✓ Congratulations! You passed!

~	1/1 points
1. We use	e the continuous version of Bayes' theorem if:
0	heta is continuous
Correll $ heta$ if $ heta$ i	ect s continuous, we use a probability density for the prior.
	Y is continuous
	$f(y\mid heta)$ is continuous
	All of the above
	None of the above
	1/1

2.

points

Consider the coin-flipping example from the lesson. Recall that the likelihood for this experiment was Bernoulli with unknown probability of heads, i.e., $f(y\mid\theta)=\theta^y(1-\theta)^{1-y}I_{\{0\leq\theta\leq1\}}\text{, and we started with a uniform prior on the interval }[0,1].$

After the first flip resulted in heads $(Y_1=1)$, the posterior for heta became $f(heta\mid Y_1=1)=2 heta I_{\{0\leq heta\leq 1\}}.$

Now use this posterior as your prior for θ before the next (second) flip. Which of the following represents the posterior PDF for θ after the second flip also results in heads $(Y_2=1)$?

$$\int f(\theta \mid Y_2 = 1) = rac{ heta \cdot 2 heta}{\int_0^1 heta \cdot 2 heta d heta} I_{\{0 \leq heta \leq 1\}}$$

Correct

This simplifies to the posterior PDF $f(\theta \mid Y_2 = 1) = 3\theta^2 I_{\{0 \leq \theta \leq 1\}}$.

Incidentally, if we assume that the two coin flips are independent, we would have arrived at the same posterior if we had again started with a uniform prior and performed a single update using $Y_1=1$ and $Y_2=1$.

$$\int f(heta \mid Y_2=1) = rac{(1- heta)\cdot 2 heta}{\int_0^1 (1- heta)\cdot 2 heta d heta} I_{\{0\leq heta\leq 1\}}$$

$$\int f(heta \mid Y_2 = 1) = rac{ heta(1- heta)\cdot 2 heta}{\int_0^1 heta(1- heta)\cdot 2 heta d heta} I_{\{0\leq heta\leq 1\}}$$



1/1 points

3.

Consider again the coin-flipping example from the lesson. Recall that we used a Uniform(0,1) prior for θ . Which of the following is a correct interpretation of $P(0.3 < \theta < 0.9) = 0.6$?



(0.3, 0.9) is a 60% credible interval for θ before observing any data.

Correct

The probability statement came from our prior, so the prior probability that θ is in this interval is 0.6.

- (0.3, 0.9) is a 60% credible interval for heta after observing Y=1.
- (0.3, 0.9) is a 60% confidence interval for θ .

	The posterior probability that $ heta \in (0.3, 0.9)$ is 0.6.
~	1 / 1 points
PDF fo followi	der again the coin-flipping example from the lesson. Recall that the posterior r $ heta$, after observing $Y=1$, was $f(\theta\mid Y=1)=2\theta I_{\{0\leq \theta\leq 1\}}.$ Which of the r is a correct interpretation of r
	(0.3, 0.9) is a 72% credible interval for $ heta$ before observing any data.
0	(0.3, 0.9) is a 72% credible interval for $ heta$ after observing $Y=1$.
	probability statement came from the posterior, so the posterior pability that $ heta$ is in this interval is 0.72.
	(0.3, 0.9) is a 72% confidence interval for $ heta$.
	The prior probability that $ heta \in (0.3, 0.9)$ is 0.72.
~	1 / 1 points
	two quantiles are required to capture the middle 90% of a distribution (thus ting a 90% equal-tailed interval)?
	0 and .9
	.025 and .975
	.10 and .90
0	.05 and .95
	of the probability mass is contained between the .05 and .95 quantiles (or valently, the 5th and 95th percentiles). 5% of the probability lies on either

side of this interval.



1/1 points

6.

Suppose you collect measurements to perform inference about a population mean θ . Your posterior distribution after observing data is $\theta \mid \mathbf{y} \sim N(0,1)$.

Report the upper end of a 95% equal-tailed interval for θ . Round your answer to two decimal places.

1.96

Correct Response

The 95% equal-tailed interval for a standard normal distribution is (-1.96, 1.96).

Because the normal distribution is symmetric and unimodal (has only one peak), the equal-tailed interval is also the highest posterior density (HPD) interval.

In R:

```
1 qnorm(p=0.975, mean=0, sd=1)
```

In Excel:

where probability=0.975, mean=0, standard_dev=1.



1/1 points

7.

What does "HPD interval" stand for?



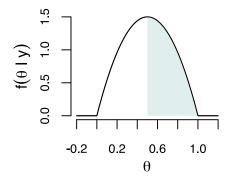
Highest posterior density interval

Correct

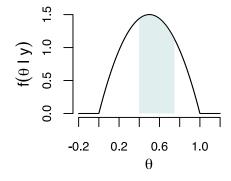
Highest point distance interval
Highest precision density interval

Highest partial density interval

- 1/1 points
- 8. Each of the following graphs depicts a 50% credible interval from a posterior distribution. Which of the intervals represents the HPD interval?
 - \bigcirc 50% interval: $heta \in (0.500, 1.000)$



 \bigcirc 50% interval: $heta \in (0.400, 0.756)$

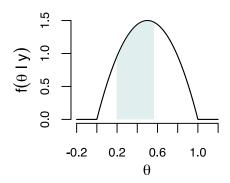


Lesson 5.3-5.4

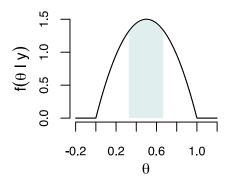
8/8 points (100%)

Quiz, 8 questions

 \bigcirc 50% interval: $heta \in (0.196, 0.567)$



 \bigcirc 50% interval: $heta \in (0.326, 0.674)$



Correct

This is the 50% credible interval with the highest posterior density values. It is the shortest possible interval containing 50% of the probability under this posterior distribution.



