

CS 3530: Assignment 1c

Fall 2014

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Exercises

Exercise 1.8b (3 points)

Problem

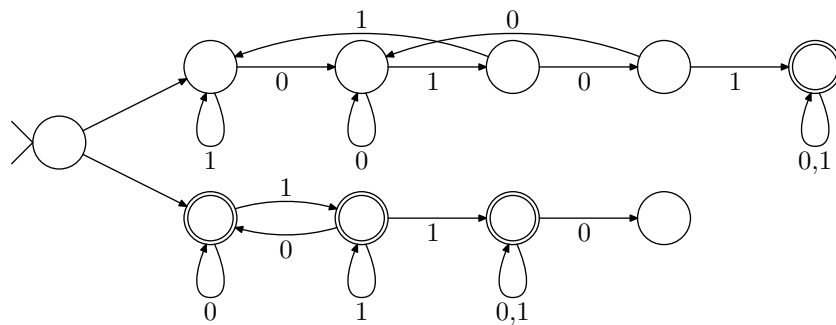
Use the construction given in the proof of Theorem 1.45 to give the state diagrams of NFAs recognizing the union of the languages given.

- b. Language: $L_1 \cup L_2$ where L_1 is the language from 1.6c and L_2 is the language from 1.6f
(note: both language are from assignment 1a)

Language from 1.6c: $\{w : w \text{ contains the substring } 0101, \text{ i.e., } w = x0101y \text{ for some } x \text{ and } y\}$

Language from 1.6f: $\{w : w \text{ doesn't contain the substring } 110\}$

Solution



Exercise 1.9b (3 points)

Problem

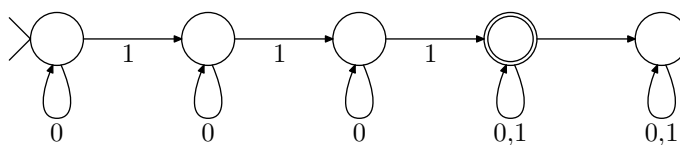
Use the construction given in the proof of Theorem 1.47 to give the state diagrams of NFAs recognizing the concatenation of the languages given.

- b. Language: $L_1 \circ L_2$ where L_1 is the language from 1.6b and L_2 is the language from 1.6m
(note: both language are from assignment 1a)

Language from 1.6b: $\{w : w \text{ contains at least three 1s}\}$

Language from 1.6m: The empty set

Solution



Exercise 1.15 (7 points)

Problem

Give a counterexample to show that the following construction fails to prove Theorem 1.49¹, the closure of the class of regular languages under the star operation.² Let $N_1 = (Q_1, \Sigma, \delta_1, q_1, F_1)$ recognize A_1 . Construct $N = (Q_1, \Sigma, \delta, q_1, F)$ as follows. N is supposed to recognize A_1^* .

- a The states of N are the states of N_1 .
- b The start state of N is the same as the start state of N_1 .
- c $F = \{q_1\} \cup F_1$.

The accept states F are the old accept states plus its start state.

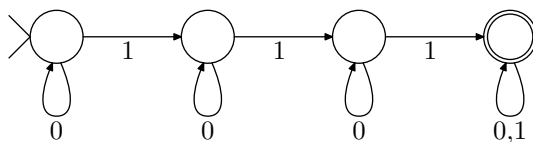
- d Define δ so that for any $q \in Q$ and any $a \in \Sigma_\varepsilon$,

$$\delta(q, a) = \begin{cases} \delta_1(q, a) & q \notin F_1 \text{ or } a \neq \varepsilon \\ \delta_1(q, a) \cup \{q_1\} & q \in F_1 \text{ and } a = \varepsilon. \end{cases}$$

(Suggestion: Show this construction graphically, as in Figure 1.50.)

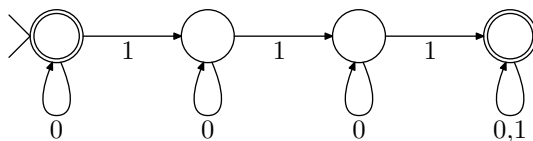
Solution Original

Language: $\{w : w \text{ contains at least three 1s}\}$



Solution Modified

$\Sigma = \{0\}$ could be a solution.



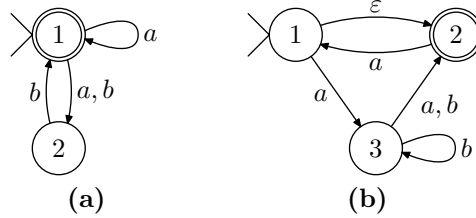
¹Theorem 1.49: The class of regular languages is closed under the star operation.

²In other words, you must present a finite automaton, N_1 , for which the constructed automaton N does not recognize the star of N_1 's language.

Exercise 1.16 (7 points)

Problem

Use the construction given in Theorem 1.39 to convert the following two nondeterministic finite automata to equivalent deterministic finite automata.



Solution

