

```
%%% inline
%%%% inlineBackend.figure_format = 'retina'
%%%% ipynbwidgets.interact
%%%% tensorflow tf
%%%% matplotlib.pyplot plt
%%%% pandas pd
%%%% sklearn.preprocessingMinMaxScaler
%%%% keras.modelsSequential
%%%% keras.layersDense, LSTM, Dropout, GRU, CuDNNLSTM, Flatten
%%%% math
%%%% sklearn.metricsmean_squared_error
%%%% tensorflow.keras.modelsmean_squared_error
%%%% tensorflow.keras.layersActivation, Dense, Dropout, LSTM
%%%% matplotlib.pyplot plt
%%%% pandas pd
%%%% sklearn.metricsmean_absolute_error
%%%% numpy np
%%%% numpy pi
%%%% tensorflow tf
```

```
In (3): class Particle_Tracking_Training_Data(tf.Module):
    def __init__(self, Nt, rings=1000):
        self.Nt = int(Nt)
        self.Ny = self.Nx = 100
        self.d = 1
        ximg = [1, 1] for i in np.arange(self.Ny):
            for j in np.arange(self.Nx):
                self.ximg = np.float32(ximg)

        x = np.arange(self.Nx) - self.Nx//2
        y = np.arange(self.Ny) - self.Ny//2
        XO, YO = np.meshgrid(x, y)
        self.X = np.float32(XO)
        self.Y = np.float32(YO)

    def rings:
        self.ring_indicator = 1

    def rings:
        self.ring_indicator = 1

    def gen_video = tf.function(
        input_signature=
            tf.TensorSpec(
                shape=self.Ny, self.Nx, self.Nt, dtype=tf.float32),
                tf.TensorSpec(
                    shape=self.Nt, dtype=tf.float32),
                tf.TensorSpec(
                    shape=1, dtype=tf.float32),
                tf.TensorSpec(
                    shape=1, dtype=tf.float32),
                tf.TensorSpec(
                    shape=1, dtype=tf.float32),
                )(self, gen_video)

    def gen_labels = tf.function(
        input_signature=
            tf.TensorSpec(
                shape=self.Ny, self.Nx, self.Nt, dtype=tf.float32),
                )(self, gen_labels)

    def call(self, kappa, a, lbacklevel, Nparticles, sigma_motion):
        ## random brownian motion paths
        ## Nt, Nparticles, 3
        xi = self.sample_motion(Nparticles, sigma_motion)

        ### translate track positions to img coords
        XALL = (self.ximg[:, :, None, None, :]
                - xi[:, None, None, :, :])
        ## Ny, Nx, Nt, Np
        r = tf.math.sqrt(XALL**2 + Y**2)
        z = xi[:, :, :, :]

        ## generate video
        I = self.gen_video(r, z, kappa, a, lbacklevel)

        ## generate labels
        labels = self.gen_labels(r)

        return I, labels, xi

    @staticmethod
    def randn(n):
        return tf.random.uniform(n, dtype=tf.float32)

    def function(
        input_signature=
            tf.TensorSpec(
                shape=1, dtype=tf.int32),
                tf.TensorSpec(
                    shape=1, dtype=tf.float32),
                )(self, nparticles, sigma_motion):
        ## boundaries
        b_lower = tf.constant(
            [-1, -1, -1], tf.float32)
        b_upper = tf.constant(
            [self.Nx+1, self.Ny+1, 1], tf.float32)
        ## uniform random initial positions
        U = tf.random.uniform(
            1, Nparticles, self.d,
            dtype=tf.float32)
        XO = b_lower + b_upper * U
        ## normal increments
        dX = tf.random.normal(
            self.Nt, Nparticles, self.d,
            stddev=sigma_motion,
            dtype=tf.float32)
        ## unbounded Brownian motion
        X = XO + tf.math.cumsum(dX, axis=1)
        ## reflected brownian motion
        ## note that this is imperfect,
        ## if increments are very large it wont work
        X = tf.math.abs(X - b_lower) + b_lower
        X = -tf.math.abs(X - b_upper) + b_upper
        return X

    def gen_video(self, r, z, kappa, a, lbacklevel):
        uw = (1 + self.rand())/2
        un = tf.floor(*self.rand())
        uampRing = uw + un * self.rand()
        ufade = uw + *self.rand()
        rmax = ufade * un/uw ** (1/2)
        ufadeMax = 1 - ufade
        ffade = (1 - ufadeMax * tf.abs(tf.tanh(z/ufade)))
        core = tf.exp(-r**2 / a**2)
        ring = ffade * tf.exp(-r**2 / a**2)
        + *uampRing * tf.cast(k<2, tf.float32)

        I = tf.transpose(
            tf.reduce_sum(
                ffade * core + self.ring_indicator * ring,
                axis=1),
            [1, 2, 3]) # Nt, Ny, Nx
        I = lbacklevel * tf.sin(
            self.rand() * pi / 10 * tf.sqrt(
                self.rand() * self.X - self.rand() * self.Y
                + self.rand() * self.Y - self.rand() * self.X))
        I = tf.random_normal(
            self.Nt, self.Ny, self.Nx,
            stddev=kappa,
            dtype=tf.float32)
        lmin = tf.reduce_min(I)
        lmax = tf.reduce_max(I)
        I = (I - lmin) / (lmax - lmin)
        I = tf.round(I * tf.imaximum(100, tf.round(100 * self.rand())))
        return I

    def gen_labels(self, r):
        R_detect = 1
        ## (Ny, Nx, Nt)
        detectors = tf.reduce_sum(
            tf.cast(R_detect, [1, 1, 1]) < R_detect, tf.int32,
            axis=1)
        ## (Nt, Ny, Nx)
        P = tf.transpose(
            tf.cast(detectors > tf.int32, [1, 2, 3])
            ## (Nt, Ny, Nx, 2)
            labels = tf.stack(["P", "I", 1])
            return labels
```

```
In (4): Nt = 1000 ## number of frames for each video
kappa = 1.0 ## standard deviation of background noise added to image
a = 1.0 ## scale factor for the size of particle spots (not true size of particles)
lbacklevel = 1.0 ## relative intensity of randomly generated background pattern in [0, 1]
Nparticles = 10 ## the number of particles (more = slower)
sigma_motion = 1.0 ## the standard deviation for particle brownian motion; should be in [0, 10]

pt = Particle_Tracking_Training_Data(Nt) ## create object instance
vid, labels, tracks = pt(kappa, a, lbacklevel, Nparticles, sigma_motion)
```

Generating the Data

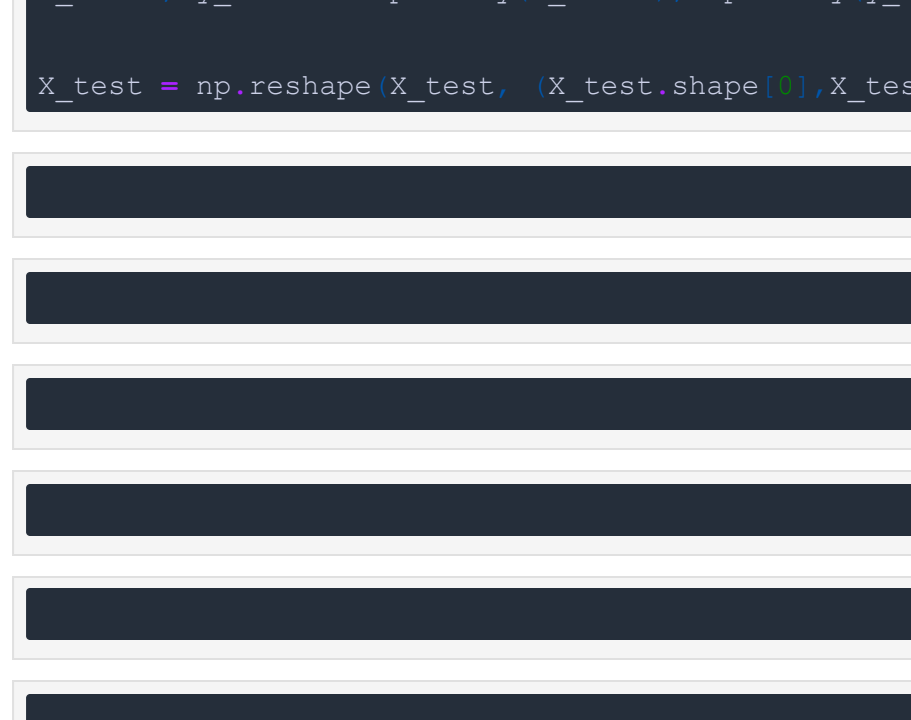
```
In (7): %matplotlib inline
fig = plt.figure(figsize=(10, 10))
imshow(vid[0], origin='lower')
plt.colorbar(vid[0], 255)
```

Detecting the Particles

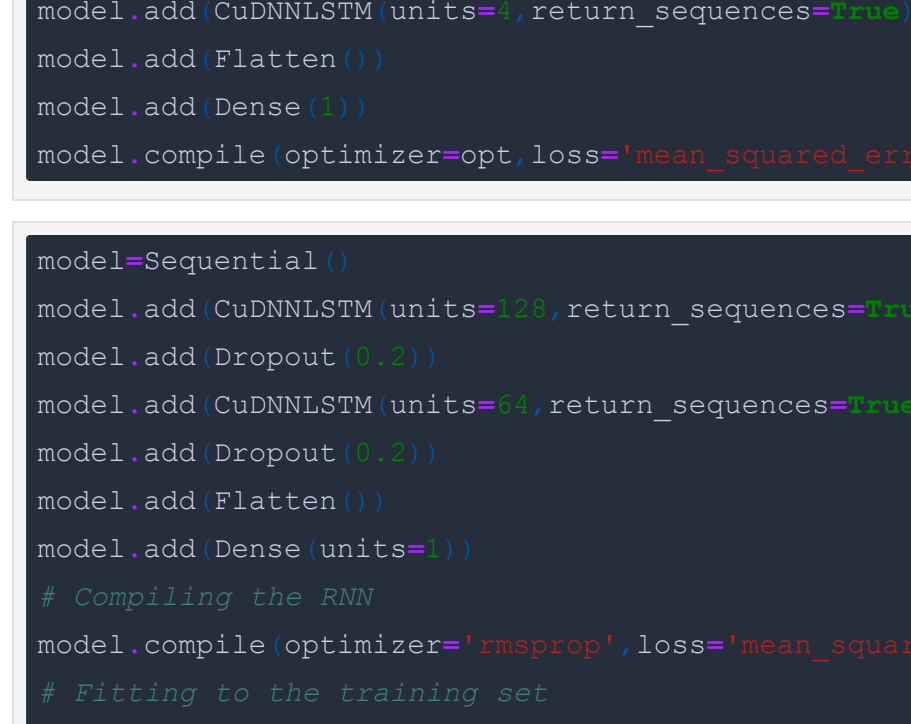
```
In (5): %matplotlib inline
fig = plt.figure(figsize=(10, 10))
imshow(vid[0], origin='lower')
plt.show_tracks(
    plot_tracks(t, 1, 1, tracks[t, 1, 1, :]),
    xlim=(0, 250),
    ylim=(0, 250))
```

Tracking the Particles

```
In (9): figure(figsize=(10, 10))
plot_tracks(1, 1, 1, tracks[1, 1, 1, :])
#ylim(-12, 300)
#ylim(-12, 300)
xlabel('X', fontsize=16)
ylabel('Y', fontsize=16)
```



```
In (11): figure(figsize=(10, 10))
plot_tracks(1, 1, 1, tracks[1, 1, 1, :])
#ylim(-12, 300)
#ylim(-12, 300)
xlabel('X', fontsize=16)
ylabel('Y', fontsize=16)
```



```
In (13): X=np.array(tracks[:, :, 1])
X_scaled=(X-np.mean(X))/np.std(X)
Y=np.array(tracks[:, :, 1])
Y_scaled=(Y-np.mean(Y))/np.std(Y)
```

```
In (16): def get_data(data):
    a_train=[]
    b_train=[]
    for i in range(len(data)):
        a_train.append(data[i][0])
        b_train.append(data[i][1])
    a_train, b_train = np.array(a_train), np.array(b_train)
    return a_train, b_train
```

```
In (17): X_train, y_train=get_data(X_scaled)
X_test, y_test=get_data(X_scaled)
Xy_train, yy_train=get_data(Y_scaled)
Xy_test, yy_test=get_data(Y_scaled)
```

```
In (18):
```

```
In (24): X_train = []
y_train = []
X_train_scaled=X_scaled
y_train_scaled=y_scaled
for i in range(len(X_scaled)):
    X_train.append(X_scaled[i])
    y_train.append(y_scaled[i])
X_train, y_train = np.array(X_train), np.array(y_train)
```

```
In (24): Xy_train = []
yy_train = []
Xy_train_scaled=Y_scaled
yy_train_scaled=yy_scaled
for i in range(len(X_scaled)):
    Xy_train.append(X_scaled[i])
    yy_train.append(yy_scaled[i])
Xy_train, yy_train = np.array(Xy_train), np.array(yy_train)
```

```
In (18): X_test = []
y_test = []
for i in range(len(X_scaled)):
    X_train.append(X_scaled[i])
    y_train.append(y_scaled[i])
X_train, y_train = np.array(X_train), np.array(y_train)
X_test = np.reshape(X_test, X_test.shape[1], X_test.shape[1, 1])
```

```
In (18):
```

```
In (18):
```

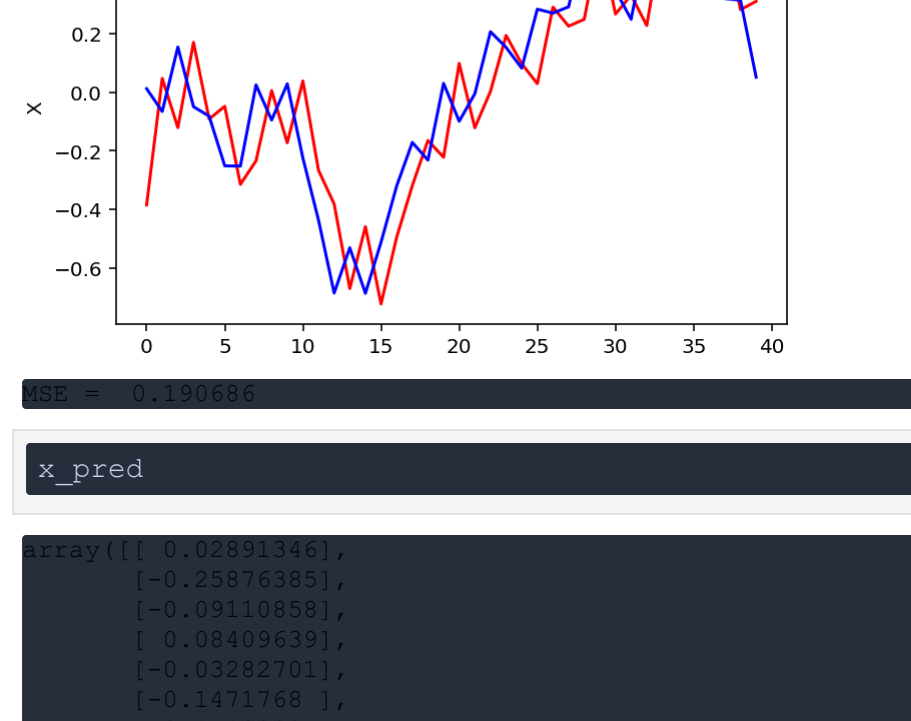
```
In (21):
```

```
In (18):
```

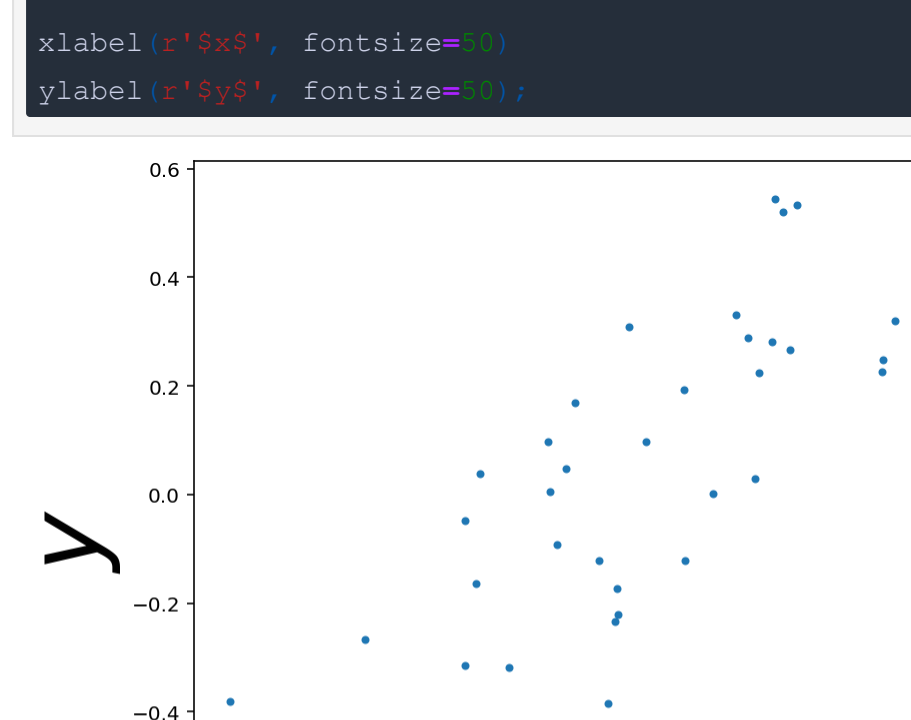
```
In (17): opt=tf.keras.optimizers.RMSprop
learning_rate=0.001
model=Sequential()
model.add(CuDNNLSTM(units=256,return_sequences=True))
model.add(CuDNNLSTM(units=128,return_sequences=True))
model.add(Dropout(0.2))
model.add(CuDNNLSTM(units=32,return_sequences=True))
model.add(CuDNNLSTM(units=16,return_sequences=True))
model.add(CuDNNLSTM(units=8,return_sequences=True))
model.add(CuDNNLSTM(units=4,return_sequences=True))
model.add(Flatten())
model.add(Dense(1))
model.compile(optimizer=opt,loss='mean_squared_error',metrics=['mean'])
```

```
In (17): model=Sequential()
model.add(CuDNNLSTM(units=16,return_sequences=True, input_shape=X_train.shape[1, 1]))
model.add(Dropout(0.2))
model.add(CuDNNLSTM(units=8,return_sequences=True))
model.add(Dropout(0.2))
model.add(Flatten())
model.add(Dense(units=1))
# compiling the RNN
model.compile(optimizer='rmsprop', loss='mean_squared_error')
# Fitting to the training set
model.fit(Xy_train, yy_train, epochs=10, batch_size=10)
```

```
In (17): model.fit(Xy_train, yy_train, epochs=10, batch_size=10, validation_data=(Xy_test[1, 1], yy_test[1, 1]))
y_pred=model.predict(Xy_test)
```

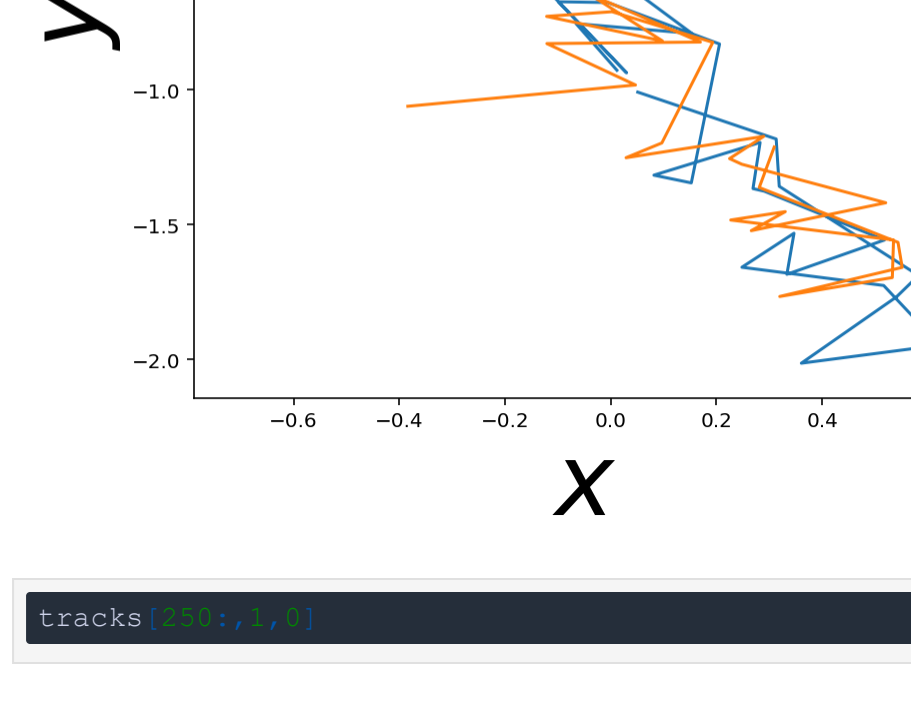


```
In (17): model.fit(X_train, y_train, epochs=10, batch_size=10, validation_data=(X_test[1, 1], y_test[1, 1]))
x_pred=model.predict(X_test)
```



```
In (17):
```

```
In (17): figure(figsize=(10, 10))
plot(y_test, yy_test)
#ylim(30, 200)
#ylim(30, 200)
xlabel('X', fontsize=16)
ylabel('Y', fontsize=16)
```



```
In (22): tracks = []
```



```
Out [227]: array([[140.96302, 1.170254, 142.06786, 143.26241, 144.45728, 145.64977,
146.84324, 1.5847, 147.95018, 149.20059,
143.422, 1.395462, 144.1718, 147.70264, 147075, 149.94284,
149.1231, 1.548424, 152.08219, 147.30364, 147187, 148.4038,
146.19507, 1.348817, 144.95454, 145.3479, 1.17107, 141.64603,
142.65339, 1.30685, 147.15245, 147.89957, 1.523137, 146.45193,
146.42144, 1.18735, 143.46026, 145.62779, 1.33328, 148.47315,
146.88373, 1.234402, 147.31697, 150.4178, 1.03902, 149.02409,
146.66056, 149.40681, 149.66666666666667])
```

In [242]:

```
values
```

Out [242]:

```
array([[150.90189,
150.52213],
[149.27074],
[151.90591],
[153.61559],
[152.69919],
[152.30331],
[152.88086],
[150.40813],
[149.56044],
[148.60457],
[148.90338],
[148.6731, ],
[151.69829],
[150.46283],
[148.69049],
[150.74453],
[152.71347],
[152.6237, ], dtype=float64])
```

In [243]:

```
y_test
```

Out [243]:

```
array([142.67259, 144.04805, 147.02259, 141.04807, 145.02157, 144.01191,
145.42044, 145.24105, 143.46936, 145.62778, 147.04528, 146.47115,
146.88373, 144.29462, 147.31657, 150.4178, 150.03002, 149.02409,
146.66056, 149.40681, 149.66666666666667])
```

In []: