

**Carleton University**

**Elec 4700 – Modelling of integrated Device**

**Assignment 1 - Monte-Carlo Modeling of Electron  
Transport**

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## Question 1: Electron Modelling

The purpose of this code is to demonstrate the use of MATLAB to determine certain values and graphs. As you can see from the code, this question displays a solution to how electrons are modelled in a silicon as particles with a given effective mass, temperature, and other constants & variables. Using these givens, we were able to define the *thermal velocity* "Vt" (assuming temperature was 300 K), the *mean free path* "MFP", while the rest of this section shows the code to print and model the random motion of electrons given some specific requirements.

### Q) What is the thermal velocity $v_{th}$ ? Assume $T = 300K$ ?

Ans) The thermal velocity, assuming T = 300K, is 132.24 km/s.

### Q) If the mean time between collisions is $T_{mn} = 0.2$ ps what is the mean free path?

Ans) The mean free path, assuming a mean time of 0.2ps, is 26.45 nm.

Program code:

```
%% Part 1:Electron Modelling

Mo    = 9.1093837e-31; %electron rest mass
Mn    = 0.26*Mo;        %effective electron mass
Temp  = 300;            %temp in kelvin
K     = 1.38064853e-23;% boltzmann's constant

%q1:What is the thermal velocity vth? Assume T = 300K.
V_th = sqrt(K*Temp/Mn);%thermal velocity calculation
V_display = V_th*1e-3;
%answer for thermal velocity
fprintf('The thermal velocity, assuming T = 300K, is %.2f km/s. \n',
V_display);

%q2:If the mean time between collisions is Tmn = 0.2 ps what is the mean free path?
T_min = 0.2e-12; %Mean time
MFP   = V_th*T_min; % mean free path
MFP_display = MFP*1e9;
%answer for the mean free path
fprintf('The mean free path, assuming a mean time of 0.2ps, is %.2f nm.\n',
MFP_display)

%q3:Write a program that will model the random motion of the electrons
L = 200e-9;%length
W = 100e-9;%Width
popSize = 20; %Electron population size
popPlot = 5; % number of subset particles on plot
time = W/V_th/100;
iter = 1000;
sim_OnOff = 1;% intialize simulation to 1 (ON), if its 0 (OFF)

%intiallize matrices and vectors
```

```

matrix1 = zeros (popSize, 4);
col = 2*popPlot;
ZE = zeros (iter, col);
ZE1 = zeros (iter,1); %1000*1 vector of zeros

%populate the figure randomly
for i = 1:popSize
    theta = rand*2*pi; % angle
    a = L*rand; b = W*rand; c = V_th*cos(theta); d = V_th*sin(theta);
    matrix1(i,:) = [a b c d];% recal: matrix1(row, column), so matrix1 (i,:)
entire thing of row i
end

%changes/iteration in matrix 1 over time
for i = 1:iter
    nextMat = time.*matrix1(:,3:4);
    matrix1(:,1:2) = matrix1(:,1:2) + nextMat;
    h = matrix1(:,1) > L;

    %calculation for matrix if greater than length
    matrix1(h,1) = matrix1(h,1) - L;
    h = matrix1(:,1) < 0;
    matrix1(h,1) = matrix1(h,1) + L;
    % calculation for matrix if greater than width
    h = matrix1(:,2) > W;
    matrix1(h,2) = 2*W - matrix1(h,2);
    matrix1(h,4) = -1*matrix1(h,4);

    h = matrix1(:,2) < 0;
    matrix1(h,2) = -1 * matrix1(h,2);
    matrix1(h,4) = -1 * matrix1(h,4);

    semiCon = Mn/K/popSize; ab = sum(matrix1(:,3).^2); cd =
sum(matrix1(:,4).^2);
    ZE1(i) = (ab + cd)*semiCon;

    %track the zeros (ZE)
    for h=1:popPlot
        s=2*h;
        ZE(i,(s):(s+1)) = matrix1(h, 1:2);
    end

    %create a simulation for every 5 changes
if sim_OnOff && mod(i,5)==0

    figure(1);
    hold on;
    plot(matrix1(1:popPlot,1)./1e-9, matrix1(1:popPlot,2)./1e-9, 'x');
    axis([0 L/1e-9 0 W/1e-9]);
    title(sprintf('Zeros for %d particles of %d Electrons with Fixed Velocity
(Part 1)',popPlot, popSize));
    xlabel(' x - (nm)');
    ylabel(' y - (nm)');

    if i > 1
        figure (2);
        hold on;

```

```

plot(time *(0:i-1), ZE1(1:i));
axis([0 time *iter min(ZE1)*0.98 max(ZE1)*1.02]);
title('Semiconductor at fixed Temperature (Part 1)');
xlabel('Time (s)');
ylabel('Temp (K)');
end
pause(0.05);
end
end

figure(1);
title(sprintf('Zeros for %d particles of %d Electrons with Fixed Velocity
(Part 1)',...
popPlot, popSize));
xlabel('x (nm)');
ylabel('y (nm)');
axis([0 L/1e-9 0 W/1e-9]);
hold on;

for i=1:popPlot
    f=i*2;
    plot(ZE(:,f)./1e-9, ZE(:,f+1)./1e-9, '-');
end

if(~sim_OnOff)
    figure (2);
    hold off;
    plot(time *(0:iter-1), ZE1);
    axis([0 time *iter min(ZE1)*0.98 max(ZE1)*1.02]);
    title(' N-type Si semiconductor at fixed Temperature');
    xlabel('Time (s)');
    ylabel('Temp (K)');
end

```

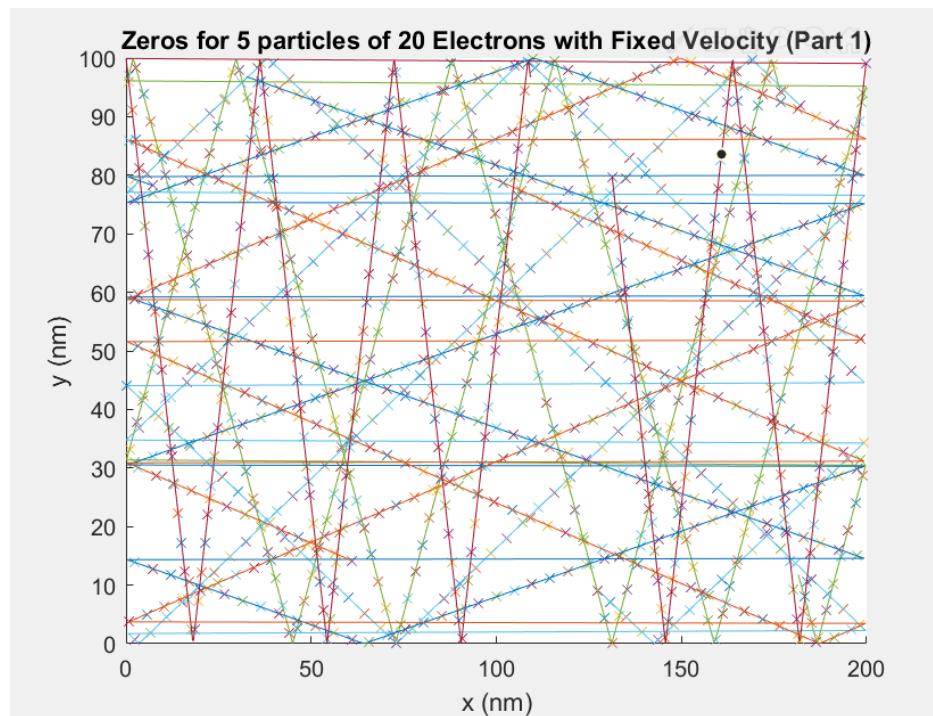


Figure 1: 2D plot of Particle Trajectory

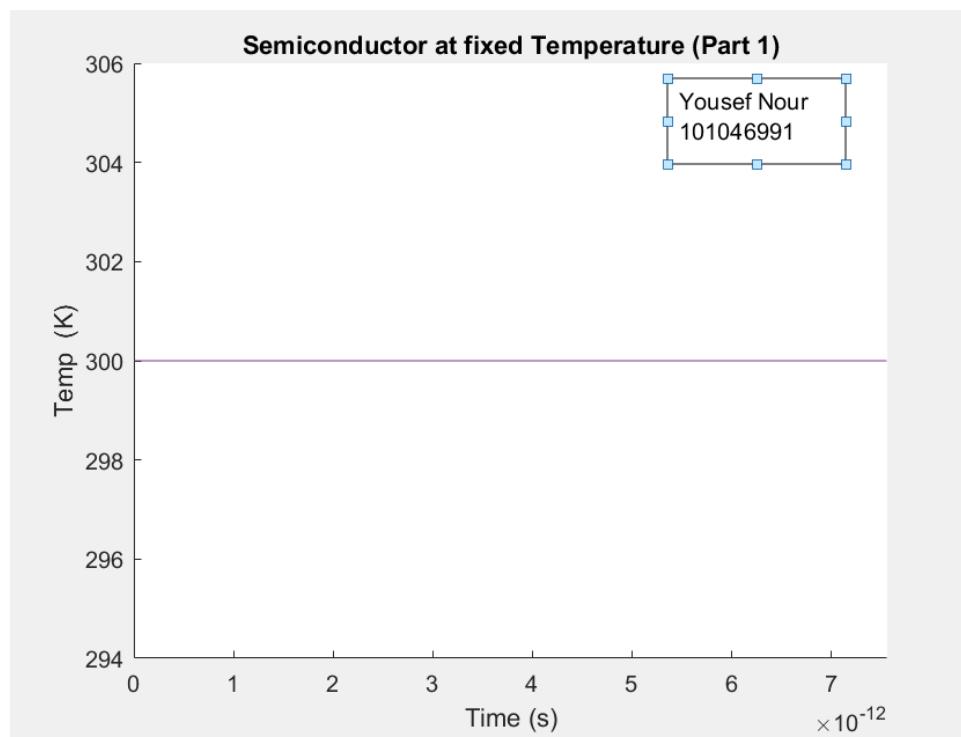


Figure 2: Temperature Plot

## Question 2: Collisions with Mean Free Path (MFP)

This part of the assignment focuses on assigning a random velocity to each of the particles at the start. Moreover, it models the scattering of the electrons using an exponential scattering probability.

Program code:

```
%% Part 2: Collisions with Mean Free Path

%Q2:Model the scattering of the electrons using an exponential scattering
probability
pScat = 1-exp(-1*time/0.2e-12);
%Create a Probability Distribution
distVal = sqrt(K*Temp/Mn);
pdfVol = makedist('Normal', 'mu', 0, 'sigma', distVal);% recal
makedist(DISTNAME,,PNAME1,PVAL1)

for i = 1:popSize
    theta = rand*2*pi;
    c = random(pdfVol);
    matrix1(i,:) = [a b c c];% recal: matrix1(row, column), so matrix1 (i,:)
entire column of row i
end

%Q3:What happens to the average temperature over time
avgTemp = sqrt((ab/popSize) + (cd/popSize));
fprintf('over time the average temp becomes: %f K.\n',avgTemp);

%Q4:Measure the actual Mean Free Path and mean time between collisions to
verify your model.

for i = 1:iter
    %record electron positions
    nextMat = time .*matrix1(:,3:4);
    matrix1(:,1:2) = matrix1(:,1:2) + nextMat;

    h = matrix1(:,1) > L;
    matrix1(h,1) = matrix1(h,1) - L;

    h = matrix1(:,1) < 0;
    matrix1(h,1) = matrix1(h,1) + L;

    h = matrix1(:,2) > W;
    matrix1(h,2) = 2 * W - matrix1(h,2);
    matrix1(h,4) = -1 * matrix1(h,4);

    h = matrix1(:,2) < 0;
    matrix1(h,2) = -1 * matrix1(h,2);
    matrix1(h,4) = -1 * matrix1(h,4);

    % spread out electrons
```

```

h = rand(popSize, 1) < pScat;
matrix1(h,3:4) = random(pdfVol, [sum(h),2]);

% Record the ZE1
semiCon = Mn/K/2/popSize; ab = sum(matrix1(:,3).^2); cd =
sum(matrix1(:,4).^2);
ZE1(i) = (ab + cd)*semiCon;

% Record positions of each electron movement thorughout the simulation
for h=1:popPlot
    ZE(i, (2*h):(2*h+1)) = matrix1(h, 1:2);
end

% Update the simulation every 5 iterations
if sim_OnOff && mod(i,5) == 0
    figure(3);
    hold on;
    plot(matrix1(1:popPlot,1)./1e-9, matrix1(1:popPlot,2)./1e-9, 'x');
    axis([0 L/1e-9 0 W/1e-9]);
    title(sprintf('Zeros for %d of %d Electrons (Part 2)',...
    popPlot, popSize));
    xlabel(' x-(nm)');
    ylabel(' y-(nm)');
end

if i > 1
    figure (4);
    hold off;
    plot(time *(0:i-1), ZE1(1:i));
    axis([0 time *iter min(ZE1)*0.98 max(ZE1)*1.02]);
    title('Semiconductor Temperature changes for every zero (Part 2)');
    xlabel('Time (s)');
    ylabel('ZE1 (K)');
end

% histogram speeds
figure (5);
w = sqrt(matrix1(:,3).^2 + matrix1(:,4).^2);
title('Histogram of Electron Speeds');
histogram(w);
xlabel('Speed (m/s)');
ylabel('particles');
pause(0.05);
end

% Show Zeroes after the simulation is over
figure(3);
title(sprintf('Zeros for %d of %d Electrons (Part 2)',...
popPlot, popSize));
xlabel('x-(nm)');
ylabel('y-(nm)');
axis([0 L/1e-9 0 W/1e-9]);
hold on;

for i=1:popPlot
plot(ZE(:,i*2)./1e-9, ZE(:,i*2+1)./1e-9, '-');
end

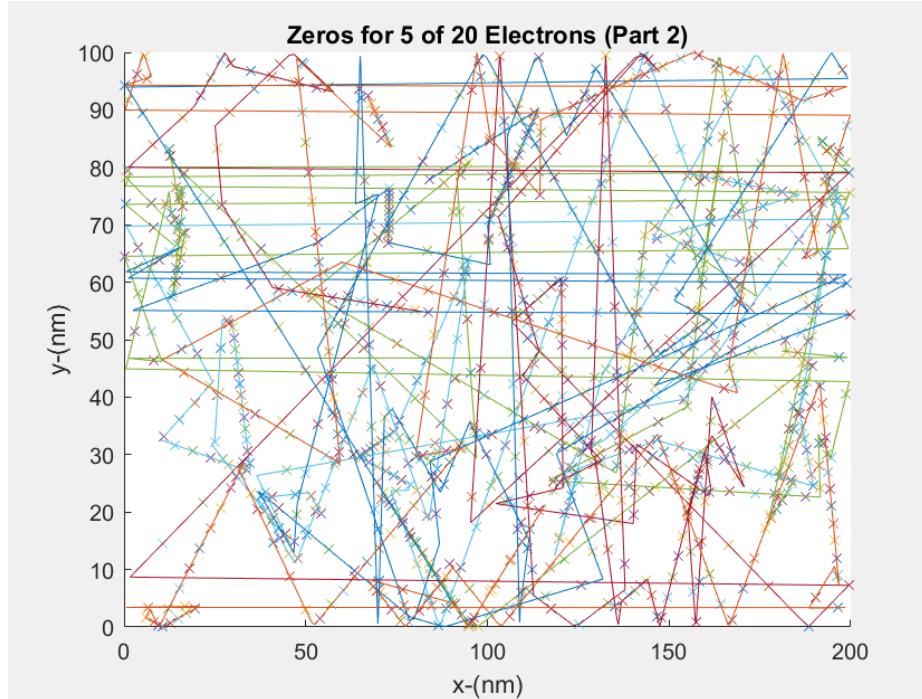
```

```

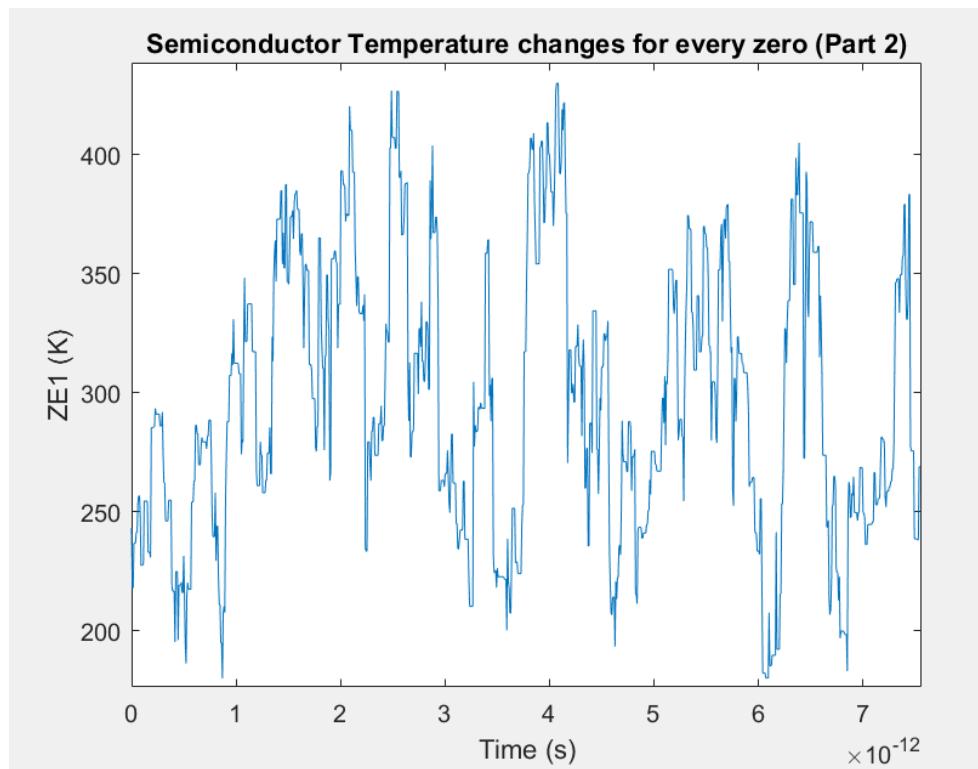
if(~sim_OnOff)
figure (4);
hold off;
plot(time *(0:iter-1), ZE1);
axis([0 time *iter min(ZE1)*0.98 max(ZE1)*1.02]);
title('Semiconductor Temperature changes for every zero (Part 2)');
xlabel('Time (s)');
ylabel('ZE1 (K)');
end

% Histogram intial electron speed
figure (5);
hold on;
title('Electron Speeds Histogram');
w = sqrt(matrix1(:,3).^2 + matrix1(:,4).^2);
histogram(w);
xlabel('Speed (m/s)');
ylabel('Number of particles');

```



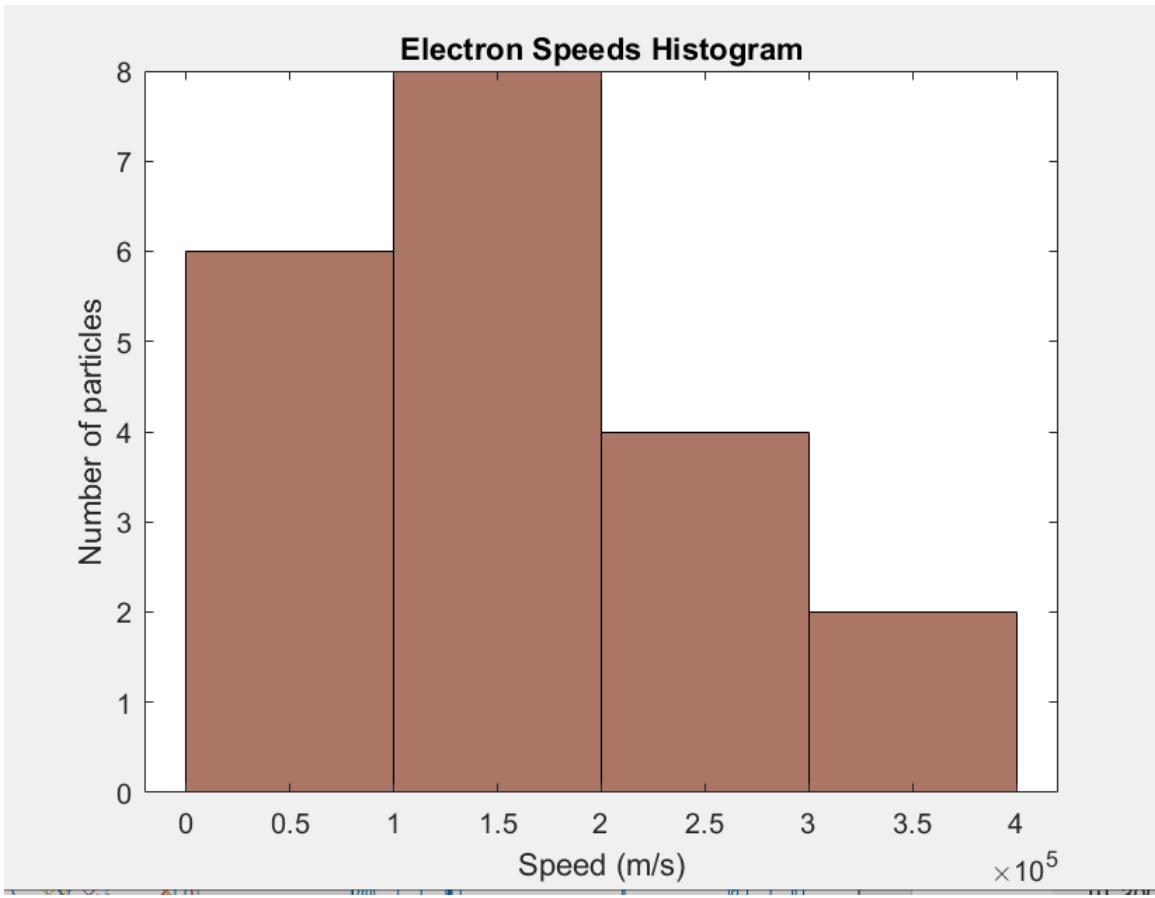
*Figure 3: 2D plot of Particle Trajectory*



*Figure 4: Temperature Plot*

**Q) What happens to the average temperature over time?**

As seen in figure 4, the temperature varies widely but does not surpass 500K or goes below 100k. Over time the average temp becomes: 132.242 K.



*Figure 5: Histogram Plot of Particle Speeds*

### Question 3: Enhancements

This portion of the assignment adds in the inner rectangle "bottle neck" boundaries to model a similar particle behaviour as the previous part of the assignment. Making all boundaries capable to be either specular or diffusive.

Program Code:

```
%% Part 3: Enhancements

sqr = 1e-9.*[80 120 0 40; 80 120 60 100];
boxes = [0 1];

for i = 1:iter
    nextMat = time .*matrix1(:,3:4);
    matrix1(:,1:2) = matrix1(:,1:2) + nextMat;

    h = matrix1(:,1) > L;
    matrix1(h,1) = matrix1(h,1) - L;

    h = matrix1(:,1) < 0;
    matrix1(h,1) = matrix1(h,1) + L;
```

```

h = matrix1(:,2) > w;
topVal =0;
bottomVal =0;

if(topVal)
    matrix1(h,2) = 2*w - matrix1(h,2);
    matrix1(h,4) = -1*matrix1(h,4);
else
% The electron recoils off at random angle
matrix1(h,2) = w;
b = sqrt(matrix1(h,3).^2 + matrix1(h,4).^2);
theta = rand([sum(h),1])*2*pi;
matrix1(h,3) = b.*cos(theta);
matrix1(h,4) = -1*abs(b.*sin(theta));
end

h = matrix1(:,2) < 0;

if(bottomVal)
    matrix1(h,2) = -1*matrix1(h,2);
    matrix1(h,4) = -1*matrix1(h,4);
else
% The electron recoils off at a random angle
matrix1(h,2) = 0;
b = sqrt(matrix1(h,3).^2 + matrix1(h,4).^2);
theta = rand([sum(h),1])*2*pi;
matrix1(h,3) = b.*cos(theta);
matrix1(h,4) = abs(b.*sin(theta));
end

% Scatter particles
h = rand(popSize, 1) < pScat;
matrix1(h,3:4) = random(pdfVol, [sum(h),2]);

semiCon = Mn/K/2/popSize; ab = sum(matrix1(:,3).^2); cd =
sum(matrix1(:,4).^2);
ZE1(i) = (ab + cd) * semiCon;

% Record positions of subset particles that will be graphed
for h=1:popPlot
    ZE(i, (2*h):(2*h+1)) = matrix1(h, 1:2);
end

% Update the simulation every 5 iterations
if sim_OnOff && mod(i,5) == 0

figure(6);
hold on;
plot(matrix1(1:popPlot,1)./1e-9, matrix1(1:popPlot,2)./1e-9, 'x');
%hold on;

% Plotting the square
for h=1:size(sqr,1)
    plot([sqr(h, 1) sqr(h, 1) sqr(h, 2) sqr(h, 2) sqr(h, 1)]./1e-9, ...
        [sqr(h, 3) sqr(h, 4) sqr(h, 4) sqr(h, 3) sqr(h, 3)]./1e-9, 'k-');

```

```

end

axis([0 L/1e-9 0 W/1e-9]);
title(sprintf('Zeros for %d of %d Electrons (Part 3)',popPlot, popSize));
xlabel('x - (nm)');
ylabel('y - (nm)');

if i > 1
    figure (7);
    hold on;
    plot(time *(0:i-1), ZE1(1:i));
    axis([0 time *iter min(ZE1(1:i))*0.98 max(ZE1)*1.02]);
    title('Semiconductor ZE1');
    xlabel('Time (s)');
    ylabel('ZE1 (K)');
end

figure (8);
hold on;
title('Electron Speeds Histogram');
b = sqrt(matrix1(:,3).^2 + matrix1(:,4).^2);
histogram(b);
xlabel('Speed (m/s)');
ylabel('Number of particles');
pause(0.03);
end

figure (6);
plot(matrix1(1:popPlot,1)./1e-9, matrix1(1:popPlot,2)./1e-9, 'x');
axis([0 L/1e-9 0 W/1e-9]);
title(sprintf('Zeros for %d of %d Electrons (Part 3)',popPlot, popSize));
xlabel('x - (nm)');
ylabel('y - (nm)');
hold on;

figure (7);
plot(time *(0:i-1), ZE1(1:i));
axis([0 time *iter min(ZE1(1:i))*0.98 max(ZE1)*1.02]);
title('Semiconductor ZE1');
xlabel('Time (s)');
ylabel('ZE1 (K)');
hold on;

figure (8);
hold on;
title('Electron Speeds Histogram');
b = sqrt(matrix1(:,3).^2 + matrix1(:,4).^2);
histogram(b);
xlabel('Speed (m/s)');
ylabel('Number of particles');

```

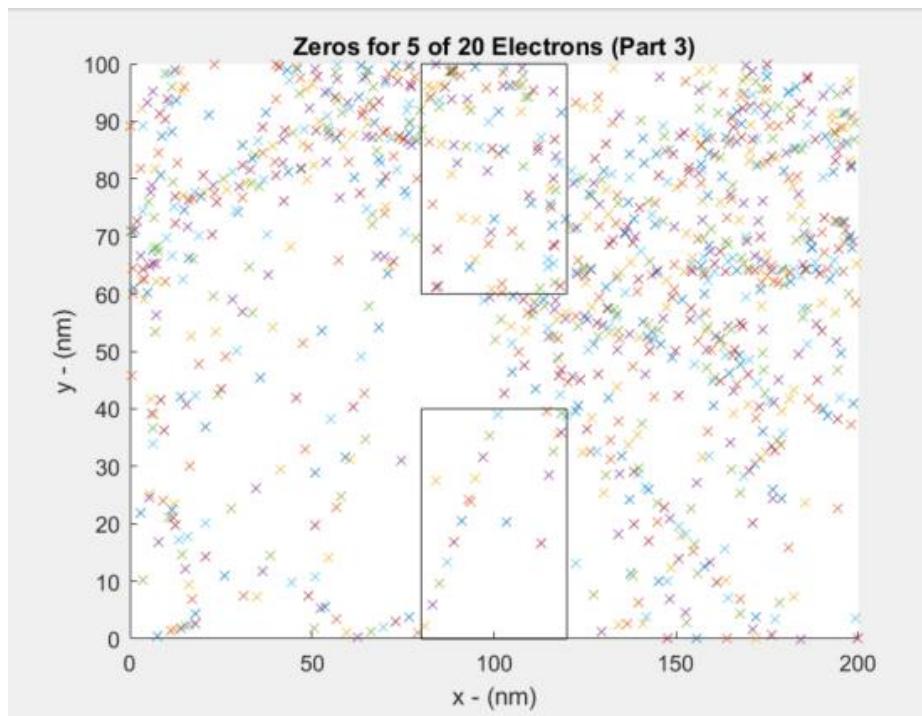


Figure 6: Particle Trajectory With “bottle-neck”

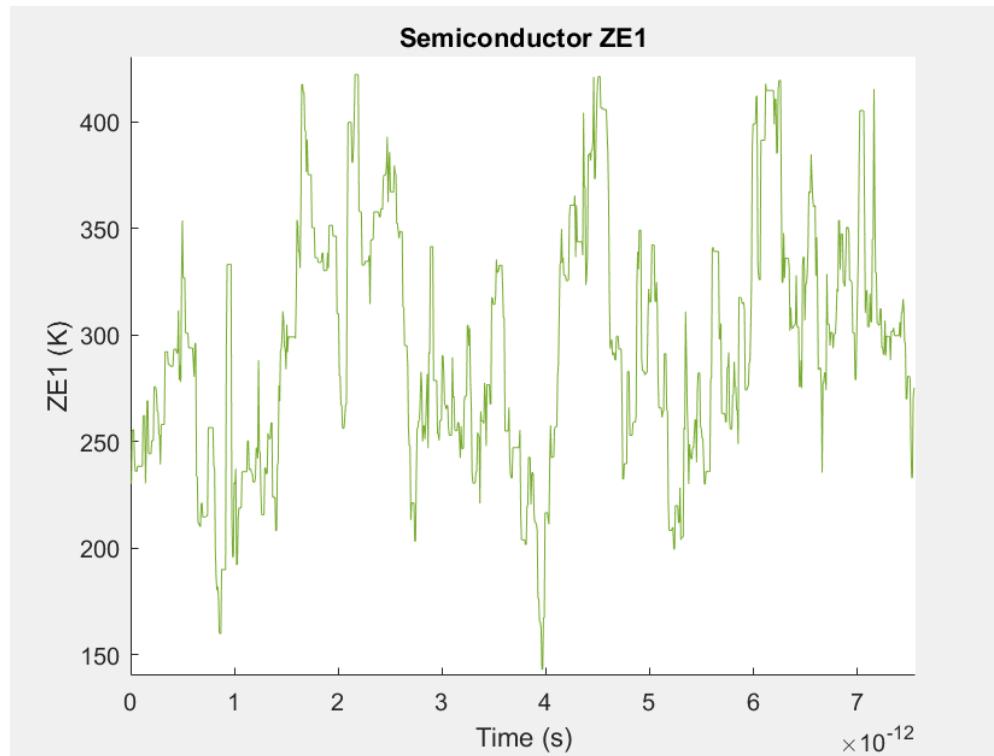


Figure 7: Temperature Plot

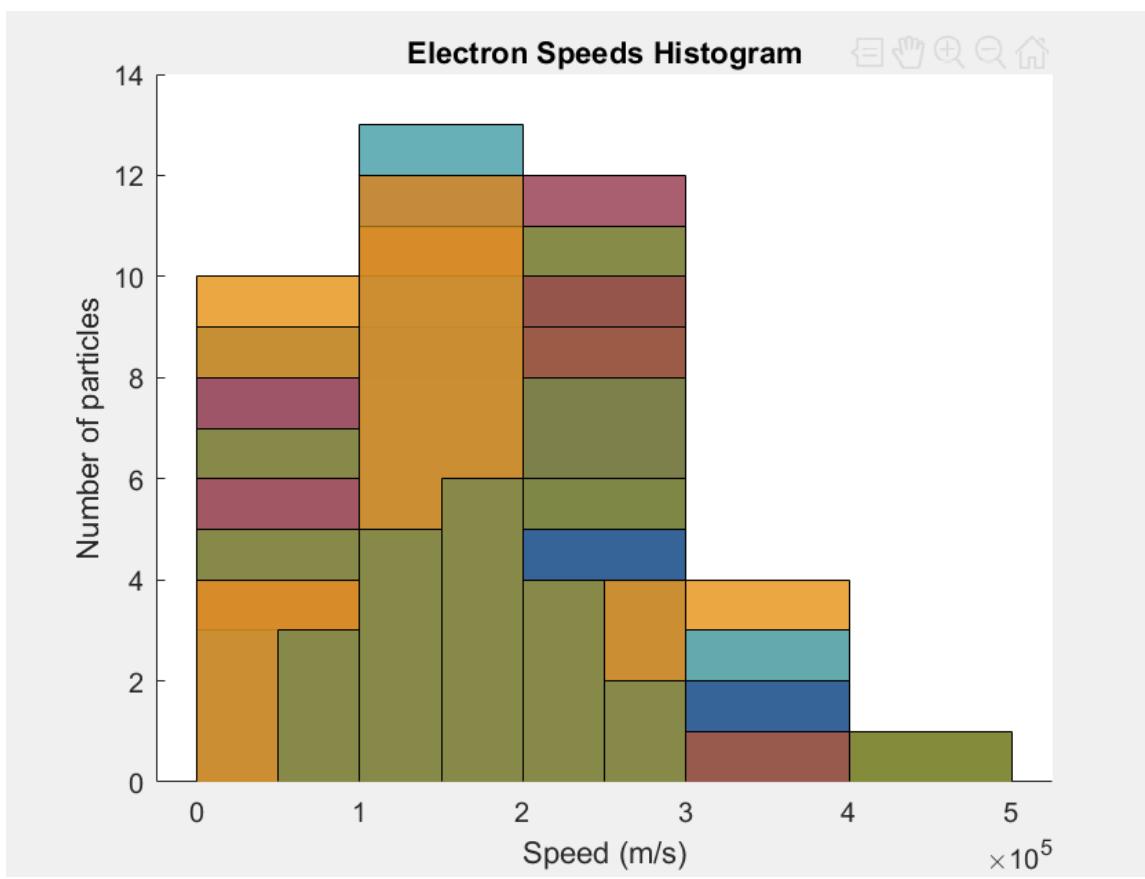


Figure 8: Histogram Plot of Particle Speeds