6

C Arrays

Now go, write it before them in a table, and note it in a book.

—Isaiah 30:8

To go beyond is as wrong as to fall short.

—Confucius

Begin at the beginning, ... and go on till you come to the end: then stop.

—Lewis Carroll



OBJECTIVES

In this chapter you will learn:

- To use the array data structure to represent lists and tables of values.
- To define an array, initialize an array and refer to individual elements of an array.
- To define symbolic constants.
- To pass arrays to functions.
- To use arrays to store, sort and search lists and tables of values.
- To define and manipulate multiple-subscripted arrays.



6.1 Introduction	n
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- 6.2 **Arrays**
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- 6.6 **Sorting Arrays**
- Case Study: Computing Mean, Median and Mode 6.7 **Using Arrays**
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- **Multiple-Subscripted Arrays** 6.9



6.1 Introduction

Arrays

- Structures of related data items
- Static entity same size throughout program
- Dynamic data structures discussed in Chapter 12

6.2 Arrays

Array

- Group of consecutive memory locations
- Same name and type
- To refer to an element, specify
 - Array name
 - Position number

Format:

arrayname [position number]

- First element at position 0
- n element array named c:

```
- c[ 0 ], c[ 1 ]...c[ n - 1 ]
```



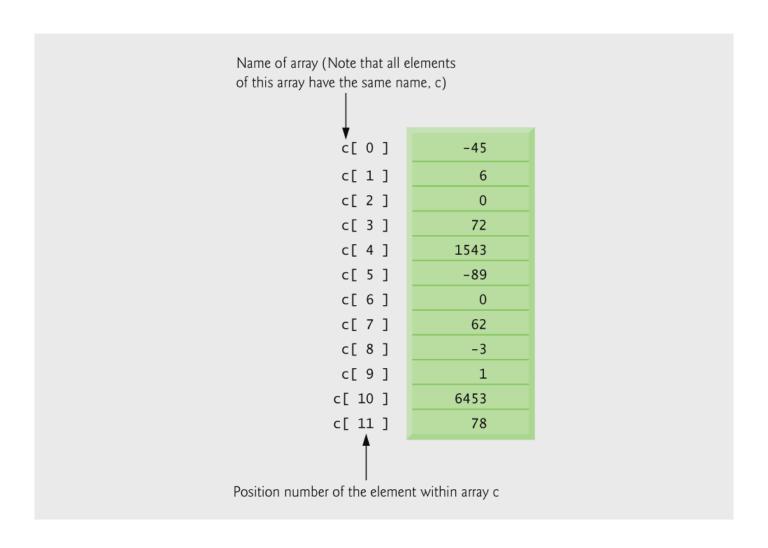


Fig. 6.1 | 12-element array.

6.2 Arrays

Array elements are like normal variables

Perform operations in subscript. If x equals 3

$$c[5-2] == c[3] == c[x]$$

It is important to note the difference between the "seventh element of the array" and "array element seven." Because array subscripts begin at 0, the "seventh element of the array" has a subscript of 6, while "array element seven" has a subscript of 7 and is actually the eighth element of the array. This is a source of "off-by-one" errors.

Ope	ratoı	rs			Associativity	Туре
[]	O				left to right	highest
++		!	(type)		right to left	unary
*	/	%			left to right	multiplicative
+	-				left to right	additive
<	<=	>	>=		left to right	relational
==	!=				left to right	equality
&&					left to right	logical AND
П					left to right	logical OR
?:					right to left	conditional
=	+=	-=	*= /=	%=	right to left	assignment
,					left to right	comma

Fig. 6.2 | Operator precedence.

6.3 Defining Arrays

- When defining arrays, specify
 - Name
 - Type of array
 - Number of elements
 arrayType arrayName[numberOfElements];
 - Examples:

```
int c[ 10 ];
float myArray[ 3284 ];
```

- Defining multiple arrays of same type
 - Format similar to regular variables
 - Example:

```
int b[ 100 ], x[ 27 ];
```



6.4 Array Examples

Initializers

int
$$n[5] = \{1, 2, 3, 4, 5\};$$

- If not enough initializers, rightmost elements become 0
 int n[5] = { 0 }
 - All elements 0
- If too many initializers, a syntax error occurs
- C arrays have no bounds checking
- If size omitted, initializers determine it

int
$$n[] = \{ 1, 2, 3, 4, 5 \};$$

- 5 initializers, therefore 5 element array



```
* 13
 /* Fig. 6.3: fig06_03.c
      initializing an array */
                                                                                       Outline
  #include <stdio.h>
  /* function main begins program execution */
  int main( void )
                                                                                       fig06_03.c
  {
7
      int n[ 10 ]; /* n is an array of 10 integers */
8
                                                                                       (1 \text{ of } 2)
      int i; /* counter */
10
     /* initialize elements of array n to 0 */
11
                                                                   for loop initializes each array
      for (i = 0; i < 10; i++) {
12
         n[ i ] = 0; /* set element at location i to 0 */
13
                                                                      element separately
      } /* end for */
14
15
16
      printf( "%s%13s\n", "Element", "Value" );
17
      /* output contents of array n in tabular format */
18
      for (i = 0; i < 10; i++) \{ \leftarrow
                                                                   for loop outputs all array elements
19
         printf( "%7d%13d\n", i, n[ i ] );
20
      } /* end for */
21
22
      return 0; /* indicates successful termination */
23
24
25 } /* end main */
```



*

fig06_03.c

 $(2 ext{ of } 2)$

```
fig06_04.c
(1 \text{ of } 2)
```

initializer list initializes all array elements simultaneously

```
int i; /* counter */
10
11
      printf( "%s%13s\n", "Element", "Value" );
12
13
      /* output contents of array in tabular format */
14
      for (i = 0; i < 10; i++) {
15
         printf( "%7d%13d\n", i, n[ i ] );
16
      } /* end for */
17
18
      return 0; /* indicates successful termination */
19
20
21 } /* end main */
```

Initializing an array with an initializer list */

/* use initializer list to initialize array n */

int $n[10] = \{32, 27, 64, 18, 95, 14, 90, 70, 60, 37\};$

/* function main begins program execution */

/* Fig. 6.4: fig06_04.c

#include <stdio.h>

int main(void)

{ 7

8

Element	Value	\circ
0	32	<u>U</u>
1	27	
2	64	
3	18	
4	95	fi
5	14	
6	90	(2
7	70	(2
8	60	
9	37	

<u>Outline</u>

fig06_04.c

(2 of 2)

Forgetting to initialize the elements of an array whose elements should be initialized.

Providing more initializers in an array initializer list than there are elements in the array is a syntax error.

```
* 19
  /* Fig. 6.5: fig06_05.c
      Initialize the elements of array s to the even integers from 2 to 20 */
                                                                                       Outline
  #include <stdio.h>
                                                     #define directive tells compiler to replace all
  #define SIZE 10 /* maximum size of array */ ←
                                                        instances of the word SIZE with 10
  /* function main begins program execution */
                                                                                      fig06_05.c
7 int main( void )
8
  {
                                                                                      (1 \text{ of } 2)
      /* symbolic constant SIZE can be used to specify array size */
      int s[ SIZE ]; /* array s has SIZE elements */ ←
                                                                 SIZE is replaced with 10 by the
10
      int j; /* counter */
11
                                                                    compiler, so array s has 10 elements
12
      for (j = 0; j < SIZE; j++) { /* set the values */}
13
         s[j] = 2 + 2 * j; \leftarrow
                                                                 for loop initializes each array
14
      } /* end for */
15
                                                                    element separately
16
      printf( "%s%13s\n", "Element", "Value" );
17
18
      /* output contents of array s in tabular format */
19
      for (j = 0; j < SIZE; j++) {
20
         printf( "%7d%13d\n", j, s[ j ] );
21
      } /* end for */
22
23
      return 0: /* indicates successful termination */
24
25
26 } /* end main */
```

Element	Value	
0	2	
1	4	
2	6	
3	8	
4	10	
5	12	
6	14	
7	16	
8	18	
9	20	

<u>Outline</u>



fig06_05.c

(2 of 2)

Ending a #define or #include preprocessor directive with a semicolon. Remember that preprocessor directives are not C statements.

Assigning a value to a symbolic constant in an executable statement is a syntax error. A symbolic constant is not a variable. No space is reserved for it by the compiler as with variables that hold values at execution time.

Software Engineering Observation 6.1

Defining the size of each array as a symbolic constant makes programs more scalable.

Good Programming Practice 6.1

Use only uppercase letters for symbolic constant names. This makes these constants stand out in a program and reminds you that symbolic constants are not variables.

Good Programming Practice 6.2

In multiword symbolic constant names, use underscores to separate the words for readability.

```
* 26
 /* Fig. 6.6: fig06_06.c
     Compute the sum of the elements of the array */
                                                                                   Outline
  #include <stdio.h>
  #define SIZE 12
  /* function main begins program execution */
                                                                                  fig06_06.c
7 int main( void )
  {
8
     /* use initializer list to initialize array */
     int a[SIZE] = \{1, 3, 5, 4, 7, 2, 99, 16, 45, 67, 89, 45\};
10
     int i: /* counter */
11
                                                                    initializer list initializes all array
     int total = 0; /* sum of array */
12
13
                                                                      elements simultaneously
     /* sum contents of array a */
14
     for (i = 0; i < SIZE; i++) {
15
                                                     for loop adds each element of the
        16
     } /* end for */
                                                        array to variable total
17
18
     printf( "Total of array element values is %d\n", total );
19
20
     return 0; /* indicates successful termination */
21
22
23 } /* end main */
```

Total of array element values is 383





fig06_07.c

(2 of 2)

29	<pre>printf("%s%17s\n", "</pre>	Rating", "Frequency");			
30					
31	<pre>/* output the frequencies in a tabular format */</pre>				
32	<pre>for (rating = 1; rating < FREQUENCY_SIZE; rating++) {</pre>				
33	<pre>printf("%6d%17d\n", rating, frequency[rating]);</pre>				
34	} /* end for */				
35					
36	<pre>return 0; /* indicate</pre>	s successful termination */			
37					
38 } /	38 } /* end main */				
_					
Ratin	ng Frequency				
	1 2				
	2 2				
	3 2				
	4 2				
	5 5				
	6 11				

28

8 9

10

/* display results */

5

1 3

Good Programming Practice 6.3

Strive for program clarity. Sometimes it may be worthwhile to trade off the most efficient use of memory or processor time in favor of writing clearer programs.

Performance Tip 6.1

Sometimes performance considerations far outweigh clarity considerations.

Referring to an element outside the array bounds.

Error-Prevention Tip 6.1

When looping through an array, the array subscript should never go below 0 and should always be less than the total number of elements in the array (size -1). Make sure the loop-terminating condition prevents accessing elements outside this range.

Error-Prevention Tip 6.2

Programs should validate the correctness of all input values to prevent erroneous information from affecting a program's calculations.

```
Outline
```

```
fig06_08.c
```

(1 of 2)

```
6 /* function main begins program execution */
7 int main( void )
8 {
     /* use initializer list to initialize array n */
9
     int n[ SIZE ] = { 19, 3, 15, 7, 11, 9, 13, 5, 17, 1 };
10
11
     int i; /* outer for counter for array elements */
     int j; /* inner for counter counts *s in each histogram bar */
12
13
     printf( "%s%13s%17s\n", "Element", "Value", "Histogram" );
14
15
16
     /* for each element of array n, output a bar of the histogram */
     for (i = 0; i < SIZE; i++) {
17
        18
19
        for (j = 1; j \le n[i]; j++) { /* print one bar */}
20
21
           printf( "%c", '*' );
          } /* end inner for */
22
23
        printf( "\n" ); /* end a histogram bar */
24
     } /* end outer for */
25
26
```

return 0; /* indicates successful termination */

1 /* Fig. 6.8: fig06_08.c

3 #include <stdio.h> #define SIZE 10

27 28

29 } /* end main */

Histogram printing program */

nested for loop prints n[i] asterisks on the ith line





Element	Value	Histogram
0	19	*********
1	3	***
2	15	*******
3	7	*****
4	11	*****
5	9	*****
6	13	******
7	5	****
8	17	*******
9	1	*

<u>Outline</u>



fig06_08.c

(2 of 2)

```
/* Fig. 6.9: fig06_09.c
      Roll a six-sided die 6000 times */
  #include <stdio.h>
 #include <stdlib.h>
  #include <time.h>
  #define SIZE 7
  /* function main begins program execution */
9 int main( void )
10 {
11
     int face; /* random die value 1 - 6 */
      int roll; /* roll counter 1-6000 */
12
      int frequency[ SIZE ] = { 0 }; /* clear counts */
13
14
     srand( time( NULL ) ); /* seed random-number generator */
15
16
```

++frequency[face]; /* replaces 26-line switch of Fig. 5.8 */

/* roll die 6000 times */

} /* end for */

face = 1 + rand() % 6;

for (roll = 1; roll <= 6000; roll++) {

17

18

19

20

21

<u>Outline</u>

```
fig06_09.c
```

(1 of 2)

for loop uses one array to track number of times each number is rolled instead of using 6 variables and a switch statement



fig06_09.c

(2 of 2)

	printf("%s%1/s\n", "Face", "Frequency");
	<pre>/* output frequency elements 1-6 in tabular format *, for (face = 1; face < SIZE; face++) {</pre>
	<pre>printf("%4d%17d\n", face, frequency[face]); } /* end for */</pre>
	<pre>return 0; /* indicates successful termination */</pre>
}	/* end main */

Face	Frequency
1	1029
2	951
3	987
4	1033
5	1010
6	990

6.4 Array Examples

- Character arrays
 - String "first" is really a static array of characters
 - - Null character '\0' terminates strings

 - Can access individual characters string1[3] is character 's'
 - Array name is address of array, so & not needed for scanf scanf("%s", string2);
 - Reads characters until whitespace encountered
 - Be careful not to write past end of array, as it is possible to do so

Common Programming Error 6.7

Not providing scanf with a character array large enough to store a string typed at the keyboard can result in destruction of data in a program and other runtime errors. This can also make a system susceptible to worm and virus attacks.

```
Treating character arrays as strings */
                                                                                       Outline
  #include <stdio.h>
  /* function main begins program execution */
  int main( void )
                                                                                      fig06_10.c
  {
7
      char string1[ 20 ]; /* reserves 20 characters */
8
                                                                                      (1 \text{ of } 2)
      char string2[] = "string literal"; /* reserves 15 characters */
      int i; /* counter */
10
                                                          string2 array is defined with one
11
                                                            element for each character, so 15
      /* read string from user into array string1 */
12
                                                            elements including null character /0
      printf("Enter a string: ");
13
      scanf( "%s", string1 ); /* input ended by whitespace character */
14
15
16
      /* output strings */
      printf( "string1 is: %s\nstring2 is: %s\n"
17
18
              "string1 with spaces between characters is:\n",
              string1, string2 );
19
20
      /* output characters until null character is reached */
21
      for ( i = 0; string1[ i ] != '\0'; i++ ) {←
22
                                                             for loop prints characters of string1
         printf( "%c ", string1[ i ] );
23
                                                               array with spaces in between
      } /* end for */
24
25
      printf( "\n" );
26
27
      return 0; /* indicates successful termination */
28
29
30 } /* end main */
```

/* Fig. 6.10: fig06_10.c

```
Enter a string: Hello there
```

string1 is: Hello

string2 is: string literal

string1 with spaces between characters is:

H e 1 1 o

<u>Outline</u>

fig06_10.c

(2 of 2)

Performance Tip 6.2

In functions that contain automatic arrays where the function is in and out of scope frequently, make the array Static so it is not created each time the function is called.

```
1 /* Fig. 6.11: fig06_11.c
      Static arrays are initialized to zero */
  #include <stdio.h>
5 void staticArrayInit( void ); /* function prototype */
6 void automaticArrayInit( void ); /* function prototype */
7
8 /* function main begins program execution */
9 int main( void )
10 {
11
      printf( "First call to each function:\n" );
      staticArrayInit();
12
      automaticArrayInit();
13
14
      printf( "\n\nSecond call to each function:\n" );
15
16
      staticArrayInit();
      automaticArrayInit();
17
18
      return 0; /* indicates successful termination */
19
20
```

21 } /* end main */

22

<u>Outline</u>

fig06_11.c

(1 of 4)



```
23 /* function to demonstrate a static local array */
24 void staticArrayInit( void )
25 {
      /* initializes elements to 0 first time function is called */
26
      static int array1[ 3 ]; ←
27
                                        static array is created only once, when
      int i; /* counter */
28
                                          staticArrayInit is first called
29
      printf( "\nValues on entering staticArrayInit:\n" );
30
31
     /* output contents of array1 */
32
      for (i = 0; i \le 2; i++) {
33
         printf( "array1[ %d ] = %d ", i, array1[ i ] );
34
      } /* end for */
35
36
      printf( "\nValues on exiting staticArrayInit:\n" );
37
38
     /* modify and output contents of array1 */
39
      for (i = 0; i \le 2; i++) {
40
         printf( "array1[ %d ] = %d ", i, array1[ i ] += 5 );
41
      } /* end for */
42
43
```

44 } /* end function staticArrayInit */

<u>Outline</u>

fig06_11.c

(2 of 4)



```
45
46 /* function to demonstrate an automatic local array */
47 void automaticArrayInit( void )
48 {
      /* initializes elements each time function is called */
49
      int array2[\frac{3}{3}] = {\frac{1}{2}, \frac{3}{3}}; \leftarrow
50
                                            automatic array is recreated every time
      int i; /* counter */
51
                                               automaticArrayInit is called
52
      printf( "\n\nValues on entering automaticArrayInit:\n" );
53
54
      /* output contents of array2 */
55
      for (i = 0; i \le 2; i++) {
56
         printf("array2[ %d ] = %d ", i, array2[ i ] );
57
      } /* end for */
58
59
      printf( "\nValues on exiting automaticArrayInit:\n" );
60
61
      /* modify and output contents of array2 */
62
      for (i = 0; i \le 2; i++) {
63
         printf( "array2[ %d ] = %d ", i, array2[ i ] += 5 );
64
      } /* end for */
65
66
67 } /* end function automaticArrayInit */
```

<u>Outline</u>

fig06_11.c
(3 of 4)



```
First call to each function:
Values on entering staticArrayInit:
array1[0] = 0  array1[1] = 0  array1[2] = 0
Values on exiting staticArrayInit:
array1[0] = 5  array1[1] = 5  array1[2] = 5
Values on entering automaticArrayInit:
array2[0] = 1 array2[1] = 2 array2[2] = 3
Values on exiting automaticArrayInit:
array2[0] = 6 array2[1] = 7 array2[2] = 8
Second call to each function:
Values on entering staticArrayInit:
array1[0] = 5  array1[1] = 5  array1[2] = 5
Values on exiting staticArrayInit:
array1[0] = 10 array1[1] = 10 array1[2] = 10
Values on entering automaticArrayInit:
array2[0] = 1 array2[1] = 2 array2[2] = 3
```

Values on exiting automaticArrayInit:

array2[0] = 6 array2[1] = 7 array2[2] = 8

Outline

fig06_11.c

(4 of 4)

Common Programming Error 6.8

Assuming that elements of a local Static array are initialized to zero every time the function in which the array is defined is called.

6.5 Passing Arrays to Functions

Passing arrays

 To pass an array argument to a function, specify the name of the array without any brackets

```
int myArray[24];
myFunction(myArray, 24);
```

- Array size usually passed to function
- Arrays passed call-by-reference
- Name of array is address of first element
- Function knows where the array is stored
 - Modifies original memory locations

Passing array elements

- Passed by call-by-value
- Pass subscripted name (i.e., myArray[3]) to function



6.5 Passing Arrays to Functions

Function prototype

```
void modifyArray( int b[], int arraySize );
```

- Parameter names optional in prototype
 - int b[] could be written int []
 - int arraySize could be simply int

Performance Tip 6.3

Passing arrays by reference makes sense for performance reasons. If arrays were passed by value, a copy of each element would be passed. For large, frequently passed arrays, this would be time consuming and would consume considerable storage for the copies of the arrays.

```
1 /* Fig. 6.12: fig06_12.c
      The name of an array is the same as &array[ 0 ] */
  #include <stdio.h>
5 /* function main begins program execution */
6 int main( void )
  {
7
      char array[ 5 ]; /* define an array of size 5 */
8
      printf( " array = \%p \setminus n\&array[0] = \%p \setminus n \&array = \%p \setminus n",
10
11
         array, &array[ 0 ], &array );
12
      return 0; /* indicates successful termination */
13
14
15 } /* end main */
     array = 0012FF78
&array[0] = 0012FF78
```

&array = 0012FF78

<u>Outline</u>

fig06_12.c



Software Engineering Observation 6.2

It is possible to pass an array by value (by using a simple trick we explain in Chapter 10).

```
Passing arrays and individual array elements to functions */
                                                                                      Outline
  #include <stdio.h>
  #define SIZE 5
  /* function prototypes */
                                                                                     fig06_13.c
                                                      Function prototype indicates
7 void modifyArray( int b[], int size ); ←
                                                         function will take an array
  void modifyElement( int e );
                                                                                     (1 \text{ of } 3)
10 /* function main begins program execution */
11 int main( void )
12 {
      int a[ SIZE ] = { 0, 1, 2, 3, 4 }; /* initialize a */
13
     int i; /* counter */
14
      printf( "Effects of passing entire array by reference:\n\nThe "
16
             "values of the original array are:\n" );
17
     /* output original array */
      for (i = 0; i < SIZE; i++) {
        printf( "%3d", a[ i ] );
      } /* end for */
22
      printf( "\n" );
     /* pass array a to modifyArray by reference */
                                                              Array a is passed to modifyArray
     modifyArray( a, SIZE ); ←
                                                                 by passing only its name
      printf( "The values of the modified array are:\n" );
30
```

/* Fig. 6.13: fig06_13.c

15

18

19

20

21

23

24 25

26

27

28

29

```
/* output modified array */
31
      for (i = 0; i < SIZE; i++) {
32
                                                                                      Outline
         printf( "%3d", a[ i ] );
33
      } /* end for */
34
35
      /* output value of a[3] */
36
                                                                                      fig06_13.c
      printf( "\n\nEffects of passing array element "
37
              "by value:\n\nThe value of a[3] is %d\n", a[ 3 ] );
38
                                                                                      (2 \text{ of } 3)
39
      modifyElement( a[ 3 ] ); /* pass array element a[ 3 ] by value */
40
41
                                                            Array element is passed to modifyElement
      /* output value of a[ 3 ] */
42
      printf( "The value of a[ 3 ] is %d\n", a[ 3 ] );
                                                               by passing a [ 3 ]
43
44
      return 0; /* indicates successful termination */
45
46
47 } /* end main */
48
49 /* in function modifyArray, "b" points to the original array "a"
      in memory */
50
51 void modifyArray( int b[], int size )
52 {
53
      int j; /* counter */
54
     /* multiply each array element by 2 */
55
      for (j = 0; j < size; j++) {
56
         b[ i ] *= 2:
57
      } /* end for */
58
59
60 } /* end function modifyArray */
```

```
61
62 /* in function modifyElement, "e" is a local copy of array element
      a[ 3 ] passed from main */
64 void modifyElement( int e )
65 <del>{</del>
66
     /* multiply parameter by 2 */
     printf( "Value in modifyElement is %d\n", e *= 2 );
67
68 } /* end function modifyElement */
Effects of passing entire array by reference:
The values of the original array are:
  0 1 2 3 4
The values of the modified array are:
  0 2 4 6 8
Effects of passing array element by value:
The value of a[3] is 6
Value in modifyElement is 12
The value of a[ 3 ] is 6
```

<u>Outline</u>

fig06_13.c

(3 of 3)

```
Demonstrating the const type qualifier with arrays */
                                                                                     Outline
  #include <stdio.h>
  void tryToModifyArray( const int b[] ); /* function prototype */
6
                                                                                     fig06_14.c
  /* function main begins program execution */
  int main( void )
                                                                                     (1 \text{ of } 2)
9
      int a[] = { 10, 20, 30 }; /* initialize a */
                                                              const qualifier tells compiler that
10
11
                                                                array cannot be changed
      tryToModifyArray( a );
12
13
      printf("%d %d %d\n", a[ 0 ], a[ 1 ], a[ 2 ] );
14
15
16
      return 0; /* indicates successful termination */
17
18 } /* end main */
19
20 /* in function tryToModifyArray, array b is const, so it cannot be
      used to modify the original array a in main. */
22 void tryToModifyArray( const int b[] )
23 {
     b[0] /= 2; /* error */
24
                                                           Any attempts to modify the array will
     b[ 1 ] /= 2; /* error */ ←
25
                                                             result in errors
     b[ 2 ] /= 2; /* error */ ←
26
27 } /* end function tryToModifyArray */
```

/* Fig. 6.14: fig06_14.c



```
Compiling...
FIG06_14.C
fig06_14.c(24) : error C2166: l-value specifies const object
fig06_14.c(25) : error C2166: l-value specifies const object
fig06_14.c(26) : error C2166: l-value specifies const object
```

<u>Outline</u>

fig06_14.c

(2 of 2)

Software Engineering Observation 6.3

The const type qualifier can be applied to an array parameter in a function definition to prevent the original array from being modified in the function body. This is another example of the principle of least privilege. Functions should not be given the capability to modify an array unless it is absolutely necessary.

6.6 Sorting Arrays

- Sorting data
 - Important computing application
 - Virtually every organization must sort some data
- Bubble sort (sinking sort)
 - Several passes through the array
 - Successive pairs of elements are compared
 - If increasing order (or identical), no change
 - If decreasing order, elements exchanged
 - Repeat

Example:

- original: 3 4 2 6 7
- pass 1: 3 2 4 6 7
- pass 2: 2 3 4 6 7
- Small elements "bubble" to the top



Performance Tip 6.4

Often, the simplest algorithms perform poorly. Their virtue is that they are easy to write, test and debug. However, more complex algorithms are often needed to realize maximum performance.

```
This program sorts an array's values into ascending order */
3 #include <stdio.h>
  #define SIZE 10
6 /* function main begins program execution */
7 int main( void )
8 {
     /* initialize a */
9
      int a[SIZE] = { 2, 6, 4, 8, 10, 12, 89, 68, 45, 37 };
10
      int pass; /* passes counter */
11
      int i; /* comparisons counter */
12
      int hold; /* temporary location used to swap array elements */
13
14
      printf( "Data items in original order\n" );
15
16
     /* output original array */
17
      for (i = 0; i < SIZE; i++) {
18
        printf( "%4d", a[ i ] );
19
      } /* end for */
20
21
     /* bubble sort */
22
     /* loop to control number of passes */
23
      for ( pass = 1; pass < SIZE; pass++ ) {
24
25
        /* loop to control number of comparisons per pass */
26
        for (i = 0; i < SIZE - 1; i++) {
27
28
```

1 /* Fig. 6.15: fig06_15.c

<u>Outline</u>

fig06_15.c

(1 of 2)



```
29
           /* compare adjacent elements and swap them if first
           element is greater than second element */
30
           if ( a[ i ] > a[ i + 1 ] ) {
31
              hold = a[i];
32
                                          If any two array elements are out of
              a[i] = a[i + 1];
33
                                             order, the function swaps them
              a[i+1] = hold;
34
           } /* end if */
35
36
        } /* end inner for */
37
38
     } /* end outer for */
39
40
      printf( "\nData items in ascending order\n" );
41
42
     /* output sorted array */
43
      for (i = 0; i < SIZE; i++) {
44
        printf( "%4d", a[ i ] );
45
      } /* end for */
46
47
     printf( "\n" );
48
49
      return 0; /* indicates successful termination */
50
51 }
Data items in original order
               8 10 12 89 68 45 37
Data items in ascending order
       4
           6
               8 10 12 37 45 68 89
```

<u>Outline</u>

fig06_15.c

(2 of 2)



6.7 Case Study: Computing Mean, Median and Mode Using Arrays

- Mean average
- Median number in middle of sorted list
 - -1, 2, 3, 4, 5
 - 3 is the median
- Mode number that occurs most often
 - **-** 1, 1, 1, 2, 3, 3, 4, 5
 - 1 is the mode

```
This program introduces the topic of survey data analysis.
      It computes the mean, median and mode of the data */
  #include <stdio.h>
  #define SIZE 99
7 /* function prototypes */
8 void mean( const int answer[] );
9 void median( int answer[] );
10 void mode( int freq[], const int answer[] );
11 void bubbleSort( int a[] );
12 void printArray( const int a[] );
14 /* function main begins program execution */
15 int main( void )
      int frequency[ 10 ] = { 0 }; /* initialize array frequency */
     /* initialize array response */
      int response[ SIZE ] =
         { 6, 7, 8, 9, 8, 7, 8, 9, 8, 9,
           7, 8, 9, 5, 9, 8, 7, 8, 7, 8,
           6, 7, 8, 9, 3, 9, 8, 7, 8, 7,
           7, 8, 9, 8, 9, 8, 9, 7, 8, 9,
           6, 7, 8, 7, 8, 7, 9, 8, 9, 2,
           7, 8, 9, 8, 9, 8, 9, 7, 5, 3,
           5, 6, 7, 2, 5, 3, 9, 4, 6, 4,
           7, 8, 9, 6, 8, 7, 8, 9, 7, 8,
           7, 4, 4, 2, 5, 3, 8, 7, 5, 6,
           4, 5, 6, 1, 6, 5, 7, 8, 7 };
```

1 /* Fig. 6.16: fig06_16.c

13

16 {

17 18

19

20 21

22 23

24

25

26

27

28

29

30

Outline

fig06_16.c

(1 of 6)





```
31
     /* process responses */
32
     mean( response );
33
     median( response );
34
     mode( frequency, response );
35
36
     return 0; /* indicates successful termination */
37
38
39 } /* end main */
41 /* calculate average of all response values */
42 void mean( const int answer[] )
43 {
     int j; /* counter for totaling array elements */
44
     int total = 0; /* variable to hold sum of array elements */
45
46
     47
48
     /* total response values */
49
     for (j = 0; j < SIZE; j++) {
50
        total += answer[ j ];
51
     } /* end for */
52
53
     printf( "The mean is the average value of the data\n"
54
             "items. The mean is equal to the total of\n"
55
             "all the data items divided by the number\n"
56
             "of data items (%d). The mean value for\n"
57
             "this run is: %d / %d = %.4f\n\n",
58
             SIZE, total, SIZE, ( double ) total / SIZE );
59
60 } /* end function mean */
```

<u>Outline</u>

fig06_16.c

(2 of 6)





```
Outline
63 void median( int answer[] )
64 {
65
      printf( "\n%s\n%s\n%s\n%s",
              "******" " Median" "******"
66
                                                                                      fig06_16.c
              "The unsorted array of responses is" );
67
68
                                                                                      (3 \text{ of } 6)
      printArray( answer ); /* output unsorted array */
69
70
      bubbleSort( answer ); /* sort array */ ←
71
                                                         Once the array is sorted, the median will be
72
                                                            the value of the middle element
      printf( "\n\nThe sorted array is" );
73
      printArray( answer ); /* output sorted array */
74
75
      /* display median element */
76
      printf( "\n\nThe median is element %d of\n"
77
              "the sorted %d element array.\n"
78
              "For this run the median is %d\n\n".
79
              SIZE / 2, SIZE, answer[SIZE / 2]);←
80
81 } /* end function median */
82
83 /* determine most frequent response */
84 void mode( int freq[], const int answer[] )
85 {
      int rating; /* counter for accessing elements 1-9 of array freq */
86
      int j; /* counter for summarizing elements 0-98 of array answer */
87
      int h; /* counter for diplaying histograms of elements in array freq */
88
      int largest = 0; /* represents largest frequency */
89
      int modeValue = 0; /* represents most frequent response */
90
```

61

62 /* sort array and determine median element's value */

```
92
      printf( "\n%s\n%s\n%s\n",
              "******" " Mode" "******");
93
94
     /* initialize frequencies to 0 */
95
     for ( rating = 1; rating <= 9; rating++ ) {</pre>
96
        freq[ rating ] = 0;
97
     } /* end for */
98
99
     /* summarize frequencies */
100
101
     for (j = 0; j < SIZE; j++) {
        ++freq[answer[j]];
102
      } /* end for */
103
104
105
     /* output headers for result columns */
106
      printf( "%s%11s%19s\n\n%54s\n%54s\n\n",
              "Response" "Frequency" "Histogram"
107
                 1 2 2", "5 0 5 0
108
                                                      5");
109
     /* output results */
110
111
      for ( rating = 1; rating <= 9; rating++ ) {</pre>
                                  ", rating, freq[ rating ] );
        printf( "%8d%11d
112
113
114
        /* keep track of mode value and largest frequency value */
        if ( freq[ rating ] > largest ) {
115
           largest = freq[ rating ];
116
           modeValue = rating;
117
118
        } /* end if */
```

91

<u>Outline</u>

fig06_16.c

(4 of 6)



```
119
120
         /* output histogram bar representing frequency value */
         for ( h = 1; h <= freq[ rating ]; h++ ) {
121
122
            printf( "*" );
         } /* end inner for */
123
124
         printf( "\n" ); /* being new line of output */
125
      } /* end outer for */
126
127
      /* display the mode value */
128
129
      printf( "The mode is the most frequent value.\n"
              "For this run the mode is %d which occurred"
130
              " %d times.\n", modeValue, largest );
131
    } /* end function mode */
132
133
134 /* function that sorts an array with bubble sort algorithm */
135 void bubbleSort( int a[] )
136
137
      int pass; /* pass counter */
      int j; /* comparison counter */
138
139
      int hold; /* temporary location used to swap elements */
140
141
      /* loop to control number of passes */
      for ( pass = 1; pass < SIZE; pass++ ) {</pre>
142
143
         /* loop to control number of comparisons per pass */
144
         for (j = 0; j < SIZE - 1; j++) {
145
146
```

<u>Outline</u>

fig06_16.c

(5 of 6)



147 /* swap elements if out of order */ if (a[j] > a[j+1]) { 148 hold = a[j]; 149 150 a[j] = a[j + 1];151 a[j+1] = hold;} /* end if */ 152 153 154 } /* end inner for */ 155 } /* end outer for */ 156 157 158 } /* end function bubbleSort */ 159 160 /* output array contents (20 values per row) */ 161 void printArray(const int a[]) 162 int j; /* counter */ 163 164 /* output array contents */ 165 for $(j = 0; j < SIZE; j++) {$ 166 167 if (i% 20 == 0) { /* begin new line every 20 values */ 168 printf("\n"); 169 } /* end if */ 170 171 172 printf("%2d", a[j]); } /* end for */ 173 174 175 } /* end function printArray */

<u>Outline</u>

fig06_16.c

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Mean

The mean is the average value of the data items. The mean is equal to the total of all the data items divided by the number of data items (99). The mean value for this run is: 681 / 99 = 6.8788

Median *****

The unsorted array of responses is 6 7 8 9 8 7 8 9 8 9 7 8 9 5 9 8 7 8 7 8 6 7 8 9 3 9 8 7 8 7 8 9 8 9 8 9 8 9 7 8 9 6 7 8 7 8 7 9 8 9 2 7 8 9 8 9 8 9 8 9 7 5 3 5 6 7 2 5 3 9 4 6 4 7 8 9 6 8 7 8 9 7 8 7 4 4 2 5 3 8 7 5 6 4 5 6 1 6 5 7 8 7

(continued on next slide...)

<u>Outline</u>

(1 of 2)



Outline

***** Mode *****

Histogram Response Frequency

*** ****

**** ****

9 ***** 23 8 27 ********

19 ******

The mode is the most frequent value. For this run the mode is 8 which occurred 27 times.

(2 of 2)

6.8 Searching Arrays

- Search an array for a key value
- Linear search
 - Simple
 - Compare each element of array with key value
 - Useful for small and unsorted arrays

```
1 /* Fig. 6.18: fig06_18.c
      Linear search of an array */
 #include <stdio.h>
  #define SIZE 100
6 /* function prototype */
7 int linearSearch( const int array[], int key, int size );
8
9 /* function main begins program execution */
10 int main( void )
11 {
      int a[ SIZE ]; /* create array a */
12
      int x; /* counter for initializing elements 0-99 of array a */
13
      int searchKey; /* value to locate in array a */
14
      int element; /* variable to hold location of searchKey or -1 */
15
16
     /* create data */
17
      for (x = 0; x < SIZE; x++) {
18
        a[x] = 2 * x;
19
```

} /* end for */

2021

<u>Outline</u>

fig06_18.c

(1 of 3)



```
22
      printf( "Enter integer search key:\n" );
      scanf( "%d", &searchKey );
23
24
      /* attempt to locate searchKey in array a */
25
      element = linearSearch( a, searchKey, SIZE );
26
27
     /* display results */
28
      if ( element !=-1 ) {
29
         printf( "Found value in element %d\n", element );
30
      } /* end if */
31
32
      else {
         printf( "Value not found\n" );
33
      } /* end else */
34
35
      return 0; /* indicates successful termination */
36
37
38 } /* end main */
39
40 /* compare key to every element of array until the location is found
      or until the end of array is reached; return subscript of element
41
      if key or -1 if key is not found */
42
43 int linearSearch( const int array[], int key, int size )
44 {
      int n; /* counter */
45
46
```

fig06_18.c

(2 of 3)



```
/* loop through array */
47
      for ( n = 0; n < size; ++n ) { ←
48
49
         if ( array[ n ] == key ) {
50
            return n; /* return location of key */
51
         } /* end if */
52
                                              Linear search algorithm searches
53
                                                 through every element in the
     } /* end for */
54
                                                 array until a match is found
55
      return -1; /* key not found */
56
57
58 } /* end function linearSearch */
Enter integer search key:
36
Found value in element 18
Enter integer search key:
37
Value not found
```

fig06_18.c

(3 of 3)

6.8 Searching Arrays

Binary search

- For sorted arrays only
- Compares middle element with key
 - If equal, match found
 - If key < middle, looks in first half of array
 - If key > middle, looks in last half
 - Repeat
- Very fast; at most n steps, where $2^n >$ number of elements
 - 30 element array takes at most 5 steps
 - $2^5 > 30$ so at most 5 steps

(1 of 6)

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```
Binary search of an array */
3 #include <stdio.h>
  #define SIZE 15
6 /* function prototypes */
7 int binarySearch( const int b[], int searchKey, int low, int high );
8 void printHeader( void );
9 void printRow( const int b[], int low, int mid, int high );
10
11 /* function main begins program execution */
12 int main( void )
13 {
      int a[ SIZE ]; /* create array a */
14
      int i; /* counter for initializing elements 0-14 of array a */
15
      int key; /* value to locate in array a */
16
      int result; /* variable to hold location of key or -1 */
17
18
     /* create data */
19
      for (i = 0; i < SIZE; i++) {
20
         a[i] = 2 * i;
21
      } /* end for */
22
23
      printf( "Enter a number between 0 and 28: " );
24
      scanf( "%d", &key );
25
26
      printHeader();
27
28
      /* search for key in array a */
29
      result = binarySearch( a, key, 0, SIZE - 1);
30
```

1 /* Fig. 6.19: fig06_19.c

```
31
      /* display results */
32
      if ( result != -1 ) {
33
         printf( "\n%d found in array element %d\n", key, result );
34
      } /* end if */
35
      else {
36
         printf( "\n%d not found\n", key );
37
      } /* end else */
38
39
      return 0: /* indicates successful termination */
40
41
42 } /* end main */
43
44 /* function to perform binary search of an array */
45 int binarySearch( const int b[], int searchKey, int low, int high )
46 {
      int middle; /* variable to hold middle element of array */
47
48
      /* loop until low subscript is greater than high subscript */
49
      while ( low <= high ) {</pre>
50
51
         /* determine middle element of subarray being searched */
52
         middle = (low + high) / 2;
53
54
         /* display subarray used in this loop iteration */
55
         printRow( b, low, middle, high );
56
57
```

fig06_19.c

(2 of 6)



```
58
         /* if searchKey matched middle element, return middle */
         if ( searchKey == b[ middle ] ) {
59
            return middle; ←
60
                                                If value is found, return its index
         } /* end if */
61
62
         /* if searchKey less than middle element, set new high */
63
         else if ( searchKey < b[ middle ] ) {</pre>
64
            high = middle - 1; /* search low end of array */
65
         } /* end else if */
66
                                     If value is too high, search the left half of array
         /* if searchKey greater than middle element, set new low */
68
         else {
69
            low = middle + 1; /* search high end of array */
70
         } /* end else */
71
                                    If value is too low, search the right half of array
72
      } /* end while */
73
74
75
      return -1; /* searchKey not found */
76
77 } /* end function binarySearch */
78
79 /* Print a header for the output */
80 void printHeader( void )
81 {
      int i; /* counter */
82
83
      printf( "\nSubscripts:\n" );
84
85
```



fig06_19.c

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```
/* output column head */
86
      for ( i = 0; i < SIZE; i++ ) {
87
         printf( "%3d ", i );
88
      } /* end for */
89
90
      printf( "\n" ); /* start new line of output */
91
92
      /* output line of - characters */
93
      for ( i = 1; i <= 4 * SIZE; i++ ) {
94
         printf( "-" );
95
      } /* end for */
96
97
      printf( "\n" ); /* start new line of output */
98
99 } /* end function printHeader */
100
101 /* Print one row of output showing the current
      part of the array being processed. */
102
103 void printRow( const int b[], int low, int mid, int high )
104 {
```

int i; /* counter for iterating through array b */

105106

<u>Outline</u>

fig06_19.c

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```
Outline
fig06_19.c
(5 of 6)
```

```
for ( i = 0; i < SIZE; i++ ) {
108
109
        /* display spaces if outside current subarray range */
110
111
        if ( i < low || i > high ) {
           printf( " ");
112
        } /* end if */
113
114
        else if ( i == mid ) { /* display middle element */
            printf( "%3d*", b[ i ] ); /* mark middle value */
115
        } /* end else if */
116
117
        else { /* display other elements in subarray */
            printf( "%3d ", b[ i ] );
118
        } /* end else */
119
120
121
      } /* end for */
122
      printf( "\n" ); /* start new line of output */
123
124} /* end function printRow */
Enter a number between 0 and 28: 25
Subscripts:
                              7 8 9 10 11 12 13 14
                      5
                          6
  0
      2
                  8 10 12 14* 16 18
                                        20 22 24 26 28
          4
                                    18 20 22* 24 26 28
                                 16
                                                 24 26* 28
                                                 24*
25 not found
                                                           (continued on next slide...)
```

107

/* loop through entire array */

Outline

fig06_19.c

(6 of 6)

```
Subscripts:

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14

------

0 2 4 6 8 10 12 14* 16 18 20 22 24 26 28

0 2 4 6* 8 10 12

8 10* 12
```

8 found in array element 4

Enter a number between 0 and 28: 6

Enter a number between 0 and 28: 8

Subscripts:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	
0	2	4	6	8	10	12	14*	16	18	20	22	24	26	28	
0	2	4	6*	8	10	12									

6 found in array element 3

6.9 Multiple-Subscripted Arrays

Multiple subscripted arrays

- Tables with rows and columns (m by n array)
- Like matrices: specify row, then column

Initialization

- int $b[2][2] = \{\{1,2\},\{3,4\}\};$
- Initializers grouped by row in braces
- If not enough, unspecified elements set to zero
 int b[2][2] = { { 1 }, { 3, 4 } };

Referencing elements

- Specify row, then column
printf("%d", b[0][1]);



Common Programming Error 6.9

Referencing a double-subscripted array element as a [x, y] instead of a [x] [y]. C interprets a [x, y] as a [y], and as such it does not cause a syntax error.

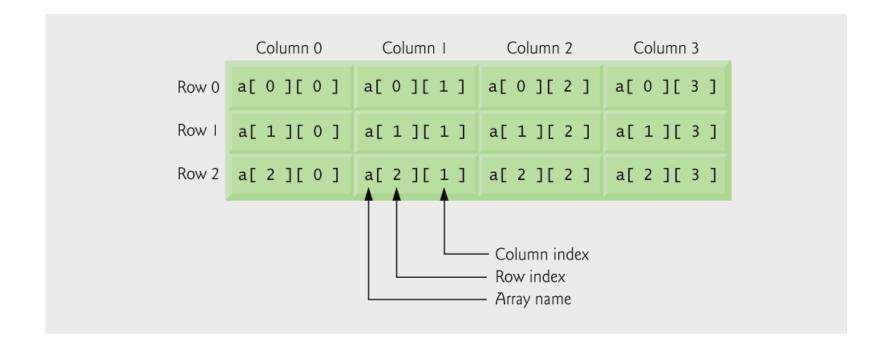


Fig. 6.20 | Double-subscripted array with three rows and four columns.

```
/* Fig. 6.21: fig06_21.c
                                                                                                          86
     Initializing multidimensional arrays */
                                                                                      Outline
  #include <stdio.h>
  void printArray( const int a[][ 3 ] ); /* function prototype */
                                                                                     fig06_21.c
  /* function main begins program execution */
  int main( void )
                                                                                     (1 \text{ of } 2)
9
     /* initialize array1, array2, array3 */
10
                                                               array1 is initialized with both rows full
      int array1[2][3] = { \{1, 2, 3\}, \{4, 5, 6\}\};
11
     int array2[ 2 ][ 3 ] = \{1, 2, 3, 4, 5\};
12
                                                       array2 and array3 are initialized only partially
     int array3[2][3] = {{1, 2}, {4}}; \leftarrow
13
14
      printf( "Values in array1 by row are:\n" );
15
     printArray( array1 );
16
17
      printf( "Values in array2 by row are:\n" );
18
      printArray( array2 );
19
20
      printf( "Values in array3 by row are:\n" );
21
      printArray( array3 );
22
23
      return 0; /* indicates successful termination */
24
25
26 } /* end main */
27
```



```
28 /* function to output array with two rows and three columns */
29 void printArray( const int a[][ 3 ])
30 {
      int i; /* row counter */
31
      int j; /* column counter */
32
33
     /* loop through rows */
34
35
      for ( i = 0; i <= 1; i++ ) {
36
         /* output column values */
37
38
         for (j = 0; j \le 2; j++) {
            printf( "%d ", a[ i ][ j ] );
39
         } /* end inner for */
40
41
42
         printf( "\n" ); /* start new line of output */
43
      } /* end outer for */
44
45 } /* end function printArray */
Values in array1 by row are:
1 2 3
4 5 6
Values in array2 by row are:
1 2 3
4 5 0
Values in array3 by row are:
1 2 0
4 0 0
```

fig06_21.c

(2 of 2)



```
/* Fig. 6.22: fig06_22.c
      Double-subscripted array example */
                                                                                       Outline
  #include <stdio.h>
  #define STUDENTS 3
  #define EXAMS 4
                                                                                       fig06_22.c
7 /* function prototypes */
8 int minimum( const int grades[][ EXAMS ], int pupils, int tests );
                                                                                       (1 \text{ of } 6)
9 int maximum( const int grades[][ EXAMS ], int pupils, int tests );
10 double average( const int setOfGrades[], int tests );
11 void printArray( const int grades[][ EXAMS ], int pupils, int tests );
12
13 /* function main begins program execution */
14 int main( void )
15 {
      int student; /* student counter */
16
17
      /* initialize student grades for three students (rows) */
18
      const int studentGrades[ STUDENTS ][ EXAMS ] =
19
         { { 77, 68, 86, 73 },
20
                                                      Each row in the array corresponds to a
           { 96, 87, 89, 78 }, ←
21
                                                         single student's set of grades
           { 70, 90, 86, 81 } };
22
23
      /* output array studentGrades */
24
      printf( "The array is:\n" );
25
      printArray( studentGrades, STUDENTS, EXAMS );
26
27
```



```
/* determine smallest and largest grade values */
28
      printf( "\n\nLowest grade: %d\nHighest grade: %d\n",
29
                                                                                      Outline
         minimum( studentGrades, STUDENTS, EXAMS ),
30
         maximum( studentGrades, STUDENTS, EXAMS ) );
31
32
      /* calculate average grade for each student */
33
                                                                                      fig06_22.c
34
      for ( student = 0; student < STUDENTS; student++ ) {</pre>
         printf( "The average grade for student %d is %.2f\n",
35
                                                                                      (2 of 6)
            student, average( studentGrades[ student ], EXAMS ) );
36
      } /* end for */
37
                                                  average function is passed a row of the array
38
      return 0; /* indicates successful termination */
39
40
41 } /* end main */
42
```

```
43 /* Find the minimum grade */
44 int minimum( const int grades[][ EXAMS ], int pupils, int tests )
45 {
46
      int i; /* student counter */
      int j; /* exam counter */
47
      int lowGrade = 100; /* initialize to highest possible grade */
48
49
      /* loop through rows of grades */
50
      for ( i = 0; i < pupils; i++ ) {</pre>
51
52
53
         /* loop through columns of grades */
         for (j = 0; j < tests; j++) {
54
55
            if ( grades[ i ][ j ] < lowGrade ) {</pre>
56
               lowGrade = grades[ i ][ j ];
57
58
            } /* end if */
59
         } /* end inner for */
60
61
      } /* end outer for */
62
63
      return lowGrade; /* return minimum grade */
64
65
66 } /* end function minimum */
```

67

<u>Outline</u>

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```
68 /* Find the maximum grade */
69 int maximum( const int grades[][ EXAMS ], int pupils, int tests )
70 {
71
      int i; /* student counter */
      int j; /* exam counter */
72
      int highGrade = 0; /* initialize to lowest possible grade */
73
74
      /* loop through rows of grades */
75
      for ( i = 0; i < pupils; i++ ) {</pre>
76
77
78
         /* loop through columns of grades */
         for (j = 0; j < tests; j++) {
79
80
            if ( grades[ i ][ j ] > highGrade ) {
81
               highGrade = grades[ i ][ j ];
82
83
            } /* end if */
84
         } /* end inner for */
85
86
      } /* end outer for */
87
88
89
      return highGrade; /* return maximum grade */
90
91 } /* end function maximum */
```

92

<u>Outline</u>

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```
93 /* Determine the average grade for a particular student */
94 double average( const int setOfGrades[], int tests )
95 {
      int i; /* exam counter */
96
      int total = 0: /* sum of test grades */
97
98
     /* total all grades for one student */
99
      for ( i = 0; i < tests; i++ ) {
100
         total += setOfGrades[ i ];
101
      } /* end for */
102
103
      return ( double ) total / tests; /* average */
104
105
106 } /* end function average */
107
108 /* Print the array */
109 void printArray( const int grades[][ EXAMS ], int pupils, int tests )
110
111
      int i; /* student counter */
      int j; /* exam counter */
112
113
114
      /* output column heads */
```

[1] [2] [3]");

[0]

printf("

115

116

<u>Outline</u>

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Outline

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```
117
      /* output grades in tabular format */
      for ( i = 0; i < pupils; i++ ) {</pre>
118
119
120
         /* output label for row */
         printf( "\nstudentGrades[%d] ", i );
121
122
123
         /* output grades for one student */
124
         for (j = 0; j < tests; j++) {
            printf( "%-5d", grades[ i ][ j ] );
125
         } /* end inner for */
126
127
      } /* end outer for */
128
129
130} /* end function printArray */
The array is:
                  [0]
                       [1]
                            [2]
                                 [3]
studentGrades[0] 77
                       68
                            86
                                 73
studentGrades[1] 96
                       87
                            89
                                 78
studentGrades[2] 70
                       90
                            86
                                 81
Lowest grade: 68
Highest grade: 96
The average grade for student 0 is 76.00
The average grade for student 1 is 87.50
The average grade for student 2 is 81.75
```

