

Analog Integrated Systems Design

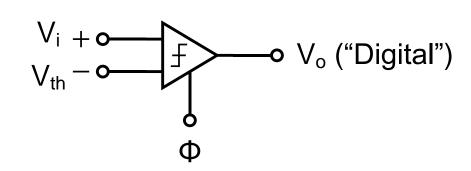
Lecture 11 Comparators

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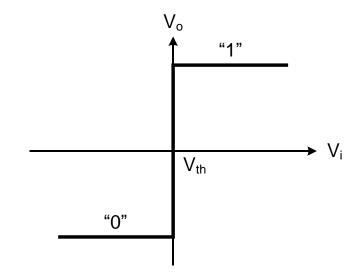
Integrated Circuits Laboratory (ICL)
Electronics and Communications Eng. Dept.
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Comparator

- ☐ The comparator circuit is the location where the digital decision is made
 - "Where nature turns into bits"
- Detects the polarity of a differential analog input signal
 - Generates a digital output (1 or 0) accordingly
- Or compares a SE input to a threshold (reference) voltage
 - Threshold-crossing detector



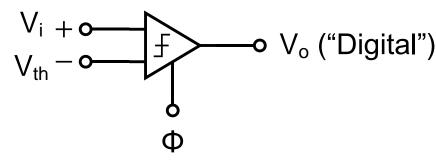
Circuit symbol



Transfer characteristic (ideal)

Comparators in ADCs

- ☐ Every analog-to-digital converter contains at least one comparator
- ☐ There are many different comparator implementations
 - There is NO universal "one design fits all" comparator
- ☐ Main design trade-off: accuracy and speed vs power consumption



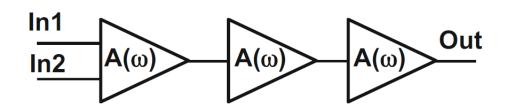
11: Comparators [Y. Chiu, EECT 7327, 2014]

Comparator Requirements

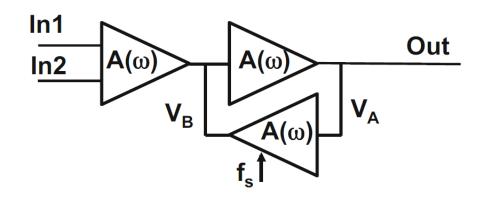
Large amplification (fine resolution / high sensitivity) Needs to translate mV or uV differential input to '0' and '1' Wide bandwidth (high speed) Accuracy Low input offset and low noise Low power consumption No memory (hysteresis) Previous comparator decision should not affect the following No metastability Any decision is better than no decision! Wide common mode input range High CMRR

Comparator Topologies

- Straight-forward amplification
 - Simple
 - Relatively slow



- Latch comparator
 - A.k.a. clocked / dynamic / regenerative comparator
 - Clock is required
 - Built-in S/H

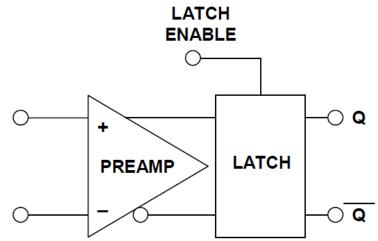


11: Comparators [M. Pelgrom, 2017]

Regeneration Example

Pre-amplification

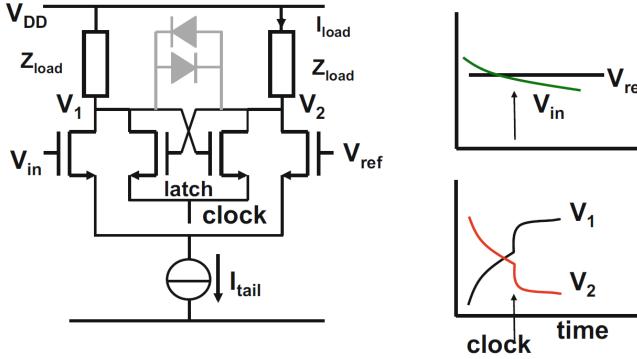
- oxdot A pre-amplifier is used before the regenerative section of the comparator is activated
 - Reduces the influence of mismatch in the regenerative section
 - Creates a form of isolation between the regeneration process and the input sources
 - No reason to boost the DC-gain to very high values (usually ≤ 10)
 - Low gain allows operations at high speed (large bandwidth)
 - Just sufficient to suppress latch mismatch and noise
- Most comparators use an input differential pair as a pre-amplifier



11: Comparators [W. Kester, ADI, 2005]

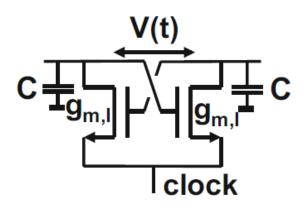
Regenerative Comparator Example

- After some amplification, a positive feedback latch activated by a clock pulse will turn the latch on
 - The latch will amplify the small input voltage difference to a large signal



11: Comparators [M. Pelgrom, 2017]

Regenerative Latch Delay

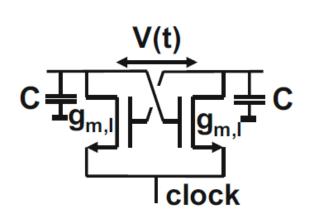


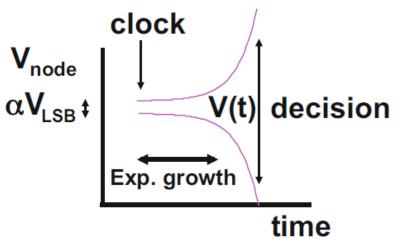
Regenerative Latch Delay

Assume the pre-amplified latch input voltage = $\Delta V_{in} = \alpha V_{LSB}$ (0 < α < 1) $\tau \approx \frac{C}{T}$

$$V(t) = \Delta V_{in} e^{+t/\tau}$$

- The exponential signal growth makes a latch a fast decision element in a regenerative comparator
- The exponential growth will continue until some non-linear limiting mechanism takes action (e.g., approaching power rails)

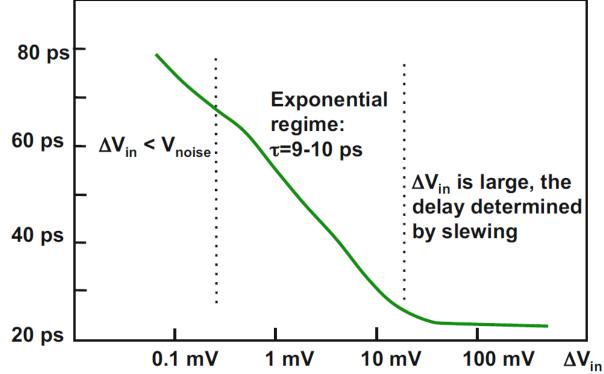




Comparator Delay Example

- The time a comparator or latch needs to form a digital signal depends on the initial overdrive voltage
 - The input differential voltage determines the delay of the comparator

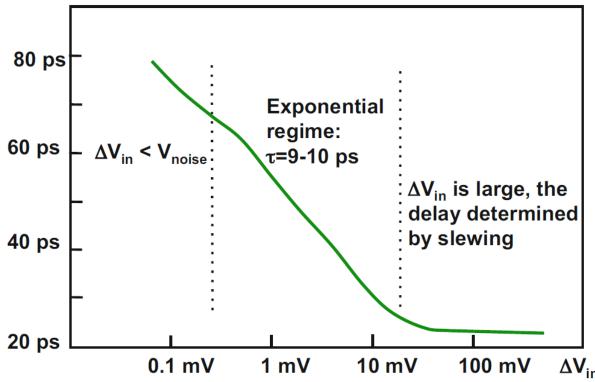
$$V(t) = \Delta V_{in} e^{+t/\tau} \rightarrow t_d = \tau \ln \frac{V_{FS}}{\Delta V_{in}} = \tau (\ln V_{FS} - \ln \Delta V_{in})$$



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Metastability

- For very small overdrive voltages, the comparator cannot reach a decision in the limited time of a half clock period (T_S)
- $oldsymbol{\square}$ The comparator will not generate a clear "zero" or "one" output level after time T_S
- ☐ The succeeding logical circuitry will behave ambiguously



11: Comparators [M. Pelgrom, 2017]

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Bit-Error Rate (BER)

- \Box Assume the pre-amplified latch input voltage = αV_{LSB} (0 < α < 1)
- lacktriangle Assume ambiguity happens when $V(T_S) < V_{FS}$

$$V(T_S) = \alpha V_{LSB} e^{+T_S/\tau} < V_{FS}$$

$$\alpha_{min} = \frac{V_{FS}}{V_{LSB}} e^{-T_S/\tau} = 2^N e^{-T_S/\tau}$$

 \blacksquare Assume V_{in} is uniformly distributed: $0 < \alpha < 1$

$$BER = \alpha_{min} = 2^N e^{-T_S/\tau}$$

Bit-Error Rate (BER)

 \square Assume V_{in} is uniformly distributed: $0 < \alpha < 1$

$$BER = \alpha_{min} = 2^N e^{-T_S/\tau}$$

- From a fundamental point of view the BER cannot be avoided completely
 - But can be made very small (10^{-13}) is possible
- ☐ Measures to improve the BER include:
 - Improving the latch speed with more current and smaller capacitances
 - Additional gain stages or a second latch
 - $\Delta V_{in} = \alpha V_{LSB}$ larger than V_{LSB} (0 < α < A, where A > 1)
 - Using special decoding scheme to avoid large code errors in case of a metastable state

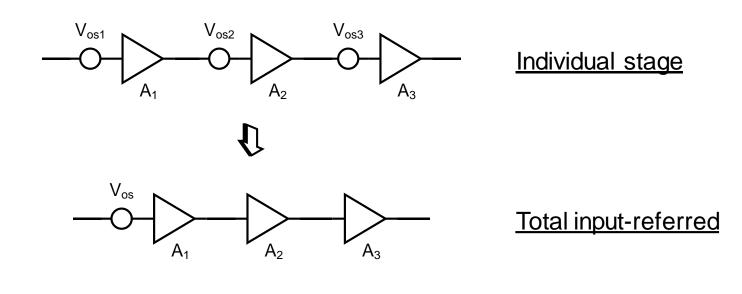
Comparator Offset Voltage

- ☐ In some types of ADCs the static random offset just generates a (random) DC-shift of the entire signal \rightarrow offset error
- ☐ In other types of ADCs the input referred random offset is crucial because it impacts both INL and DNL
 - $0.5LSB > 3\sigma_{in.os}$

Static vs Dynamic Offset

- Offset voltage has static and dynamic components
 - Static offset:
 - 1. Systematic offset (due to systematic mismatch): can be minimized by good design and matched layout
 - 2. Random offset (due to random mismatch): reduced by using large devices but cannot be eliminated (Pelgrom's model)
 - Static offset is dominant in preamplifiers
 - Dynamic offset:
 - Due to imbalanced switching effects and capacitive load mismatch
 - Dynamic offset is dominant in latches

Multistage Preamplifier Offset

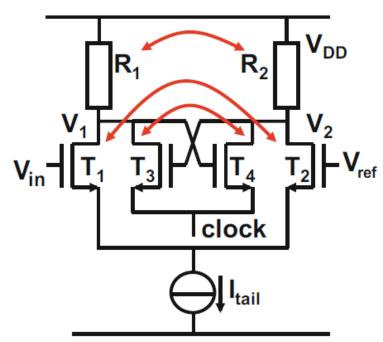


$$A_{T} = A_{1} \cdot A_{2} \cdot A_{3}$$

$$V_{os} = V_{os1} + \frac{V_{os2}}{A_{1}} + \frac{V_{os3}}{A_{1} \cdot A_{2}}$$

Comparator Static Offset

$$\sigma_{Vin}^2 = \sigma_{VT,12}^2 + \frac{g_{m,34}^2}{g_{m,12}^2} \sigma_{VT,34}^2 + \frac{I_{load}^2}{g_{m,12}^2} \frac{\sigma_R^2}{R_{1,2}^2}$$

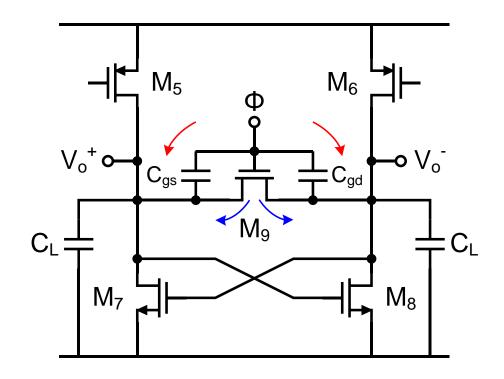


11: Comparators [M. Pelgrom, 2017]

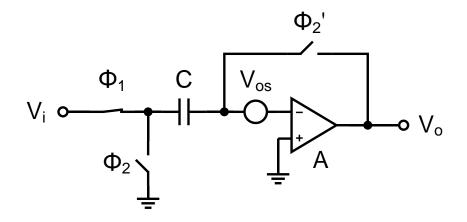
Latch Dynamic Offset

- ☐ M5-6: input pair
- M7-8: cross-coupled load (regenerative)
- ☐ M9: reset switch

- ☐ Dynamic offset due to:
 - Imbalanced CI and CF
 - Imbalanced load capacitance
 - Mismatch between M₅ and M₆
 - Mismatch between M₇ and M₈
 - Clock routing

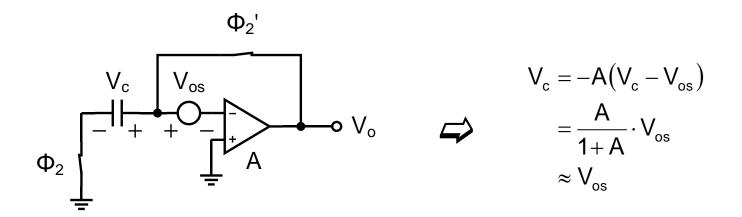


- ☐ AC coupling at input with input-referred offset stored in C
- ☐ Two-phase operation
 - Phase (Φ2) is used to store offset



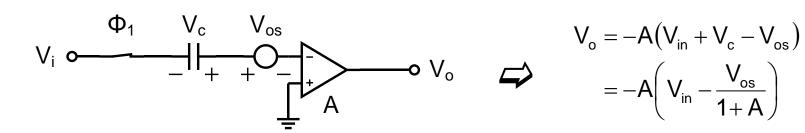
11: Comparators [Y. Chiu, EECT 7327, 2014]

- Offset Storage Phase Φ_2
 - Closed-loop stability required (amplifier in unity-gain feedback)



Ref: J. L. McCreary and P. R. Gray, "All-MOS charge redistribution analog-to-digital conversion techniques. I," JSSC, vol. 10, pp. 371-379, issue 6, 1975.

- Amplifying Phase Φ_1
 - Offset cancellation is incomplete if A is finite
 - Input AC coupling attenuates signal gain

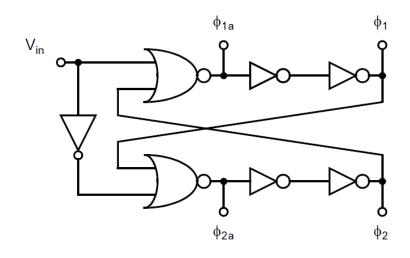


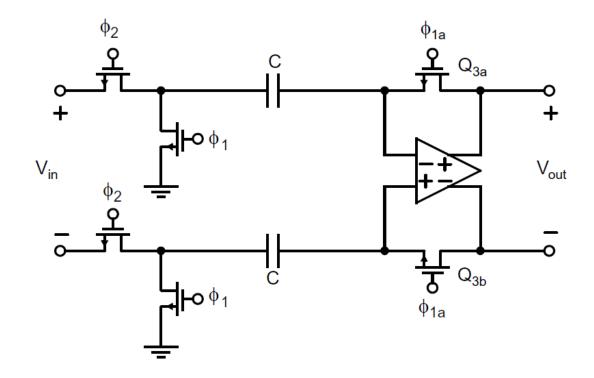
$$V_{o} = -A(V_{in} + V_{c} - V_{os})$$
$$= -A(V_{in} - \frac{V_{os}}{1 + A})$$

Input - referred offset :

$$V_{\text{os,in}} = \, \frac{V_{\text{os}}}{1 + A}$$

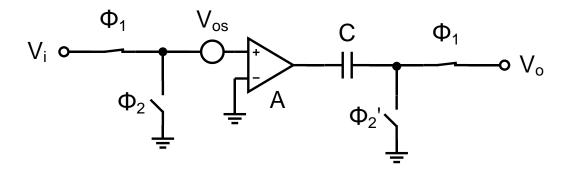
- Fully differential operation to mitigate charge injection and clock feedthrough errors.
 - Necessary for any high precision switched-capacitor integrated circuits





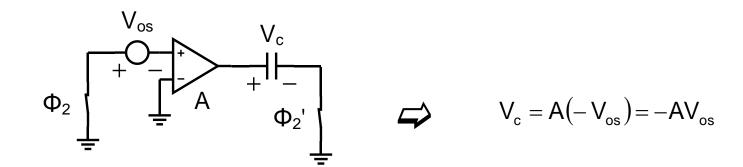
11: Comparators [Johns and Martin, 2012]

- ☐ AC coupling at output with offset stored in C
- The gain (A) must be small and stable (independent of Vo)
- ☐ Does not work for high-gain amplifier



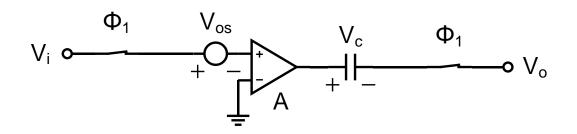
11: Comparators [Y. Chiu, EECT 7327, 2014]

- Offset Storage Φ_2
 - Closed-loop stability is not required
 - CF (clock feedthrough) and CI (charge injection) of Φ2' gets divided by A when referred to input



Ref: R. Poujois and J. Borel, "A low drift fully integrated MOSFET operational amplifier," JSSC, vol. 13, pp. 499-503, issue 4, 1978.

- Amplifying Phase Φ_1
 - Cancellation is complete if A is constant (independent of Vo)
 - AC coupling at output attenuates signal gain



$$V_{o} = A(V_{i} - V_{os}) + AV_{os}$$

$$= AV_{in}$$

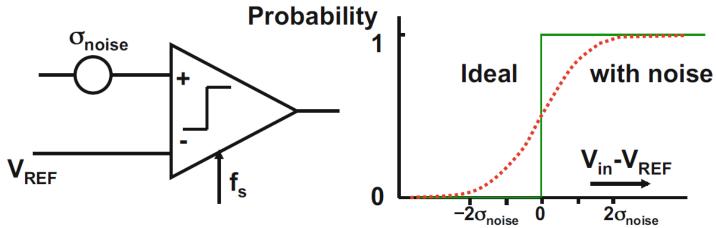
Input - referred offset :
$$V_{os,in} = 0$$

Comparator Noise

- ☐ The input referred noise voltage acts as time varying input offset
- If the thermal noise dominates:

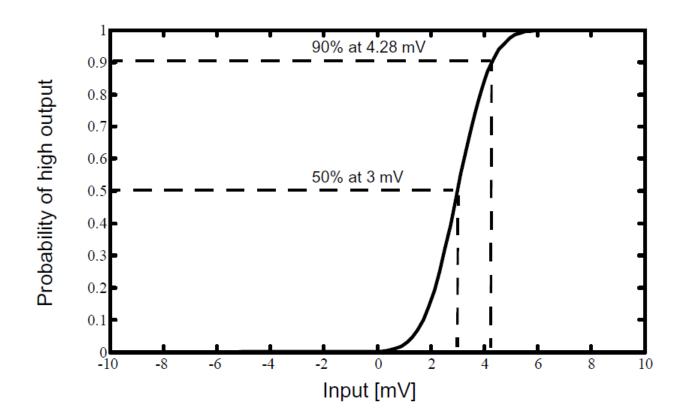
$$v_{nout,rms}^2 = v_{nin}^2(f) \times A_v^2 \times B_N = \frac{4kT\gamma_{eff}}{g_m} \times A_v^2 \times B_N$$
$$v_{nin,rms} = \sqrt{\frac{4kT\gamma_{eff}}{g_m} \times B_N}$$

☐ Trade-off between noise, speed, and power consumption



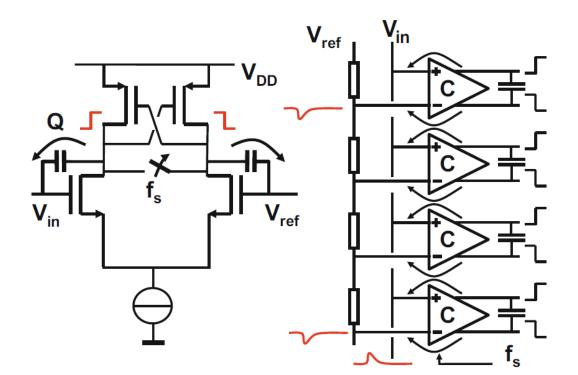
Quiz: Offset and Noise

 \Box Calculate the offset and noise from the shown measured comparator characteristics.



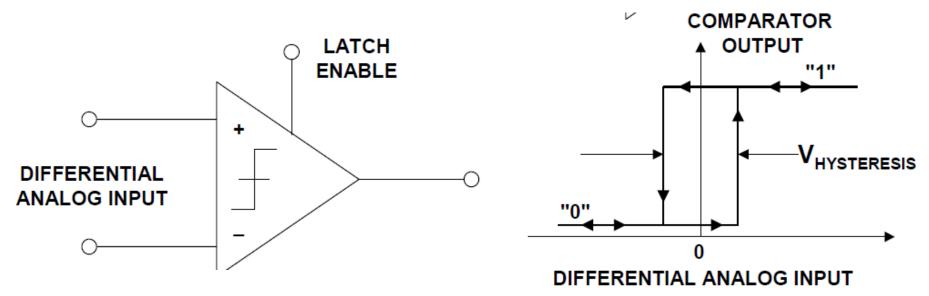
Kickback Noise

- ☐ The output has sharp voltage transitions
- lacksquare C_{gd} will pass these fast edges to V_{in} and V_{ref} causing "kickback"
 - Reference voltage disturbance must settle before next sample
- \square Reducing C_{ad} by reducing sizing will make mismatch worse
- ☐ The output swing can be reduced by using limiting circuits



Hysteresis

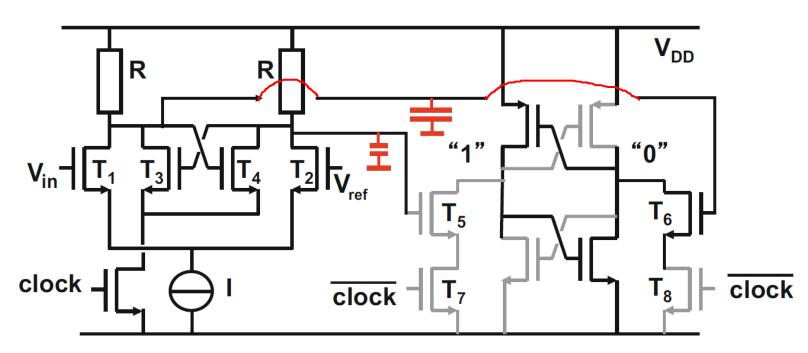
- ☐ Hysteresis: the comparator remembers its previous state.
- ☐ Either intentionally or as an unwanted consequence of the topology.
- Schmitt-trigger comparators use the hysteresis threshold to avoid unwanted transitions in case of noise signals
- ☐ The resolution of the comparator can be no less than the hysteresis
 - Large values of hysteresis are generally BAD for a high resolution comparator



11: Comparators [W. Kester, ADI, 2005]

Hysteresis Example

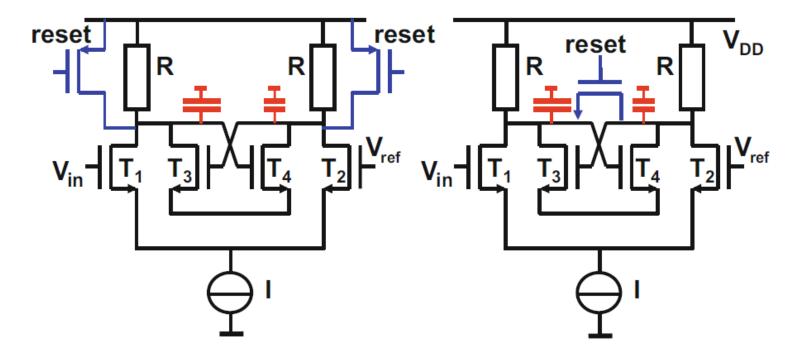
- ☐ A pre-latch stage that is connected to a second stage consisting of a full digital latch activated by the inverse clock
- \Box For the example below: ON transistor (T6) has much higher capacitance than T5
- □ The unequal capacitive loading favors a similar signal in the first latch → The consequence is a comparator with hysteresis.



11: Comparators [M. Pelgrom, 2017]

Removing Hysteresis

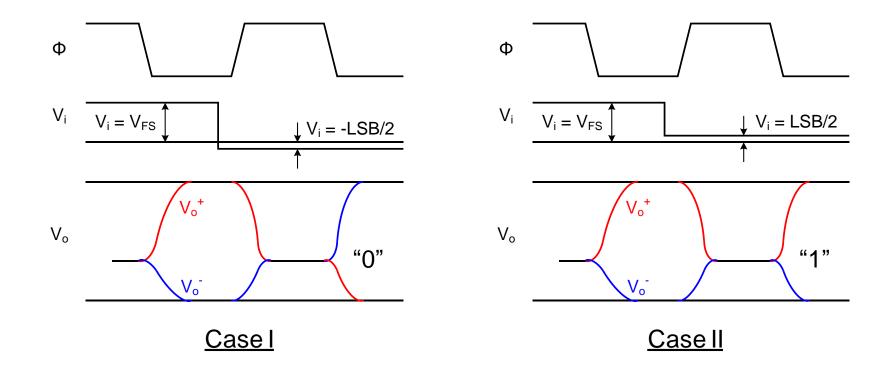
☐ The previous state can be removed by resetting the latch in the comparator



11: Comparators [M. Pelgrom, 2017]

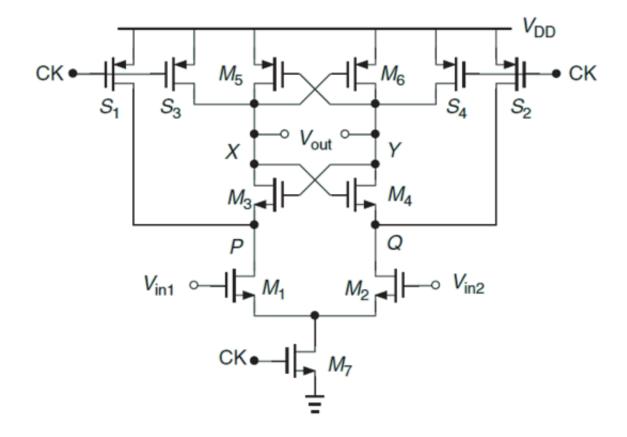
Overdrive Recovery Test

- ☐ A small input (±0.5 LSB) is applied to the comparator input in a cycle right after a full-scale input is applied
 - The comparator should be able to resolve to the right output in either case → memoryless



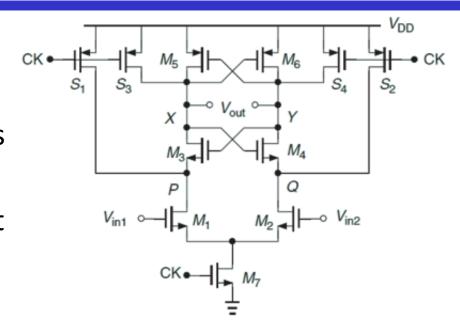
11: Comparators [Y. Chiu, EECT 7327, 2014]

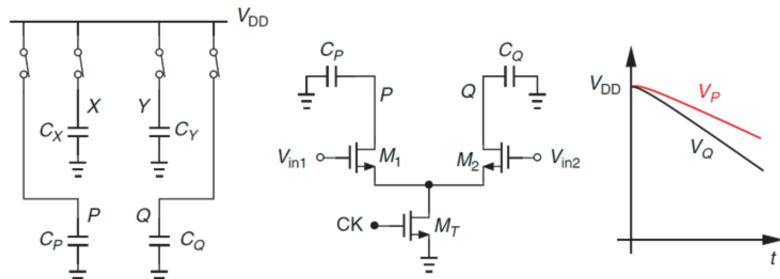
- ☐ A popular latch design used in the StrongARM MPU in the 1990s
 - The input offset is relatively large (pre-amp or calib required)
 - Many modified versions exist



11: Comparators [B. Razavi, 2015]

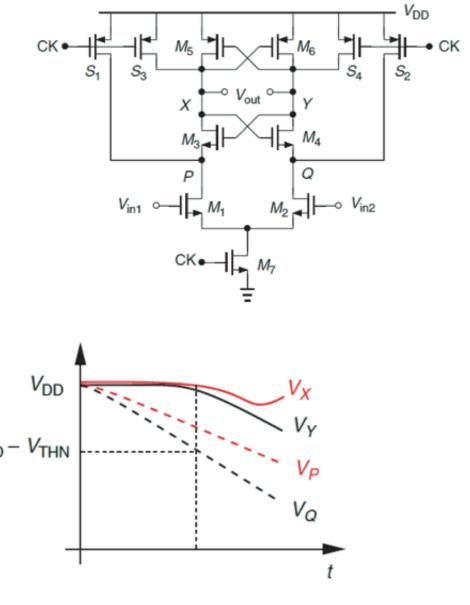
- ☐ Precharge phase: CK = 0
- □ S1-4
 - Reset the latch and remove previous states (hysteresis)
 - Keep M3-6 initially off reducing their offset contribution
- Amplification phase: CK = 1



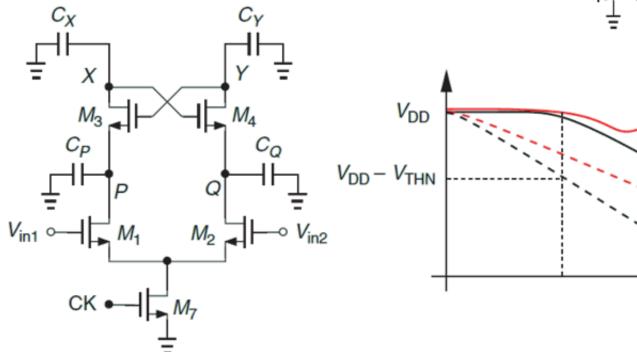


11: Comparators = = = [B. Razavi, 2015]

- NMOS cross-coupled pair (M3,4) turns on
- M3,4 and M5,6 act as cross-coupled CMOS inverters
 - No static current flows

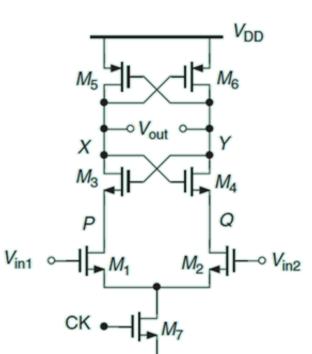


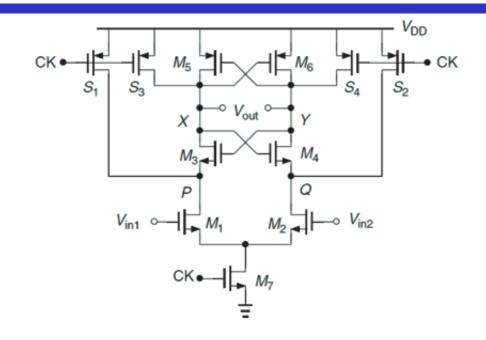
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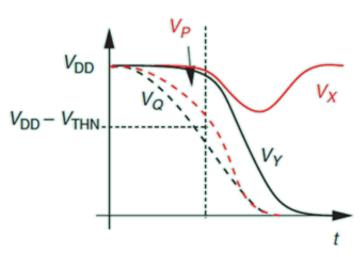


[B. Razavi, 2015] 11: Comparators

- ☐ PMOS cross-coupled pair (M5,6) turns on
- Positive feedback brings one node to VDD and the other to GND





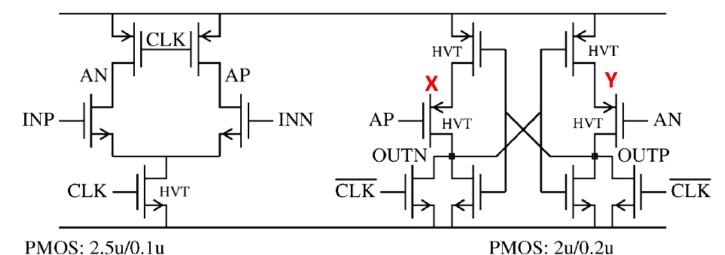


11: Comparators

[B. Razavi, 2015]

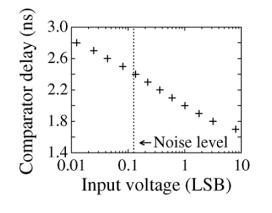
Fast Low-leakage Dynamic Comparator

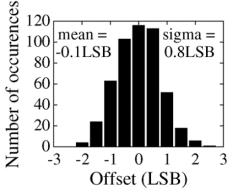
Comparator for low-power 8-bit SAR ADC (LSB = 3.2mV)

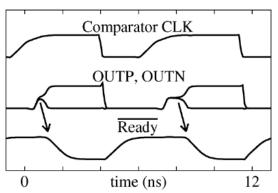


NMOS: 2.5u/0.1u NMOS: 8u/0.4u (Diff. pair), 2.5u/0.2u (Tail switch)

pair), 2.5u/0.2u (Tail switch) NMOS: 0.4u/0.1u







References

- ☐ M. Pelgrom, Analog-to-Digital Conversion, Springer, 3rd ed., 2017.
- W. Kester, The Data Conversion Handbook, ADI, Newnes, 2005.
- T. C. Carusone, D. Johns, and K. W. Martin, "Analog Integrated Circuit Design," Wiley, 2nd ed., 2012.
- ☐ B. Boser and H. Khorramabadi, EECS 247 (previously EECS 240), Berkeley.
- ☐ B. Murmann, EE 315, Stanford.
- ☐ Y. Chiu, EECT 7327, UTD.

Thank you!