2019 HMMT G1

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Let d be a real number such that every non-degenerate quadrilateral has at least two interior angles with measure less than d degrees. What is the minimum possible value for d?

I claim that $d=\boxed{120}$ is optimal. First, observe that for any angle measure $\theta<120^\circ$, a quadrilateral with angles $\theta,\theta,\theta,360^\circ-\theta$ exists so $d\geq 120$. Now if a non-degenerate quadrilateral had three interior angles with measure at least 120 degrees, then the measure of the fourth interior angle must be at most 0 degrees, contradiction. So $d\leq 120$ and thus d=120 as desired.

