

CS540 Introduction to Artificial Intelligence

Lecture 7

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Based on lecture slides by Jerry Zhu, Yingyu Liang, and Charles Dyer

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Socrative Test

Admin

- Socrative Student Login: Room CS540E.
- Use Socrative Room CS540 (without the E) for anonymous feedback.
- A: I haven't started P1.
- B: I have started P1.
- C: I have finished part 1.
- D: I have finished P1.
- E: What is P1?

Computer Vision Examples, Part I

Motivation

- Image segmentation
- Image retrieval
- Image colorization
- Image reconstruction
- Image super-resolution
- Image synthesis
- Image captioning

Computer Vision Examples, Part II

Motivation

- Style transfer
- Object tracking
- Visual question answering
- Human pose estimation
- Medical image analysis

Image Features Diagram

Motivation



One Dimensional Convolution

Definition

- The convolution of a vector $x = (x_1, x_2, \dots, x_m)$ with a filter $w = (w_{-k}, w_{-k+1}, \dots, w_{k-1}, w_k)$ is:

$$a = (a_1, a_2, \dots, a_m) = x * w$$

$$a_j = \sum_{t=-k}^k w_t x_{j-t}, j = 1, 2, \dots, m$$

$\overbrace{\quad\quad\quad}^{\leftarrow} \quad \overbrace{W \cdot X}$

- w is also called a kernel (different from the kernel for SVMs).
- The elements that do not exist are assumed to be 0.

Two Dimensional Convolution

Definition

- The convolution of an $m \times m$ matrix X with a $(2k + 1) \times (2k + 1)$ filter W is:

$$A = X * W$$

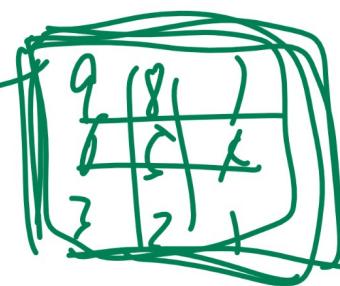
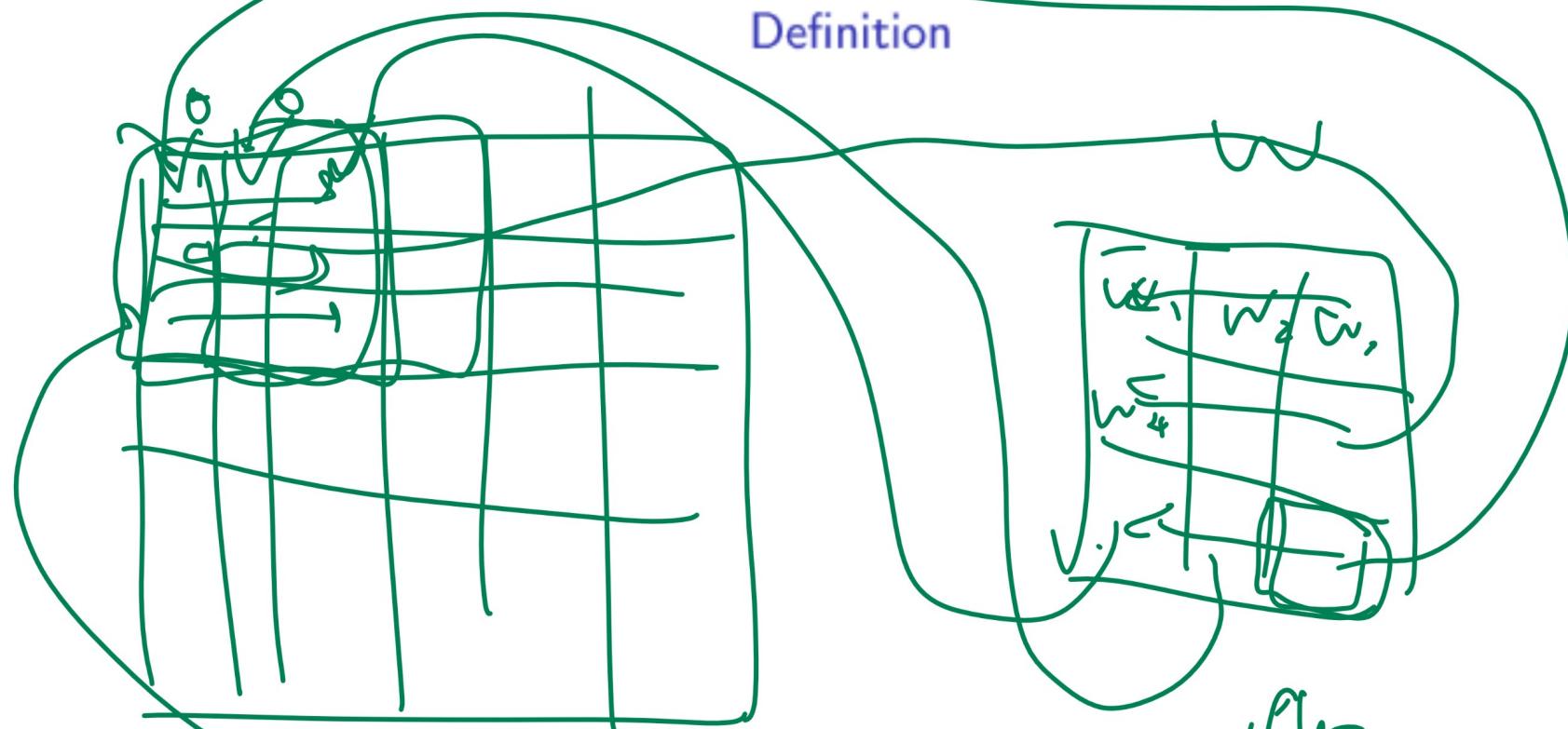
$$A_{j,j'} = \sum_{s=-k}^k \sum_{t=-k}^k W_{s,t} X_{j-s, j-t}, j, j' = 1, 2, \dots, m$$

$\mathcal{W} \cdot \mathcal{X}$

- The matrix W is indexed by (s, t) for $s = -k, -k + 1, \dots, k - 1, k$ and $t = -k, -k + 1, \dots, k - 1, k$.
- The elements that do not exist are assumed to be 0.

Convolution Diagram

Definition



$$\begin{matrix} & x_1 & x_2 & x_3 \\ x_4 & & x & \end{matrix}$$

Image Gradient

Definition

- The gradient of an image is defined as the change in pixel intensity due to the change in the location of the pixel.

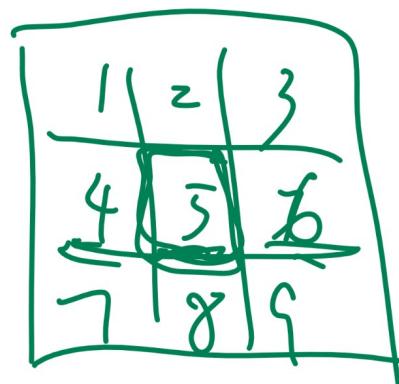
$$\frac{\partial I(s, t)}{\partial s} \approx \frac{I\left(s + \frac{\varepsilon}{2}, t\right) - I\left(s - \frac{\varepsilon}{2}, t\right)}{\varepsilon}, \varepsilon = 1$$
$$\frac{\partial I(s, t)}{\partial t} \approx \frac{I\left(s, t + \frac{\varepsilon}{2}\right) - I\left(s, t - \frac{\varepsilon}{2}\right)}{\varepsilon}, \varepsilon = 1$$

Image Derivative Filters

Definition

- The gradient can be computed using convolution with the following filters.

$$w_x = [-1 \ 0 \ 1], w_y = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$$



$$\nabla_x I_5 = -2$$

$$\nabla_y I_5 = -6$$

Sobel Filter

Definition

- The Sobel filters also are used to approximate the gradient of an image.

$$W_x = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, W_y = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 0 & -2 \\ 1 & 0 & -1 \end{bmatrix}$$

$$\nabla_x I = W_x * I$$

$$\nabla_y I = W_y * I$$

Gradient of Images

Definition

- The gradient of an image I is $(\nabla_x I, \nabla_y I)$.

$$\underline{\nabla_x I} = W_x * I, \underline{\nabla_y I} = W_y * I$$



- The gradient magnitude G and gradient direction Θ are the following.

either
horizontal
or vertical edges,

$$G = \sqrt{\nabla_x^2 + \nabla_y^2}$$
$$\Theta = \arctan \left(\frac{\nabla_y}{\nabla_x} \right)$$



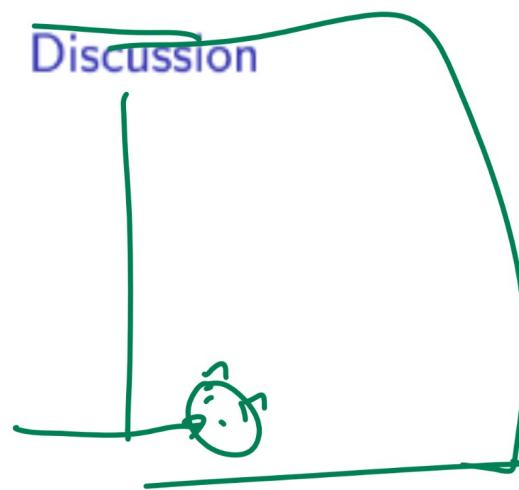
Gradient of Images Demo

Definition



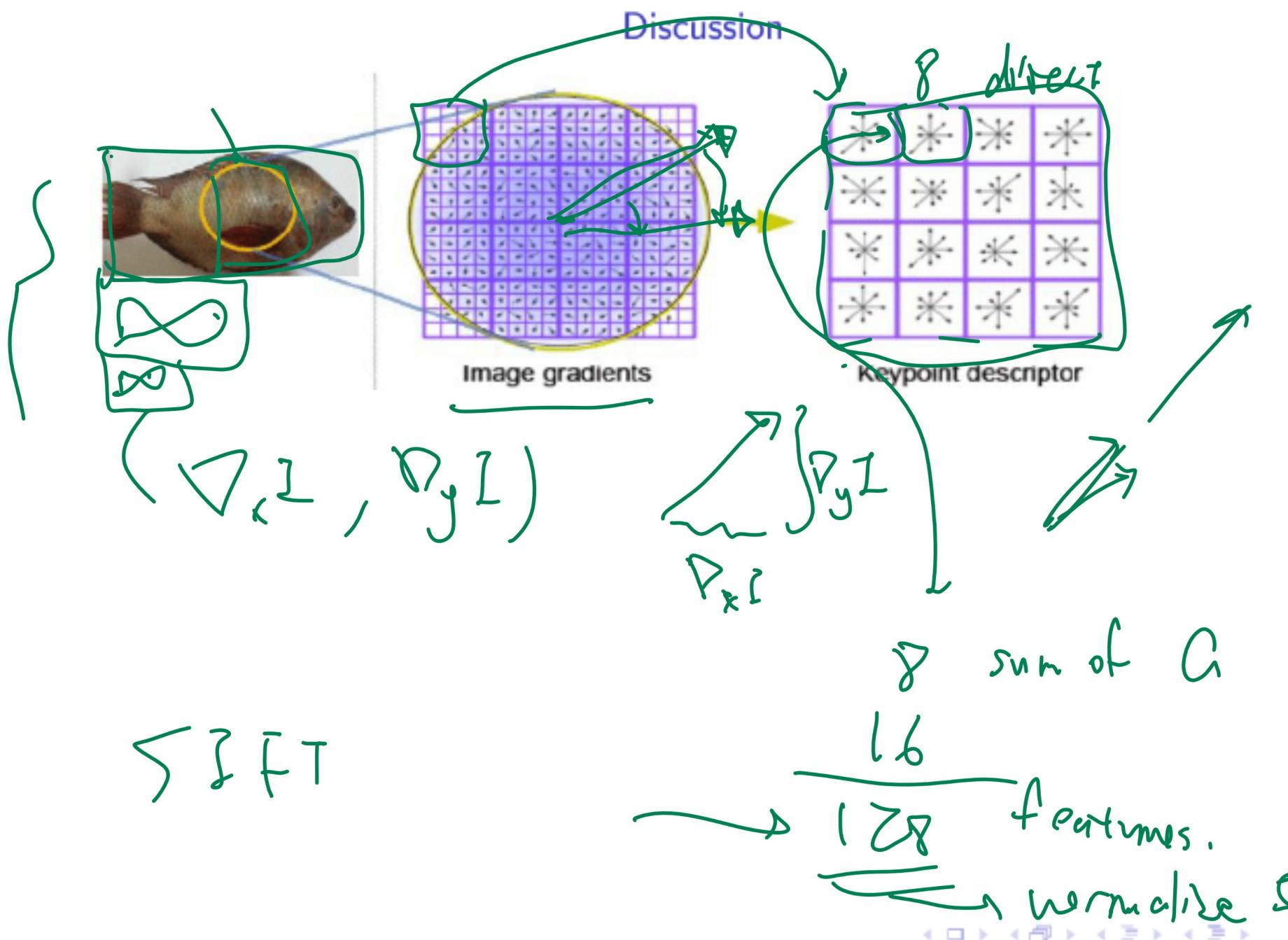
SIFT

Discussion



- Scale Invariant Feature Transform (SIFT) features are features that are invariant to changes in the location, scale, orientation, and lighting of the pixels.

Histogram Binning Diagram



HOG

Discussion

- Histogram of Oriented Gradients features is similar to SIFT but does not use dominant orientations.

↑ d.hccfuns

Matching vs Classification Diagram

Discussion

