

Lecture 18

Negative Numbers in Binary

We use modular arithmetic, so for a 4-bit binary number,

$$5 - 1 = 5 + (-1) = 5 + 15 = 4$$

if we ignore the final carry.

- There are different ways to implement this, e.g. 2's complement that we use, where given n bits, $-k = 2^n - k$
 - Example: $n = 4, k = 1 \Rightarrow -k = 15$
 - Example: $n = 4, k = 6, \Rightarrow -k = 10$
 - Example: $n = 5, k = 13, \Rightarrow -k = 19$
- The maximum value that can be represented is then reduced by half, where the first bit denotes the sign
- To represent the same number with more bits, extend the required number of bits on the left by the first digit, e.g.
 - $0b1011 = 0b1111011$
 - $0b0011 = 0b00000011$
- Short cut calculation: $-k = \sim k + 1$
 - e.g. $2 = 0b0010, -2 = 0b1110$
 - e.g. $1 = 0b0001, -1 = 0b1111$

Addition/Subtraction

- using the same adder as before
- supply 1 input mux to decide addition or subtraction
- output = $A + B \wedge \text{mux} + \text{mux}$ (second mux acts as carry in)

Overflow

- $7+1$ in a 4-bit signed binary becomes -8
- If members have opposite signs, overflow cannot occur
- overflow is equivalent to $s_{n-1} \wedge \text{cout}$ for an n -bit signed binary