

Derived primitives (continued)

A parser for recognizing a complete string

```
string :: String \rightarrow Parser String string [] = pure [] string (x:xs) = pure (:) <*> char x <*> string xs

Applying a parser several times: many (0 or more), some (at least once) many :: (Alternative f) \Rightarrow f a \rightarrow f [a] — works for f = Parser many x = some x <|> pure [] some :: (Alternative f) \Rightarrow f a \rightarrow f [a] some x = pure (:) <*> x <*> many x
```

More primitives

Parser for identifiers, numbers, and spacing Examples: ident :: Parser String >>> parse ident "ab4 def" ident = (:) <\$> lower <*> many alphanum Just ("ab4"," def") nat :: Parser Int >>> parse nat "123 abc" nat = read <\$> some digit Just (123," abc") int :: Parser Int >>> parse int "-123 abc" int = negate <\$ char '-' <*> nat Just (-123," abc")<|> nat >>> parse (space *> nat) space :: Parser () " 123"

Just (123,"")

space = many (sat isSpace) *> pure ()

Handling spaces

Primitive that ignores spaces before and after applying a parser

```
token :: Parser a → Parser a token p = space *> p <* space

Primitives that ignore spaces

natural :: Parser Int natural = token nat symbol :: String → Parser String symbol xs = token (string xs)
```

Handling spaces

Primitives that ignore spaces

```
natural :: Parser Int.
  symbol :: String \rightarrow Parser String
Example: parsing an non-empty list of natural numbers
  nats :: Parser [Int]
  nats = do symbol "["
             n ← natural
             ns \leftarrow many (do \{ symbol ","; natural \})
             symbol "]"
             pure (n:ns)
```

A parser for expressions

Grammar in EBNF

A parser for expressions

Translation into Haskell (first (incomplete) attempt)

Add "actions" to construct expression tree

Add "actions" to construct expression tree (Applicative style)

```
Add "actions" to construct expression tree (Applicative style)
  expr, term, factor :: Parser Expr
  expr = term
     <|> Add <$> term <* symbol "+" <*> expr
  term = factor
     <|> Mul <$> factor <* symbol "*" <*> term
  factor = Lit <$> natural
       <|> symbol "(" *> expr <* symbol ")"</pre>
Let's try this parser
  >>> parse expr "123"
  Just (Lit 123,"")
```

```
Add "actions" to construct expression tree (Applicative style)
  expr, term, factor :: Parser Expr
  expr = term
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  factor = Lit <$> natural
       <|> symbol "(" *> expr <* symbol ")"</pre>
Let's try this parser
  >>> parse expr "123 + 5"
  Just (Lit 123."+ 5") — unexpected!
```

What's wrong?

(<|>) is left-biased, if the left parser succeeds, then (<|>) succeeds as well without trying the right parser

```
expr = term
    <|> do { t \leftarrow term; symbol "+"; e \leftarrow expr; pure (Add t e) }
```

the second parser wil never succeed if the first didn't.

We first modify our grammar by factoring out common parts.

```
expr ::= term ("+" expr | "")
term ::= factor ("*" term | "")
factor ::= digit { digit } | "(" expr ")"
```

A parser for expressions: correct version

Translation into Haskell is straightforward

```
\begin{array}{l} \mathsf{expr} = \mathbf{do} \ \mathsf{t} \leftarrow \mathsf{term} \\ \qquad \mathsf{Add} \ \mathsf{t} < \mathsf{\$} \ \mathsf{symbol} \ "+" < \!\!\!*> \mathsf{expr} \ < \!\!\!|> \ \mathsf{pure} \ \mathsf{t} \\ \mathsf{term} = \mathbf{do} \ \mathsf{f} \leftarrow \mathsf{factor} \\ \qquad \mathsf{Mul} \ \mathsf{f} < \!\!\!\$ \ \mathsf{symbol} \ "*" < \!\!\!*> \mathsf{term} \ < \!\!\!|> \ \mathsf{pure} \ \mathsf{f} \\ \mathsf{factor} = \mathsf{Lit} < \!\!\!\$> \mathsf{natural} \\ \qquad < \!\!\!|> \ \mathsf{symbol} \ "(" \ *> \ \mathsf{expr} < \!\!\!* \ \mathsf{symbol} \ ")" \end{array}
```

Now

```
>>> parse expr "123 + 5"

Just (Add (Lit 123) (Lit 5),"")
```

A parser for expressions: correct version

More examples

```
>>> parse expr "123 + 5"
Just (Add (Lit 123) (Lit 5),"")
>>> parse expr "1 + 2*3"
Just (Add (Lit 1) (Mul (Lit 2) (Lit 3)),"")
>>> parse expr "123 + 5 +"
Just (Add (Lit 123) (Lit 5),"+")
```

More combinators

One or more items, separated by sep

```
sepBy1 :: Parser a \rightarrow Parser b \rightarrow Parser [a]
p 'sepBy1' sep = (:) <$> p <*> many (sep *> p)
```

Zero or more items, separated by sep

```
sepBy :: Parser a \rightarrow Parser b \rightarrow Parser [a] p 'sepBy' sep = p 'sepBy1' sep <|> pure []
```

Example:

```
>>> parse (int 'sepBy' symbol ",") "1,2,-3" 
Just ([1,2,-3],"")
```

Top level parser

Make sure the whole input is consumed

```
parseAll :: Parser a \rightarrow String \rightarrow Maybe a parseAll p inp = case parse p inp of

Just (x, []) \rightarrow Just x

Nothing
```

Example

```
>>> parse expr "1 + "
Just (Lit 1, "+ ")
>>> parseAll expr "1 + "
Nothing
>>> parseAll expr "1 + 2"
Just (Add (Lit 1) (Lit 2))
```

Consider this grammar

```
expr ::= term "+" expr | term "-" expr | term
```

We want to parse "1 - 2 + 3" as (1 - 2) + 3, not 1 - (2 + 3).

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Need a left-recursive grammar

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Consider this grammar

```
expr ::= term "+" expr | term "-" expr | term
We want to parse "1 - 2 + 3" as (1 - 2) + 3, not 1 - (2 + 3).
Need a left-recursive grammar
  expr ::= expr "+" term | expr "-" term | term
In Haskell:
  expr = do \{ t_1 \leftarrow expr; symbol "+"; t_2 \leftarrow term; pure (Add t_1 t_2) \}
     <|> do \{t_1 \leftarrow expr; symbol "-"; t_2 \leftarrow term; pure (Sub t_1 t_2)\}
     <|> term
```

Consider this grammar

```
expr ::= term "+" expr | term "-" expr | term
We want to parse "1 - 2 + 3" as (1-2) + 3, not 1 - (2+3).
Need a left-recursive grammar
  expr ::= expr "+" term | expr "-" term | term
In Haskell:
  expr = do \{ t_1 \leftarrow expr; symbol "+"; t_2 \leftarrow term; pure (Add t_1 t_2) \}
      \langle \rangle do { t<sub>1</sub> \leftarrow expr; symbol "-"; t<sub>2</sub> \leftarrow term; pure (Sub t<sub>1</sub> t<sub>2</sub>) }
      <|> term
```

To parse an expr, first parse an expr...

All leaves are terms, so

```
\mathsf{expr} \; ::= \mathsf{term} \; \left\{ \text{"+" term } \mid \text{ "-" term} \right\}
```

```
All leaves are terms, so  \begin{array}{lll} & & & \\ & & \text{expr} & ::= \text{ term } \{\text{"+" term } | \text{ "-" term}\} \\ & & \text{In Haskell} \\ & & & \text{expr} & :: \text{ Parser Expr} \\ & & \text{expr} & = \text{ foldl } (\backslash t \text{ suffix} \rightarrow \text{ suffix } t) < \$ > \text{ term } < \ast > \text{ many exprSuffix} \\ & & \text{exprSuffix} & :: \text{ Parser } (\text{Expr} \rightarrow \text{Expr}) \\ & & \text{exprSuffix} & = (\backslash t_2 \rightarrow \backslash t_1 \rightarrow \text{Add } t_1 \ t_2) < \$ \text{ symbol "+" } < \ast > \text{ term} \\ & & < | > (\backslash t_2 \rightarrow \backslash t_1 \rightarrow \text{Sub } t_1 \ t_2) < \$ \text{ symbol "-" } < \ast > \text{ term} \\ \end{array}
```

```
All leaves are terms, so
  expr := term exprSuffix
  exprSuffix ::= "+" term exprSuffix | "-" term exprSuffix | ""
In Haskell
  expr :: Parser Expr
  expr = do \{ t_1 \leftarrow term : exprSuffix t_1 \}
    where
    exprSuffix t<sub>1</sub>
         = do { symbol "+"; t_2 \leftarrow \text{term}; exprSuffix (Add t_1 t_2) }
       <> do { symbol "-"; t_2 \leftarrow term; exprSuffix (Sub t_1 t_2) }
       < > pure t<sub>1</sub>
```

```
All leaves are terms, so
  expr ::= term exprSuffix
  exprSuffix ::= "+" term exprSuffix | "-" term exprSuffix | ""
In Haskell
  expr :: Parser Expr
  expr = manyInfixL term (Add <\s symbol "+" <\> Sub <\s symbol "-")
  manyInfixL :: Parser a \rightarrow Parser (a \rightarrow a \rightarrow a) \rightarrow Parser a
  manyInfixL px po = px \gg = go
    where
    go x_1 = do \{ f \leftarrow po; x_2 \leftarrow px; go (f x_1 x_2) \}
         <|> pure x<sub>1</sub>
```

Take away

Summary

- Specify a parser with combinators
- Close to EBNF grammar
- Two styles
 - Applicative: Add <\$>term <*symbol "+"<*>term
 - Monadic: do $\{t_1 \leftarrow \text{term}; \text{ symbol "+"}; t_2 \leftarrow \text{term}; \text{ pure } (Add t_1 t_2)\}$
- Libraries for more combinators, error handling, etc.