

Final Progress Report: Quantum Clustering Educational Module

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1 Executive Summary

This final report presents the complete development of a quantum clustering educational module across two major milestones. Milestone 1 established the foundational framework covering classical and quantum clustering concepts, while Milestone 2 addressed key feedback and implemented significant improvements to enhance the learning experience. The result is a comprehensive educational module that effectively bridges classical machine learning concepts with quantum computing applications in clustering algorithms.

2 Project Overview

The quantum clustering educational module aims to provide students with a practical introduction to quantum machine learning concepts, specifically focusing on clustering algorithms. The module combines theoretical content with hands-on coding exercises, progressing systematically from classical approaches to quantum implementations while maintaining educational effectiveness and student engagement.

3 Milestone 1: Foundation Development

3.1 Initial Implementation Scope

Milestone 1 established the foundation for the quantum clustering educational module, building a comprehensive learning experience that covers both classical and quantum approaches to clustering algorithms.

3.2 Core Components Implemented

3.2.1 Introduction to Clustering and Quantum Clustering

Created a complete introduction section that explains:

- What clustering is and why it matters
- Basic concepts of unsupervised machine learning
- Introduction to quantum computing applications in clustering
- Overview of quantum advantages in machine learning

3.2.2 Classical K-Means Clustering

Built a comprehensive section covering classical approaches:

- Literature review of traditional k-means algorithms
- Code demonstration with implementation on synthetic data
- MCQ quiz to test student understanding of classical concepts

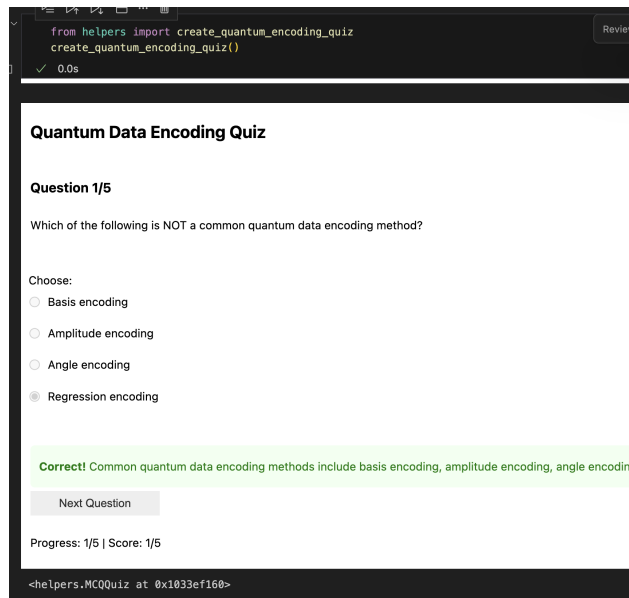


Figure 1: MCQ quiz in jupyter notebook

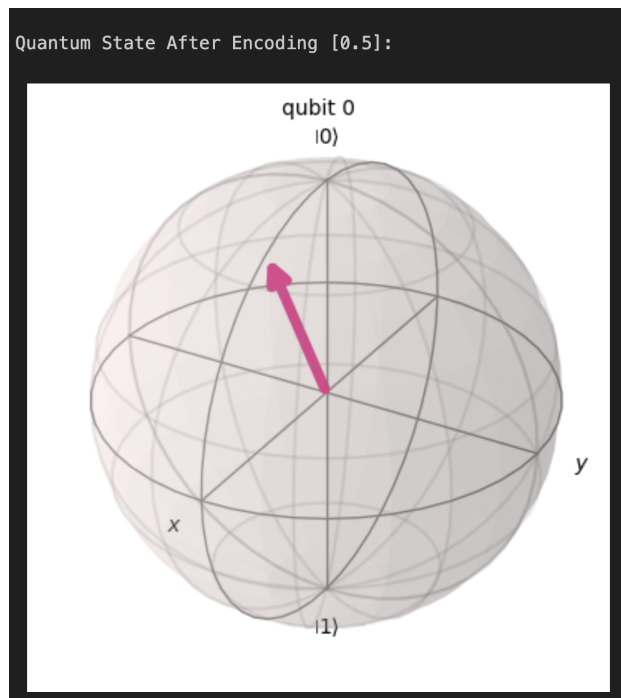


Figure 2: Bloch sphere visualization in jupyter notebook

3.2.3 Quantum Encoding Strategies

Developed content on quantum data encoding:

- Literature review of quantum encoding methods
- Code demonstrations with visual representations
- Circuit diagrams showing quantum encoding processes
- Bloch sphere visualizations to show quantum states
- MCQ quiz covering quantum encoding concepts

3.2.4 Quantum K-Means Implementation

Created the core quantum clustering content:

- Literature review of quantum k-means algorithms
- Code demonstration implementing quantum k-means on synthetic data
- Used state fidelity as the distance metric for quantum similarity
- Analysis section explaining quantum advantages and limitations
- Swap test implementation for quantum distance computation
- Code demo showing swap test on synthetic data
- MCQ quiz testing quantum k-means understanding

3.2.5 Practical Challenges Section

Added real-world considerations:

- Discussion of current quantum hardware limitations
- Noise and error considerations in quantum implementations
- Scalability challenges for quantum clustering
- Comparison between classical and quantum performance

3.2.6 Educational Structure

Organized content for effective learning:

- Clear progression from classical to quantum concepts
- Multiple assessment points throughout the module
- Interactive coding components
- Visual aids and demonstrations

4 Milestone 2: Enhancement and Refinement

4.1 Addressing Feedback and Improvements

Milestone 2 focused on addressing key problems identified from Milestone 1 feedback and implementing significant improvements to enhance the educational effectiveness of the module.

4.2 Key Improvements Implemented

4.2.1 Enhanced Data Representation

Replaced oversimplified synthetic data with more realistic, messy datasets:

- Changed from too-perfect data to messy synthetic data
- Demonstrates why clustering algorithms are necessary
- Provides students with a more realistic learning experience
- Better reflects real-world data challenges

4.2.2 Improved Conceptual Explanations

Added explanations for quantum concepts that were insufficient in Milestone 1:

- Comprehensive analysis of quantum K-means implementation with angle encoding
- Clear explanation of fidelity and its mathematical formula
- Introduction to Swap Test for distance computation
- Explanation of why Swap Test is more sophisticated than direct fidelity measurement
- Enhanced theoretical foundations for quantum concepts

4.2.3 Comprehensive Benchmarking Section

Added a dedicated section comparing classical and quantum clustering performance:

- Benchmarking the performance of classical and quantum clustering algorithms
- Silhouette score comparison between approaches
- Inertia (Sum of Squared Errors) comparison
- Runtime comparison and analysis
- Discussion of when each approach is most effective

4.2.4 Complete Exercise Framework

Developed a comprehensive exercise section with structured learning activities:

- Code templates that students fill in to reinforce learning
- Helpful hints and guidance when students encounter difficulties
- Exercises designed for different skill levels (easy and advanced)
- Progressive difficulty to build confidence and competence

8.2 - Implement a Simple Quantum K-means Step

Fill in the blanks to assign each data point to the nearest centroid using quantum similarity.

```
# Assume X_scaled is your dataset and centroids is a numpy array of current centroids
# Both are already angle-encoded/scaled appropriately

def assign_clusters(X_scaled, centroids):
    n_samples = X_scaled.shape[0]
    n_clusters = centroids.shape[0]
    labels = np.zeros(n_samples, dtype=int)
    for i in range(n_samples):
        similarities = []
        for j in range(n_clusters):
            # TODO: Compute quantum similarity between X_scaled[i] and centroids[j]
            # sim = ...
            similarities.append(sim)
        # TODO: Assign to the cluster with the highest similarity (or lowest distance)
        # labels[i] = ...
    return labels
```

▼ Hint 1: Similarity Calculation

Use your `quantum_similarity` function from Exercise 1.

► Hint 2: Cluster Assignment

Figure 3: Exercise section in jupyter notebook

4.2.5 Visual Algorithm Guide

Created a comprehensive visual flowchart illustrating the quantum clustering process:

- Step-by-step visual representation of the quantum clustering algorithm
- Clear process flow that helps students understand the methodology

- Enhanced visual learning support for complex concepts

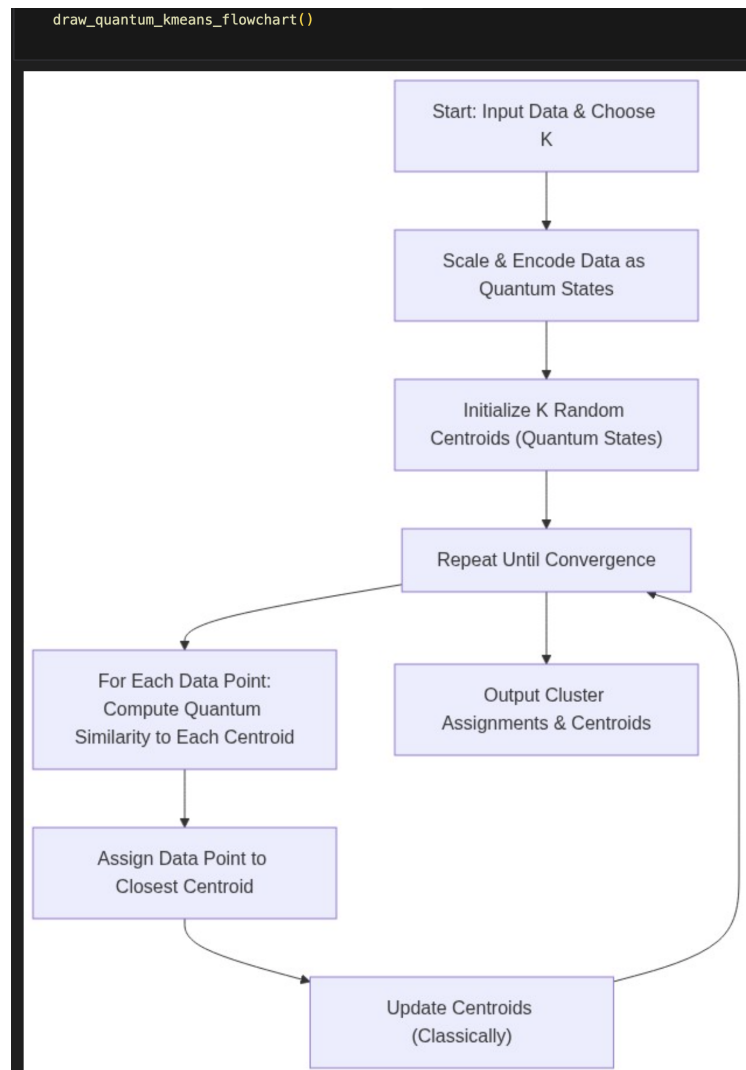


Figure 4: Algorithm flow chart

4.2.6 Enhanced Introduction to Unsupervised Learning

Added foundational content to support student preparation:

- Simple, accessible explanation of unsupervised learning concepts
- Provides necessary background knowledge before diving into clustering
- Bridges the gap between general machine learning and specific clustering applications
- Ensures all students have adequate preparation regardless of background

5 Final Module Components

The completed quantum clustering educational module now includes:

5.1 Theoretical Foundation

- Introduction to unsupervised learning
- Classical clustering algorithms and theory
- Quantum computing principles relevant to clustering
- Quantum encoding strategies and implementations

5.2 Practical Implementation

- Classical K-means implementation with realistic data
- Quantum K-means implementation with angle encoding
- Swap test implementation for quantum distance computation
- Comprehensive benchmarking framework

5.3 Assessment and Engagement

- Multiple-choice quizzes throughout the module
- Hands-on coding exercises with templates and hints
- Visual learning aids including Bloch sphere visualizations
- Algorithm flowcharts for process understanding

5.4 Advanced Topics

- Discussion of quantum hardware limitations
- Noise and error considerations in quantum implementations
- Scalability challenges and future directions
- Comparative analysis of classical vs. quantum approaches

6 Final Submission Enhancements

Following the completion of Milestone 2, additional improvements were implemented to address remaining feedback and enhance the educational value of the module.

6.1 Explanation of Algorithm Behavior

Added a comprehensive section explaining why classical and quantum clustering results appear similar:

- Discussed dataset characteristics (bimodal, linearly separable nature)
- Explanation of how quantum similarity measures behave for simple datasets
- Discussion of low feature complexity limitations in 2D space
- Clear guidance on when quantum clustering advantages would emerge:
 - High-dimensional data spaces
 - Complex, non-linear cluster boundaries
 - Graph-based or combinatorial problems
 - Constrained optimization scenarios

This addition helps students understand that the similar performance is expected behavior rather than a limitation of the implementation, providing important context for interpreting results.

6.2 Corrected Visualization Labels

Fixed visualization issues identified in feedback:

- Corrected plot labels to properly show "Classical K-means Clustering" vs "Quantum K-means Clustering"
- Ensured accurate side-by-side comparison of both approaches
- Maintained consistent color schemes and formatting across visualizations

6.3 Interactive Learning Components

Implemented interactive visualization features to enhance student engagement:

- Created an interactive slider widget for dynamic cluster number selection
- Real-time visualization updates as students adjust the number of clusters
- Enhanced understanding of how cluster number affects algorithm performance

These interactive components provide students with immediate feedback and encourage experimentation, making the learning experience more engaging and intuitive.

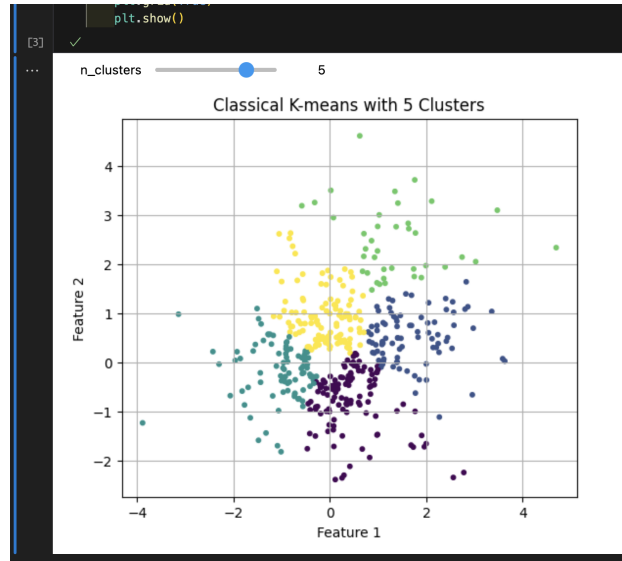


Figure 5: Interactive slider for cluster number selection

6.4 Quantum Spectral Clustering

Implemented quantum spectral clustering:

- Demo on limitation of k-means clustering on circular data
- Classical spectral clustering refresher
- Attempt quantum spectral clustering on circular data
- MCQ quiz on spectral clustering
- Coding exercise on quantum spectral clustering similarity matrix

7 Educational Impact and Outcomes

The final quantum clustering educational module:

- Provides a comprehensive introduction to quantum machine learning concepts
- Bridges classical and quantum clustering approaches effectively
- Offers hands-on experience with realistic datasets and challenges
- Includes multiple assessment and engagement mechanisms
- Supports diverse learning styles through visual, textual, and interactive content
- Prepares students for advanced study in quantum machine learning

8 Conclusion

The development of this quantum clustering educational module across two milestones has resulted in a comprehensive learning resource that effectively combines theoretical foundations with practical implementation experience. The improvements made in Milestone 2 addressed key feedback points and significantly enhanced the educational value of the module.

The final product provides students with a solid foundation in both classical and quantum clustering concepts, hands-on coding experience, and the analytical tools needed to compare and evaluate different approaches. Through a combination of theoretical content, practical exercises, visual aids, and assessment mechanisms, the module introduces students to the exciting field of quantum machine learning while maintaining educational rigor and accessibility.

This module serves as an effective bridge between classical machine learning concepts and emerging quantum computing applications, preparing students for the future of computational intelligence and quantum-enhanced algorithms.