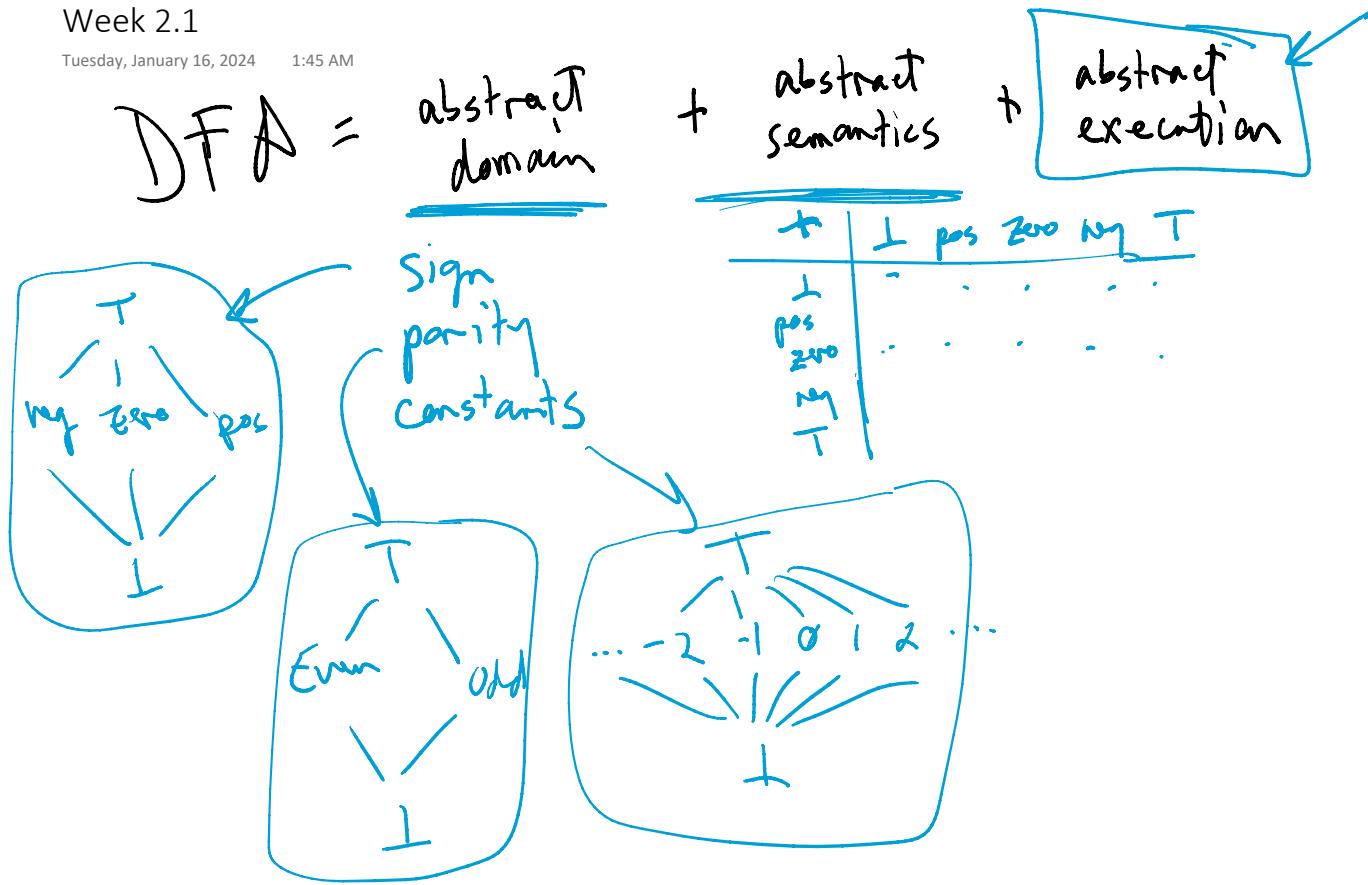


## Week 2.1

Tuesday, January 16, 2024 1:45 AM



### abstract execution

↳ flow-sensitive analysis : Computes a result for each program point

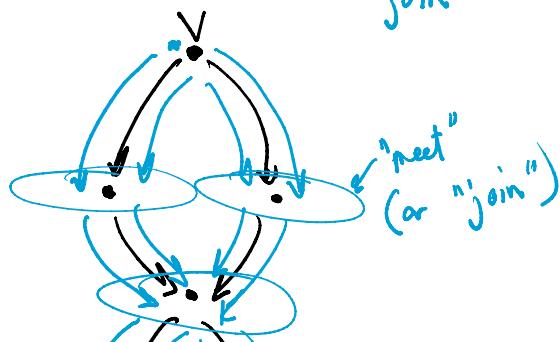
$$x = -2 [x \mapsto \text{my}]$$

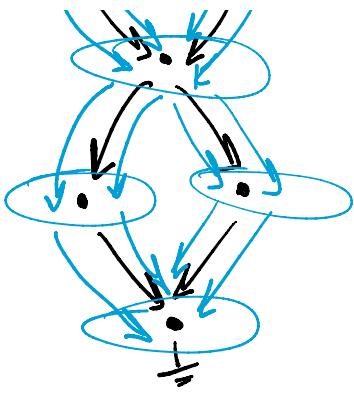
$$x = 2 [x \mapsto \text{pos}]$$

↳ in contrast to flow-insensitive analysis

MOP ("meet" over all paths)

↳ "join"





## MFP (maximal/minimal fixpoint)

- treat the abstract semantics as a system of equations  $\hat{=}$  compute their fixpoint (specifically, the "most precise" fixpoint)

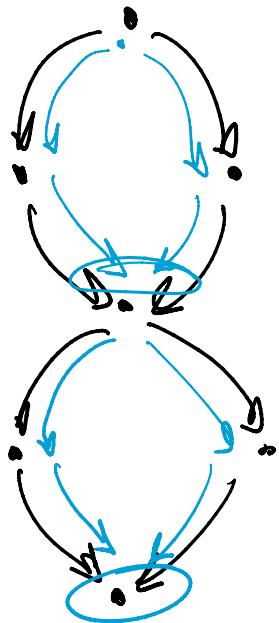
### fixpoint

- $f(x) = X$
- there can be  $\emptyset$ , 1, finite, or infinite fixpoints
- $f(x) = X^2$       fixpoints =  $\{\emptyset, 1\}$   
least fixpoint =  $\emptyset$

MFP: assign abstract values to each program point s.t. if we execute the abstract semantics then we get 1. same result

the abstract semantics  
the same result

↳ want the most precise values



What is relation between MFP sol'n  
vs. the Mop sol'n?

↳ an analysis is distributive iff

$$\text{for abstract semantics } F, \text{join}(F(x), F(y)) = F(\text{join}(x, y))$$

↳ for a distributive analysis, Mop = MFP

otherwise  $MFP \sqsubseteq Mop$

"less precise"

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1. Finding an intra-procedural, pointer-reasoning

defining an intraprocedural, pointer-conservative  
integer-based analysis

need

- abstract domain
- abstract semantics
- MFP worklist alg

MFP Worklist alg

setup

- map "bb2store": BasicBlock  $\mapsto$  entry abstract store
- $bb2store['entry']$  = initial abstract store
  - L parameters & globals set to T  
(int'-typed)
- Worklist of basic blocks
  - L queue, stack, polarity queue, ...
- initially, worklist contains 'entry'

analysis

while worklist is not empty:

$bb = \text{worklist.pop()}$

let  $\sigma = bb2store[bb]$

execute  $bb$  on  $\sigma$ , updating  $\sigma$  as appropriate

this is a copy

execute  $bb$  on  $\sigma$ , updating  $\sigma$  as appropriate  
at terminal:

for each target basic block  $bb'$ :

$$bb2store[bb'] = bb2store[bb'] \sqcup \sigma$$

if  $bb2store[bb']$  changed:

put  $bb'$  on worklist

we end w/  $bb2store$  mapping to entry abstract stores

we might want exit abstract store

↳ just take  $bb2store$ , execute each basic block once,  
remember the result