

# Setup

## Load packages

```
library(ggplot2)
library(dplyr)
library(statsr)
library(BAS)

library(MASS)

library(GGally)
library(broom)
```

## Load data

```
load("movies.Rdata")
```

## Part 1: Data

This data is a random sample of movies released before 2016 and collected from the IMDB and Rotten Tomatoes movie database. Therefore, the results of this analysis can only be generalized to the sampled population from said databases; considering the breadth of these databases, though technically not true, the results are most likely generalizable to all Western (American and European) films released before 2016.

Since the data is collected from past information and no random assignment of treatment is performed (basically impossible to implement in an experiment) only associations rather than causations can be found.

## Part 2: Data manipulation

```
movies_manipulate <- movies

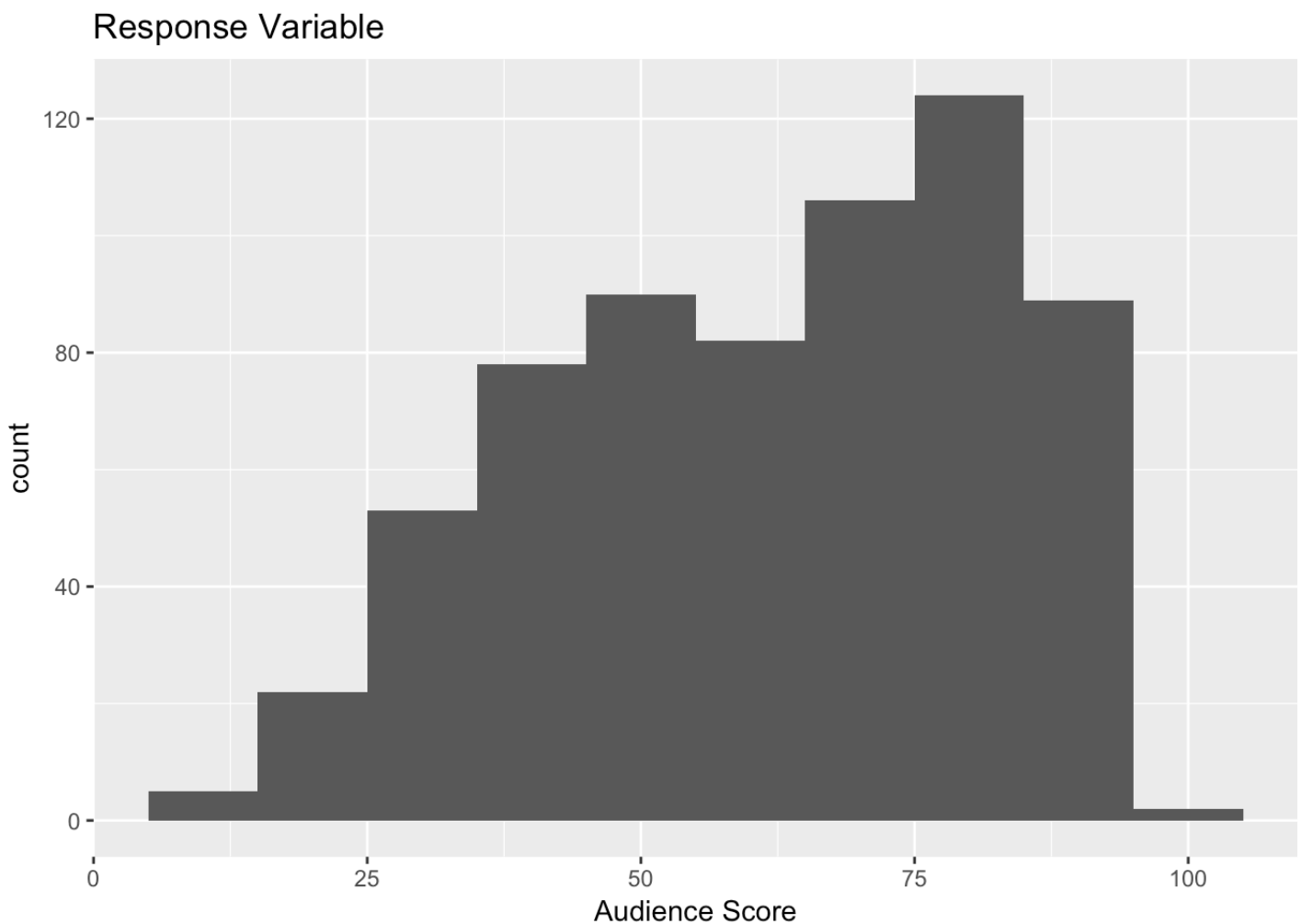
as.character(as.numeric(movies_manipulate$thtr_rel_month)) %>%
  str(thtr_rel_month)
```

```
## chr [1:651] "4" "3" "8" "10" "9" "1" "1" "11" "9" "3" "6" "12" "1" ...
```

```
movies_manipulate <- mutate (movies_manipulate,
  feature_film = ifelse(title_type == 'Feature Film', 'Yes', 'No'),
  drama = ifelse(genre == 'Drama', 'Yes', 'No'),
  mpaa_rating_R = ifelse(mpaa_rating == 'R', 'Yes', 'No'),
  oscar_season = ifelse(thtr_rel_month >= 10, 'Yes', 'No'),
  summer_season = ifelse(thtr_rel_month >= 5 & thtr_rel_month <= 8, 'Yes', 'No'))
```

## Part 3: Exploratory data analysis

```
# Response Variable: Audience Score
ggplot(data = movies_manipulate, aes(x = audience_score)) + geom_histogram(binwidth =
10) + labs(x = "Audience Score", title = "Response Variable")
```



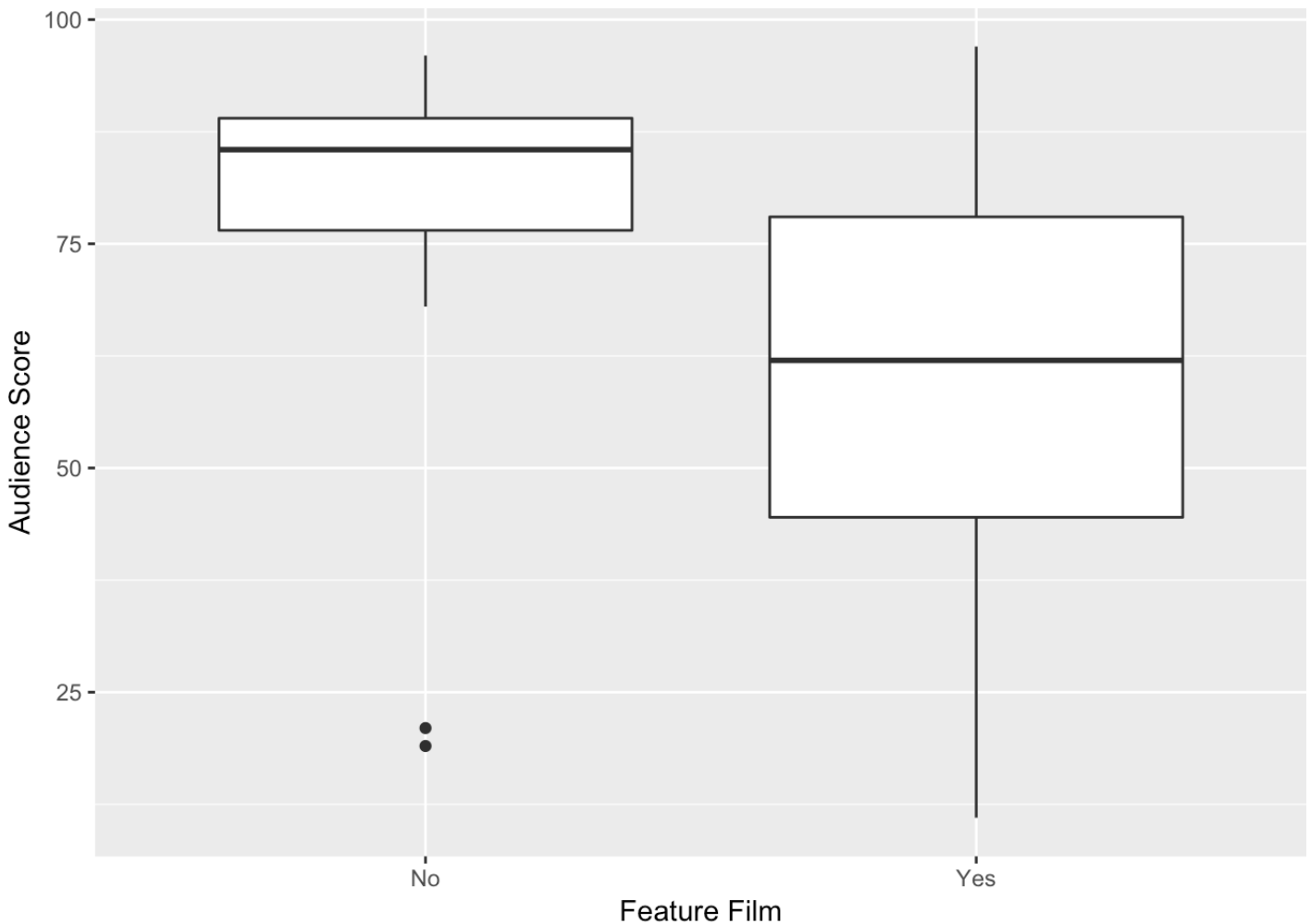
```
summary(movies_manipulate$audience_score)
```

##	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
##	11.00	46.00	65.00	62.36	80.00	97.00

*# The graph shows the data as skewed left. That being said, the mean (65) and the median (62.36) are similar to one another, which normally only occurs when the data is roughly normal.*

*# Feature Film*

```
ggplot(data = movies_manipulate, aes(x = feature_film, y = audience_score)) + geom_boxplot() + labs(x = "Feature Film", y = "Audience Score")
```



*# Feature Films are roughly normally distributed in regards to audience score whereas non-feature films appear to be right-skewed; non-feature films tend to have a higher audience score based upon this plot.*

```
movies_manipulate %>%  
  group_by(feature_film) %>%  
  summarise(mean_FF = mean(audience_score), sd_FF = sd(audience_score),  
            median_FF = median(audience_score), IQR_FF = IQR(audience_score),  
            n = n())
```

```
## # A tibble: 2 x 6
##   feature_film mean_FF sd_FF median_FF IQR_FF      n
##   <chr>         <dbl> <dbl>      <dbl> <dbl> <int>
## 1 No           81.0  13.6      85.5   12.5   60
## 2 Yes          60.5  19.8       62    33.5  591
```

*# Summary statistics confirm that films that are not feature films are right skewed (mean = 81; median = 85.5 [IQR = 12.5]) in their audience score. Feature films were normally distributed (mean = 60.5; sd = 19.8). This data supports the results of the plot in that non-feature films had higher audience scores. It should be noted that there was a smaller sample of non-feature films, which may imply that there is not enough data to draw a strong conclusion.*

```
bayes_inference(y = audience_score, x = feature_film, data = movies_manipulate,
  statistic = "mean", type = "ht",
  null = 0, alternative = "twosided",
  prior = "JZS", rscale = 1,
  method = "theoretical")
```

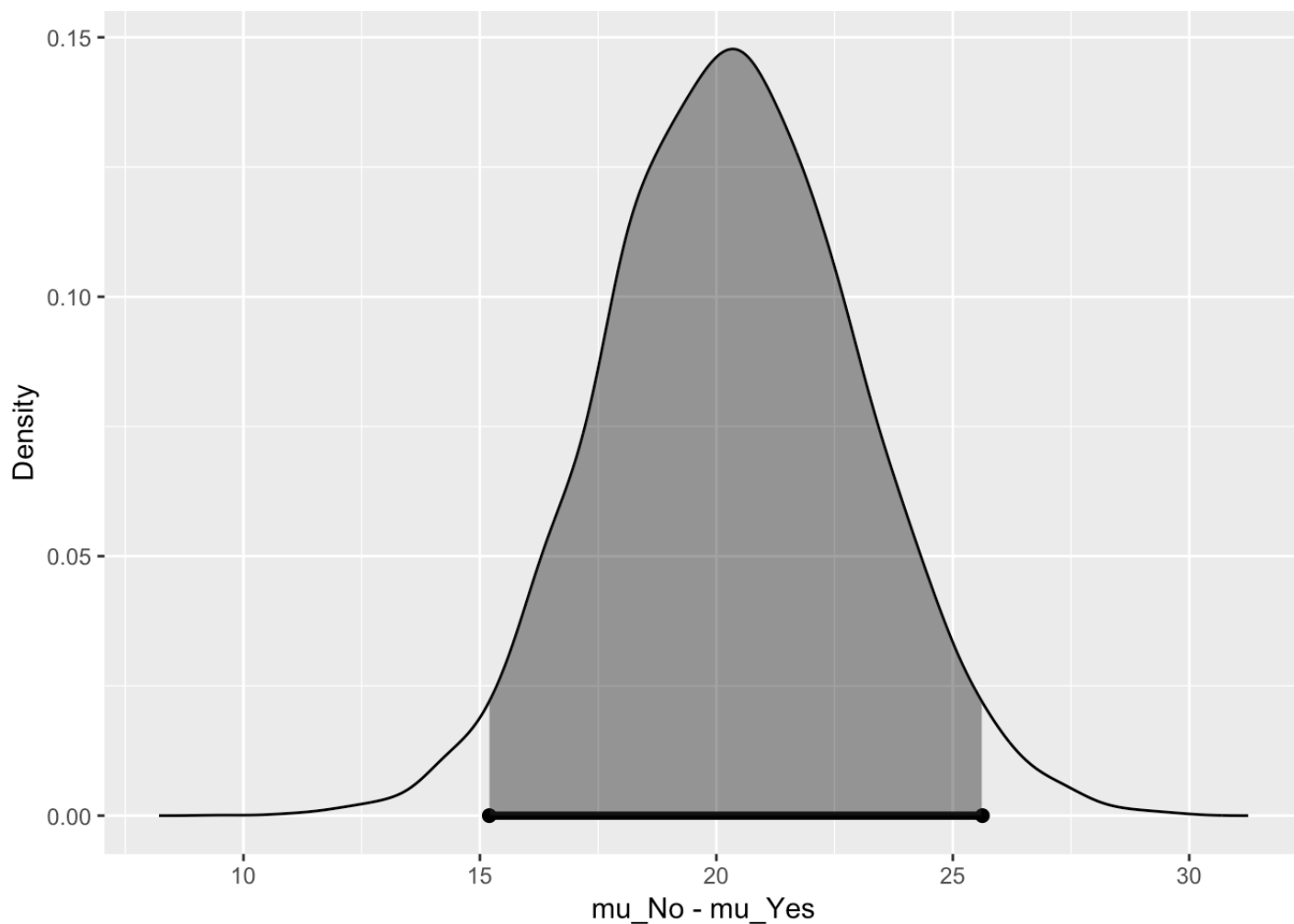
```

## Response variable: numerical, Explanatory variable: categorical (2 levels)
## n_No = 60, y_bar_No = 81.05, s_No = 13.5764
## n_Yes = 591, y_bar_Yes = 60.4653, s_Yes = 19.824
## (Assuming Zellner-Siow Cauchy prior on the difference of means. )
## (Assuming independent Jeffreys prior on the overall mean and variance. )
## Hypotheses:
## H1: mu_No = mu_Yes
## H2: mu_No != mu_Yes
##
## Priors: P(H1) = 0.5 P(H2) = 0.5
##
## Results:
## BF[H2:H1] = 338337769673
## P(H1|data) = 0
## P(H2|data) = 1
##
## Posterior summaries for under H2:
## Response variable: numerical, Explanatory variable: categorical (2 levels)
## n_No = 60, y_bar_No = 81.05, s_No = 13.5764
## n_Yes = 591, y_bar_Yes = 60.4653, s_Yes = 19.824
## (Assuming Zellner-Siow Cauchy prior for difference in means)
## (Assuming independent Jeffrey's priors for overall mean and variance)
##
##
## Posterior Summaries
##


|                   | 2.5%        | 25%         | 50%        | 75%        | 97.5%       |
|-------------------|-------------|-------------|------------|------------|-------------|
| ## overall mean   | 68.1555171  | 69.7737209  | 70.657337  | 71.543891  | 73.332208   |
| ## mu_No - mu_Yes | 15.1986086  | 18.5036997  | 20.308571  | 22.121333  | 25.625392   |
| ## sigma^2        | 335.8981696 | 361.1724847 | 374.739157 | 388.808661 | 418.660797  |
| ## effect size    | 0.7783184   | 0.9551485   | 1.049415   | 1.144329   | 1.327966    |
| ## n_0            | 15.8499761  | 175.2344256 | 426.630287 | 862.365611 | 2381.008934 |


## 95% Cred. Int.: (15.1986 , 25.6254)

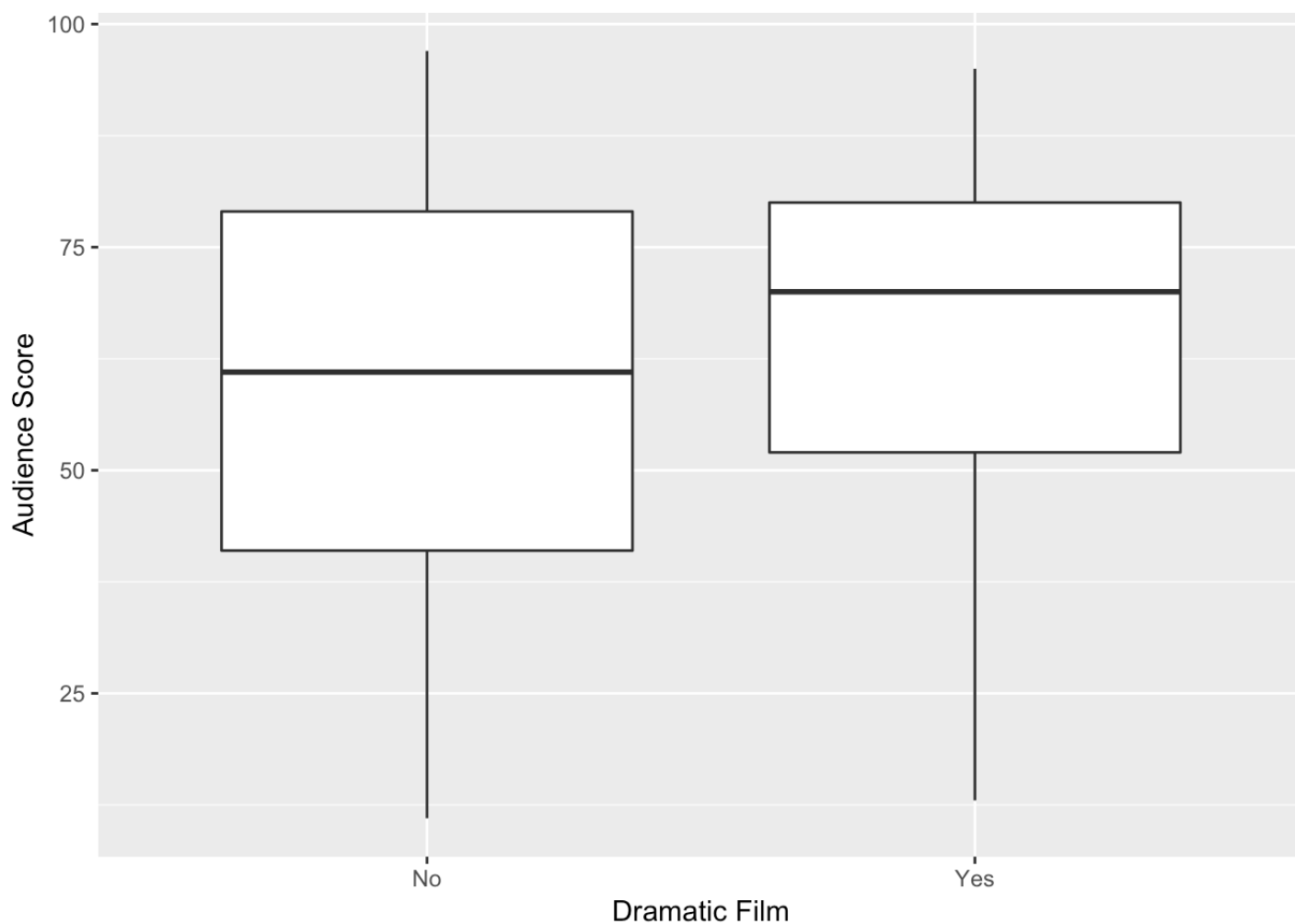
```



*# Based upon the Bayes Factor there is very strong evidence that the distinction between feature films and non-feature films has an effect upon audience score. The probability that a non-feature film has on average 15 to 25 higher audience score is 0.95.*

*# Drama*

```
ggplot(data = movies_manipulate, aes(x = drama, y = audience_score)) + geom_boxplot() + labs(x = "Dramatic Film", y = "Audience Score")
```



*# Dramatic films appear to be left skewed though the median value of audience score is greater than that of non-dramatic films. Non-dramatic films appear to be normally distributed.*

```
movies_manipulate %>%
  group_by(drama) %>%
  summarise(mean_dr = mean(audience_score), sd_dr = sd(audience_score),
            median_dr = median(audience_score), IQR_dr = IQR(audience_score),
            n = n())
```

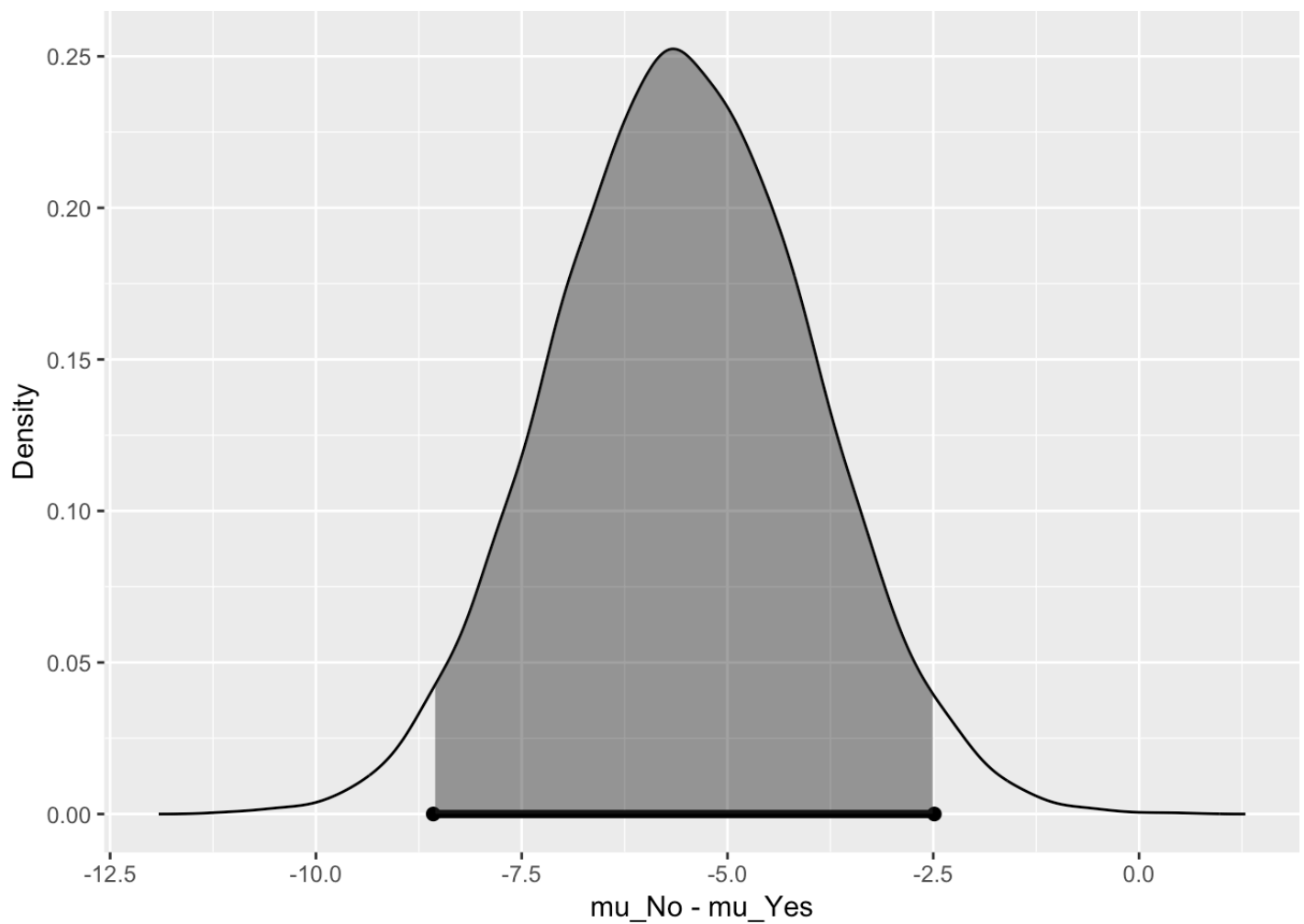
```
## # A tibble: 2 x 6
##   drama mean_dr sd_dr median_dr IQR_dr    n
##   <chr>   <dbl> <dbl>     <dbl> <dbl> <int>
## 1 No      59.7  21.3       61     38  346
## 2 Yes     65.3  18.5       70     28  305
```

*# Dramatic films have a median\* audience score of 70 with an IQR of 28. (\*Due to the skewed distribution of data, evidenced by vastly different median and mean values the median and IQR data is provided.) Non-dramatic films had a mean audience score of 59.7 with a standard deviation of 21 points.*

```
bayes_inference(y = audience_score, x = drama, data = movies_manipulate,
                statistic = "mean", type = "ht",
                null = 0, alternative = "twosided",
                prior = "JZS", rscale = 1,
                method = "theoretical")
```

```
## Response variable: numerical, Explanatory variable: categorical (2 levels)
## n_No = 346, y_bar_No = 59.7312, s_No = 21.2775
## n_Yes = 305, y_bar_Yes = 65.3475, s_Yes = 18.5418
## (Assuming Zellner-Siow Cauchy prior on the difference of means. )
## (Assuming independent Jeffreys prior on the overall mean and variance. )
## Hypotheses:
## H1: mu_No = mu_Yes
## H2: mu_No != mu_Yes
##
## Priors: P(H1) = 0.5 P(H2) = 0.5
##
## Results:
## BF[H2:H1] = 31.9101
## P(H1|data) = 0.0304
## P(H2|data) = 0.9696
##
## Posterior summaries for under H2:
## Response variable: numerical, Explanatory variable: categorical (2 levels)
## n_No = 346, y_bar_No = 59.7312, s_No = 21.2775
## n_Yes = 305, y_bar_Yes = 65.3475, s_Yes = 18.5418
## (Assuming Zellner-Siow Cauchy prior for difference in means)
## (Assuming independent Jeffrey's priors for overall mean and variance)
##
##
## Posterior Summaries
##
##          2.5%          25%          50%          75%
## overall mean    60.9759384  61.9985457  62.5446289  63.0543697
## mu_No - mu_Yes  -8.5740119  -6.6073995  -5.5556489  -4.4907638
## sigma^2        360.3449253  387.1630038  401.5538468  416.8317642
## effect size     -0.4276108  -0.3303862  -0.2770954  -0.2234412
## n_0             33.4898862  353.3138667  834.5173375 1687.7365093
##
##          97.5%
## overall mean    64.0748098
## mu_No - mu_Yes  -2.4870239
## sigma^2        448.9100662
## effect size     -0.1233749
## n_0             4419.3541422
## 95% Cred. Int.: (-8.574 , -2.487)
```

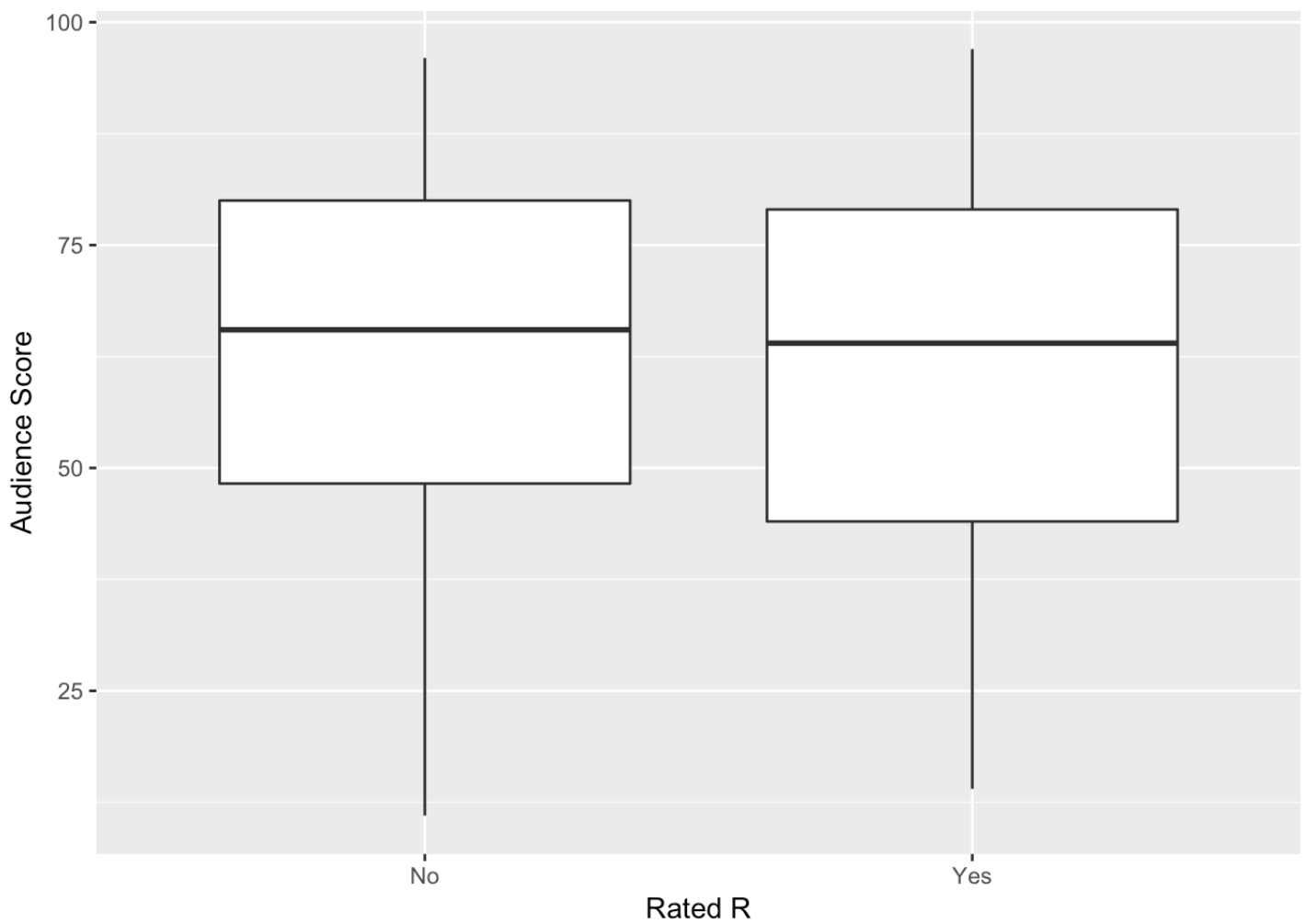




*# There is strong evidence ( $BF = 30$ ) that dramatic movies on average have a lower audience score. There is a 95% probability that non-dramatic films score 8.6 to 2.4 points lower than dramatic films on average.*

*# MPAA Rating R*

```
ggplot(data = movies_manipulate, aes(x = mpaa_rating_R, y = audience_score)) + geom_boxplot() + labs(x = "Rated R", y = "Audience Score")
```



*# Movies rated R appears normally distributed whereas films not rated R appear to be left skewed.*

```
movies_manipulate %>%
  group_by(mpaa_rating_R) %>%
  summarise(mean_R = mean(audience_score), sd_R = sd(audience_score),
            median_R = median(audience_score), IQR_R = IQR(audience_score),
            n = n())
```

```
## # A tibble: 2 x 6
##   mpaa_rating_R mean_R  sd_R median_R IQR_R      n
##   <chr>          <dbl> <dbl>    <dbl> <dbl> <int>
## 1 No           62.7  20.3    65.5  31.8  322
## 2 Yes          62.0  20.2    64    35   329
```

*# Films rated R have a median audience rating of 64 and an IQR of 35 (\*statistics for skewed data reported as the mean is different from the median). Films not rated R have a median score of 65.5 and an IQR of 32.*

```
bayes_inference(y = audience_score, x = mpaa_rating_R, data = movies_manipulate,
               statistic = "mean", type = "ht",
               null = 0, alternative = "twosided",
               prior = "JZS", rscale = 1,
               method = "theoretical")
```

```
## Response variable: numerical, Explanatory variable: categorical (2 levels)
```

```
## n_No = 322, y_bar_No = 62.6894, s_No = 20.3167
```

```
## n_Yes = 329, y_bar_Yes = 62.0426, s_Yes = 20.1559
```

```
## (Assuming Zellner-Siow Cauchy prior on the difference of means. )
```

```
## (Assuming independent Jeffreys prior on the overall mean and variance. )
```

```
## Hypotheses:
```

```
## H1: mu_No = mu_Yes
```

```
## H2: mu_No != mu_Yes
```

```
##
```

```
## Priors: P(H1) = 0.5 P(H2) = 0.5
```

```
##
```

```
## Results:
```

```
## BF[H1:H2] = 14.8147
```

```
## P(H1|data) = 0.9368
```

```
## P(H2|data) = 0.0632
```

```
##
```

```
## Posterior summaries for under H2:
```

```
## Response variable: numerical, Explanatory variable: categorical (2 levels)
```

```
## n_No = 322, y_bar_No = 62.6894, s_No = 20.3167
```

```
## n_Yes = 329, y_bar_Yes = 62.0426, s_Yes = 20.1559
```

```
## (Assuming Zellner-Siow Cauchy prior for difference in means)
```

```
## (Assuming independent Jeffrey's priors for overall mean and variance)
```

```
##
```

```
##
```

```
## Posterior Summaries
```

```
##           2.5%           25%           50%           75%
```

```
## overall mean    60.8116797  61.81924671  62.36110365  6.289304e+01
```

```
## mu_No - mu_Yes  -2.4772052  -0.46468660   0.61345815  1.660548e+00
```

```
## sigma^2        368.1590809  394.24302103  409.40801289  4.248300e+02
```

```
## effect size     -0.1223484  -0.02293481   0.03041908  8.241127e-02
```

```
## n_0            31.8340778  389.22770189  905.94172383  1.821753e+03
```

```
##           97.5%
```

```
## overall mean    63.9094670
```

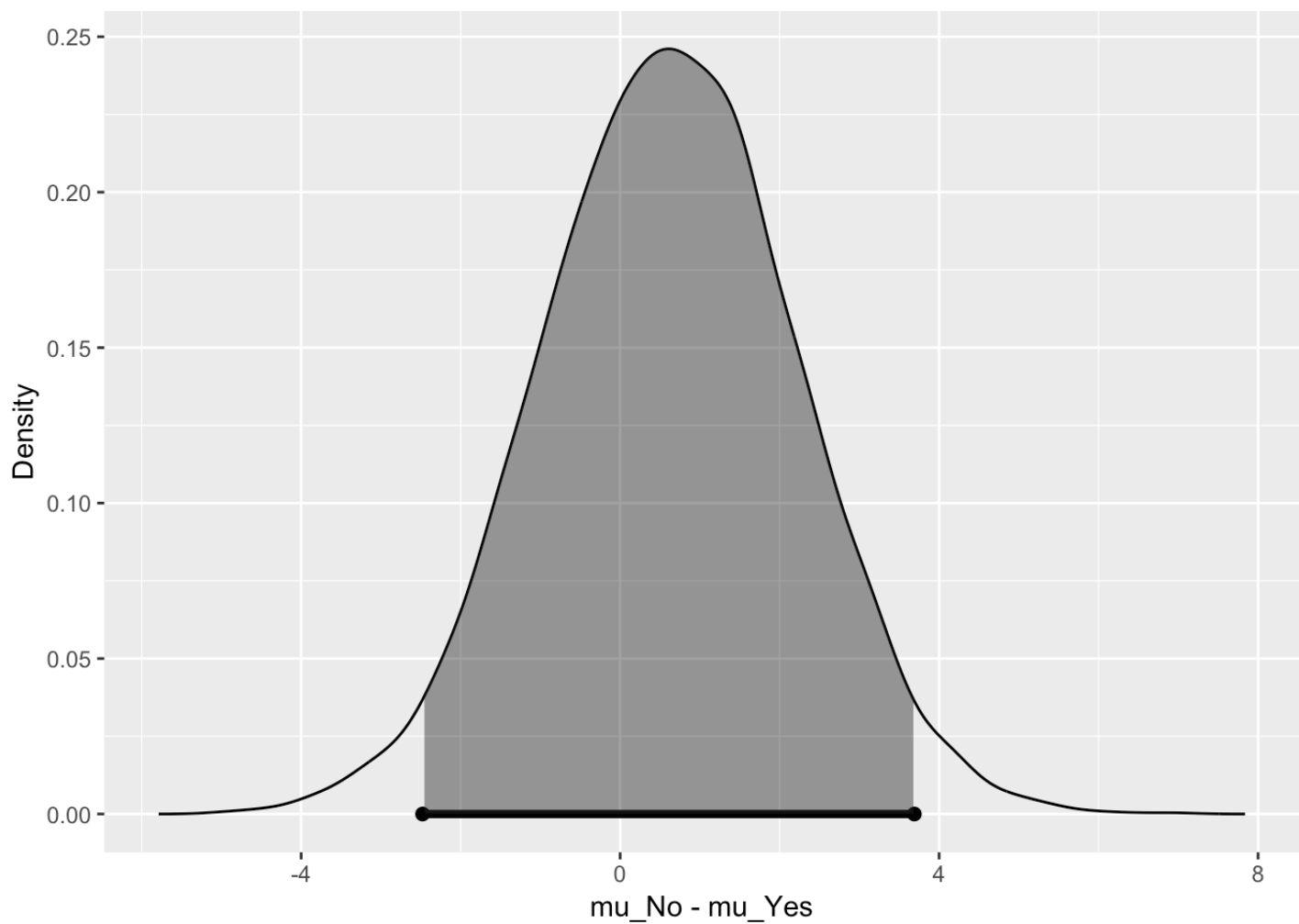
```
## mu_No - mu_Yes   3.6895443
```

```
## sigma^2        458.7342050
```

```
## effect size      0.1815429
```

```
## n_0            4727.8516693
```

```
## 95% Cred. Int.: (-2.4772 , 3.6895)
```

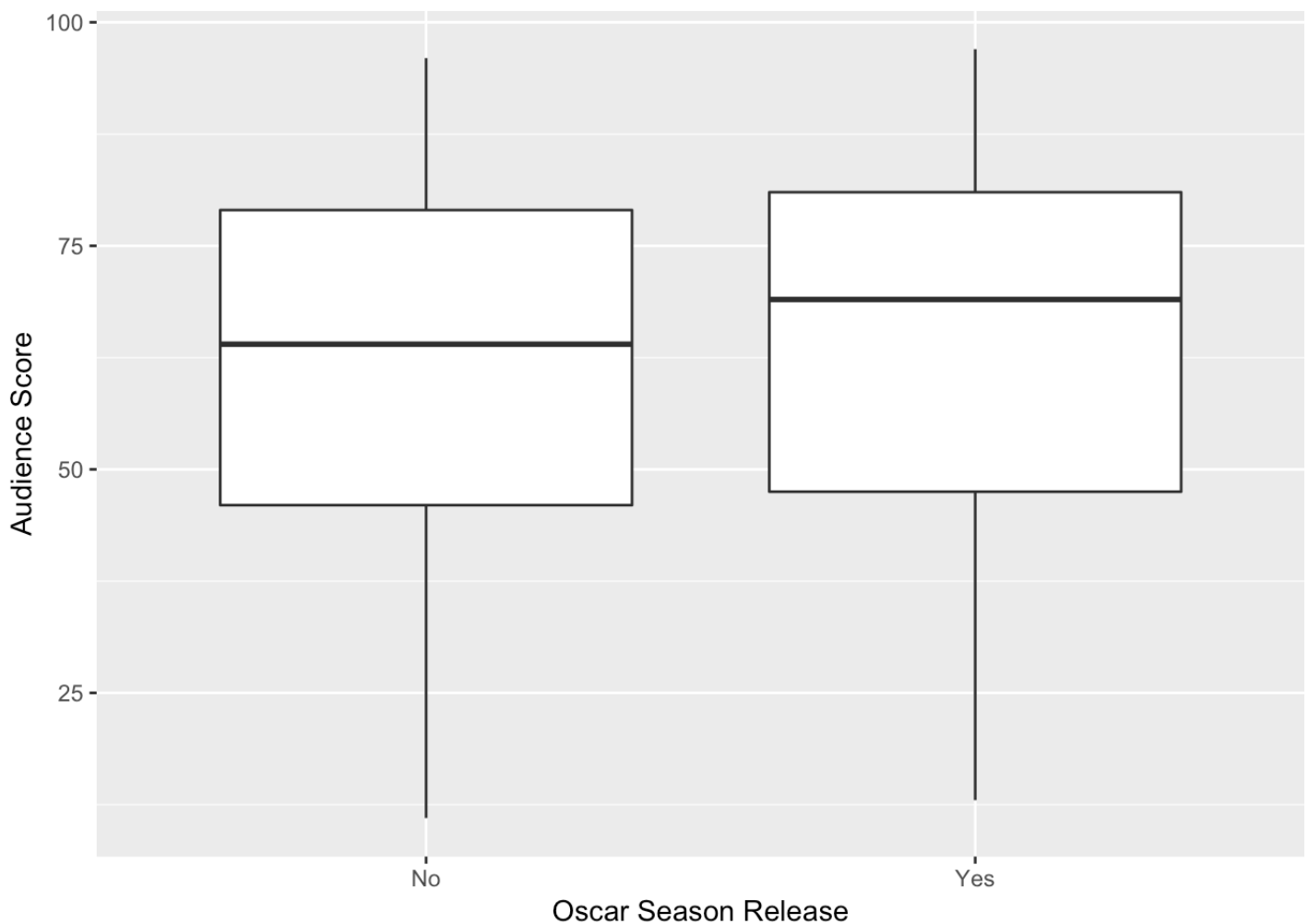


```
# BF = 14.81; 95 = -2.45, 3.77
```

*# Though the Bayes factor provides positive evidence that R-rated films and not-R-rated films have on average different audience scores, the credible intervals includes the value 0 therefore suggesting that there is no significant difference in audience scores between the groups.*

```
# Oscar Season
```

```
ggplot(data = movies_manipulate, aes(x = oscar_season, y = audience_score)) + geom_boxplot() + labs(x = "Oscar Season Release", y = "Audience Score")
```



*# Data for movies released during Oscar season (or not released during Oscar season) appear similar for both categories and slightly left skewed.*

```
movies_manipulate %>%
  group_by(oscar_season) %>%
  summarise(mean_oscar = mean(audience_score), sd_oscar = sd(audience_score),
            median_oscar = median(audience_score), IQR_oscar = IQR(audience_score),
            n = n())
```

```
## # A tibble: 2 x 6
##   oscar_season mean_oscar sd_oscar median_oscar IQR_oscar      n
##   <chr>         <dbl>    <dbl>         <dbl>    <dbl> <int>
## 1 No           61.8     20.1           64       33    460
## 2 Yes          63.7     20.5           69      33.5   191
```

*# Movies released during Oscar season have a median audience score of 69 with an IQR of 33. Movies not released during Oscar season have a median audience score of 64 with an IQR of 33.*

```
bayes_inference(y = audience_score, x = oscar_season, data = movies_manipulate,
                statistic = "mean", type = "ht",
                null = 0, alternative = "twosided",
                prior = "JZS", rscale = 1,
                method = "theoretical")
```

## Response variable: numerical, Explanatory variable: categorical (2 levels)

## n\_No = 460, y\_bar\_No = 61.813, s\_No = 20.1196

## n\_Yes = 191, y\_bar\_Yes = 63.6859, s\_Yes = 20.4612

## (Assuming Zellner-Siow Cauchy prior on the difference of means. )

## (Assuming independent Jeffreys prior on the overall mean and variance. )

## Hypotheses:

## H1: mu\_No = mu\_Yes

## H2: mu\_No != mu\_Yes

##

## Priors: P(H1) = 0.5 P(H2) = 0.5

##

## Results:

## BF[H1:H2] = 8.2858

## P(H1|data) = 0.8923

## P(H2|data) = 0.1077

##

## Posterior summaries for under H2:

## Response variable: numerical, Explanatory variable: categorical (2 levels)

## n\_No = 460, y\_bar\_No = 61.813, s\_No = 20.1196

## n\_Yes = 191, y\_bar\_Yes = 63.6859, s\_Yes = 20.4612

## (Assuming Zellner-Siow Cauchy prior for difference in means)

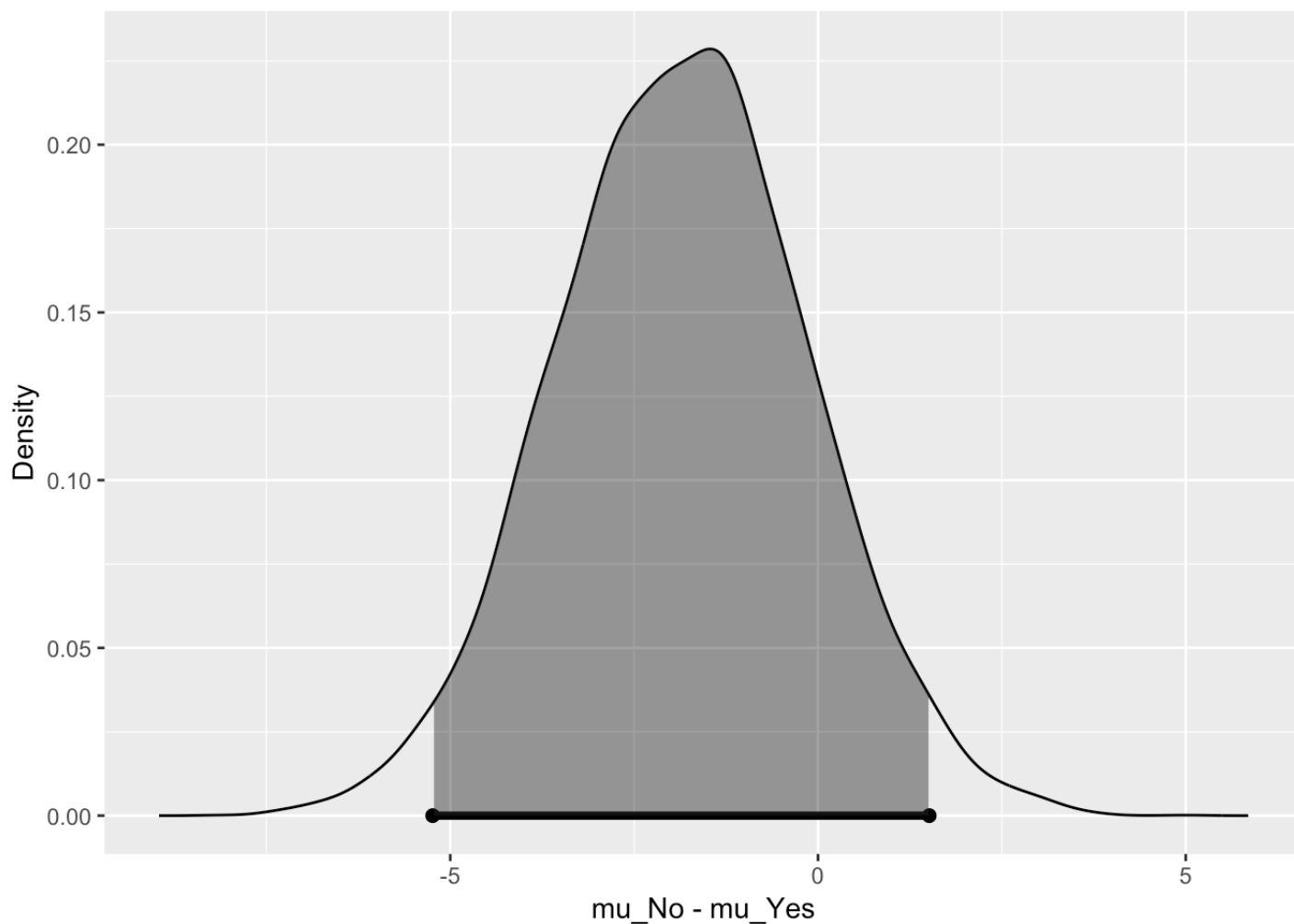
## (Assuming independent Jeffrey's priors for overall mean and variance)

##

##

## Posterior Summaries

	2.5%	25%	50%	75%
## overall mean	61.0369416	62.1619740	62.74285510	63.32904822
## mu_No - mu_Yes	-5.2391091	-2.9975694	-1.83595206	-0.70603033
## sigma^2	367.0655532	393.5273529	408.58674743	424.40316507
## effect size	-0.2587563	-0.1482319	-0.09088762	-0.03459618
## n_0	35.6509347	367.8029755	905.42544547	1771.71970917
##	97.5%			
## overall mean	6.444667e+01			
## mu_No - mu_Yes	1.512721e+00			
## sigma^2	4.567457e+02			
## effect size	7.409905e-02			
## n_0	4.699248e+03			
## 95% Cred. Int.: (-5.2391 , 1.5127)				

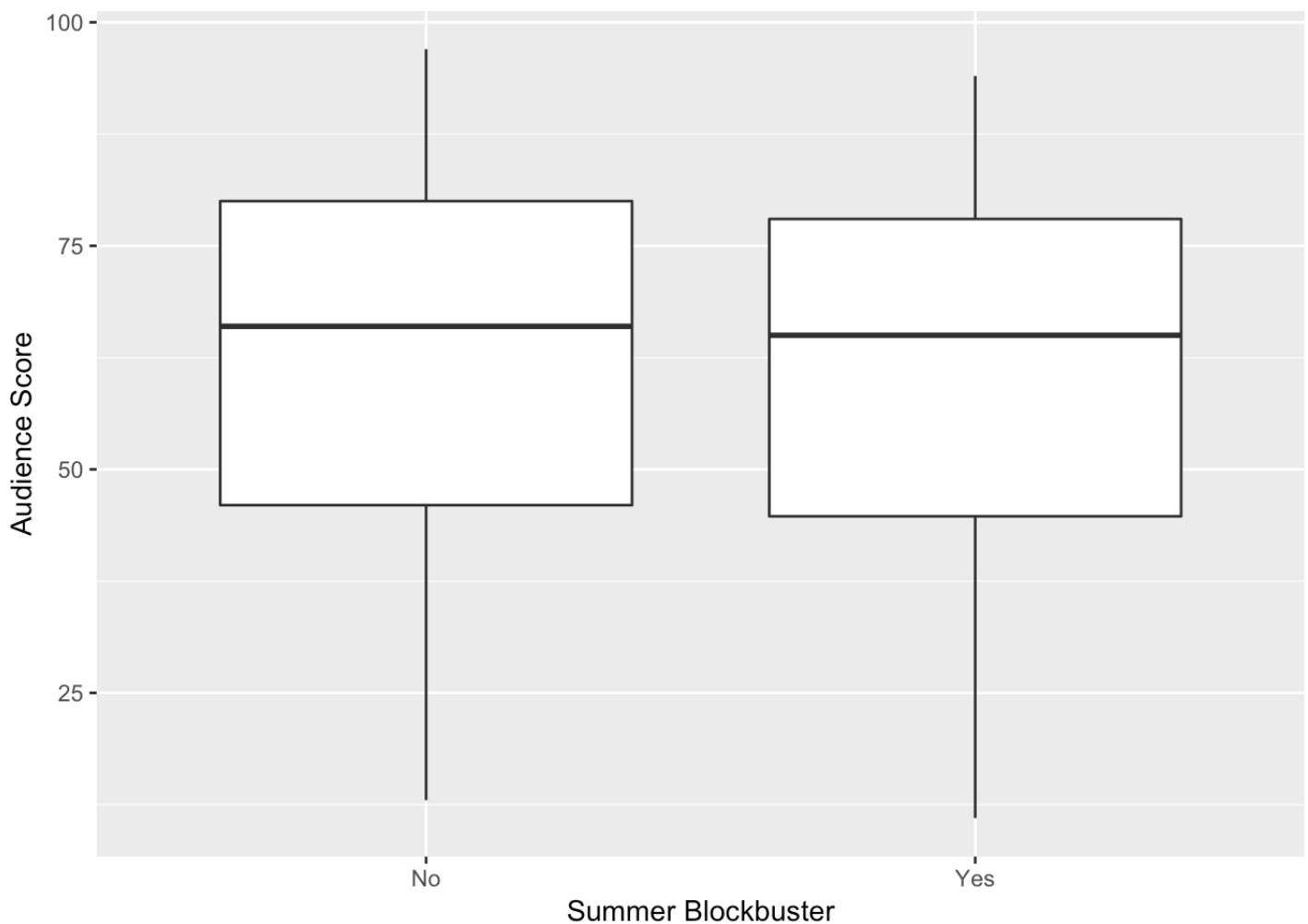


```
# BF = 8.23; 95 = -5.35, 1.53
```

*# Though the Bayes factor provides positive evidence that films released during Oscar season and films not released during Oscar season have on average different audience scores, the credible intervals includes the value 0 therefore suggesting that there is no significant difference in audience scores between the groups.*

```
# Summer Season
```

```
ggplot(data = movies_manipulate, aes(x = summer_season, y = audience_score)) + geom_boxplot() + labs(x = "Summer Blockbuster", y = "Audience Score")
```



*# Data for movies released during summer season appear similar for both categories and slightly left skewed.*

```
movies_manipulate %>%
  group_by(summer_season) %>%
  summarise(mean_summer = mean(audience_score), sd_summer = sd(audience_score),
            median_summer = median(audience_score), IQR_summer = IQR(audience_score),
            n = n())
```

```
## # A tibble: 2 x 6
##   summer_season mean_summer sd_summer median_summer IQR_summer      n
##   <chr>          <dbl>    <dbl>         <dbl>    <dbl> <int>
## 1 No           62.6      20.4          66        34    443
## 2 Yes          61.8      19.9          65       33.2   208
```



*# Movies released during summer season have a median audience score of 66 with an IQR of 34. Movies not released during summer season have a median audience score of 65 with an IQR of 33.*

```
bayes_inference(y = audience_score, x = summer_season, data = movies_manipulate,
                statistic = "mean", type = "ht",
                null = 0, alternative = "twosided",
                prior = "JZS", rscale = 1,
                method = "theoretical")
```

```
## Response variable: numerical, Explanatory variable: categorical (2 levels)
```

```
## n_No = 443, y_bar_No = 62.623, s_No = 20.3857
```

```
## n_Yes = 208, y_bar_Yes = 61.8077, s_Yes = 19.9083
```

```
## (Assuming Zellner-Siow Cauchy prior on the difference of means. )
```

```
## (Assuming independent Jeffreys prior on the overall mean and variance. )
```

```
## Hypotheses:
```

```
## H1: mu_No = mu_Yes
```

```
## H2: mu_No != mu_Yes
```

```
##
```

```
## Priors: P(H1) = 0.5 P(H2) = 0.5
```

```
##
```

```
## Results:
```

```
## BF[H1:H2] = 13.4039
```

```
## P(H1|data) = 0.9306
```

```
## P(H2|data) = 0.0694
```

```
##
```

```
## Posterior summaries for under H2:
```

```
## Response variable: numerical, Explanatory variable: categorical (2 levels)
```

```
## n_No = 443, y_bar_No = 62.623, s_No = 20.3857
```

```
## n_Yes = 208, y_bar_Yes = 61.8077, s_Yes = 19.9083
```

```
## (Assuming Zellner-Siow Cauchy prior for difference in means)
```

```
## (Assuming independent Jeffrey's priors for overall mean and variance)
```

```
##
```

```
##
```

```
## Posterior Summaries
```

```
##           2.5%           25%           50%           75%
```

```
## overall mean    60.5420961  61.64057090  62.20322073  6.279452e+01
```

```
## mu_No - mu_Yes  -2.5643373  -0.36310847   0.81764689  1.928377e+00
```

```
## sigma^2        368.2520323  394.33023170  409.28235192  4.254782e+02
```

```
## effect size     -0.1267592  -0.01784972   0.04030192  9.526388e-02
```

```
## n_0            33.3172332  377.44936723  913.84753962  1.822056e+03
```

```
##           97.5%
```

```
## overall mean    63.9088331
```

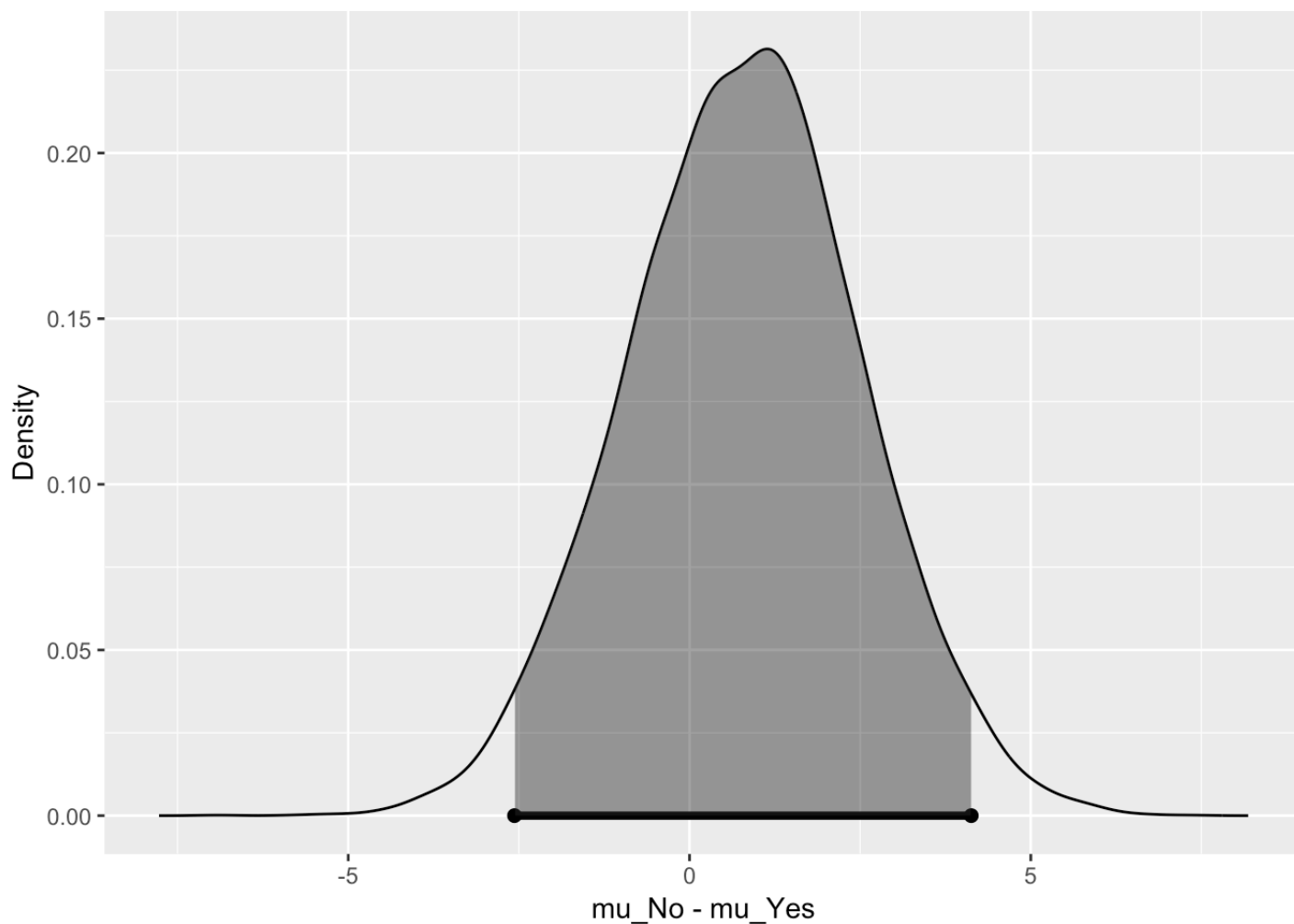
```
## mu_No - mu_Yes   4.1275295
```

```
## sigma^2        458.2827053
```

```
## effect size     0.2042352
```

```
## n_0            4753.7880722
```

```
## 95% Cred. Int.: (-2.5643 , 4.1275)
```

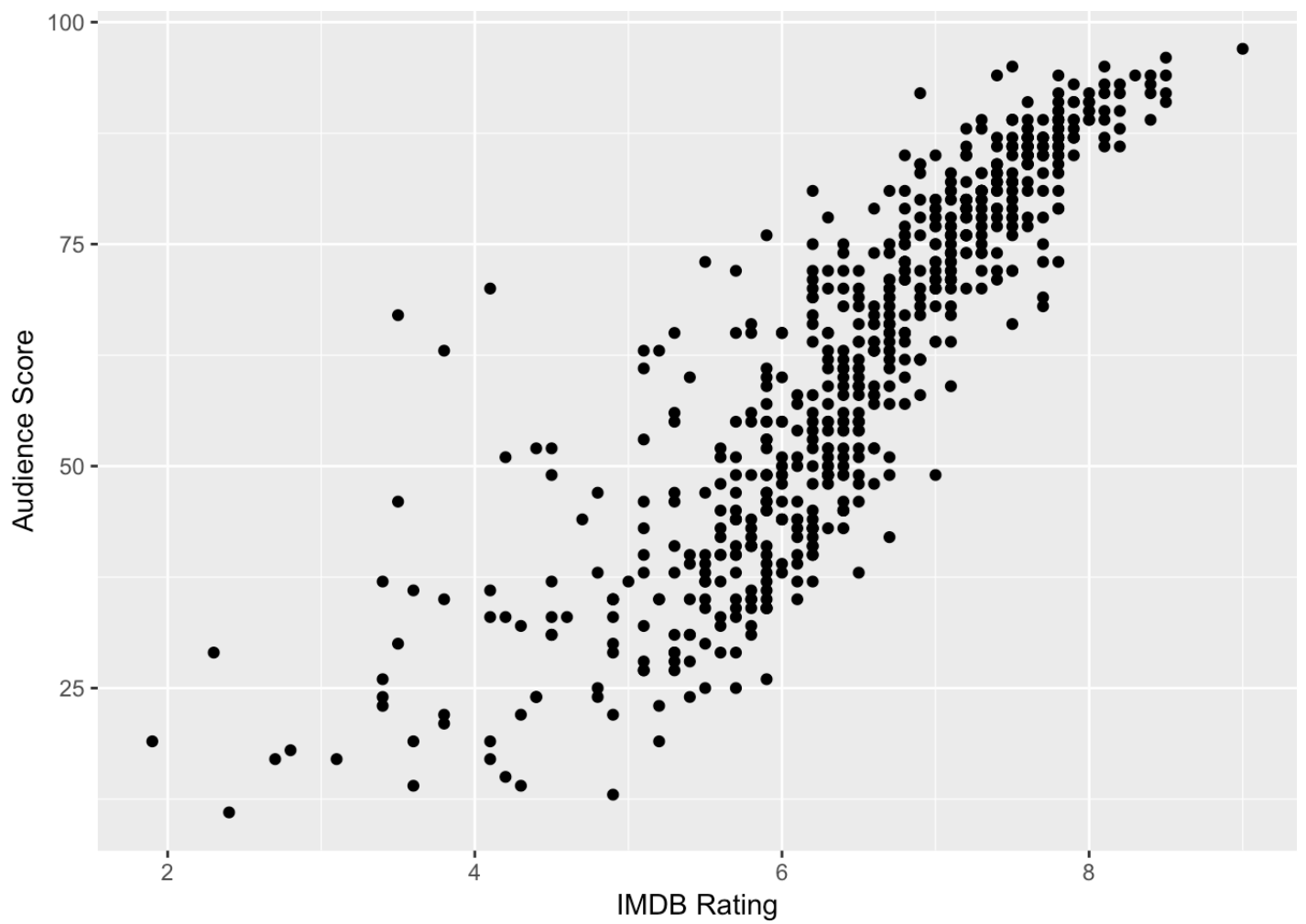


```
# BF = 13.4; 95 = -2.59, 4.10
```

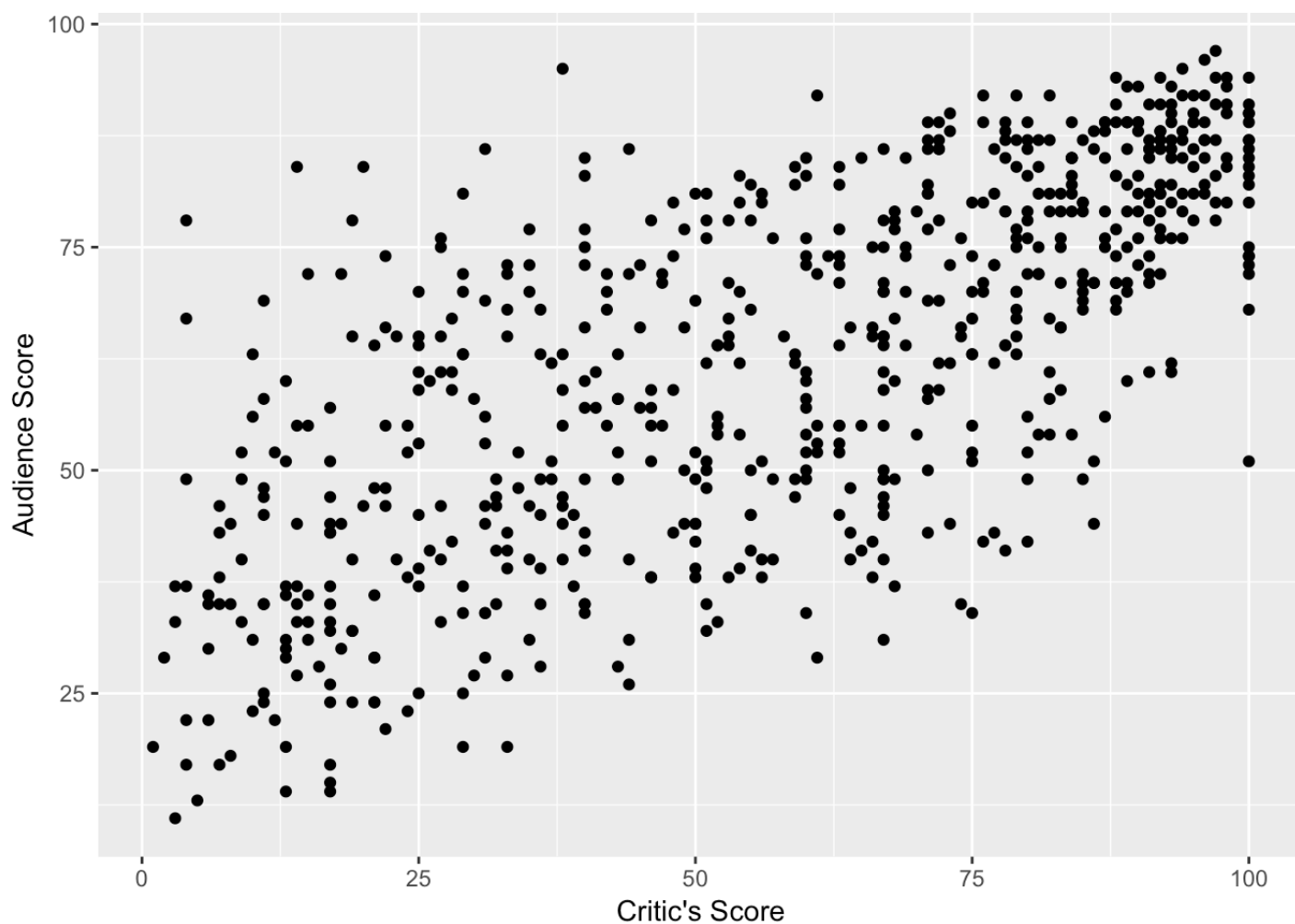
```
# Though the Bayes factor provides positive evidence that films released during summer season and films not released during summer season have on average different audience scores, the credible intervals includes the value 0 therefore suggesting that there is no significant difference in audience scores between the groups.
```

```
# Based upon later model selection; EDA on imdb rating and critics score
```

```
ggplot(data = movies_manipulate, aes(x = imdb_rating, y = audience_score)) + geom_point() + labs(x = "IMDB Rating", y = "Audience Score")
```



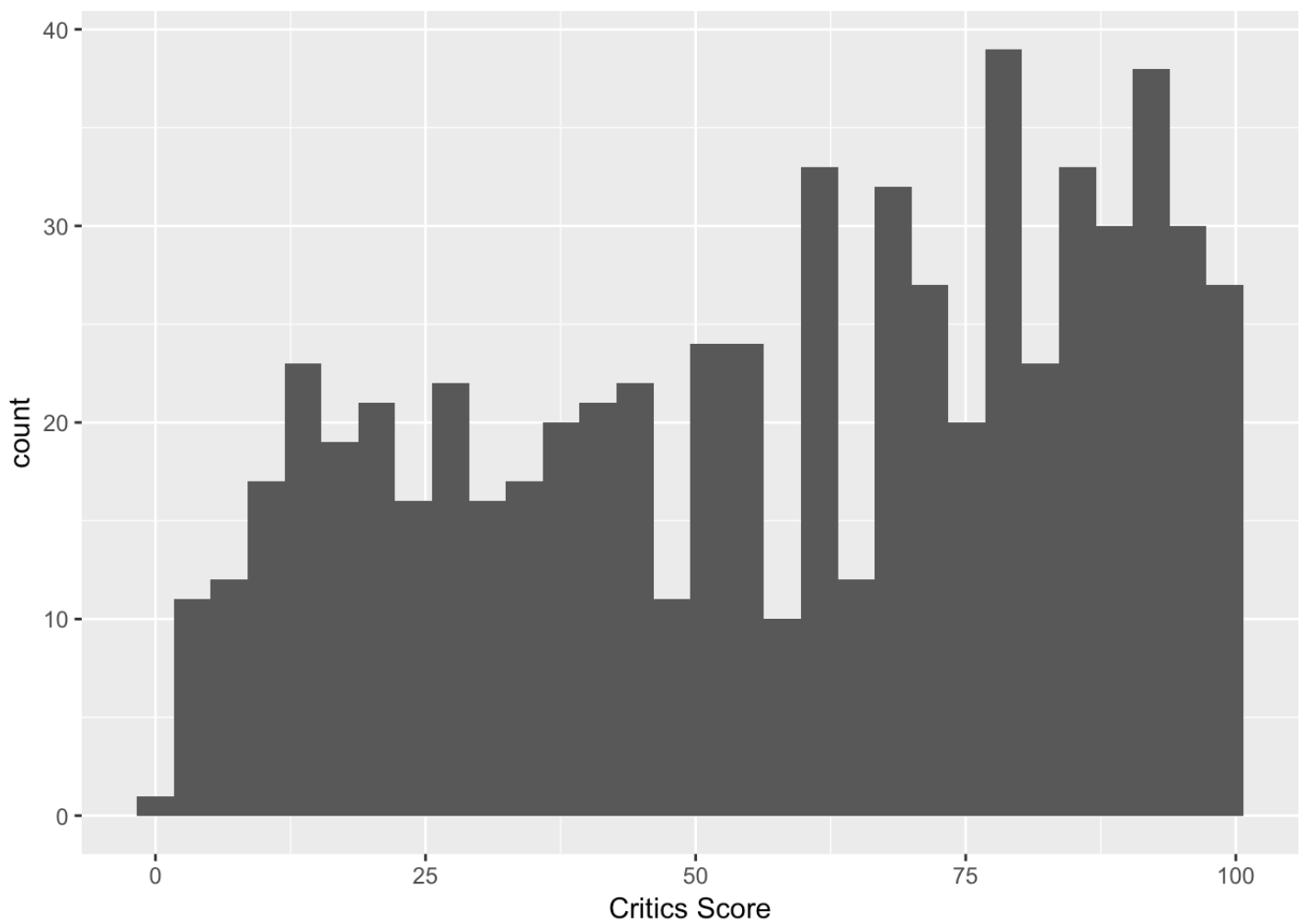
```
ggplot(data = movies_manipulate, aes(x = critics_score, y = audience_score)) + geom_point() + labs(x = "Critic's Score", y = "Audience Score")
```



*# Simply based upon this visualization it looks as if there may be a linear relationship between both the variables IMDB rating and Critics score and audience score respectively.*

```
ggplot(data = movies_manipulate, aes(x = critics_score)) + geom_histogram() + labs(x = "Critics Score")
```

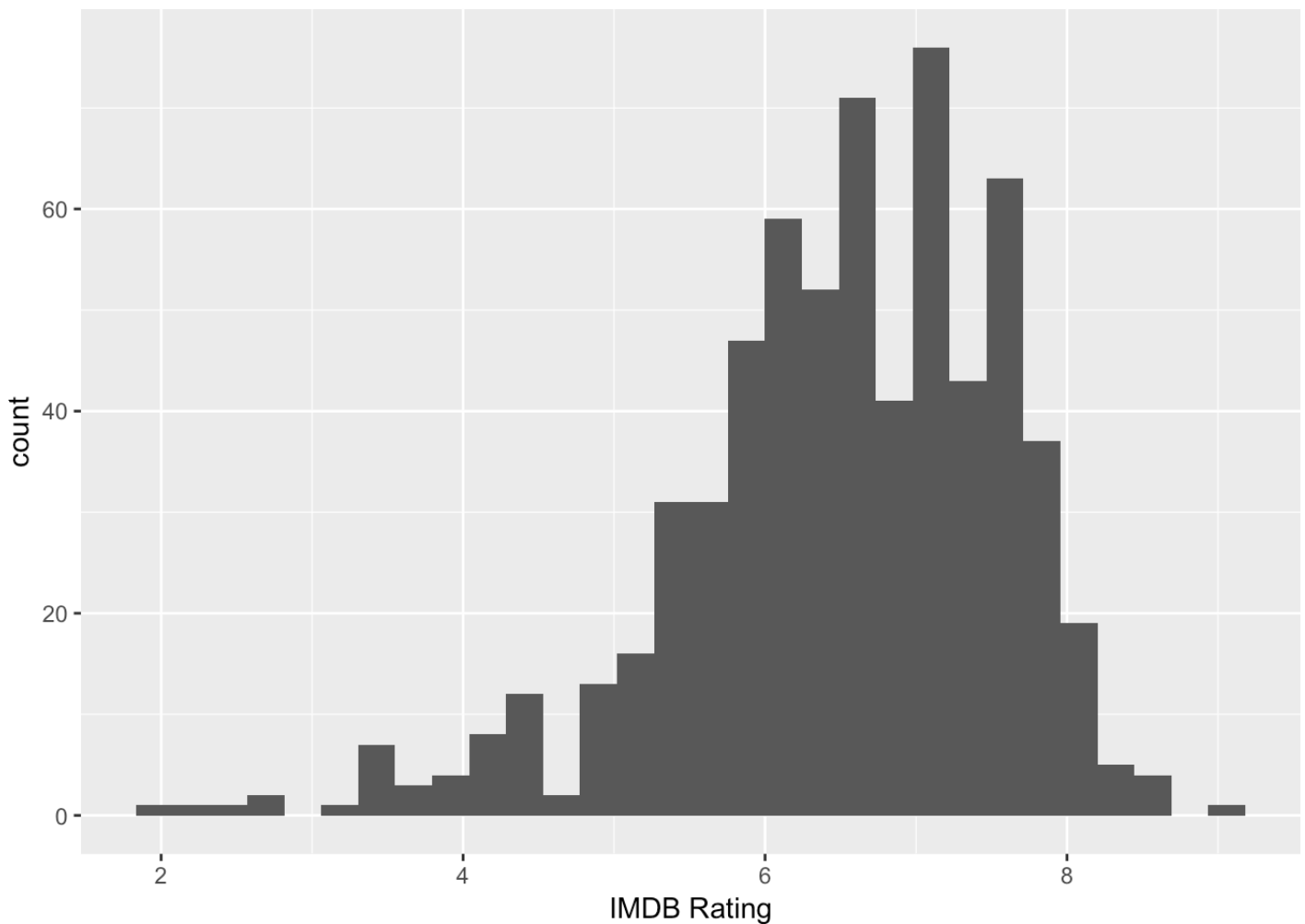
```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



*# There appears to be a uniform distribution of critics scores.*

```
ggplot(data = movies_manipulate, aes(x = imdb_rating)) + geom_histogram() + labs(x =  
"IMDB Rating")
```

```
## `stat_bin()` using `bins = 30`. Pick better value with `binwidth`.
```



*# There appears to be a slightly left-skewed distribution of IMDB ratings though the data appears slightly normal.*

## Part 4: Modeling

```
# Variables of Interest
audience_score_var <- movies_manipulate %>%
  dplyr::select(audience_score, feature_film, drama, runtime, mpaa_rating_R, thtr_rel_
_year, oscar_season, summer_season, imdb_rating, imdb_num_votes, critics_score, best_
pic_nom, best_pic_win, best_actor_win, best_actress_win, best_dir_win, top200_box)
audience_score_var <- na.omit(audience_score_var)
```

```
# Model
audience_score_var_freq <- lm(audience_score ~ ., data = audience_score_var)
tidy(audience_score_var_freq)
```

```
## # A tibble: 17 x 5
##   term                estimate  std.error statistic  p.value
##   <chr>              <dbl>      <dbl>      <dbl>    <dbl>
## 1 (Intercept)       124.        77.5         1.61 1.09e- 1
## 2 feature_filmYes   -2.25        1.69        -1.33 1.83e- 1
## 3 dramaYes          1.29        0.877        1.47 1.41e- 1
## 4 runtime           -0.0561      0.0242       -2.32 2.04e- 2
## 5 mpaa_rating_RYes  -1.44        0.813       -1.78 7.60e- 2
## 6 thtr_rel_year     -0.0766      0.0383       -2.00 4.63e- 2
## 7 oscar_seasonYes   -0.533       0.997       -0.535 5.93e- 1
## 8 summer_seasonYes  0.911        0.949        0.959 3.38e- 1
## 9 imdb_rating       14.7         0.607       24.3 2.03e-92
## 10 imdb_num_votes    0.00000723   0.00000452    1.60 1.10e- 1
## 11 critics_score     0.0575      0.0222        2.59 9.73e- 3
## 12 best_pic_nomyes   5.32        2.63         2.02 4.33e- 2
## 13 best_pic_winyes   -3.21        4.61        -0.697 4.86e- 1
## 14 best_actor_winyes -1.54        1.18        -1.31 1.91e- 1
## 15 best_actress_winyes -2.20       1.30        -1.69 9.23e- 2
## 16 best_dir_winyes   -1.23        1.73        -0.713 4.76e- 1
## 17 top200_boxyes     0.848        2.78         0.305 7.61e- 1
```

```
summary(audience_score_var_freq)
```

```
##
## Call:
## lm(formula = audience_score ~ ., data = audience_score_var)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -28.594  -6.156   0.157   5.909  53.125
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    1.244e+02  7.749e+01   1.606  0.10886
## feature_filmYes -2.248e+00  1.687e+00  -1.332  0.18323
## dramaYes        1.292e+00  8.766e-01   1.474  0.14087
## runtime        -5.614e-02  2.415e-02  -2.324  0.02042 *
## mpaa_rating_RYes -1.444e+00  8.127e-01  -1.777  0.07598 .
## thtr_rel_year   -7.657e-02  3.835e-02  -1.997  0.04628 *
## oscar_seasonYes -5.333e-01  9.967e-01  -0.535  0.59280
## summer_seasonYes 9.106e-01  9.493e-01   0.959  0.33778
## imdb_rating     1.472e+01  6.067e-01  24.258 < 2e-16 ***
## imdb_num_votes   7.234e-06  4.523e-06   1.600  0.11019
## critics_score    5.748e-02  2.217e-02   2.593  0.00973 **
## best_pic_nomyes  5.321e+00  2.628e+00   2.025  0.04330 *
## best_pic_winyes  -3.212e+00  4.610e+00  -0.697  0.48624
## best_actor_winyes -1.544e+00  1.179e+00  -1.310  0.19068
## best_actress_winyes -2.198e+00  1.304e+00  -1.686  0.09229 .
## best_dir_winyes  -1.231e+00  1.728e+00  -0.713  0.47630
## top200_boxyes    8.478e-01  2.782e+00   0.305  0.76067
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.975 on 633 degrees of freedom
## Multiple R-squared:  0.763, Adjusted R-squared:  0.757
## F-statistic: 127.3 on 16 and 633 DF, p-value: < 2.2e-16
```

```
# Statistically significant predictive variables: runtime, year released, imdb rating
, critics score and whether the picture was nominted for an acedemy award
# NB Imdb rating had the lowest p-value followed by critics score
# Simple frequentist linear regression results this just gives a basis to compare Bay
esian Results with
```

```
# Bayesian Regression using ZS-null prior as done in week 5 lab.
bma_ZS <- bas.lm(audience_score ~ ., data = audience_score_var,
                 prior = "ZS-null",
                 modelprior = uniform())
summary(bma_ZS)
```



##	P(B != 0   Y)	model 1	model 2	model 3
## Intercept	1.00000000	1.0000	1.00000000	1.00000000
## feature_filmYes	0.06796946	0.0000	0.00000000	0.00000000
## dramaYes	0.04591717	0.0000	0.00000000	0.00000000
## runtime	0.46420058	0.0000	1.00000000	0.00000000
## mpaa_rating_RYes	0.20274450	0.0000	0.00000000	0.00000000
## thtr_rel_year	0.09499813	0.0000	0.00000000	0.00000000
## oscar_seasonYes	0.07749797	0.0000	0.00000000	0.00000000
## summer_seasonYes	0.08335823	0.0000	0.00000000	0.00000000
## imdb_rating	1.00000000	1.0000	1.00000000	1.00000000
## imdb_num_votes	0.06115184	0.0000	0.00000000	0.00000000
## critics_score	0.88078574	1.0000	1.00000000	1.00000000
## best_pic_nomyes	0.13684669	0.0000	0.00000000	0.00000000
## best_pic_winyes	0.04215714	0.0000	0.00000000	0.00000000
## best_actor_winyes	0.14642057	0.0000	0.00000000	1.00000000
## best_actress_winyes	0.14444247	0.0000	0.00000000	0.00000000
## best_dir_winyes	0.06936269	0.0000	0.00000000	0.00000000
## top200_boxyes	0.04998566	0.0000	0.00000000	0.00000000
## BF	NA	1.0000	0.8702806	0.2236679
## PostProbs	NA	0.1388	0.1208000	0.0311000
## R2	NA	0.7525	0.7549000	0.7539000
## dim	NA	3.0000	4.0000000	4.0000000
## logmarg	NA	443.9495	443.8105657	442.4519125
##	model 4	model 5		
## Intercept	1.00000000	1.00000000		
## feature_filmYes	0.00000000	0.00000000		
## dramaYes	0.00000000	0.00000000		
## runtime	0.00000000	1.00000000		
## mpaa_rating_RYes	1.00000000	1.00000000		
## thtr_rel_year	0.00000000	0.00000000		
## oscar_seasonYes	0.00000000	0.00000000		
## summer_seasonYes	0.00000000	0.00000000		
## imdb_rating	1.00000000	1.00000000		
## imdb_num_votes	0.00000000	0.00000000		
## critics_score	1.00000000	1.00000000		
## best_pic_nomyes	0.00000000	0.00000000		
## best_pic_winyes	0.00000000	0.00000000		
## best_actor_winyes	0.00000000	0.00000000		
## best_actress_winyes	0.00000000	0.00000000		
## best_dir_winyes	0.00000000	0.00000000		
## top200_boxyes	0.00000000	0.00000000		
## BF	0.2217602	0.2055844		
## PostProbs	0.0308000	0.0285000		
## R2	0.7539000	0.7563000		
## dim	4.0000000	5.0000000		
## logmarg	442.4433468	442.3676066		

```
coef_bma <- coefficients(bma_ZS)
confint(coef_bma)
```

```
##              2.5%          97.5%          beta
## Intercept      6.158491e+01 6.312665e+01 6.234769e+01
## feature_filmYes -1.287607e+00 0.000000e+00 -1.081424e-01
## dramaYes       0.000000e+00 0.000000e+00 1.791132e-02
## runtime        -8.332129e-02 0.000000e+00 -2.534532e-02
## mpaa_rating_RYes -2.126881e+00 1.803519e-04 -3.073124e-01
## thtr_rel_year  -5.603212e-02 0.000000e+00 -4.771859e-03
## oscar_seasonYes -1.033925e+00 0.000000e+00 -8.221176e-02
## summer_seasonYes -2.994753e-03 1.130680e+00 8.984037e-02
## imdb_rating     1.369330e+01 1.659671e+01 1.496477e+01
## imdb_num_votes  -1.198173e-09 1.673640e-06 2.242282e-07
## critics_score   0.000000e+00 1.057024e-01 6.227229e-02
## best_pic_nomyes -2.549020e-03 5.011251e+00 5.323609e-01
## best_pic_winyes 0.000000e+00 0.000000e+00 -1.090880e-02
## best_actor_winyes -2.568386e+00 0.000000e+00 -2.897874e-01
## best_actress_winyes -2.884651e+00 6.602460e-03 -3.146149e-01
## best_dir_winyes  -1.558993e+00 0.000000e+00 -1.227043e-01
## top200_boxyes   0.000000e+00 0.000000e+00 9.039557e-02
## attr(,"Probability")
## [1] 0.95
## attr(,"class")
## [1] "confint.bas"
```

```
# Most likely model (P = 0.1388) includes: Intercept, IMDB Rating, Critics Score
```

```
# Which Model to Use
```

```
BMA <- predict(bma_ZS, estimator = "BMA", se.fit = TRUE)
BPM <- predict(bma_ZS, estimator = "BPM", se.fit = TRUE)
variable.names(BPM) # intercept, runtime, imdb rating, critics score
```

```
## [1] "Intercept"      "runtime"         "imdb_rating"     "critics_score"
```

```
HPM <- predict(bma_ZS, estimator = "HPM", se.fit = TRUE)
variable.names(HPM) # intercept, imdb rating, critics score
```

```
## [1] "Intercept"      "imdb_rating"     "critics_score"
```

```
MPM <- predict(bma_ZS, estimator = "MPM", se.fit = TRUE)
variable.names(MPM) # intercept, imdb rating, critics score
```

```
## [1] "Intercept"      "imdb_rating"     "critics_score"
```

```
coef_bma$conditionalmeans[BPM$best,]
```

```
##          Intercept      feature_filmYes      dramaYes
##      6.234769e+01      -3.006730e+01      8.840792e+00
##          runtime      mpaa_rating_RYes      thtr_rel_year
##      4.728376e-02      4.521207e-01      -2.833207e-01
##      oscar_seasonYes      summer_seasonYes      imdb_rating
##      3.505303e-01      1.001027e+00      0.000000e+00
##      imdb_num_votes      critics_score      best_pic_nomyes
##      6.337589e-05      0.000000e+00      0.000000e+00
##      best_pic_winyes      best_actor_winyes      best_actress_winyes
##      -3.367846e+00      -5.371803e-01      -1.769083e+00
##      best_dir_winyes      top200_boxyes
##      2.316835e+00      0.000000e+00
```

```
coef_bma$conditionalsd[BPM$best,]
```

```
##          Intercept      feature_filmYes      dramaYes
##      6.804999e-01      2.538711e+00      1.459679e+00
##          runtime      mpaa_rating_RYes      thtr_rel_year
##      4.125407e-02      1.390988e+00      6.470565e-02
##      oscar_seasonYes      summer_seasonYes      imdb_rating
##      1.707232e+00      1.629747e+00      0.000000e+00
##      imdb_num_votes      critics_score      best_pic_nomyes
##      6.967107e-06      0.000000e+00      0.000000e+00
##      best_pic_winyes      best_actor_winyes      best_actress_winyes
##      7.292645e+00      2.023775e+00      2.238431e+00
##      best_dir_winyes      top200_boxyes
##      2.964864e+00      0.000000e+00
```

```
coef_bma$conditionalmeans[HPM$best,]
```

```
##          Intercept      feature_filmYes      dramaYes
##      62.34769231      -2.07202300      0.89520178
##          runtime      mpaa_rating_RYes      thtr_rel_year
##      -0.05311811      0.00000000      -0.06067619
##      oscar_seasonYes      summer_seasonYes      imdb_rating
##      0.00000000      1.27584824      14.85788275
##      imdb_num_votes      critics_score      best_pic_nomyes
##      0.00000000      0.05741522      5.17974190
##      best_pic_winyes      best_actor_winyes      best_actress_winyes
##      0.00000000      0.00000000      -2.20909892
##      best_dir_winyes      top200_boxyes
##      -1.55509439      0.00000000
```

```
coef_bma$conditionalsd[HPM$best,]
```

```
##          Intercept      feature_filmYes      dramaYes
##          0.39202101      1.59028105      0.85845797
##          runtime      mpaa_rating_RYes      thtr_rel_year
##          0.02280168      0.00000000      0.03656349
##          oscar_seasonYes      summer_seasonYes      imdb_rating
##          0.00000000      0.85055972      0.58455686
##          imdb_num_votes      critics_score      best_pic_nomyes
##          0.00000000      0.02212119      2.32607865
##          best_pic_winyes      best_actor_winyes      best_actress_winyes
##          0.00000000      0.00000000      1.29684984
##          best_dir_winyes      top200_boxyes
##          1.65045573      0.00000000
```

```
MPM_coef = bas.lm(audience_score ~ ., data = audience_score_var,
                  prior="ZS-null",
                  modelprior = uniform(),
                  bestmodel = bma_ZS$probne0 > .5,
                  n.models=1)
coef(MPM_coef)
```

```
##
## Marginal Posterior Summaries of Coefficients:
##
## Using BMA
##
## Based on the top 1 models
##          post mean  post SD  post p(B != 0)
## Intercept          62.34769    0.39549    1.00000
## feature_filmYes      0.00000    0.00000    0.00000
## dramaYes            0.00000    0.00000    0.00000
## runtime             0.00000    0.00000    0.00000
## mpaa_rating_RYes    0.00000    0.00000    0.00000
## thtr_rel_year       0.00000    0.00000    0.00000
## oscar_seasonYes     0.00000    0.00000    0.00000
## summer_seasonYes    0.00000    0.00000    0.00000
## imdb_rating         14.64833    0.56593    1.00000
## imdb_num_votes      0.00000    0.00000    0.00000
## critics_score        0.07316    0.02161    1.00000
## best_pic_nomyes     0.00000    0.00000    0.00000
## best_pic_winyes     0.00000    0.00000    0.00000
## best_actor_winyes   0.00000    0.00000    0.00000
## best_actress_winyes 0.00000    0.00000    0.00000
## best_dir_winyes     0.00000    0.00000    0.00000
## top200_boxyes       0.00000    0.00000    0.00000
```

```
ci_BMA <- confint(BMA, parm = "pred")
opt_BMA <- which.max(BMA$fit)
ci_BMA[opt_BMA,]
```

```
##      2.5%      97.5%      pred
## 78.89563 119.33803 99.76999
```

```
ci_HPM <- confint(HPM, parm = "pred")
opt_HPM <- which.max(HPM$fit)
ci_HPM[opt_HPM,]
```

```
##      2.5%      97.5%      pred
## 82.06589 121.87606 101.97097
```

```
ci_MPM <- confint(MPM, parm = "pred")
opt_MPM <- which.max(MPM$fit)
ci_MPM[opt_MPM,]
```

```
##      2.5%      97.5%      pred
## 82.06589 121.87606 101.97097
```

```
ci_BPM <- confint(BPM, parm = "pred")
opt_BPM <- which.max(BPM$fit)
ci_BPM[opt_BPM,]
```

```
##      2.5%      97.5%      pred
## 77.36827 117.60091 97.48459
```

```

# Variables of interest for each model (BMA, MPM, HPM, MPM) listed above
# CI refers to maximum audience score of a picture based on variables from respective
models (there is a 95% probability that the top rated movie is scored between L and U
)
# BMA: Intercept: 62.3 (95% CI: 61.6-63.1); IMDB Rating: 15.0 (95% CI: 13.7-16.5); c
ritics score: 0.062 (95% CI: 0.0-0.11)
# BMA Model: 99.8 (95% CI: 79.6-120.7)

# BPM: Intercept: 62.3 (sd: 0.55); Runtime: 0.068 (sd: 0.032); IMDB Rating: 0.0 (sd:
0.0); critics score: 0.45 (sd: 0.22)
# BPM Model: 97.5 (95% CI: 77.4-117.6)

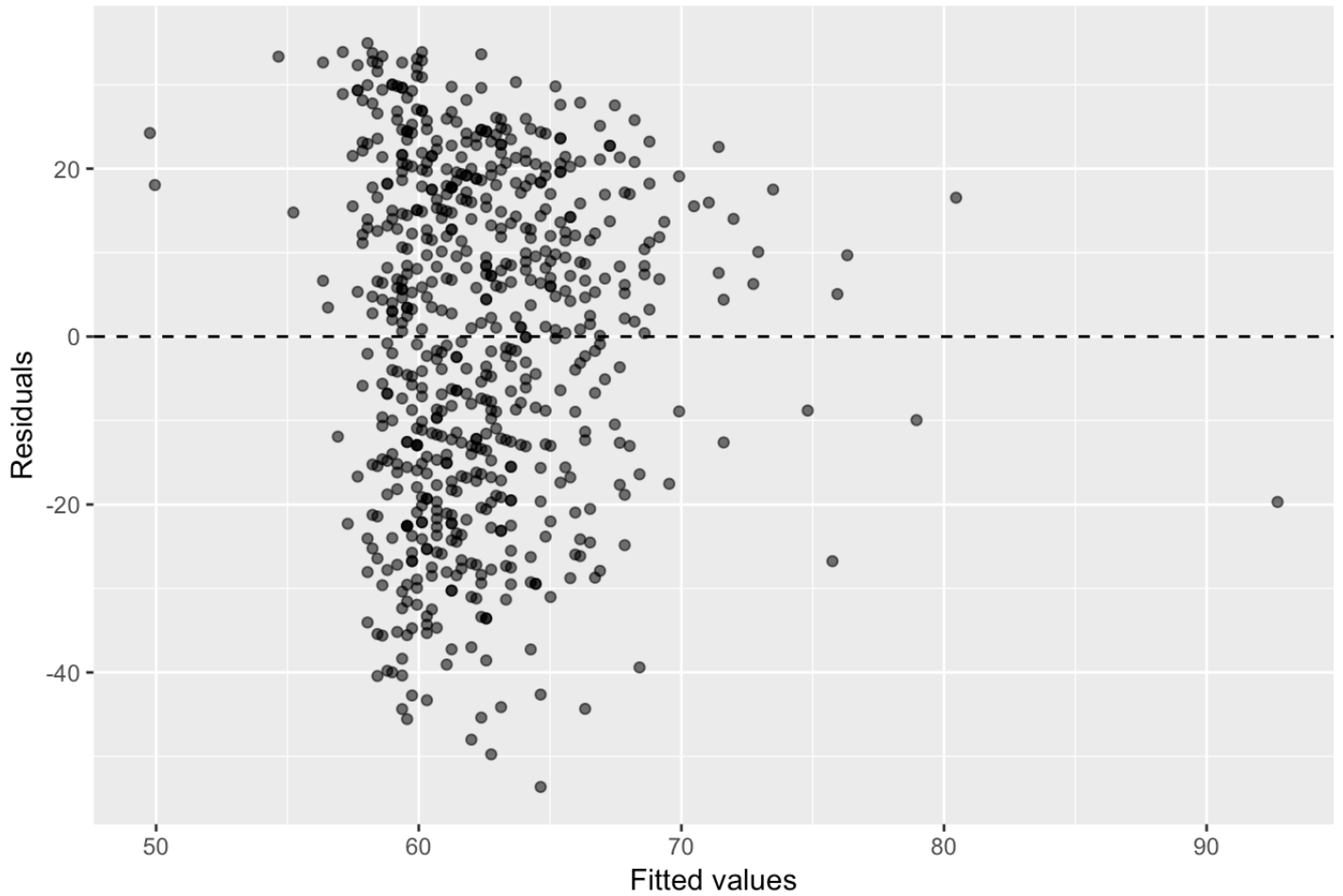
# HPM Intercept: 62.3 (sd: 0.54); IMDB Rating: 0.0 (sd: 0.0); critics score: 0.42 (sd
: 0.22)
# HPM Model: 102.0 (95% CI: 82.0-121.9)

# MPM Intercept: 62.3 (sd: 0.40); IMDB Rating: 14.65 (sd: 0.57); critics score: 0.073
(sd: 0.20)
# MPM Model: 102.0 (95% CI: 82.0-121.9)

# Prior to model selection diagnostics will be performed on continuous variables; che
cks assumptions for Bayesian Regression are true
# Simple Linear Model (Non-Bayesian)
lm_audience_runtime <- lm(audience_score ~ runtime, data = movies_manipulate)
lm_audience_imdb_rating <- lm(audience_score ~ imdb_rating, data = movies_manipulate)
lm_audience_critics_score <- lm(audience_score ~ critics_score, data = movies_manipul
ate)
# Augment; obtaint residual and fitted values
lm_audience_runtime_aug <- augment(lm_audience_runtime)
lm_audience_imdb_rating_aug <- augment(lm_audience_imdb_rating)
lm_audience_critics_score_aug <- augment(lm_audience_critics_score)
# Linearity and Constant Variance
ggplot(data = lm_audience_runtime_aug, aes(x = .fitted, y = .resid)) +
  geom_point(alpha = 0.6) +
  geom_hline(yintercept = 0, linetype = "dashed") +
  labs(x = "Fitted values", y = "Residuals", title = "Runtime")

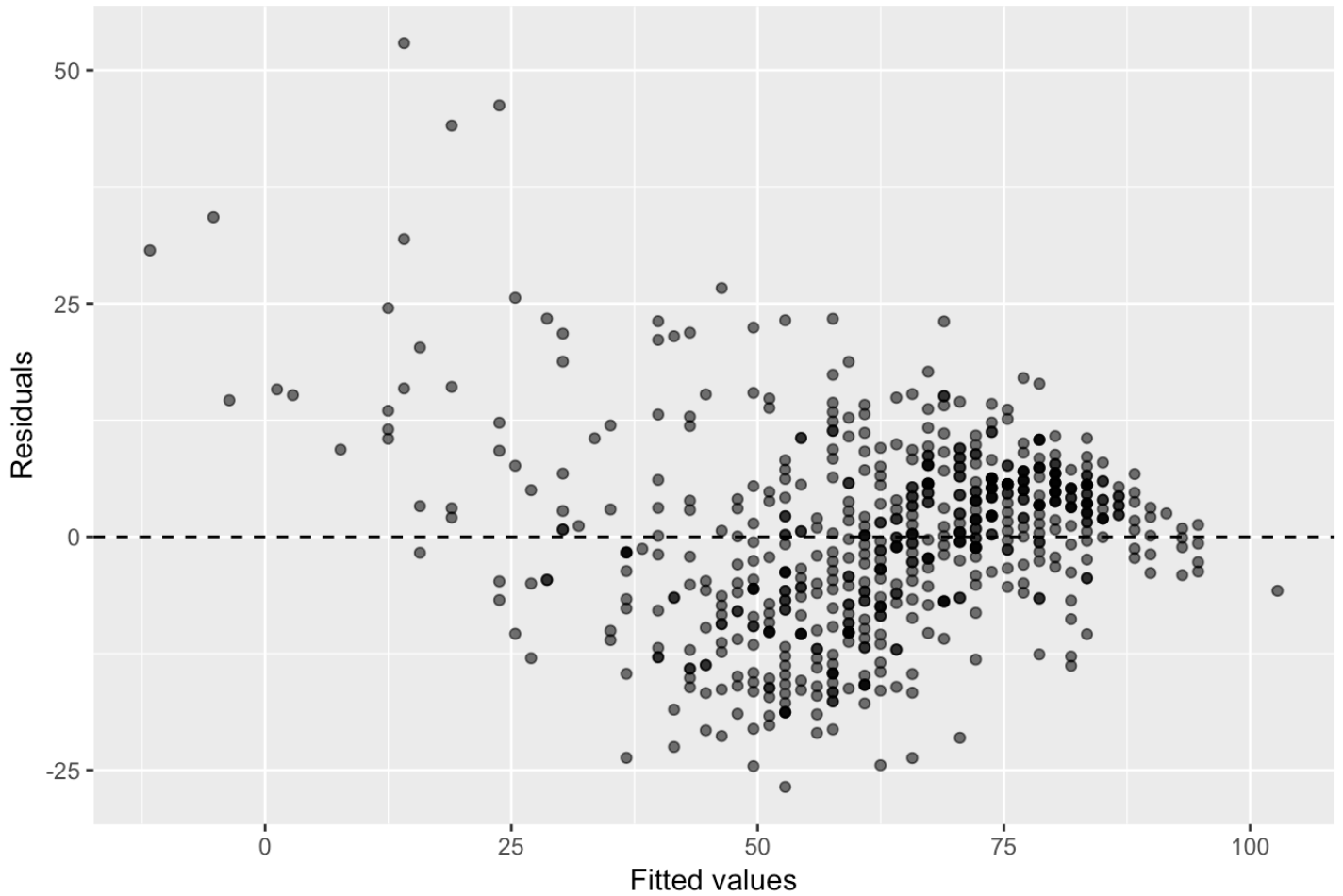
```

## Runtime



```
# The distribution of residuals about the value 0 is not random
ggplot(data = lm_audience_imdb_rating_aug, aes(x = .fitted, y = .resid)) +
  geom_point(alpha = 0.6) +
  geom_hline(yintercept = 0, linetype = "dashed") +
  labs(x = "Fitted values", y = "Residuals", title = "IMDB Rating")
```

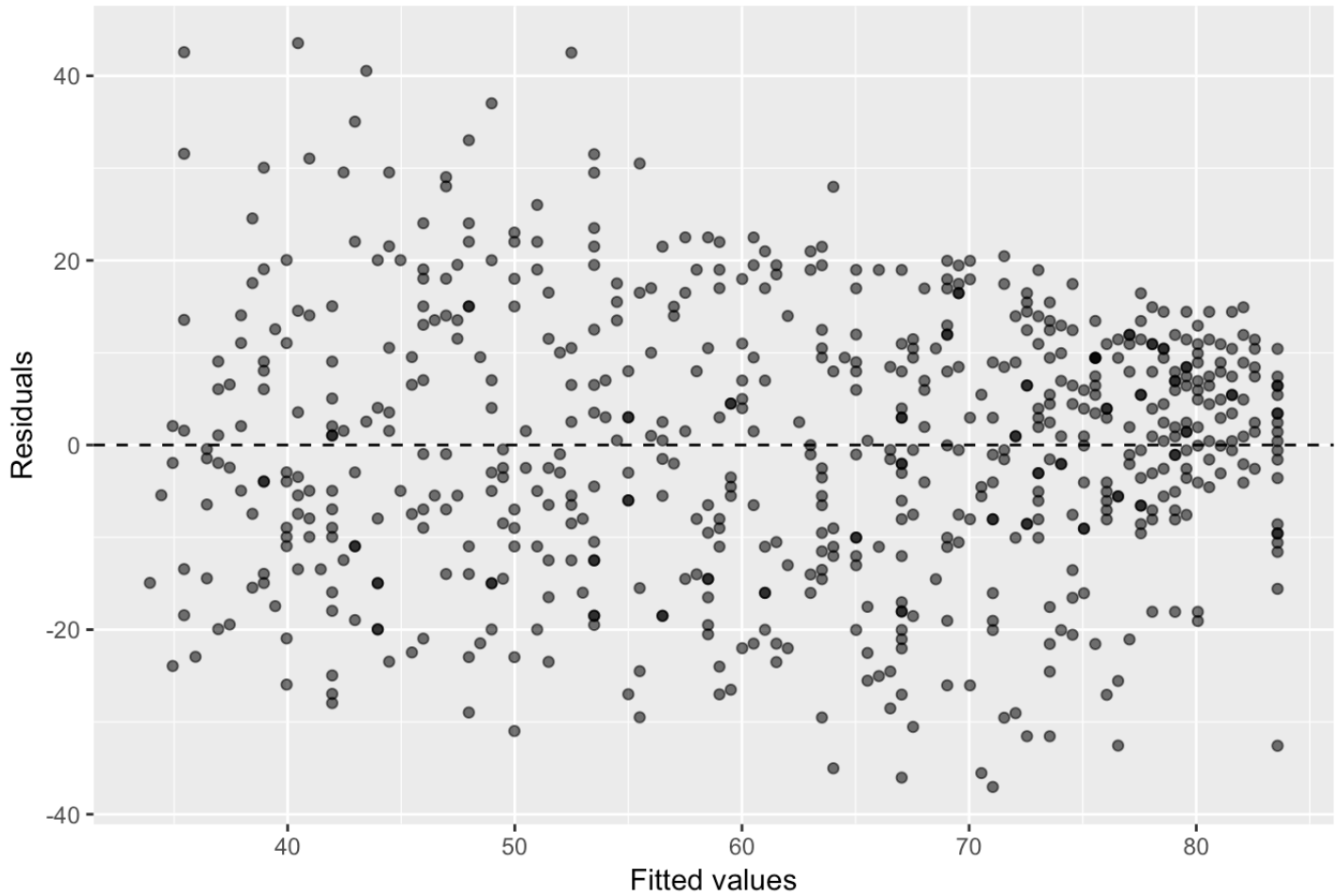
## IMDB Rating



```
# The distribution of residuals about the value 0 is not entirely random, but has less obvious structure than the residual values from runtime
ggplot(data = lm_audience_critics_score_aug, aes(x = .fitted, y = .resid)) +
  geom_point(alpha = 0.6) +
  geom_hline(yintercept = 0, linetype = "dashed") +
  labs(x = "Fitted values", y = "Residuals", title = "Critics Score")
```

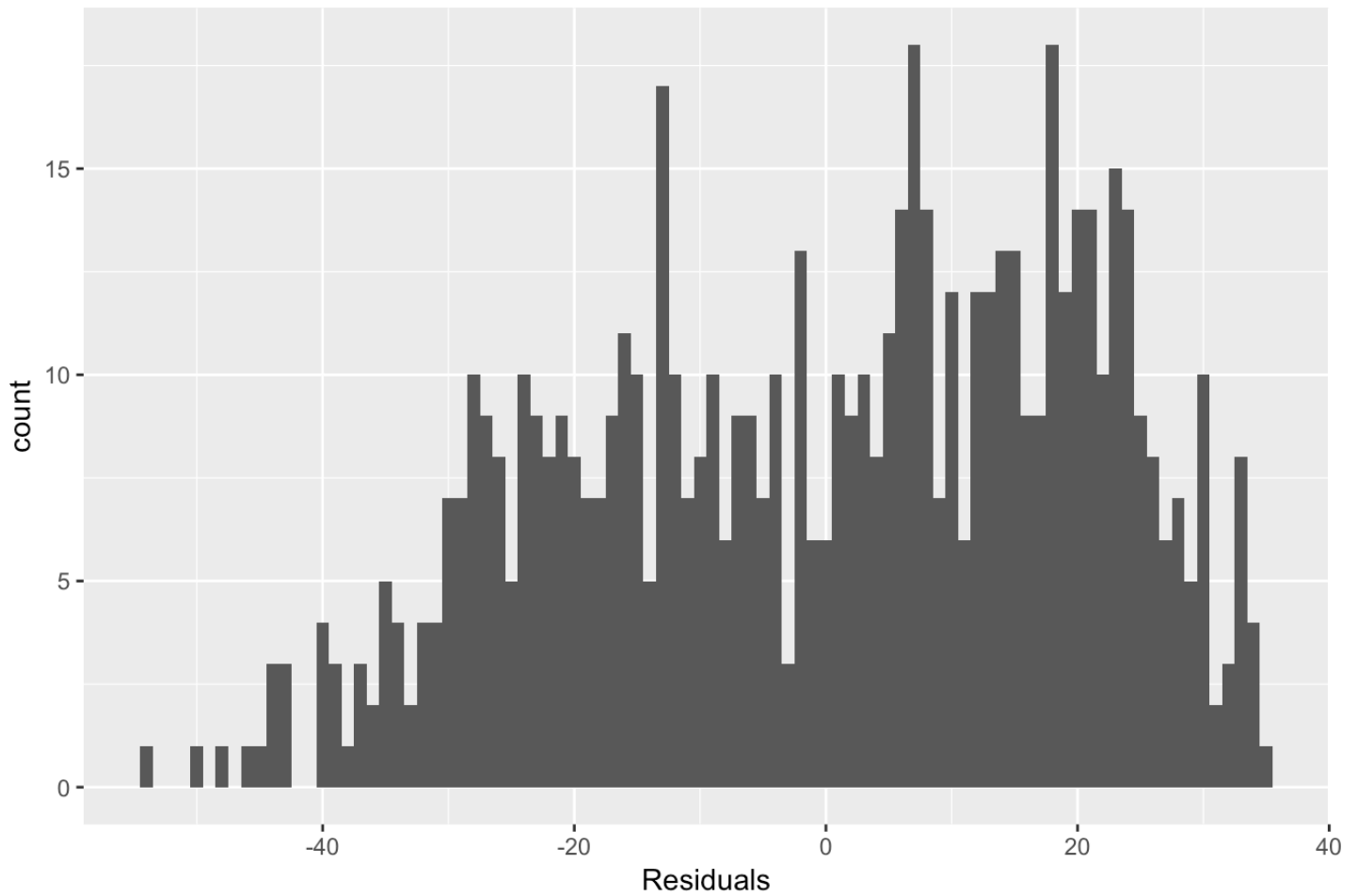


## Critics Score



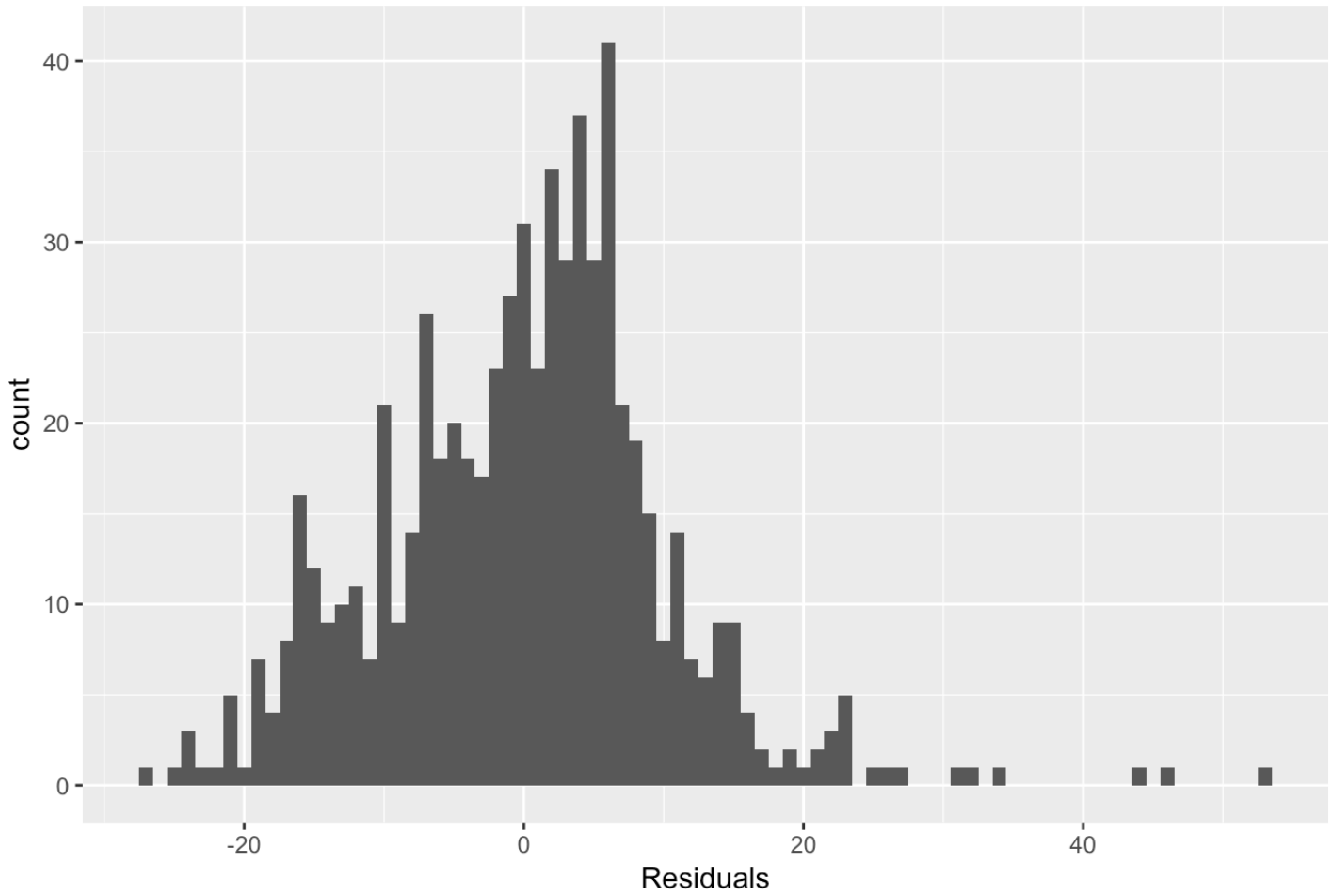
```
# The distribution of residuals about the value 0 random suggesting linearity
# Normality
ggplot(data = lm_audience_runtime_aug, aes(x = .resid)) +
  geom_histogram(binwidth = 1) +
  labs(x = "Residuals", title = "Runtime")
```

## Runtime



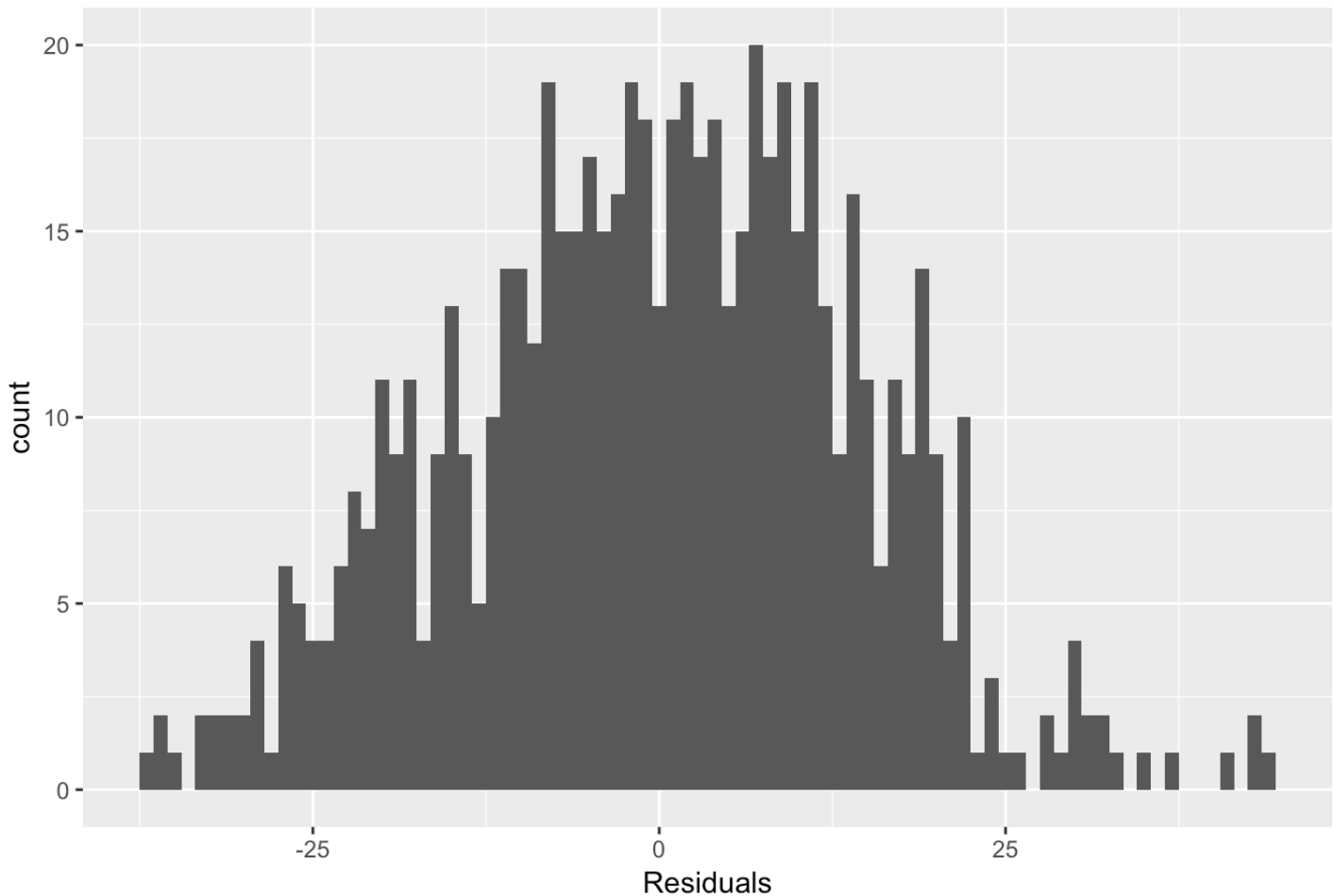
```
# The residuals do not appear to be normally distributed  
ggplot(data = lm_audience_imdb_rating_aug, aes(x = .resid)) +  
  geom_histogram(binwidth = 1) +  
  labs(x = "Residuals", title = "IMDB Rating")
```

## IMDB Rating



```
# The residuals appears to be roughly normal  
ggplot(data = lm_audience_critics_score_aug, aes(x = .resid)) +  
  geom_histogram(binwidth = 1) +  
  labs(x = "Residuals", title = "Critics Score")
```

## Critics Score



*# The residuals show roughly a normal shape though the distribution is broad*

*# Final Model*

*# Variables included in all four models (BMA, BPM, HPM, MPM) are imdb rating and critics score. Based on the parsimonious theory (Occam's razor) it makes sense to choose a model that only has those variables, which removes BPM from final model selection. Runtime, the variable only found in the BPM model, also does not appear to follow the requirements for linearity and normality of residuals, which supports its removal from final model.*

*# Using BIC to confirm model variable selection above is correctly done:*

*# BIC full model*

*BIC(audience\_score\_var\_freq) # BIC = 4934.145*

*## [1] 4934.145*

```
lm_post_models <- lm(audience_score ~ imdb_rating + critics_score, data = audience_score_var)
```

```
BIC(lm_post_models) # BIC = 4871.63
```

```
## [1] 4871.629
```

```
# AIC
```

```
AIC_Step_AS <- stepAIC(audience_score_var_freq, direction = "backward")
```

```
## Start: AIC=3006.94
```

```
## audience_score ~ feature_film + drama + runtime + mpaa_rating_R +  
##   thtr_rel_year + oscar_season + summer_season + imdb_rating +  
##   imdb_num_votes + critics_score + best_pic_nom + best_pic_win +  
##   best_actor_win + best_actress_win + best_dir_win + top200_box  
##
```

	Df	Sum of Sq	RSS	AIC
## - top200_box	1	9	62999	3005.0
## - oscar_season	1	28	63018	3005.2
## - best_pic_win	1	48	63038	3005.4
## - best_dir_win	1	51	63040	3005.5
## - summer_season	1	92	63081	3005.9
## - best_actor_win	1	171	63160	3006.7
## - feature_film	1	177	63166	3006.8
## <none>			62990	3006.9
## - drama	1	216	63206	3007.2
## - imdb_num_votes	1	255	63244	3007.6
## - best_actress_win	1	283	63273	3007.9
## - mpaa_rating_R	1	314	63304	3008.2
## - thtr_rel_year	1	397	63386	3009.0
## - best_pic_nom	1	408	63398	3009.1
## - runtime	1	538	63527	3010.5
## - critics_score	1	669	63659	3011.8
## - imdb_rating	1	58556	121545	3432.2

```
##
```

```
## Step: AIC=3005.04
```

```
## audience_score ~ feature_film + drama + runtime + mpaa_rating_R +  
##   thtr_rel_year + oscar_season + summer_season + imdb_rating +  
##   imdb_num_votes + critics_score + best_pic_nom + best_pic_win +  
##   best_actor_win + best_actress_win + best_dir_win  
##
```

	Df	Sum of Sq	RSS	AIC
## - oscar_season	1	26	63025	3003.3
## - best_pic_win	1	49	63047	3003.5
## - best_dir_win	1	52	63051	3003.6
## - summer_season	1	94	63093	3004.0
## - best_actor_win	1	169	63168	3004.8
## - feature_film	1	176	63175	3004.8
## <none>			62999	3005.0
## - drama	1	214	63213	3005.2
## - best_actress_win	1	279	63278	3005.9
## - imdb_num_votes	1	302	63301	3006.1
## - mpaa_rating_R	1	330	63329	3006.4

```
## - best_pic_nom      1      404  63403 3007.2
## - thtr_rel_year     1      415  63414 3007.3
## - runtime           1      535  63534 3008.5
## - critics_score     1      681  63680 3010.0
## - imdb_rating       1     58606 121604 3430.5
```

```
##
```

```
## Step: AIC=3003.31
```

```
## audience_score ~ feature_film + drama + runtime + mpaa_rating_R +
##   thtr_rel_year + summer_season + imdb_rating + imdb_num_votes +
##   critics_score + best_pic_nom + best_pic_win + best_actor_win +
##   best_actress_win + best_dir_win
```

```
##
```

	Df	Sum of Sq	RSS	AIC
## - best_pic_win	1	46	63071	3001.8
## - best_dir_win	1	56	63081	3001.9
## - best_actor_win	1	174	63200	3003.1
## - summer_season	1	177	63202	3003.1
## - feature_film	1	182	63207	3003.2
## <none>			63025	3003.3
## - drama	1	222	63247	3003.6
## - best_actress_win	1	281	63307	3004.2
## - imdb_num_votes	1	302	63328	3004.4
## - mpaa_rating_R	1	329	63354	3004.7
## - best_pic_nom	1	387	63412	3005.3
## - thtr_rel_year	1	410	63436	3005.5
## - runtime	1	587	63613	3007.3
## - critics_score	1	679	63704	3008.3
## - imdb_rating	1	58603	121628	3428.6

```
##
```

```
## Step: AIC=3001.78
```

```
## audience_score ~ feature_film + drama + runtime + mpaa_rating_R +
##   thtr_rel_year + summer_season + imdb_rating + imdb_num_votes +
##   critics_score + best_pic_nom + best_actor_win + best_actress_win +
##   best_dir_win
```

```
##
```

	Df	Sum of Sq	RSS	AIC
## - best_dir_win	1	94	63165	3000.7
## - best_actor_win	1	163	63234	3001.5
## - feature_film	1	171	63242	3001.5
## - summer_season	1	174	63245	3001.6
## <none>			63071	3001.8
## - drama	1	220	63291	3002.0
## - imdb_num_votes	1	271	63342	3002.6
## - best_actress_win	1	294	63365	3002.8
## - mpaa_rating_R	1	330	63401	3003.2
## - best_pic_nom	1	342	63414	3003.3
## - thtr_rel_year	1	397	63468	3003.9
## - runtime	1	586	63657	3005.8
## - critics_score	1	680	63751	3006.8
## - imdb_rating	1	58858	121929	3428.2

```

##
## Step: AIC=3000.75
## audience_score ~ feature_film + drama + runtime + mpaa_rating_R +
##     thtr_rel_year + summer_season + imdb_rating + imdb_num_votes +
##     critics_score + best_pic_nom + best_actor_win + best_actress_win
##
##           Df Sum of Sq    RSS    AIC
## - summer_season      1      167  63332 3000.5
## - best_actor_win      1      171  63336 3000.5
## - feature_film        1      183  63348 3000.6
## <none>                                63165 3000.7
## - drama               1      228  63394 3001.1
## - imdb_num_votes      1      247  63412 3001.3
## - best_actress_win    1      299  63464 3001.8
## - best_pic_nom        1      326  63491 3002.1
## - mpaa_rating_R       1      345  63510 3002.3
## - thtr_rel_year       1      368  63533 3002.5
## - critics_score       1      651  63816 3005.4
## - runtime             1      673  63839 3005.6
## - imdb_rating         1     58895 122061 3426.9
##
## Step: AIC=3000.46
## audience_score ~ feature_film + drama + runtime + mpaa_rating_R +
##     thtr_rel_year + imdb_rating + imdb_num_votes + critics_score +
##     best_pic_nom + best_actor_win + best_actress_win
##
##           Df Sum of Sq    RSS    AIC
## - feature_film        1      156  63488 3000.1
## <none>                                63332 3000.5
## - best_actor_win      1      195  63527 3000.5
## - drama               1      204  63536 3000.6
## - imdb_num_votes      1      260  63592 3001.1
## - best_pic_nom        1      297  63629 3001.5
## - best_actress_win    1      297  63629 3001.5
## - mpaa_rating_R       1      356  63688 3002.1
## - thtr_rel_year       1      361  63693 3002.2
## - runtime             1      690  64022 3005.5
## - critics_score       1      732  64064 3005.9
## - imdb_rating         1     58763 122095 3425.1
##
## Step: AIC=3000.06
## audience_score ~ drama + runtime + mpaa_rating_R + thtr_rel_year +
##     imdb_rating + imdb_num_votes + critics_score + best_pic_nom +
##     best_actor_win + best_actress_win
##
##           Df Sum of Sq    RSS    AIC
## - drama               1      121  63609 2999.3
## - imdb_num_votes      1      173  63661 2999.8
## <none>                                63488 3000.1
## - best_actor_win      1      219  63706 3000.3

```

```
## - thtr_rel_year      1      277  63765 3000.9
## - best_pic_nom       1      291  63778 3001.0
## - best_actress_win   1      306  63794 3001.2
## - mpaa_rating_R      1      453  63941 3002.7
## - runtime            1      715  64203 3005.3
## - critics_score      1      875  64363 3007.0
## - imdb_rating        1     63189 126677 3447.1
##
## Step: AIC=2999.3
## audience_score ~ runtime + mpaa_rating_R + thtr_rel_year + imdb_rating +
##     imdb_num_votes + critics_score + best_pic_nom + best_actor_win +
##     best_actress_win
##
##              Df Sum of Sq    RSS    AIC
## - imdb_num_votes  1      148  63757 2998.8
## <none>                        63609 2999.3
## - best_actor_win   1      209  63818 2999.4
## - thtr_rel_year    1      272  63881 3000.1
## - best_actress_win 1      274  63883 3000.1
## - best_pic_nom     1      307  63916 3000.4
## - mpaa_rating_R    1      391  64000 3001.3
## - runtime          1      631  64240 3003.7
## - critics_score    1      916  64525 3006.6
## - imdb_rating      1     63434 127043 3447.0
##
## Step: AIC=2998.81
## audience_score ~ runtime + mpaa_rating_R + thtr_rel_year + imdb_rating +
##     critics_score + best_pic_nom + best_actor_win + best_actress_win
##
##              Df Sum of Sq    RSS    AIC
## <none>                        63757 2998.8
## - thtr_rel_year    1      201  63958 2998.9
## - best_actor_win   1      219  63976 2999.0
## - best_actress_win 1      266  64023 2999.5
## - mpaa_rating_R    1      367  64124 3000.5
## - best_pic_nom     1      442  64199 3001.3
## - runtime          1      519  64276 3002.1
## - critics_score    1      879  64635 3005.7
## - imdb_rating      1     67356 131113 3465.4
```

```
# Using the variables from the model with the lowest AIC score
lm_post_AIC <- lm(audience_score ~ runtime + mpaa_rating_R + thtr_rel_year + imdb_rating +
  critics_score + best_pic_nom + best_actor_win + best_actress_win, data = audience_score_var)
BIC(lm_post_AIC) # BIC = 4890.2
```

```
## [1] 4890.199
```



*# The BIC using the variables selected from the models above lowers the BIC score. Stepwise model that yields the lowest AIC value, which is used in some model selection processes, produced a model or group of variables that did not have a lower BIC than the model created from the above information.*

*# Penn State College of Human Health: "So what's the bottom line? In general, it might be best to use AIC and BIC together in model selection."*

*# Ultimately the BMA model is chosen as the best model as it has the least number of variables, which themselves produce lowest BIC. It is chosen above the HPM and MPM models because those models have a predicted maximum value greater than 100, which is impossible under the Rotten Tomato scoring rubric.*

*# For every 1 increase in IMDB rating audience score increases on average by 15 points; there is a 0.95 probability that for every increase in IMDB rating the audience score increases on average between 13.7 and 16.5 points; for every 1 increase in critics score the audience score increases on average by 0.062 points; there is a 0.95 probability that for every 1 point increase in critics score the audience score increases on average between 0 to 0.11 points.*

## Part 5: Prediction

```
# Manchester by the Sea
MS_b <- data.frame(77, 'Yes', 'Yes', 137, 'Yes', 2016, 'Yes', 'No', 7.8, 198685, 95,
'yes', 'no', 'yes', 'no', 'no', 'no')
colnames(MS_b) = colnames(audience_score_var)
```

MS\_b

```
## audience_score feature_film drama runtime mpaa_rating_R thtr_rel_year
## 1 77 Yes Yes 137 Yes 2016
## oscar_season summer_season imdb_rating imdb_num_votes critics_score
## 1 Yes No 7.8 198685 95
## best_pic_nom best_pic_win best_actor_win best_actress_win best_dir_win
## 1 yes no yes no no
## top200_box
## 1 no
```

```
summary(MS_b)
```

```
## audience_score feature_film drama runtime mpaa_rating_R
## Min. :77 Yes:1 Yes:1 Min. :137 Yes:1
## 1st Qu.:77 1st Qu.:137
## Median :77 Median :137
## Mean :77 Mean :137
## 3rd Qu.:77 3rd Qu.:137
## Max. :77 Max. :137
## thtr_rel_year oscar_season summer_season imdb_rating imdb_num_votes
## Min. :2016 Yes:1 No:1 Min. :7.8 Min. :198685
## 1st Qu.:2016 1st Qu.:7.8 1st Qu.:198685
## Median :2016 Median :7.8 Median :198685
## Mean :2016 Mean :7.8 Mean :198685
## 3rd Qu.:2016 3rd Qu.:7.8 3rd Qu.:198685
## Max. :2016 Max. :7.8 Max. :198685
## critics_score best_pic_nom best_pic_win best_actor_win best_actress_win
## Min. :95 yes:1 no:1 yes:1 no:1
## 1st Qu.:95
## Median :95
## Mean :95
## 3rd Qu.:95
## Max. :95
## best_dir_win top200_box
## no:1 no:1
##
##
##
##
##
```

```
# The BIC prior is chosen based on week 5 lab and the discussion board responses.
MS_baslm_b <- bas.lm(audience_score ~ ., data = audience_score_var,
                     prior = 'BIC',
                     modelprior = uniform())
colnames(MS_b) = colnames(audience_score_var)

MS_baslm_b
```

```
##
## Call:
## bas.lm(formula = audience_score ~ ., data = audience_score_var,
##       prior = "BIC", modelprior = uniform())
##
##
## Marginal Posterior Inclusion Probabilities:
##      Intercept      feature_filmYes      dramaYes
##      1.00000      0.06537      0.04320
##      runtime      mpaa_rating_RYes      thtr_rel_year
##      0.46971      0.19984      0.09069
##      oscar_seasonYes      summer_seasonYes      imdb_rating
##      0.07506      0.08042      1.00000
##      imdb_num_votes      critics_score      best_pic_nomyes
##      0.05774      0.88855      0.13119
##      best_pic_winyes      best_actor_winyes      best_actress_winyes
##      0.03985      0.14435      0.14128
##      best_dir_winyes      top200_boxyes
##      0.06694      0.04762
```

```
summary(MS_baslm_b)
```

##	P(B != 0   Y)	model 1	model 2	model 3
## Intercept	1.00000000	1.0000	1.00000000	1.00000000
## feature_filmYes	0.06536947	0.0000	0.00000000	0.00000000
## dramaYes	0.04319833	0.0000	0.00000000	0.00000000
## runtime	0.46971477	1.0000	0.00000000	0.00000000
## mpaa_rating_RYes	0.19984016	0.0000	0.00000000	0.00000000
## thtr_rel_year	0.09068970	0.0000	0.00000000	0.00000000
## oscar_seasonYes	0.07505684	0.0000	0.00000000	0.00000000
## summer_seasonYes	0.08042023	0.0000	0.00000000	0.00000000
## imdb_rating	1.00000000	1.0000	1.00000000	1.00000000
## imdb_num_votes	0.05773502	0.0000	0.00000000	0.00000000
## critics_score	0.88855056	1.0000	1.00000000	1.00000000
## best_pic_nomyes	0.13119140	0.0000	0.00000000	0.00000000
## best_pic_winyes	0.03984766	0.0000	0.00000000	0.00000000
## best_actor_winyes	0.14434896	0.0000	0.00000000	1.00000000
## best_actress_winyes	0.14128087	0.0000	0.00000000	0.00000000
## best_dir_winyes	0.06693898	0.0000	0.00000000	0.00000000
## top200_boxyes	0.04762234	0.0000	0.00000000	0.00000000
## BF	NA	1.0000	0.9968489	0.2543185
## PostProbs	NA	0.1297	0.1293000	0.0330000
## R2	NA	0.7549	0.7525000	0.7539000
## dim	NA	4.0000	3.0000000	4.0000000
## logmarg	NA	-3615.2791	-3615.2822108	-3616.6482224
##	model 4	model 5		
## Intercept	1.00000000	1.00000000		
## feature_filmYes	0.00000000	0.00000000		
## dramaYes	0.00000000	0.00000000		
## runtime	0.00000000	1.00000000		
## mpaa_rating_RYes	1.00000000	1.00000000		
## thtr_rel_year	0.00000000	0.00000000		
## oscar_seasonYes	0.00000000	0.00000000		
## summer_seasonYes	0.00000000	0.00000000		
## imdb_rating	1.00000000	1.00000000		
## imdb_num_votes	0.00000000	0.00000000		
## critics_score	1.00000000	1.00000000		
## best_pic_nomyes	0.00000000	0.00000000		
## best_pic_winyes	0.00000000	0.00000000		
## best_actor_winyes	0.00000000	0.00000000		
## best_actress_winyes	0.00000000	0.00000000		
## best_dir_winyes	0.00000000	0.00000000		
## top200_boxyes	0.00000000	0.00000000		
## BF	0.2521327	0.2391994		
## PostProbs	0.0327000	0.0310000		
## R2	0.7539000	0.7563000		
## dim	4.0000000	5.0000000		
## logmarg	-3616.6568544	-3616.7095127		

```
MS_pred_bd = predict(MS_baslm_b, newdata = MS_b, estimator = "BMA", se.fit = TRUE)
MS_pred_bd$fit # 83.50
```

```
## [1] 83.49721
```

```
# CI
MS_pred_bd_ci <- confint(MS_pred_bd, estimator = "BMA")
MS_pred_bd_ci # CI: 63.3.-103.4
```

```
##           2.5%    97.5%    pred
## [1,] 63.98796 104.4521 83.49721
## attr(,"Probability")
## [1] 0.95
## attr(,"class")
## [1] "confint.bas"
```

```
# Sensitivity Analysis to see how other prediction methods compare with the results above.
MS_pred_ba = predict(MS_baslm_b, newdata = MS_b, estimator = "HPM", se.fit = TRUE)
MS_pred_ba$fit # 82.91
```

```
## [1] 82.90536
## attr(,"model")
## [1] 0 3 8 10
## attr(,"best")
## [1] 8776
## attr(,"estimator")
## [1] "HPM"
```

```
MS_pred_ba_ci <- confint(MS_pred_ba, estimator = "HPM")
MS_pred_ba_ci # CI: 63.1-102.7
```

```
##           2.5%    97.5%    pred
## [1,] 63.11821 102.6925 82.90536
## attr(,"Probability")
## [1] 0.95
## attr(,"class")
## [1] "confint.bas"
```

## Part 6: Conclusion

Though many variables were collected during the sampling process only several of them are statistically significant in the simple linear regression model for explaining audience score. After applying Bayesian linear regression even fewer variables were found to be significantly associated with audience score. BIC was primarily used to determine which variables should be included in the analysis as well as the BMA prediction method.

The research question is which variables are associated with audience score and is it possible to predict the audience score of a movie using Bayesian linear regression. Having found the predictive model a regression was run and the variables for the movie Manchester by the Sea were entered into the model. The predicted audience score is 83.5. There is a 0.95 probability that Manchester by the Sea receives an audience score on average between 63.3 and 103.4.

Manchester by the Sea received an audience rating of 77, which sits within the credible interval found in the prediction stage. The biggest concern with this prediction is the large credible interval, which suggests a lack of accuracy. That being said, the predicted value was close to the actual value therefore there is some validity in using this model to predict the audience score of movies released in 2016.