# Lesson 9

Quiz, 10 questions

1 point

1.
**For Questions 1-3, refer to the bus waiting time example from the lesson.**

Recall that we used the conjugate gamma prior for $\lambda$, the arrival rate in busses per minute. Suppose our prior belief about this rate is that it should have mean 1/20 arrivals per minute with standard deviation 1/5. Then the prior is $\mathrm{Gamma}(a, b)$ with $a = 1/16$.

- Find the value of $b$. Round your answer to two decimal places.

Enter answer here

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1 point

2.
Bus waiting times:

Suppose that we wish to use a prior with the same mean (1/20), but with effective sample size of one arrival. Then the prior for $\lambda$ is $\mathrm{Gamma}(1, 20)$.

In addition to the original $Y_1 = 12$, we observe the waiting times for four additional busses: $Y_2 = 15$, $Y_3 = 8$, $Y_4 = 13.5$, $Y_5 = 25$.

Recall that with multiple (independent) observations, the posterior for $\lambda$ is $\mathrm{Gamma}(\alpha, \beta)$ where $\alpha = a + n$ and $\beta = b + \sum y_i$.

- What is the posterior mean for $\lambda$? Round your answer to two decimal places.

Enter answer here

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1
point

3.
Bus waiting times:

- Continuing Question 2, use R or Excel to find the posterior probability that $\lambda < 1/10$? Round your answer to two decimal places.

Enter answer here

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1
point

4.
**For Questions 4-10, consider the following earthquake data:**

The United States Geological Survey maintains a list of significant earthquakes worldwide. We will model the rate of earthquakes of magnitude 4.0+ in the state of California during 2015. An iid exponential model on the waiting time between significant earthquakes is appropriate if we assume:

1. earthquake events are independent,
2. the rate at which earthquakes occur does not change during the year, and
3. the earthquake hazard rate does not change (i.e., the probability of an earthquake happening tomorrow is constant regardless of whether the previous earthquake was yesterday or 100 days ago).

Let $Y_i$ denote the waiting time in days between the ith earthquake and the following earthquake. Our model is $Y_i \overset{\text{iid}}{\sim} \text{Exponential}(\lambda)$ where the expected waiting time between earthquakes is $E(Y) = 1/\lambda$ days.

Assume the conjugate prior $\lambda \sim \text{Gamma}(a, b)$. Suppose our prior expectation for $\lambda$ is 1/30, and we wish to use a prior effective sample size of one interval between earthquakes.

- What is the value of $a$?

Enter answer here

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1
point

5.
Earthquake data:

- What is the value of $b$?

Enter answer here

1
point

6.
Earthquake data:

The significant earthquakes of magnitude 4.0+ in the state of California during 2015 occurred on the following dates (http://earthquake.usgs.gov/earthquakes/browse/significant.php?year=2015):

January 4, January 20, January 28, May 22, July 21, July 25, August 17, September 16, December 30.

- Recall that we are modeling the waiting times between earthquakes in days. Which of the following is our data vector?

○ **y** = (3, 16, 8, 114, 60, 4, 23, 30, 105)

○ **y** = (16, 8, 114, 60, 4, 23, 30, 105)

○ **y** = (3, 16, 8, 114, 60, 4, 23, 30, 105, 1)

○ **y** = (0, 0, 4, 2, 0, 1, 1, 3)

1
point

7.
Earthquake data:

- The posterior distribution is $\lambda \mid \mathbf{y} \sim \text{Gamma}(\alpha, \beta)$. What is the value of $\alpha$?

Enter answer here

1
point

8.
Earthquake data:

- The posterior distribution is $\lambda \mid \mathbf{y} \sim \mathrm{Gamma}(\alpha, \beta)$. What is the value of $\beta$?

Enter answer here

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1
point

9.
Earthquake data:

- Use R or Excel to calculate the upper end of the 95% equal-tailed credible interval for $\lambda$, the rate of major earthquakes in events per day. Round your answer to two decimal places.

Enter answer here

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1
point

10.
Earthquake data:

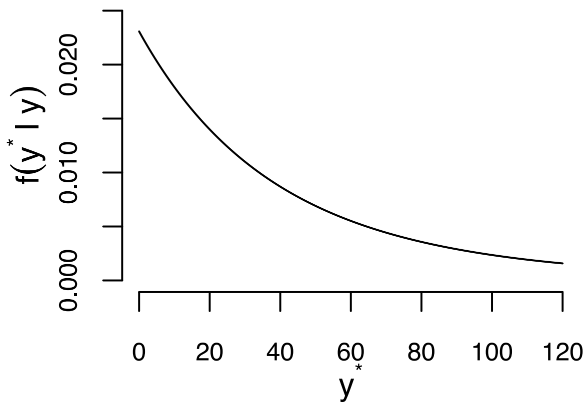
The posterior predictive density for a new waiting time $y^*$ in days is:

$$f(y^* \mid \mathbf{y}) = \int f(y^* \mid \lambda) \cdot f(\lambda \mid \mathbf{y}) d\lambda = \frac{\beta^{\alpha}\Gamma(\alpha+1)}{(\beta+y^*)^{\alpha+1}\Gamma(\alpha)} I_{\{y^* \geq 0\}} = \frac{\beta^{\alpha}\alpha}{(\beta+y^*)^{\alpha+1}} I_{\{y^* \geq 0\}}$$

where $f(\lambda \mid \mathbf{y})$ is the $\mathrm{Gamma}(\alpha, \beta)$ posterior found earlier. Use R or Excel to evaluate this posterior predictive PDF.

- Which of the following graphs shows the posterior predictive distribution for $y^*$?

○



0.000
0.010
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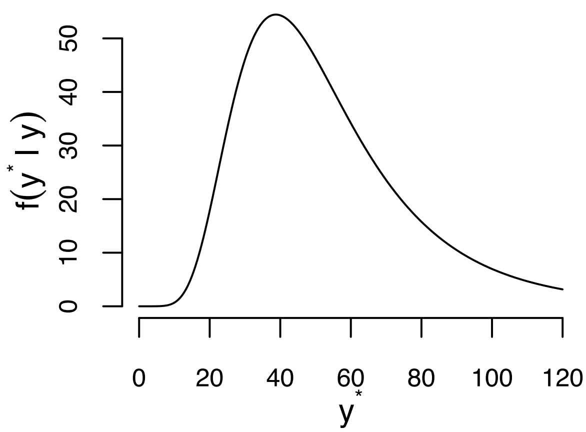
f(y* I y)
0
20
40
60
80
100
120
y*

0
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f(y* I y)
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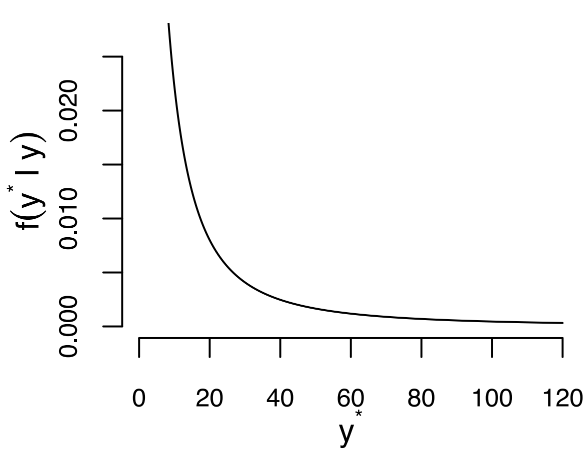
y*

0.000
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f(y* I y)
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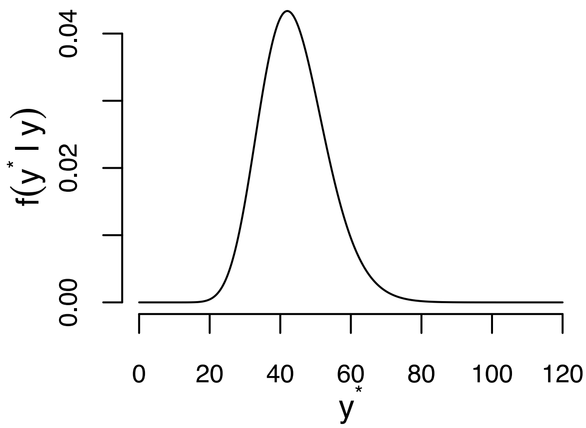


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