

Q1(a).

Candidate key : { A, B, D }

{ A, B }  $\rightarrow$  { C }, ABD  $\rightarrow$  ABCD (Augmentation and reflexivity)

{ B, D }  $\rightarrow$  { E, F }, ABD  $\rightarrow$  ABDEF (Augmentation and reflexivity)

{ A, D }  $\rightarrow$  { G, H }, ABD  $\rightarrow$  ABDGH (Augmentation and reflexivity)

{ A }  $\rightarrow$  { I }, ABD  $\rightarrow$  ABDI (Augmentation and reflexivity)

{ H }  $\rightarrow$  { J }, because { A, D }  $\rightarrow$  { G, H } and { H }  $\rightarrow$  { J } hence ABD  $\rightarrow$  ABDJ (Transitivity)

Union all of them : ABD  $\rightarrow$  ABCDEFGHIJ

Thus, the key of R = { A, B, D }

Q1(b).

R1 = { A, B, C }

R2 = { B, D, E, F }

R3 = { A, D, G, H, J } ( merge { A, D }  $\rightarrow$  { G, H } and { H }  $\rightarrow$  { J } )

R4 = { A, I }

Q1(c).

R1 = { A, B, C }

R2 = { B, D, E, F }

R3-1 = { A, D, G, H }

R3-2 = { H, J }

R4 = { A, I }

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Q2(a).

There is no multi-value in R, it's in 1NF

Find key first:

Key = { Course\_no, Sec\_no, Semester, Year } and { Room\_no, Days\_hours, Semester, Year }

{ CN }  $\rightarrow$  { OD, CH, CL } happened partial dependency

So R is in 1NF.

Q2(b).

( All attribute in short term when calculate )

R = { CN, SN, OD, CH, CL, IS, S, Y, DH, RN, NS }

Candidate key : { CN, SN, S, Y } and { RN, DH, S, Y }

{ CN }  $\rightarrow$  { OD, CH, CL }

{ CN, SN, S, Y }  $\rightarrow$  { DH, RN, NS, IS }

{ RN, DH, S, Y }  $\rightarrow$  { IS, CN, SN }

(1) Check candidate key : { CN, SN, S, Y }

{ CN, SN, S, Y }  $\rightarrow$  { DH, RN, NS, IS } and { CN }  $\rightarrow$  { OD, CH, CL }

Hence { CN, SN, S, Y }  $\rightarrow$  { CN, SN, S, Y, DH, RN, NS, IS, OD, CH, CL } = R

So { CN, SN, S, Y } is key

(2) Check candidate key : { RN, DH, S, Y }

$\{ RN, DH, S, Y \} \rightarrow \{ IS, CN, SN \}$  and  $\{ CN \} \rightarrow \{ OD, CH, CL \}$

Hence  $\{ RN, DH, S, Y \} \rightarrow \{ RN, DH, S, Y, IS, CN, SN, OD, CH, CL \}$

By  $\{ CN, SN, S, Y \} \rightarrow \{ DH, RN, NS, IS \}$  found NS can depend on  $\{ CN, SN, S, Y \}$

which already in  $\{ RN, DH, S, Y \}^+$

Hence  $\{ RN, DH, S, Y \} \rightarrow \{ RN, DH, S, Y, IS, CN, SN, OD, CH, CL, NS \} = R$

So  $\{ RN, DH, S, Y \}$  is also a key

Ans:  $K_1 = \{ \text{Course\_no, Sec\_no, Semester, Year} \}$

$K_2 = \{ \text{Room\_no, Days\_hours, Semester, Year} \}$

**Q2(c).**

$R = \{ CN, SN, OD, CH, CL, IS, S, Y, DH, RN, NS \}$

$\{ CN \} \rightarrow \{ OD, CH, CL \}$

$\{ CN, SN, S, Y \} \rightarrow \{ DH, RN, NS, IS \}$

$\{ RN, DH, S, Y \} \rightarrow \{ IS, CN, SN \}$

Remove the transitive dependency. ( Separate R )

$\{ CN \} \rightarrow \{ OD, CH, CL \}$

Got  $R_1 = \{ CN, OD, CH, CL \}$  with Key =  $\{ CN \}$

$\{ RN, DH, S, Y \} \rightarrow \{ IS, CN, SN \}$ ,

$\{ RN, DH, S, Y \} \rightarrow \{ RN, DH, S, Y, IS, CN, SN \}$

Now  $\{ RN, DH, S, Y \}^+$  include  $\{ CN, SN, S, Y \}$ ,

$\{ RN, DH, S, Y \} \rightarrow \{ RN, DH, S, Y, IS, CN, SN, NS \}$  will keep the FD of  $\{ CN, SN, S, Y \}$

Hence  $\{ RN, DH, S, Y \} \rightarrow \{ RN, DH, S, Y, IS, CN, SN, NS \}$

Got  $R_2 = \{ RN, DH, S, Y, IS, CN, SN, NS \}$  with key =  $\{ CN, SN, S, Y \}$

Ans:

$R_1 = \{ \text{Course\_no, Offering\_dept, Credit\_hours, Course\_level} \}$

FD in  $R_1$

$\{ \text{Course\_no} \} \rightarrow \{ \text{Offering\_dept, Credit\_hours, Course\_level} \}$

$R_2 = \{ \text{Room\_no, Days\_hours, Semester, Year, Instructor\_ssn, Course\_no, Sec\_no, No\_of\_students} \}$

FD in  $R_2$

$\{ \text{Course\_no, Sec\_no, Semester, Year} \} \rightarrow \{ \text{Days\_hours, Room\_no, No\_of\_students, Instructor\_ssn} \}$

$\{ \text{Room\_no, Days\_hours, Semester, Year} \} \rightarrow \{ \text{Instructor\_ssn, Course\_no, Sec\_no} \}$

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**Q3(a).**

$( 30 + 9 + 9 + 40 + 10 + 8 + 1 + 4 + 4 ) + 1 = 116$  bytes

**Q3(b).**

$Bfr = \text{floor}( 512 / 116 ) = 4$  records / block

$b = 30000 / 4 = 7500$

**Q3(c)(i).**

$R_i = ( SSN + P ) = ( 9 + 6 ) = 15$  bytes

$bfr_i = \text{floor}( B / R_i ) = \text{floor}( 512 / 15 ) = 34$  index records / block

**Q3(c)(ii).**

$r_1 = \text{number of file blocks } b = 7500 \text{ entries}$

$b_1 = \text{ceiling}( r_1 / bfr_i ) = \text{ceiling}( 7500 / 34 ) = 221 \text{ blocks}$

**Q3(c)(iii).**

$r_2 = b_1 = 221 \text{ entries}$

$b_2 = \text{ceiling}( r_2 / bfr_i ) = \text{ceiling}( 221 / 34 ) = 7 \text{ blocks}$

$r_3 = b_2 = 7 \text{ entries}$

$b_3 = \text{ceiling}( r_3 / bfr_i ) = \text{ceiling}( 7 / 34 ) = 1$

Because  $b_3 = 1$  is the top index level

So the number of levels is 3.

**Q3(c)(iv).**

$b_i = b_1 + b_2 + b_3 = 221 + 7 + 1 = 229 \text{ blocks}$

**Q3(c)(v).**

Number of block accesses to search for a record = the number of levels + 1 = 3 + 1 = 4

**Q3(d)(i).**

$R_i = ( \text{SSN} + P ) = ( 9 + 6 ) = 15 \text{ bytes}$

$bfr_i = \text{floor}( B / R_i ) = \text{floor}( 512 / 15 ) = 34 \text{ index records / block}$

**Q3(d)(ii).**

$r_1 = \text{number of file records } r = 30000 \text{ entries}$

$b_1 = \text{ceiling}( r_1 / bfr_i ) = \text{ceiling}( 30000 / 34 ) = 883 \text{ blocks}$

**Q3(d)(iii).**

$r_2 = b_1 = 883 \text{ entries}$

$b_2 = \text{ceiling}( r_2 / bfr_i ) = \text{ceiling}( 883 / 34 ) = 26 \text{ blocks}$

$r_3 = b_2 = 26 \text{ entries}$

$b_3 = \text{ceiling}( r_3 / bfr_i ) = \text{ceiling}( 26 / 34 ) = 1$

Because  $b_3 = 1$  is the top index level

So the number of levels is 3.

**Q3(d)(iv).**

$b_i = b_1 + b_2 + b_3 = 883 + 26 + 1 = 910 \text{ blocks}$

**Q3(d)(v).**

Number of block accesses to search for a record = the number of levels + 1 = 3 + 1 = 4

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**Q4**

Primary Index is on the ordering key field of an ordered file.

Secondary Indexes is on any non-ordering field of a file (ordered, unordered or hashed)

Clustering Indexes is on the ordering non-key field of a file (ordered)