# CS 3530: Assignment 1d

Fall 2014

Name: Eric Beilmann

## **Problems**

## Problem 1.60 (10 points)

#### Problem

Let  $\Sigma = \{a, b\}$ . For each  $k \geq 1$ , let  $C_k$  be the language consisting of all strings that contain an a exactly kplaces from the right-hand end. Thus  $C_k = \Sigma^* a \Sigma^{k-1}$ . Describe an NFA with k+1 states that recognizes  $C_k$ , both in terms of a state diagram and a formal description.

#### Solution Description

 $N = (Q, \Sigma, \delta, q_0, F)$ 

 $Q = \{0,\,1,\,\dots\,\,,\,k\}$ 

 $\Sigma = \{A,\,B\}$ 

 $q_0 = \{0\}$  $F = \{k\}$ 

 $\delta =$ 

 $\delta(q_k, A) = q_{k+1}$  for all k-1 > 0

 $\delta(q_k, A) = q_1 \text{ for } k_{max}$ 

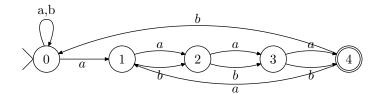
 $\delta(q_0, A) = q_0$ 

 $\delta(q_k, B) = q_{k+1}$  for all k-1 > 1

 $\delta(q_k, B) = q_0 \text{ for } k_{max}$ 

 $\delta(q_0, B) = q_0$ 

#### **Solution Diagram**



## Problem 1.62 (10 points)

#### Problem

Let  $\Sigma = \{a, b\}$ . For each  $k \geq 1$ , let  $D_k$  be the language consisting of all strings that have at least one a among the last k symbols. Thus  $D_k = \Sigma^* a(\Sigma \cup \varepsilon)^{k-1}$ . Describe a DFA with at most k+1 states that recognizes  $D_k$ , both in terms of a state diagram and a formal description.

### Solution Description

$$\begin{split} \mathbf{D} &= (\mathbf{Q}, \, \Sigma, \, \delta, \, q_0, \, \mathbf{F}) \\ \mathbf{Q} &= \{0, \, 1, \, \dots, \, \mathbf{k}\} \\ \Sigma &= \{\mathbf{A}, \, \mathbf{B}\} \\ q_0 &= \{0\} \\ \mathbf{F} &= \{1, \, \dots, \, k\} \\ \delta &= \end{split}$$

$$\begin{array}{l} \delta(q_k,A) = q_{k+1} \text{ for all k-1} > 0 \\ \delta(q_k,A) = q_k \text{ for } k_{max} \end{array}$$

$$\begin{split} &\delta(q_k,B) = q_{k+1} \text{ for all k-1} > 1 \\ &\delta(q_k,B) = q_0 \text{ for } k_{max} \\ &\delta(q_0,B) = q_0 \end{split}$$

### Solution Diagram

