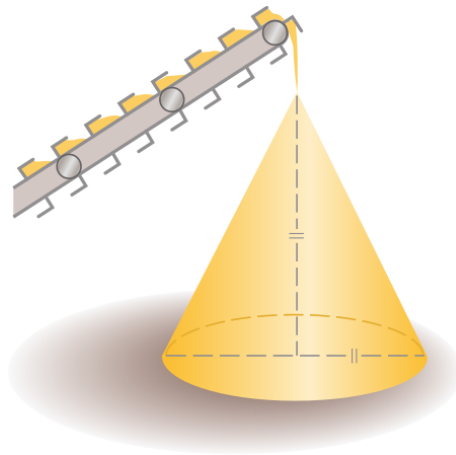
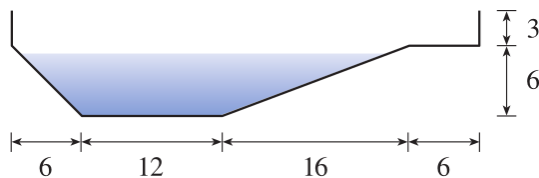


- 3.9.23 Use the fact that the distance (in meters) a dropped stone falls after t seconds is $d = 4.9t^2$. A woman stands near the edge of a cliff and drops a stone over the edge. Exactly one second later she drops another stone. One second after that, how fast is the distance between the two stones changing?

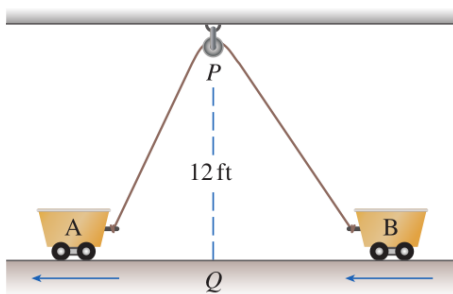
- 3.9.29 Gravel is being dumped from a conveyor belt at a rate of $30 \text{ ft}^3/\text{min}$, and its coarseness is such that it forms a pile in the shape of a cone whose base diameter and height are always equal. How fast is the height of the pile increasing when the pile is 10 ft high?



- 3.9.30 A swimming pool is 20 ft wide, 40 ft long, 3 ft deep at the shallow end, and 9 ft deep at its deepest point. A cross-section is shown in the figure. If the pool is being filled at a rate of $0.8 \text{ ft}^3/\text{min}$, how fast is the water level rising when the depth at the deepest point is 5 ft?



- 3.9.44 Two carts, A and B , are connected by a rope 39 ft long that passes over a pulley P . The point Q is on the floor 12 ft directly beneath P and between the carts. Cart A is being pulled away from Q at a speed of 2 ft/s. How fast is cart B moving toward Q at the instant when cart A is 5 ft from Q ?



3.9.53 Suppose that the volume V of a rolling snowball increases so that $\frac{dV}{dt}$ is proportional to the surface area of the snowball at time t . Show that the radius r increases at a constant rate, that is $\frac{dr}{dt}$ is constant.

3.10.48 When blood flows along a blood vessel, the flux F (the volume of blood per unit time that flows past a given point) is proportional to the fourth power of the radius R of the blood vessel:

$$F = kR^4$$

(This is known as Poiseuille's Law) A partially clogged artery can be expanded by an operation called angioplasty, in which a balloon-tipped catheter is inflated inside the artery in order to widen it and restore normal blood flow.

Show that the relative change in F is about four times the relative change in R . How will a 5% increase in the radius affect the flow of blood?

3.10.50 In physics textbooks, the period T of a pendulum of length L is often given as $T \approx 2\pi\sqrt{L/g}$, provided that the pendulum swings through a relatively small arc. In the course of deriving this formula, the equation $a_T = -g \sin \theta$ for the tangential acceleration of the bob of the pendulum is obtained, and then $\sin \theta$ is replaced by θ with the remark that for small angles, θ (in radians) is very close to $\sin(\theta)$.

- (a) Verify the linear approximation at 0 for the sine function: $\sin \theta \approx \theta$
- (b) If $\theta = \pi/18$ (equivalent to 10°) and we approximate $\sin \theta$ by θ , what is the percentage error?
- (c) Use a graph to determine the values of θ for which $\sin \theta$ and θ differ by less than 2%. What are the values in degrees?

3.10.52 Suppose that we don't have a formula $g(x)$ but we know that $g(2) = -4$ and $g'(x) = \sqrt{x^2 + 5}$ for all x .

- (a) Use a linear approximation to estimate $g(1.95)$ and $g(2.05)$.
- (b) Are your estimates in part (a) too large or too small? Explain.

4.1.45 Find the critical numbers of the function: $f(\theta) = 2 \cos(\theta) + \sin^2(\theta)$.

4.1.50 A formula for the *derivative* of a function f is given. How many critical numbers does f have?

$$f'(x) = \frac{100 \cos^2 x}{10 + x^2} - 1$$

4.1.60 Find the absolute maximum/minimum values of f on the given interval.

$$f(x) = \frac{e^x}{1 + x^2}, [0, 3]$$

4.1.63 Find the absolute maximum/minimum values of f on the given interval.

$$f(x) = x^{-2} \ln x, \left[\frac{1}{2}, 4 \right]$$

4.1.66 Find the absolute maximum/minimum values of f on the given interval.

$$f(x) = x - 2 \tan^{-1} x, [0, 4]$$