

ECE 571: Lab 4

Date: 2022-03-25

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The following results of 6 tasks are generated by 6 C programs (`task1.c` – `task6.c`), whose scheduling are integrated the attached script file `run_tasks.sh`. The `readme.md` file is a good description for attached files.

Task 1: Deriving the Private Key

For the private key $\langle d, n \rangle$, n is known. According to calculation procedure of RSA, d is
`3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB`

Task 2: Encrypting a Message

With the public key $\langle e, n \rangle$, the encrypted cipher:

`6FB078DA550B2650832661E14F4F8D2CFAEF475A0DF3A75CACDC5DE5CFC5FADC`

Task 3: Decrypting a Message

$C = M^e \bmod n$: `50617373776F72642069732064656573`

Task 4: Signing a Message

a. plaintext: `I owe you $2000.`

signature: `55A4E7F17F04CCFE2766E1EB32ADDBA890BBE92A6FBE2D785ED6E73CCB35E4CB`

b. plaintext: `I owe you $3000.`

signature: `BCC20FB7568E5D48E434C387C06A6025E90D29D848AF9C3EBAC0135D99305822`

It can be seen that although there is only 1-bit change in the plaintext sequence, the generated signatures differ in many bits. That is similar to the diffusion effect.

Task 5: Verifying a Signature

Origin message: 4C61756E63682061206D6973736C652E

decrypted message from signature: 4C61756E63682061206D697373696C652E

Comparing the origin message and decrypted message from signature with the private key $\langle d, n \rangle$, they are different. Thus the signature is not from Alice.

When the tail two-bit data are changed from 2F to 3F, the decrypted message is 91471927C80DF1E42C154FB4638CE8BC726D3D66C83A4EB6B7BE0203B41AC294. The difference of the new decrypted message with the original message shows that "signature" techniques are very efficient and effective.

Task 6: Manually Verifying an X.509 Certificate

Herein I use the certification from `arizona.edu`, which is encrypted by RSA-256.

Step 1: download certification from the server

They are save into `ccc.txt`, `cc0.pem`, `cc1.pem`.

Step 2: extract $\langle e, n \rangle$

n :

```
AC0CF548619B14F2E2E8D67235A54A0D69C402B66EAE0EB32444D7C43EC667F61F607C090A2
C74D80BB7E51EC5325DD28FCE2D58C5A9FB57D52EB4035524315799832730C908309CC88C6E
3525A03D2D024E159B49A929139DC625A3EF41B409C63B96B01A4F532ECE66A773B07DC366D
AD200BE613AEC3A92BCD5C68CAEE971FBA1743643F6A51DBD82E8DC1A3FB1D15BD44BD78EF6
5B4275C9EC1743760CBBED853BFFB769A4F44C3631BAD94003FADF2564B9A8ECACA5958B7D7
FD628E7872A4DBD3FAF0E0F25D3BD3E2F99782B4B3A01AA75800BCA2EE366EAEDE1B0B0407F
580E1858104D94933F407A56824A1022EC602A44F9DB471D087A64F9A7924D
```

e : 10001 (hexadecimal)

```
(base) root@kali:~/# openssl x809 -in cc0.pem -noout -modulus
Modulus=AC0CF548619B14F2E2E8D67235A54A0D69C402B66EAE0EB32444D7C43EC667F61F607C090A2
4F532ECE66A773B07DC366DAD200BE613AEC3A92BCD5C68CAEE971FBA1743643F6A51DBD82E8DC1A3FB1D15BD44BD78EF6
5B4275C9EC1743760CBBED853BFFB769A4F44C3631BAD94003FADF2564B9A8ECACA5958B7D7FD628E7872A4DBD3FAF0E0F25D3BD3E2F99782B4B3A01AA75800BCA2EE366EAEDE1B0B0407F
580E1858104D94933F407A56824A1022EC602A44F9DB471D087A64F9A7924D
```

Both of them can be obtained from the detailed field data, by means of command `openssl x509 -in cc0.pem -text -noout` to extract.

```
Subject: C = US, postalCode = 85721, ST = Arizona, L = Tucson,
Subject Public Key Info:
  Public Key Algorithm: rsaEncryption
    RSA Public-Key: (2048 bit)
      Modulus:
        00:ac:0c:f5:48:61:9b:14:f2:e2:e8:d6:72:35:a5:
        4a:0d:69:c4:02:b6:6e:ae:0e:b3:24:44:d7:c4:3e:
        c6:67:f6:1f:60:7c:09:0a:2c:74:d8:0b:b7:e5:1e:
        c5:32:5d:d2:8f:ce:2d:58:c5:a9:fb:57:d5:2e:b4:
        03:55:24:31:57:99:83:27:30:c9:08:30:9c:c8:8c:
        6e:35:25:a0:3d:2d:02:4e:15:9b:49:a9:29:13:9d:
        c6:25:a3:ef:41:b4:09:c6:3b:96:b0:1a:4f:53:2e:
        ce:66:a7:73:b0:7d:c3:66:da:d2:00:be:61:3a:ec:
        3a:92:bc:d5:c6:8c:ae:e9:71:fb:a1:74:36:43:f6:
        a5:1d:bd:82:e8:dc:1a:3f:b1:d1:5b:d4:4b:d7:8e:
        f6:5b:42:75:c9:ec:17:43:76:0c:bb:ed:85:3b:ff:
        b7:69:a4:f4:4c:36:31:ba:d9:40:03:fa:df:25:64:
        b9:a8:ec:ac:a5:95:8b:7d:7f:d6:28:e7:87:2a:4d:
        bd:3f:af:0e:0f:25:d3:bd:3e:2f:99:78:2b:4b:3a:
        01:aa:75:80:0b:ca:2e:e3:66:ea:ed:e1:b0:b0:40:
        7f:58:0e:18:58:10:4d:94:93:3f:40:7a:56:82:4a:
        10:22:ec:60:2a:44:f9:db:47:1d:08:7a:64:f9:a7:
        92:4d
      Exponent: 65537 (0x10001)
  X509v3 extensions:
```

Step 3: extract the signature

```
100      Signature Algorithm: sha256WithRSAEncryption
101          56:0d:27:1b:4b:80:e3:c9:4e:09:bc:d6:39:0a:1c:f3:5b:3c:
102          53:a5:c8:49:67:ca:46:38:25:9a:6a:29:73:00:e0:12:13:1d:
103          43:1f:bc:da:3b:60:9a:62:00:f0:23:e0:4f:89:ae:4d:88:39:
104          9f:42:cd:59:65:53:e0:ec:0f:4c:f4:34:98:2c:69:f6:7a:62:
105          6e:51:65:d3:d4:27:0b:70:d4:76:5c:6f:6b:6c:25:b6:b8:0e:
106          c7:ce:73:da:8f:14:26:f5:64:10:5d:07:ec:76:90:a6:b5:c5:
107          e5:d1:25:82:98:fd:6f:a2:a8:16:2d:a5:e8:ae:f0:3d:3d:81:
108          73:c7:5b:35:40:35:7d:0b:12:97:62:30:e0:a8:3f:c0:36:89:
109          4b:72:29:ad:cb:49:5c:75:5a:2c:fe:84:aa:63:07:d6:66:d8:
110          a1:99:55:2a:57:88:7a:48:e6:a6:e7:30:78:0b:41:75:cc:b8:
111          9f:6f:6d:cc:d1:d8:2f:c4:20:1e:a6:a0:1d:24:f2:b6:af:3c:
112          cf:db:f2:a9:6a:c1:df:38:d4:ae:0f:c1:95:72:04:73:cd:74:
113          2c:5f:41:b4:2e:90:ec:14:b2:6b:55:71:90:95:ac:a7:a9:b1:
114          46:5c:03:f3:1b:1b:b3:7d:dd:65:48:fb:69:ca:83:33:5f:25:
115          3a:0c:96:a5
```

Step 4: extract the body of server's certification

It is in file `cc0_body.bin`.

Step 5: verify the certification

Task 6: Manually Verifying an X.509 Certificate

M_dec 419D0C8FED6BA6CDB771B6D64051F75101BE3CE2CB19C51D375E6A4DED832E54DF7562469557D437F0B094982F1D28CD79166A41354FC439E1A0865EE323C62FF2649FA4C1E581480C1A6D01D4867A79A897B1365F5933742728CA3CD6972024BC870D3EC8C30392160A6DD713BC43391DAD777C4201D40B239BE76EE87E32A98AFA0249FD6AAA35C1A7D0015E4832FCC8D0973987DDDEBD065AED9B054A1A51A1F329841F09BD395D8FBB418D8D7ECD38502B9331B3E2B1B5CEE3205260361F91F7876A58D3C71E5B1CC9DE9DB4B67474F88F98C7B1396A6FE81FF54886B96840BB7F51E633BF79620C93445EFE46AF5FC198E2E21949D53E7A075C090EEC86

correct hash for comparision: 30b8e177f6a24835fc21df98ac41a7a91d2ac4a5172f4ee5050f489e9412e79d