

Artificial Intelligence 1

Lab 2

Roeland Lindhout (s2954524) & Younes Moustaghfir (s2909758)
AI2/AI3

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N-queens problem

The problem at hand is about the n-queens problem. It is an expansion of the 8-queens problem, which has often been discussed in previous courses. The goal is to place "n" number of queens on an $n \times n$ sized board, in such a way that they are not able to hit each other. For sizes bigger than 4, more solutions are possible.

The way to solve such a problem can be done in various ways. One approach, is to randomly place queens on the board until they accidentally have one of the right configurations. Obviously, this can be done more effectively. The first way we try to solve this, is by the hill-climbing approach. This basically means, that for every row, we look at which position is better than the previous position, and then choose that one. Still a blunt way to solve the problem, but already more sophisticated than randomly trying. The problem with this, is that it often gets stuck in local maxima. The second approach, is by simulated annealing. Simulated annealing is similar to hill-climbing, but it includes random moves, to avoid the problem with the local maxima. The way you decide when to make a random jump, is based on a relationship between the "temperature" (in this case, the number of correct queens) and the elapsed time. As the time increases, less random jumps are made. The final approach is with a generic algorithm. A genetic algorithm works much more differently. First of all, it does not use an initial state, but an initial population. This initial population is then sorted on their "fitness", which is the number of correctly placed queens. The best few are allowed to reproduce, i.e. make new states. This is done by combining two states. There is also a small chance of a random mutation in the newly produced state. By mixing up the parents and including the mutations, the population will approach the solution state, until one of the children is the correct solution.

0.1 Hill Climbing algorithm

We will be solving this problem using three different algorithms. First, we will use Hill Climbing to solve this. This is a quite straightforward algorithm. If, in

your search space, the neighbour has a higher value, go to that neighbour and repeat that process until you've found a maximum. In the case of the n-queens problem, you look at all the positions in a column and select the one with the highest value.

For this algorithm, we look at each neighbouring state of the current column. We then evaluate each position that the queen can go to. We do that for each queen and then move that queen to the position with the highest evaluation.

This approach is quite simple and therefore not that effective. The algorithm will not always find a solution. For the unmodified code, 6 out of 20 times in average, the algorithm was able to find a solution. We've therefore tried some improvements for the code. Hill Climbing can get stuck in local optima and then it's unable to find the global optimum. We therefore implemented something that when the algorithm is stuck, it chooses a random queen to randomly move so that it might get out of this local optimum. With this improvement, we see its success rate in Table 1. This table is in the Appendix

This algorithm does quite well up to 7 queens, after that its performance declines. The modified code did better than the original code.

0.2 Simulated Annealing algorithm

Simulated Annealing is somewhat the same as Hill Climbing, but better. Hill Climbing is able to get stuck in local maxima, therefore not always returning the optimal solution. Simulated Annealing allows "bad moves". With these "bad moves", it is able to escape local maxima and find a global maximum.

For Simulated Annealing, we figured that the temperature function should be something like: $T(t) = T0 * t$, where we filled in 400 for the starting temperature and t should be something around 0.99. We have used this function to lower the temperature until it has reached a certain value, in our case: 0.001. This sets the maximum amount of iterations, because if the temperature drops below that certain value, the while loop of our program stops. With these values, SA is quite similar to Hill Climbing. The difference is that we have implemented a function *ExpMove()* that decides whether a "bad move" should be made. This is where we differ from the pseudocode as well. We look at a current position and the maximum of a column to decide whether a bad move is accepted.

For simulated Annealing, we have noticed a few things. First of all, the algorithm usually finds a solution within 50 steps. When it did not find a solution after 50 steps, its chance of finding one is very small. As might have been clear by the previous sentence, the program does not always find a solution. For a number of queens above 10 this only gets worse. Why does it get worse? For more than 10 queens, the search space gets too big for our algorithm and the "bad move" that the algorithm takes will help the algorithm.

Genetic algorithm

The genetic algorithm consists of three functions. The first function describes the mutation. The mutation is as random as possible. It takes a random queen,

and places this at a random, new position, similar to how the random-search algorithm was implemented. Next, there is a function to sort the population. The population is sorted based on the evaluateState function from the given program. This evaluation is stored on the last place in the array. For every item in the array, the evaluation is compared to the evaluation of the next one, and then shifted until they are all in the right place. The next function is the real implementation of the program. First, a 2D array is made, with a size of the number of queens to the power of 2. This is chosen, because the number of different places the queens can stand, also increases exponentially. The first dimension represents the population, the second represents the configuration of the separate parents. The parents are initially randomly produced. After this, the population is sorted and the crossover can begin. The crossover is done with the best 20 % of the population. This was chosen to keep a fairly large amount of different configurations, but not too much. The crossover is done in pairs, so the first of the population pairs with the second, the third with the fourth and so forth. A random number between 0 and the number of queens is chosen. The first parent gives it's rows up to and including this number, and the second parent starting from this number. In this way, the child is a crossover between the parents. The child is placed at the last place in the population, thereby replacing the worst of the population. Then, 4 % of the children receive a mutation. This seems like a high number, but we thought it was necessary, because the initial population is randomly produced, and therefore it is quite possible that there are position that are not included in any of the parents, and we try to include these positions in the population by these mutations. Then, the population is once again sorted, and the process continues until the solution is found. The population is immediately sorted after the child is made, so the process is sped up, if the child is better than the first 20 %. Finally, the final state is printed.

The program is very fast for problems up to 8. It is also able to solve problems with 8 and 9 queens, but this can take quite long. It does always find a solution. It all depends on the random initialization of the population. If this is done very unfortunately, it takes longer. Problems bigger than 9, have not found a solution yet. We tried a problem with 10 queens, but after 15 minutes we gave up, expecting it not to find a solution ever. The valgrind output is the following for $n = 8$:

```

1          Number of queens (1<=nqueens<100): 8
2          Algorithm: (1) Random search (2) Hill climbing (3)
                Simulated Annealing (4) Genetic algorithm: 4
3          Final state is
4          ....q...
5          .....q.
6          .q.....
7          ...q....
8          .....q
9          q.....
10         ..q.....

```

```

11      ....q..
12      ==26906==
13      ==26906==  HEAP SUMMARY:
14      ==26906==    in use at exit: 0 bytes in 0 blocks
15      ==26906== total heap usage: 65 allocs, 65 frees, 2,816
        bytes allocated
16      ==26906==
17      ==26906== All heap blocks were freed -- no leaks are
        possible
18      ==26906==
19      ==26906== For counts of detected and suppressed errors,
        rerun with: -v
20      ==26906== ERROR SUMMARY: 0 errors from 0 contexts
        (suppressed: 0 from 0)

```

Nim

The game of Nim is about a stack of items, from which each player can take 1 to 3 items each turn, after which the other player's turn is. You lose when you have to take the last item. The players in our program are thought to be playing optimally. Playing optimally means that in each situation, the best possible choice is made, based on the best possible choice in the next turn of the opponent. Doing this, it can quickly be predicted who wins. For $n=3$, MAX, who begins, will take 2, leaving only 1 for MIN, who then loses. For $n=4$, MAX will take 3, once again leaving only one for MIN, who will once again lose. For $n=5$, assuming optimal play, MIN will win. First, MAX will take 3, and then MIN will take 1, leaving only 1 for MAX to take. No matter what MAX does at his/her first turn, MIN will be able to do a finishing move. For $n=6$, MAX will win. MAX will start by taking 1 item, which will result in the same situation as discussed before this one, only from the perspective of MIN.

Program description and evaluation

The program is fairly simple. We kept the basic structure of the given program, but we placed everything into one function. First, it is checked if the state is one. In this case, MAX has lost, and therefore -1 is returned. If this is not the case, the different moves are evaluated. Each move is recursively passed onto the function again, only negated, to show that it is MIN's turn. This is assigned to a variable. If this variable is better than best, this variable becomes the new best. Initially, best was set to $-\infty$. The move that was the best, is stored in the variable bestmove. This is printed at the end. At this point, all moves have been decided, and printed at once. This function is used the same way as in the original program, with the only change that it does not use the variable turn.

The program always find a solution, but somehow not always the most optimal solution, from MAX's point of view. The more items there are at the beginning, the longer it takes to find an answer. Up to ± 35 , the time it takes is not too long, but after this, the program becomes very slow.

Source code

Listing 1: nqueens.c

```
1  /* nqueens.c: (c) Arnold Meijster (a.meijster@rug.nl) */
2
3  #include <stdio.h>
4  #include <stdlib.h>
5  #include <math.h>
6  #include <time.h>
7  #include <assert.h>
8
9  #define MAXQ 100
10
11 #define FALSE 0
12 #define TRUE 1
13
14 #define ABS(a) ((a) < 0 ? -(a) : (a))
15
16 int nqueens; /* number of queens: global variable */
17 int queens[MAXQ]; /* queen at (r,c) is represented by queens[r] == c */
18
19 void initializeRandomGenerator() {
20     /* this routine initializes the random generator. You are not
21      * supposed to understand this code. You can simply use it.
22      */
23     time_t t;
24     srand((unsigned) time(&t));
25 }
26
27 /* Generate an initial position.
28  * If flag == 0, then for each row, a queen is placed in the first
29     column.
30  * If flag == 1, then for each row, a queen is placed in a random column.
31  */
32 void initiateQueens(int flag) {
33     int q;
34     for (q = 0; q < nqueens; q++) {
35         queens[q] = (flag == 0 ? 0 : random() % nqueens);
36     }
37 }
38
39 /* returns TRUE if position (row0,column0) is in
40  * conflict with (row1,column1), otherwise FALSE.
```

```

40  */
41  int inConflict(int row0, int column0, int row1, int column1) {
42      if (row0 == row1) return TRUE; /* on same row, */
43      if (column0 == column1) return TRUE; /* column, */
44      if (ABS(row0-row1) == ABS(column0-column1)) return TRUE; /* diagonal */
45      return FALSE; /* no conflict */
46  }
47
48  /* returns TRUE if position (row,col) is in
49   * conflict with any other queen on the board, otherwise FALSE.
50   */
51  int inConflictWithAnotherQueen(int row, int col) {
52      int queen;
53      for (queen=0; queen < nqueens; queen++) {
54          if (inConflict(row, col, queen, queens[queen])) {
55              if ((row != queen) || (col != queens[queen])) return TRUE;
56          }
57      }
58      return FALSE;
59  }
60
61  /* print configuration on screen */
62  void printState() {
63      int row, column;
64      printf("\n");
65      for(row = 0; row < nqueens; row++) {
66          for(column = 0; column < nqueens; column++) {
67              if (queens[row] != column) {
68                  printf (".");
69              } else {
70                  if (inConflictWithAnotherQueen(row, column)) {
71                      printf("Q");
72                  } else {
73                      printf("q");
74                  }
75              }
76          }
77          printf("\n");
78      }
79  }
80
81  /* move queen on row q to specified column, i.e. to (q,column) */
82  void moveQueen(int queen, int column) {
83      if ((queen < 0) || (queen >= nqueens)) {
84          fprintf(stderr, "Error in moveQueen: queen=%d "
85                  "(should be 0<=queen<%d)...Abort.\n", queen, nqueens);
86          exit(-1);
87      }
88      if ((column < 0) || (column >= nqueens)) {
89          fprintf(stderr, "Error in moveQueen: column=%d "

```

```

90         "(should be 0<=column<%d)...Abort.\n", column, nqueens);
91     exit(-1);
92 }
93 queens[queen] = column;
94 }
95
96 /* returns TRUE if queen can be moved to position
97 * (queen,column). Note that this routine checks only that
98 * the values of queen and column are valid! It does not test
99 * conflicts!
100 */
101 int canMoveTo(int queen, int column) {
102     if ((queen < 0) || (queen >= nqueens)) {
103         fprintf(stderr, "Error in canMoveTo: queen=%d "
104             "(should be 0<=queen<%d)...Abort.\n", queen, nqueens);
105         exit(-1);
106     }
107     if (column < 0 || column >= nqueens) return FALSE;
108     if (queens[queen] == column) return FALSE; /* queen already there */
109     return TRUE;
110 }
111
112 /* returns the column number of the specified queen */
113 int columnOfQueen(int queen) {
114     if ((queen < 0) || (queen >= nqueens)) {
115         fprintf(stderr, "Error in columnOfQueen: queen=%d "
116             "(should be 0<=queen<%d)...Abort.\n", queen, nqueens);
117         exit(-1);
118     }
119     return queens[queen];
120 }
121
122 /* returns the number of pairs of queens that are in conflict */
123 int countConflicts() {
124     int cnt = 0;
125     int queen, other;
126     for (queen=0; queen < nqueens; queen++) {
127         for (other=queen+1; other < nqueens; other++) {
128             if (inConflict(queen, queens[queen], other, queens[other])) {
129                 cnt++;
130             }
131         }
132     }
133     return cnt;
134 }
135
136 /* evaluation function. The maximal number of queens in conflict
137 * can be 1 + 2 + 3 + 4 + .. + (nqueens-1)=(nqueens-1)*nqueens/2.
138 * Since we want to do ascending local searches, the evaluation
139 * function returns (nqueens-1)*nqueens/2 - countConflicts().

```

```

140  */
141  int evaluateState() {
142      return (nqueens-1)*nqueens/2 - countConflicts();
143  }
144
145  int selectRandom(int n) {
146      int i;
147      i = 0 + random() % (n-0);
148      return i;
149  }
150
151  /*****
152
153  /* A very silly random search 'algorithm' */
154  #define MAXITER 1000
155  void randomSearch() {
156      int queen, iter = 0;
157      int optimum = (nqueens-1)*nqueens/2;
158
159      while (evaluateState() != optimum) {
160          printf("iteration %d: evaluation=%d\n", iter++, evaluateState());
161          if (iter == MAXITER) break; /* give up */
162          /* generate a (new) random state: for each queen do ...*/
163          for (queen=0; queen < nqueens; queen++) {
164              int pos, newpos;
165              /* position (=column) of queen */
166              pos = columnOfQueen(queen);
167              /* change in random new location */
168              newpos = pos;
169              while (newpos == pos) {
170                  newpos = random() % nqueens;
171              }
172              moveQueen(queen, newpos);
173          }
174      }
175      if (iter < MAXITER) {
176          printf ("Solved puzzle. ");
177      }
178      printf ("Final state is");
179      printState();
180  }
181
182  /*****
183
184  void hillClimbing() {
185      int newqueen, newpos, pos, ev;
186      int queen, iter = 0;
187      int optimum = (nqueens-1)*nqueens/2;
188      int max = 0;
189      int i ,x;

```



```

190
191 while ((evaluateState()) != optimum) {
192     printf("iteration %d: evaluation=%d\n", iter++, evaluateState());
193     if (iter == MAXITER) break; /* give up */
194     ev = evaluateState();
195     for (queen=0; queen < nqueens; queen++) {
196         pos = columnOfQueen(queen);
197         for(i = 0; i < nqueens; i++) {
198             moveQueen(queen, i);
199             if(evaluateState() > max) {
200                 newpos = i;
201                 max = evaluateState();
202                 newqueen = queen;
203             }
204             else if (evaluateState() == max) {
205                 x = random() % 2;
206                 switch (x) {
207                     case 0:
208                         newpos = i;
209                         break;
210                     case 1:
211                         newpos = random() % nqueens;
212                         break;
213                 }
214                 newqueen = queen;
215             }
216             moveQueen(queen, pos);
217         }
218         if (evaluateState() == ev) {
219             moveQueen(queen, random() % nqueens);
220         }
221     }
222     moveQueen(newqueen, newpos);
223 }
224 if (iter < MAXITER) {
225     printf ("Solved puzzle. ");
226 }
227 printf ("Final state is");
228 printState();
229 }
230
231
232
233 /*****
234
235 int ExpMove(int dE, double iter) {
236     int random1;
237     double E;
238     E = exp((dE/iter)/nqueens*nqueens) * 100;
239     random1 = random() % 101;

```

```

240     if(E > random1) {
241         return 1;
242     }
243     else {
244         return 0;
245     }
246 }
247
248 void simulatedAnnealing() {
249     int dE, newqueen, ev;
250     int queen, iter = 0, i;
251     int optimum = (nqueens-1)*nqueens/2;
252     int max = 0, current;
253     double temp = 50.0, alpha = 0.95;
254     double epsilon = 0.01;
255
256     while (temp > epsilon) {
257         ev = evaluateState();
258         printf("iteration %d: evaluation=%d\n", iter++, evaluateState());
259         if(ev == optimum) break;
260         int newpos;
261         for (queen=0; queen < nqueens; queen++) {
262             int pos;
263             /* position (=column) of queen */
264             pos = columnOfQueen(queen);
265             for(i = 0; i < nqueens; i++) {
266                 moveQueen(queen, i);
267                 current = evaluateState();
268                 if(current > max) {
269                     newpos = i;
270                     max = evaluateState();
271                     newqueen = queen;
272                 }
273                 dE = max - current;
274                 if(ExpMove(dE, temp)) {
275                     newpos = random() % nqueens;
276                 }
277                 if(dE < 0) {
278                     if(ExpMove(dE, temp)) {
279                         newpos = random() % nqueens;
280                     }
281                 }
282                 moveQueen(queen, pos);
283             }
284
285         }
286         moveQueen(newqueen, newpos);
287         temp *= alpha;
288     }
289     if (ev == optimum) {

```

```

290     printf ("Solved puzzle. ");
291 }
292 printf ("Final state is");
293 printState();
294 }
295
296
297 /*****
298
299 void mutation () {
300     // a random queen is moved to a random, new position (based on
        randomSearch)
301     int pos,newpos,queen;
302     queen = random() % nqueens;
303     pos = columnOfQueen(queen);
304     newpos = pos;
305     while (newpos == pos) {
306         newpos = random() % nqueens;
307     }
308     moveQueen(queen, newpos);
309 }
310
311 void sortPopulation (int size, int **arr) {
312     int i, n, value;
313     // Population is sorted on the evaluated stated, which is stored in the
        last position of the array.
314     for (i = 1; i < size; i++) {
315         value = arr[i][nqueens];
316         n = i;
317         while ((n > 0) && (arr[n-1][nqueens] > value)) {
318             arr[n] = arr[n-1];
319             n--;
320         }
321         arr[n] = arr[i];
322     }
323 }
324
325
326 void geneticAlgorithm() {
327
328     int optimum = (nqueens-1)*nqueens/2;
329     int m;
330     int i, n, q;
331     int **arr;
332     int size = pow(nqueens,2);
333
334     arr = malloc(size*sizeof(int *));
335     assert(arr != NULL);
336     // make initial population of size 100
337     for(i = 0; i < size; i++) {

```

```

338     arr[i] = malloc((nqueens+1)*sizeof(int));
339     assert(arr[i] != NULL);
340     for (q = 0; q < nqueens; q++) {
341         arr[i][q] = random() %nqueens;
342     }
343     arr [i][nqueens] = evaluateState();
344 }
345
346     sortPopulation(size, arr);
347
348     /* Cross-over:pick a random queen n, then the positions of the queens
349        after n of 1 parent
350        and in front of n of the other parent */
351
352     while (evaluateState() != optimum ) {
353         // The best 20% of the population can reproduce
354         for (i = 0; i < size/5; i+=2) {
355             int randomPlace = random () %nqueens;
356             for (n = 0; n <= randomPlace; n++) {
357                 // the worst population members are hereby deleted
358                 arr [size-1][n] = arr[i][n];
359                 arr [size-1][nqueens-n] = arr[i+1][nqueens-n];
360                 // random mutation occurs 4% of the time
361                 m = random() % 100;
362                 if (m < 5) {
363                     mutation();
364                 }
365                 arr[size-1][nqueens] = evaluateState();
366                 sortPopulation(size, arr);
367             }
368         }
369
370         printf ("Final state is");
371         printState();
372
373         for (i = 0; i < size; i++) {
374             free(arr[i]);
375         }
376         free(arr);
377     }
378
379     /*****
380
381
382     int main(int argc, char *argv[]) {
383         int algorithm;
384
385         do {
386             printf ("Number of queens (1<=nqueens<=%d): ", MAXQ);

```

```

387     scanf ("%d", &nqueens);
388 } while ((nqueens < 1) || (nqueens > MAXQ));
389
390 do {
391     printf ("Algorithm: (1) Random search (2) Hill climbing ");
392     printf ("(3) Simulated Annealing (4) Genetic algorithm: ");
393     scanf ("%d", &algorithm);
394 } while ((algorithm < 1) || (algorithm > 4));
395
396 initializeRandomGenerator();
397
398
399 if (algorithm != 4) {
400     initiateQueens(1);
401     printf("\nInitial state:");
402     printState();
403 }
404
405 switch (algorithm) {
406 case 1: randomSearch(); break;
407 case 2: hillClimbing(); break;
408 case 3: simulatedAnnealing(); break;
409 case 4: geneticAlgorithm(); break;
410 }
411
412 return 0;
413 }

```

Listing 2: nim.c

```

1  #include <stdio.h>
2  #include <stdlib.h>
3
4  #define MAX 0
5  #define MIN 1
6
7  #define INFINITY 9999999
8
9  int negaMax(int state) {
10     int move, bestmove, best = -INFINITY;
11     int m;
12     if (state == 1) {
13         return -1;
14     }
15     for (move = 1; move <= 3; move++) {
16         if (state - move > 0) {
17             m = -negaMax(state - move);
18             if (m > best) {
19                 best = m;

```

```

20         bestmove = move;
21     }
22 }
23 }
24 return bestmove;
25 }
26
27
28 void playNim(int state) {
29     int turn = 0;
30     while (state != 1) {
31         int action = negaMax(state);
32         printf("%d: %s takes %d\n", state,
33             (turn==MAX ? "Max" : "Min"), action);
34         state = state - action;
35         turn = 1 - turn;
36     }
37     printf("1: %s loses\n", (turn==MAX ? "Max" : "Min"));
38 }
39
40 int main(int argc, char *argv[]) {
41     if ((argc != 2) || (atoi(argv[1]) < 3)) {
42         fprintf(stderr, "Usage: %s <number of sticks>, where ", argv[0]);
43         fprintf(stderr, "<number of sticks> must be at least 3!\n");
44         return -1;
45     }
46
47     playNim(atoi(argv[1]));
48
49     return 0;
50 }

```

Appendix

Table 1: Succes rate of modified algorithm

| Number of Queens | Succesrate |
|------------------|------------|
| 4 | 100% |
| 5 | 100% |
| 6 | 100% |
| 7 | 100% |
| 8 | 50% |
| 9 | 35% |
| 10 | 20% |
| 11 | 20% |
| 12 | 10% |
| 13 | 5% |