## CS 3530: Assignment 7b

Fall 2014

## **Problems**

Problem 4.19 (20 points)

## Problem

Let  $S = \{\langle M \rangle : M \text{ is a DFA that accepts } w^{\mathcal{R}} \text{ whenever it accepts } w\}$ . Show that S is decidable.

## Solution

First construct a DFA N that accepts w. Then construct a DFA P (which is  $\mathcal{M}^{\mathcal{R}}$ ) that accepts the reverse of the DFA M by flipping the transitions and the start and accept states. Then we need to determine if the DFAs N and P are in  $\langle M \rangle$ . We can determine if N and P are in  $\langle M \rangle$  by determining the symmetric difference between the DFAs in M and N or P to determine they are equivalent.