Calculus Exercise

Week 10 (5.4, 5.5)

ID: Name:

5.4.22 Find the general indefinite integral.

$$\int \sec t (\sec t + \tan t) dt$$

5.4.54 Evaluate the definite integral.

$$\int_0^{\frac{3\pi}{2}} |\sin x| dx$$

5.4.72 The acceleration function a(t) in m/s<sup>2</sup> and the initial velocity v(0) are given for a particle moving along a line. Find (a) the velocity at time t and (b) the distance traveled during the given time interval.

$$a(t) = 2t + 3, \ v(0) = -4, \ 0 \le t \le 3.$$

5.4.77 The marginal cost of manufacturing x yards of a certain fabric is

$$C'(x) = 3 - 0.01x + 0.000006x^2$$

(in dollars per yard). Find the increase in cost if the production level is raised from 2000 yards to 4000 yards.

5.5.80 Evaluate the definite integral.

$$\int_{1}^{16} \frac{x^{\frac{1}{2}}}{1 + x^{\frac{3}{4}}} dx$$

5.5.83 Evaluate

$$\int_{-2}^{2} (x+3)\sqrt{4-x^2} dx$$

by writing it as a sum of two integrals and interpreting one of those integrals in terms of an area.

5.5.94 If f is continuous and  $\int_0^9 f(x)dx = 4$ , find  $\int_0^3 x f(x^2)dx$ .

5.5.98 If f is continuous on  $[0,\pi]$ , use the substitution  $u=\pi-x$  to show that

$$\int_0^{\pi} x f(\sin x) dx = \frac{\pi}{2} \int_0^{\pi} f(\sin x) dx.$$

5.5.99 Use 5.5.98 to evaluate the integral

$$\int_0^\pi \frac{x \sin x}{1 + \cos^2 x} dx.$$